## Machine Learning HW

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### 1. What environments the members are using:

Use Jupyter as the environment

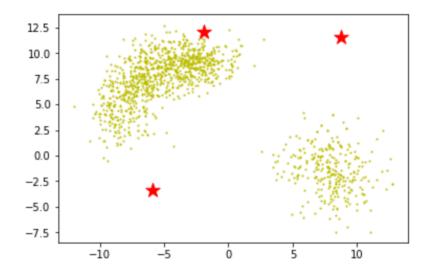
#### 2. K-means code and result:

\*Feature: X, Y Target: pitch\_type

```
%matplotlib inline
from copy import deepcopy
import numpy as np
import pandas as pd
from matplotlib import pyplot as plt
import random
#read data
source = pd.read_csv('data_noah.csv')
data = source[['x','y','pitch_type']]
data = data.replace("CH","0")
data = data.replace("FF","1")
data = data.replace("CU","2")
#select feature
f1 = data['x'].values
f2 = data['y'].values
X_ori = data.values
X = X_{ori}[:,0:2]
X = X.astype(float)
target = X_ori[:,2]
target = target.astype(float)
k=3
```

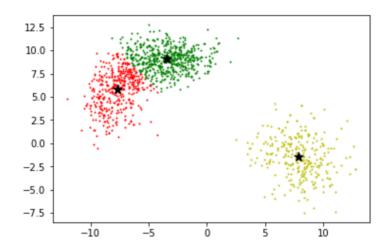
```
#choose three random points
x_cen = [];
for i in range (3):
    x_cen.append(random.uniform(np.min(X[:,0]), np.max(X[:,0])))
y_cen = []
for i in range (3):
    y_cen.append(random.uniform(np.min(X[:,1]), np.max(X[:,1])))
print("x : ", x_cen)
print("y : ", y_cen)
C = np.dstack((x_cen,y_cen))
C = C[0]
plt.scatter(f1, f2, c='y', s=1)
plt.scatter(x_cen, y_cen, marker='*', s=200, c='r')
C_arg = np.argsort(C[:,0])
C = C[C_arg]
```

```
x : [8.772388334549944, -1.92753183025558, -5.864938578235353]
y : [11.593149728113907, 12.039029544109336, -3.421305046088942]
```



```
#repeat calculating the means of each cluster until it converges
pitch_type = np.zeros(len(X))
C_origin = np.zeros(C.shape)
f=0
while np.linalg.norm(C - C_origin, None) !=0:
    f=f+1
    cost=0
    for i in range(len(X)):
        dis = np.linalg.norm(X[i] - C, axis=1)
        pitch_type[i] = np.where(dis==np.min(dis))[0][0]
    C_origin = C.copy()
    for i in range(k):
        points = [X[j] for j in range(len(X)) if pitch_type[j] == i]
        C[i] = np.mean(points, axis=0)
    C_arg = np.argsort(C[:,0])
    C = C[C_arg]
####cost function
    for i in range(k):
        points2 = np.array([X[j] for j in range(len(X)) if pitch_type[j] == i])
        x_distance = points2[:,0] - C[i,0]
        x_distance_power = np.power(x_distance,2)
        y_distance = points2[:,1] - C[i,1]
        y_distance_power = np.power(y_distance,2)
        distance = np.sum(x_distance_power) + np.sum(y_distance_power)
        costi = distance / points2[:,0].size
        cost += costi
    print('%2d' %f," cost = ",round(cost,6))
#draw the plot
colors = ['r', 'g', 'y']
fig, ax = plt.subplots()
for i in range(k):
        points = np.array([X[j] for j in range(len(X)) if pitch_type[j] == i])
        ax.scatter(points[:, 0], points[:, 1], s=1, c=colors[i])
ax.scatter(C[:, 0], C[:, 1], marker='*', s=100, c='black')
```

