FIFA20 Regression Problems

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R. Markdown

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When you click the **Knit** button a document will be generated that includes both content as well as the output of any embedded R code chunks within the document. You can embed an R code chunk like this:

```
library(ggplot2)
library(dplyr)
##
## Attaching package: 'dplyr'
## The following objects are masked from 'package:stats':
##
##
       filter, lag
## The following objects are masked from 'package:base':
##
       intersect, setdiff, setequal, union
##
library(tidyr)
library(stringr)
library(data.table)
##
## Attaching package: 'data.table'
## The following objects are masked from 'package:dplyr':
##
##
       between, first, last
library(rio)
## Warning: package 'rio' was built under R version 3.6.2
library(modelr)
library(purrr)
## Attaching package: 'purrr'
```

```
## The following object is masked from 'package:data.table':
##
##
       transpose
f20 <- fread('D:/NEU/Spring 2020/SML/Project/Datasets/players 20.csv')
f20 <- as_tibble(f20)
f20 <- f20 %>% select(-player_url, -long_name, -dob, -player_positions, -body_type, -real_face,
                      -real_face, -player_tags, -loaned_from, -joined, -contract_valid_until,
                      -nation_position, -nation_jersey_number, -player_traits)
f20 <- f20 %>% select(-(66:91))
View(f20)
f20_sans_gks <- f20 %>% select(-gk_diving, -gk_handling, -gk_kicking, -gk_reflexes,
                               -gk_speed, -gk_positioning, -goalkeeping_diving,
                               -goalkeeping_handling, -goalkeeping_kicking,
                               -goalkeeping_positioning, -goalkeeping_reflexes)
f20_gks <- f20%>% select(age, height_cm, weight_kg, overall, potential, value_eur, wage_eur,
                         international_reputation, weak_foot, release_clause_eur, gk_diving, gk_handlin
                         gk_positioning) %>%
 filter(!is.na(gk_diving))
dim(f20_gks)
## [1] 2036
              16
```

