

theoretical exercise 7

Pattern Recognition (2018)

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Exercise T-7.1

Problem

You are given the exponential distribution

$$f_X(x|\Theta) = f_X(x|\lambda) = \lambda e^{-\lambda x}$$

defined for $x > 0$ and $\lambda > 0$. Mathematically determine the Maximum-likelihood solution for parameter λ if you are given a set of training samples $D = x_1, x_2, \dots, x_n$

Solution

$$L(\vec{x}, \lambda) = \prod_{i=1}^n f(x_i|\lambda) = \prod_{i=1}^n \lambda e^{-\lambda x_i} = \lambda^n e^{-\lambda \sum_{i=1}^n x_i} \quad (1)$$