<matplotlib.collections.PathCollection at 0x17e5cd80588>



## 3. Cost function and accuracy:

$$COST = \sum_{i=1}^{10} rac{1}{|C_i|} \sum_{x \in C_i} \|x - C_i\|^2$$

Calculate every distance between every point and their own center, and sum them which are in the same cluster, then divide the cluster's size.

```
####cost function
for i in range(k):
    points2 = np.array([X[j] for j in range(len(X)) if pitch_type[j] == i])
    x_distance = points2[:,0] - C[i,0]
    x_distance_power = np.power(x_distance,2)
    y_distance = points2[:,1] - C[i,1]
    y_distance_power = np.power(y_distance,2)
    distance = np.sum(x_distance_power) + np.sum(y_distance_power)
    costi = distance / points2[:,0].size
    cost += costi
    print('%2d' %f," cost = ",round(cost,6))
```

```
1 cost = 217.450046

2 cost = 111.628087

3 cost = 19.12643

4 cost = 18.692223

5 cost = 18.593864

6 cost = 18.521015

7 cost = 18.515944

8 cost = 18.516584

9 cost = 18.510021

10 cost = 18.512433

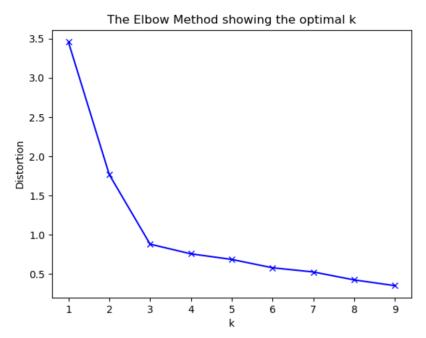
11 cost = 18.512433
```

```
#accuracy: check the difference between predicted result and target
wrong=0
for i in range(len(target)):
    if target[i]!=pitch_type[i]:
        wrong = wrong+1
accuracy = 1-(wrong/len(target))
print("accuracy =", accuracy)
```

accuracy = 0.8001514004542014

# 4. Why choose k=3:

The technique to determine k called the elbow method.



We can see that the improvement will decline, at some point rapidly, creating the elbow shape. That point is the optimal value, and it is 3.

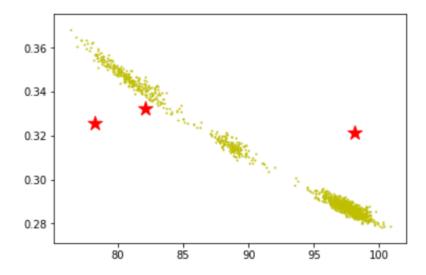
## 5. Another two attributes to partition:

\*Feature: ftime, speed Target: pitch\_type
Only screenshot the code differ from above

```
#select features
f1 = data['speed'].values
f2 = data['ftime'].values
X_ori = data.values
X = X_ori[:,0:2]
X = X.astype(float)
target = X_ori[:,2]
target = target.astype(float)
k=3
```

```
#choose three random points
x_cen = [];
for i in range (3):
    x_cen.append(random.uniform(np.min(X[:,0]), np.max(X[:,0])))
y_cen = []
for i in range (3):
    y_cen.append(random.uniform(np.min(X[:,1]), np.max(X[:,1])))
print("x : ", x_cen)
print("y : ", y_cen)
C = np.dstack((x_cen,y_cen))
C = C[0]
plt.scatter(f1, f2, c='y', s=1)
plt.scatter(x_cen, y_cen, marker='*', s=200, c='r')
C_arg = np.argsort(C[:,0])
C = C[C_arg]
```

x : [98.13424189440241, 82.1190603775276, 78.25840281449148] y : [0.3211879839606597, 0.33247955238350235, 0.32581194351288767]



<sup>\*</sup>Cost function result and accuracy:

```
1 cost = 14.530882

2 cost = 10.554894

3 cost = 6.294323

4 cost = 5.223014

5 cost = 5.089737

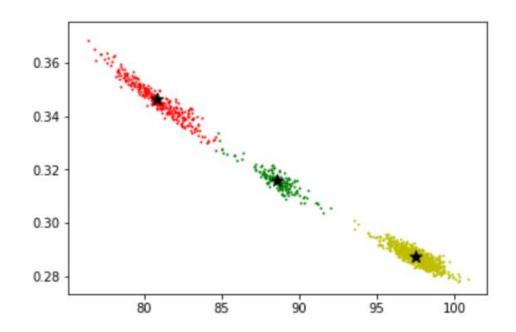
6 cost = 5.047699

7 cost = 5.047699
```

```
wrong=0
for i in range(len(target)):
    if target[i]!=pitch_type[i]:
        wrong = wrong+1
accuracy = 1-(wrong/len(target))
print("accuracy =", accuracy)
```

accuracy = 0.9947009841029523

<sup>\*</sup>Result:



#### 6. KD-tree code

Divide into two parts, and do it recursively, we use median to be divided point.

```
class Node(namedtuple('Node', 'location left_child right_child')):
    def __repr__(self):
        return pformat(tuple(self))

def kdtree(point_list, depth=0):
    try:
        k = len(point_list[0])
    except IndexError:
        return None
    axis = depth % k
    point_list.sort(key=itemgetter(axis))
    median = len(point_list) // 2
    return Node(
        location=point_list[median],
        left_child=kdtree(point_list[median], depth + 1),
        right_child=kdtree(point_list[median + 1:], depth + 1)
)
```

### 7. Result of KD-tree