LINEAR MODEL: FULL SUBSET SELECTION

```
library(purrr)
#Players excluding GKs:
#Full subset selection:
full_subset_model <- lm(wage_eur~. , data = subset(f20_sans_gks, select = c(- short_name, -sofifa_id, -:
     -team_position, -team_jersey_number, -work_rate)))
#Summary of the model for feature selection:
summary(full_subset_model)
##
## Call:
## lm(formula = wage_eur ~ ., data = subset(f20_sans_gks, select = c(-short_name,
##
       -sofifa_id, -nationality, -club, -preferred_foot, -team_position,
##
       -team_jersey_number, -work_rate)))
##
## Residuals:
               1Q Median
##
       Min
                                3Q
                                       Max
```

```
## -146004
            -1879
                     -259
                             1444 233741
##
## Coefficients:
##
                               Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                             -2.742e+04 5.361e+03 -5.114 3.20e-07 ***
## age
                                                     5.729 1.03e-08 ***
                              2.683e+02 4.682e+01
## height cm
                              5.398e+01 2.714e+01
                                                     1.989 0.046685 *
## weight kg
                              4.949e+01 2.340e+01
                                                     2.114 0.034503 *
## overall
                             -2.067e+01 5.186e+01 -0.399 0.690133
## potential
                             -2.464e+01
                                         3.688e+01 -0.668 0.504103
## value_eur
                              1.070e-03
                                         1.441e-04
                                                     7.430 1.15e-13 ***
## international_reputation
                              1.099e+04
                                         3.227e+02 34.039 < 2e-16 ***
## weak_foot
                              2.334e+01 1.489e+02
                                                     0.157 0.875459
## skill_moves
                             -3.619e+02 2.191e+02 -1.651 0.098658 .
                              9.435e-04 7.287e-05 12.948 < 2e-16 ***
## release_clause_eur
## pace
                              2.154e+02
                                         3.045e+02
                                                     0.707 0.479370
## shooting
                              1.501e+02
                                         3.087e+02
                                                     0.486 0.626826
## passing
                              5.321e+02
                                         3.062e+02
                                                     1.738 0.082291
## dribbling
                             -6.434e+01 3.083e+02 -0.209 0.834715
## defending
                             -1.747e+01
                                         3.089e+02 -0.057 0.954901
## physic
                              5.189e+02 3.089e+02
                                                     1.680 0.092966
## attacking crossing
                             -7.655e+01 6.242e+01 -1.226 0.220088
                                         1.397e+02 -0.585 0.558866
## attacking_finishing
                             -8.168e+01
## attacking_heading_accuracy 2.647e+01
                                         3.379e+01
                                                     0.783 0.433530
## attacking_short_passing
                             -2.078e+02 1.101e+02 -1.888 0.059087 .
## attacking_volleys
                             -2.061e+00
                                         2.008e+01 -0.103 0.918242
## skill_dribbling
                              3.765e+01 1.554e+02
                                                     0.242 0.808512
## skill_curve
                             -1.398e+01 1.979e+01 -0.706 0.480070
## skill_fk_accuracy
                             -6.462e+01 1.885e+01 -3.428 0.000611 ***
## skill_long_passing
                             -1.008e+02 4.866e+01 -2.071 0.038414 *
## skill_ball_control
                              5.921e+01
                                         9.608e+01
                                                     0.616 0.537727
## movement_acceleration
                             -1.146e+02 1.376e+02 -0.832 0.405166
## movement_sprint_speed
                             -1.148e+02 1.688e+02 -0.680 0.496344
## movement_agility
                              2.743e+01 3.417e+01
                                                     0.803 0.422011
## movement_reactions
                             -8.340e+00
                                         2.672e+01
                                                   -0.312 0.754974
## movement_balance
                              2.852e+01 2.088e+01
                                                     1.366 0.171975
## power shot power
                             -1.399e+01 6.326e+01 -0.221 0.824964
## power_jumping
                             -1.621e+01 1.807e+01 -0.897 0.369784
                                         7.799e+01
                                                   -1.929 0.053718
## power_stamina
                             -1.505e+02
## power_strength
                             -2.948e+02 1.550e+02 -1.902 0.057163
## power long shots
                             -3.684e+01 6.332e+01 -0.582 0.560715
## mentality_aggression
                             -1.024e+02 6.261e+01 -1.636 0.101915
## mentality_interceptions
                              1.101e+01 6.343e+01
                                                     0.174 0.862160
## mentality_positioning
                              2.730e+00 2.107e+01
                                                     0.130 0.896912
## mentality_vision
                             -9.625e+01 6.317e+01 -1.524 0.127598
                                                     0.303 0.761932
## mentality_penalties
                              6.046e+00
                                         1.996e+01
## mentality_composure
                             -4.049e+01
                                         1.681e+01 -2.408 0.016054 *
## defending_marking
                             -2.233e+01
                                         9.350e+01 -0.239 0.811226
## defending_standing_tackle
                              1.081e+01
                                         9.499e+01
                                                     0.114 0.909405
## defending_sliding_tackle
                              4.495e+01 3.691e+01
                                                     1.218 0.223362
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 10880 on 15031 degrees of freedom
```

```
## (3201 observations deleted due to missingness)
## Multiple R-squared: 0.7642, Adjusted R-squared: 0.7635
## F-statistic: 1082 on 45 and 15031 DF, p-value: < 2.2e-16

#Features that influence wage the mmost:
#age, height, weight, value, international_reputation, release clause, skill fk accuracy,
#skill long passing and mentality composure.</pre>
```

FORWARD FEATURE SELECTION:

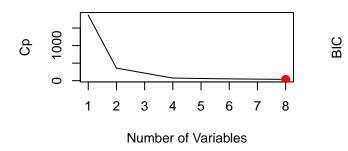
```
#Forward selection:
library(leaps)
## Warning: package 'leaps' was built under R version 3.6.2
ffs_fit <- regsubsets(wage_eur~., data= subset(f20_sans_gks, select = c(- short_name, -sofifa_id, -nati
     -team_position, -team_jersey_number, -work_rate)), method = "forward")
ffs_fit_summary <- summary(ffs_fit)</pre>
coef(ffs_fit, 8)
##
                (Intercept)
                                                                      value_eur
                                                  age
##
              -1.531218e+04
                                         2.750047e+02
                                                                  1.017169e-03
## international_reputation
                                  release_clause_eur
                                                            attacking_crossing
##
               1.130867e+04
                                         9.590736e-04
                                                                  3.040206e+01
##
          skill fk accuracy
                                 mentality_composure defending_sliding_tackle
##
              -2.954003e+01
                                        -4.094771e+01
                                                                   1.444362e+01
names(ffs_fit)
  [1] "np"
                    "nrbar"
                                "d"
                                             "rbar"
                                                         "thetab"
                                                                      "first"
## [7] "last"
                    "vorder"
                                 "tol"
                                             "rss"
                                                         "bound"
                                                                      "nvmax"
## [13] "ress"
                    "ir"
                                 "nbest"
                                             "lopt"
                                                         "il"
                                                                      "ier"
## [19] "xnames"
                    "method"
                                "force.in" "force.out" "sserr"
                                                                      "intercept"
## [25] "lindep"
                    "nullrss"
                                 "nn"
                                             "call"
#The features influencing wage the most: age, value, international reputation,
#release clause, attacking crossing, fk accuracy, mentality composure and sliding tackle.
```

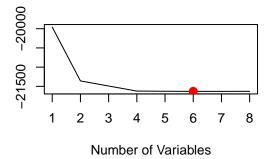
RRS, Adjr2, Cp and BIC measures:

[1] 8

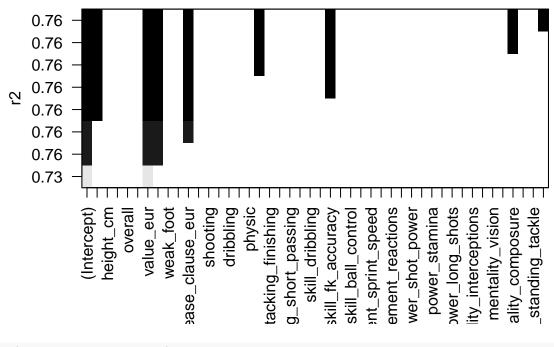
```
par(mfrow=c(2,2))
plot(ffs_fit_summary$rss,xlab="Number of Variables",ylab="RSS",type="l")
plot(ffs_fit_summary$adjr2,xlab="Number of Variables",ylab="Adjusted RSq",type="l")
which.max(ffs_fit_summary$adjr2)
```

```
points(8,ffs_fit_summary$adjr2[8], col="red",cex=2,pch=20)
plot(ffs_fit_summary$cp,xlab="Number of Variables",ylab="Cp",type='l')
which.min(ffs_fit_summary$cp)
## [1] 8
points(8,ffs_fit_summary$cp[8],col="red",cex=2,pch=20)
which.min(ffs_fit_summary$bic)
## [1] 6
plot(ffs_fit_summary$bic,xlab="Number of Variables",ylab="BIC",type='l')
points(6,ffs_fit_summary$bic[8],col="red",cex=2,pch=20)
                                                 Adjusted RSq
                                                      0.735 0.755
RSS
     1.80e+12
               2
                   3
                                     7
                                                                2
                                                                    3
                                                                             5
                                                                                  6
                                                                                      7
                            5
                                 6
                                          8
                                                                                          8
                 Number of Variables
                                                                  Number of Variables
```

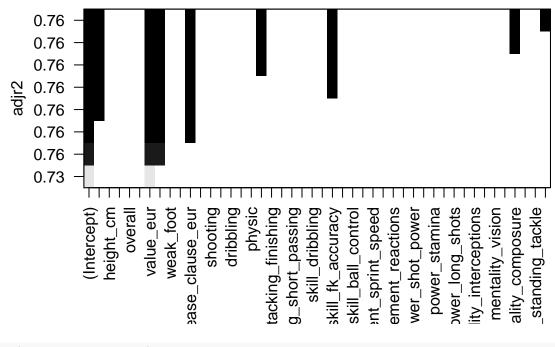




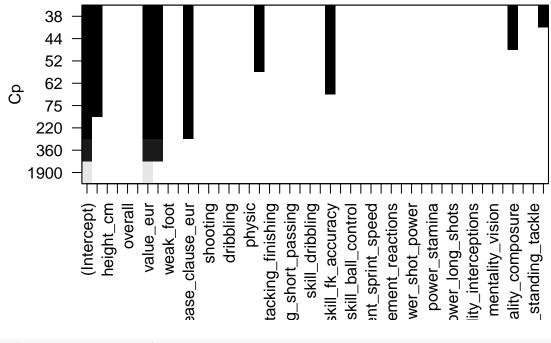
```
plot(ffs_fit,scale="r2")
```



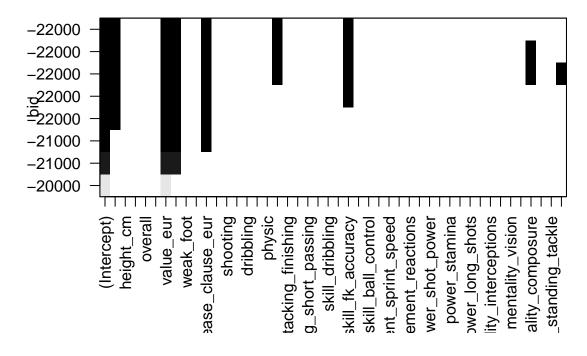
plot(ffs_fit,scale="adjr2")



plot(ffs_fit,scale="Cp")



plot(ffs_fit,scale="bic")



LINEAR MODEL FOR GKs:

```
#Full subset selection for goalkeepers:
full_subset_model_gk <- lm(wage_eur~. , data=f20_gks)</pre>
summary(full_subset_model_gk)
##
## lm(formula = wage_eur ~ ., data = f20_gks)
##
## Residuals:
     Min
              1Q Median
                            3Q
                                  Max
## -94672 -1453
                   -247
                           971
                                93820
##
## Coefficients:
##
                              Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                            -3.783e+04 8.467e+03 -4.468 8.38e-06 ***
                             2.385e+02 7.442e+01
                                                     3.205 0.001374 **
## age
## height_cm
                             1.267e+02 4.860e+01
                                                     2.606 0.009235 **
                                                   -0.794 0.427347
## weight_kg
                            -2.958e+01 3.726e+01
## overall
                            -4.649e+01
                                        2.624e+02
                                                   -0.177 0.859380
                             3.106e+01 7.232e+01
## potential
                                                     0.429 0.667635
## value_eur
                             1.382e-03 3.850e-04
                                                     3.588 0.000341 ***
```

international_reputation 1.123e+04 6.415e+02 17.501 < 2e-16 ***

```
-9.520e+01 2.672e+02 -0.356 0.721697
## weak foot
                         5.419e-04 1.909e-04 2.839 0.004577 **
## release_clause_eur
                          1.948e+01 8.892e+01 0.219 0.826589
## gk diving
                           6.669e+00 7.886e+01 0.085 0.932615
## gk_handling
## gk_kicking
                           2.660e+01 4.076e+01 0.653 0.514086
## gk reflexes
                          3.978e+01 8.655e+01 0.460 0.645840
                          1.196e+01 1.981e+01
                                                 0.604 0.546133
## gk speed
                          -7.618e+01 8.010e+01 -0.951 0.341693
## gk_positioning
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 7801 on 1887 degrees of freedom
    (133 observations deleted due to missingness)
## Multiple R-squared: 0.7969, Adjusted R-squared: 0.7953
## F-statistic: 493.6 on 15 and 1887 DF, p-value: < 2.2e-16
#Features that influence goalkeeper's wage:
#age, height, value, international reputation and release clause.
```

Stepwise Forward selection for GKs:

```
ffs_fit_gks <- regsubsets(wage_eur ~ ., data = f20_gks, method = "forward")
ffs_fit_gks_summary <- summary(ffs_fit_gks)</pre>
coef(ffs_fit_gks, 8)
##
                (Intercept)
                                                                      height_cm
                                                  age
##
              -3.616198e+04
                                         2.125745e+02
                                                                   1.240526e+02
##
                                                                      value_eur
                  weight_kg
                                              overall
              -3.100028e+01
                                         9.906753e+01
                                                                   1.383660e-03
## international_reputation
                                   release_clause_eur
                                                                 gk_positioning
               1.125060e+04
                                         5.396116e-04
                                                                  -9.921888e+01
##
#features selected in stepwise forward selection: age, height, weight, overall, value,
#international reputation, release clause, qk positioning.
```

RSS, Adjr2, Cp and BIC measures:

```
par(mfrow=c(2,2))
plot(ffs_fit_gks_summary$rss,xlab="Number of Variables",ylab="RSS",type="l")

plot(ffs_fit_gks_summary$adjr2,xlab="Number of Variables",ylab="Adjusted RSq",type="l")
which.max(ffs_fit_gks_summary$adjr2)

## [1] 5

points(5,ffs_fit_gks_summary$adjr2[8], col="red",cex=2,pch=20)

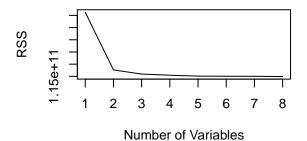
plot(ffs_fit_gks_summary$cp,xlab="Number of Variables",ylab="Cp",type='l')
which.min(ffs_fit_gks_summary$cp)
```

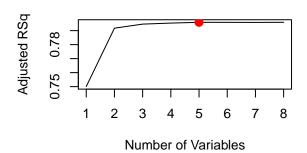
[1] 5

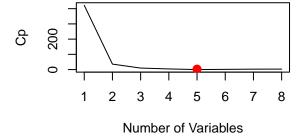
```
points(5,ffs_fit_gks_summary$cp[8],col="red",cex=2,pch=20)
which.min(ffs_fit_gks_summary$bic)
```

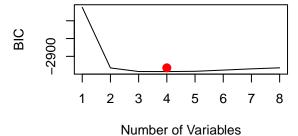
[1] 4

```
plot(ffs_fit_gks_summary$bic,xlab="Number of Variables",ylab="BIC",type='1')
points(4,ffs_fit_gks_summary$bic[8],col="red",cex=2,pch=20)
```









Player overall: FULL SUBSET SELECTION

##

```
## Call:
## lm(formula = overall ~ ., data = subset(f20_sans_gks, select = c(-short_name,
      -sofifa id, -nationality, -club, -preferred foot, -team position,
       -team_jersey_number, -work_rate)))
##
##
## Residuals:
               10 Median
      Min
                               30
                                      Max
## -8.4004 -1.0488 0.0897 1.1475 6.5464
##
## Coefficients:
                               Estimate Std. Error t value Pr(>|t|)
                             -9.654e+00 8.403e-01 -11.489 < 2e-16 ***
## (Intercept)
## age
                              5.249e-01 6.003e-03 87.440 < 2e-16 ***
                             -2.408e-03 4.269e-03 -0.564 0.57277
## height_cm
                              2.221e-02 3.678e-03
                                                    6.038 1.60e-09 ***
## weight_kg
## potential
                              4.359e-01 4.583e-03 95.117 < 2e-16 ***
                              2.693e-07 2.260e-08 11.920
## value_eur
                                                           < 2e-16 ***
## wage eur
                             -5.115e-07 1.283e-06 -0.399
                                                           0.69013
## international_reputation
                             -5.828e-01 5.247e-02 -11.107 < 2e-16 ***
## weak foot
                             -4.847e-02 2.342e-02 -2.070
                                                           0.03846 *
## skill_moves
                              6.198e-01 3.410e-02 18.177
                                                          < 2e-16 ***
## release_clause_eur
                             -6.941e-08 1.151e-08 -6.030 1.68e-09 ***
                             -3.707e-02 4.789e-02 -0.774 0.43885
## pace
                             -9.474e-03 4.855e-02 -0.195
                                                           0.84529
## shooting
## passing
                              6.387e-02 4.817e-02 1.326 0.18489
## dribbling
                              3.710e-02 4.850e-02
                                                    0.765 0.44428
## defending
                              3.170e-02 4.858e-02
                                                    0.653
                                                           0.51409
## physic
                              7.853e-02 4.858e-02
                                                    1.616
                                                           0.10604
## attacking_crossing
                             -2.320e-03 9.818e-03 -0.236 0.81321
## attacking_finishing
                              2.060e-02 2.198e-02
                                                    0.937 0.34865
## attacking_heading_accuracy 4.109e-02 5.305e-03
                                                    7.745 1.02e-14 ***
## attacking_short_passing
                              4.569e-02 1.732e-02
                                                    2.639
                                                           0.00833 **
## attacking_volleys
                             -5.089e-03
                                        3.158e-03 -1.612
                                                           0.10708
                             -1.655e-02 2.444e-02 -0.677
## skill_dribbling
                                                           0.49820
## skill curve
                             -6.744e-03
                                        3.113e-03 -2.166
                                                           0.03029 *
                             -2.544e-03 2.967e-03 -0.858
## skill_fk_accuracy
                                                           0.39110
## skill long passing
                             -1.495e-02 7.654e-03 -1.953 0.05080 .
## skill_ball_control
                              8.123e-02 1.510e-02
                                                    5.380 7.57e-08 ***
## movement acceleration
                              4.323e-02 2.164e-02
                                                    1.997 0.04581 *
## movement_sprint_speed
                              4.676e-02 2.654e-02
                                                    1.762 0.07814 .
                             -4.594e-03 5.374e-03 -0.855
## movement agility
                                                           0.39269
                              1.333e-01 4.060e-03 32.832 < 2e-16 ***
## movement reactions
## movement balance
                             -1.015e-02 3.284e-03 -3.091
                                                           0.00200 **
## power_shot_power
                              1.767e-02 9.949e-03
                                                    1.776 0.07583
## power_jumping
                             -2.382e-03 2.843e-03 -0.838
                                                           0.40205
## power_stamina
                              8.426e-03 1.227e-02
                                                    0.687
                                                           0.49220
## power_strength
                             -1.101e-02
                                        2.438e-02 -0.452
                                                           0.65147
## power_long_shots
                             -5.450e-03 9.960e-03 -0.547
                                                           0.58424
## mentality_aggression
                             -1.603e-02 9.849e-03 -1.628
                                                           0.10354
## mentality_interceptions
                             -1.202e-02
                                        9.977e-03 -1.205
                                                           0.22829
## mentality_positioning
                             -3.210e-02 3.304e-03 -9.716 < 2e-16 ***
## mentality vision
                             -4.422e-02 9.930e-03 -4.453 8.54e-06 ***
## mentality_penalties
                             -4.867e-03 3.139e-03 -1.551 0.12103
                              5.370e-02 2.609e-03 20.584 < 2e-16 ***
## mentality composure
```

```
## defending_marking 7.630e-03 1.471e-02 0.519 0.60391
## defending_standing_tackle 1.191e-03 1.494e-02 0.080 0.93648
## defending_sliding_tackle -1.385e-02 5.806e-03 -2.386 0.01705 *
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 1.712 on 15031 degrees of freedom
## (3201 observations deleted due to missingness)
## Multiple R-squared: 0.9388, Adjusted R-squared: 0.9387
## F-statistic: 5127 on 45 and 15031 DF, p-value: < 2.2e-16
```

Player overall: STEPWISE FORWARD SELECTION

```
ovr_ffs_model <- regsubsets(overall ~ ., data= subset(f20_sans_gks, select = c(- short_name, -sofifa_id
     -team_position, -team_jersey_number, -work_rate)), method = "forward")
ovr_ffs_model_summary <- summary(ovr_ffs_model)</pre>
ovr_ffs_model
## Subset selection object
## Call: regsubsets.formula(overall ~ ., data = subset(f20_sans_gks, select = c(-short_name,
       -sofifa_id, -nationality, -club, -preferred_foot, -team_position,
       -team_jersey_number, -work_rate)), method = "forward")
## 45 Variables (and intercept)
##
                               Forced in Forced out
## age
                                   FALSE
                                              FALSE
## height_cm
                                   FALSE
                                              FALSE
                                   FALSE
## weight_kg
                                              FALSE
## potential
                                   FALSE
                                              FALSE
## value_eur
                                   FALSE
                                              FALSE
                                   FALSE
## wage_eur
                                              FALSE
## international_reputation
                                   FALSE
                                              FALSE
## weak foot
                                   FALSE
                                              FALSE
## skill_moves
                                   FALSE
                                              FALSE
## release_clause_eur
                                   FALSE
                                              FALSE
## pace
                                   FALSE
                                              FALSE
## shooting
                                   FALSE
                                              FALSE
## passing
                                   FALSE
                                              FALSE
## dribbling
                                   FALSE
                                              FALSE
## defending
                                   FALSE
                                              FALSE
## physic
                                   FALSE
                                              FALSE
## attacking_crossing
                                   FALSE
                                              FALSE
## attacking_finishing
                                              FALSE
                                   FALSE
## attacking_heading_accuracy
                                   FALSE
                                              FALSE
                                   FALSE
## attacking_short_passing
                                              FALSE
## attacking_volleys
                                   FALSE
                                              FALSE
## skill_dribbling
                                   FALSE
                                              FALSE
## skill curve
                                   FALSE
                                              FALSE
## skill_fk_accuracy
                                   FALSE
                                              FALSE
## skill_long_passing
                                   FALSE
                                              FALSE
## skill_ball_control
                                  FALSE
                                              FALSE
## movement_acceleration
                                              FALSE
                                  FALSE
```

FALSE

FALSE

movement_sprint_speed

```
## movement_agility
                                  FALSE
                                              FALSE
## movement_reactions
                                  FALSE
                                              FALSE.
                                              FALSE
## movement balance
                                  FALSE
                                              FALSE
## power_shot_power
                                  FALSE
## power_jumping
                                  FALSE
                                              FALSE
## power stamina
                                  FALSE
                                              FALSE
## power strength
                                  FALSE
                                              FALSE
## power_long_shots
                                              FALSE
                                  FALSE
## mentality_aggression
                                  FALSE
                                              FALSE
## mentality_interceptions
                                  FALSE
                                              FALSE
## mentality_positioning
                                  FALSE
                                              FALSE
## mentality_vision
                                  FALSE
                                              FALSE
## mentality_penalties
                                  FALSE
                                              FALSE
                                  FALSE
                                              FALSE
## mentality_composure
## defending_marking
                                  FALSE
                                              FALSE
## defending_standing_tackle
                                  FALSE
                                              FALSE
## defending_sliding_tackle
                                  FALSE
                                              FALSE
## 1 subsets of each size up to 8
## Selection Algorithm: forward
coef(ovr_ffs_model, 8)
##
           (Intercept)
                                                      potential
                                                                           value_eur
                                        age
##
         -8.923078e+00
                              5.460395e-01
                                                   4.982575e-01
                                                                       1.193610e-07
  skill ball control movement reactions
##
                                                  power stamina
                                                                     power_strength
                              1.481190e-01
                                                   4.578565e-02
                                                                        5.293419e-02
          1.075874e-01
## mentality_composure
          4.926088e-02
```

RSS, Adjr2, Cp and BIC measures:

```
par(mfrow=c(2,2))
plot(ovr_ffs_model_summary$rss,xlab="Number of Variables",ylab="RSS",type="1")
plot(ovr_ffs_model_summary$adjr2,xlab="Number of Variables",ylab="Adjusted RSq",type="1")
which.max(ovr_ffs_model_summary$adjr2)

## [1] 8

points(8,ovr_ffs_model_summary$adjr2[8], col="red",cex=2,pch=20)
plot(ovr_ffs_model_summary$cp,xlab="Number of Variables",ylab="Cp",type='l')
which.min(ovr_ffs_model_summary$cp)

## [1] 8

points(8,ovr_ffs_model_summary$cp[8],col="red",cex=2,pch=20)
which.min(ovr_ffs_model_summary$cp[8],col="red",cex=2,pch=20)
which.min(ovr_ffs_model_summary$bic)
```

```
plot(ovr_ffs_model_summary$bic,xlab="Number of Variables",ylab="BIC",type='1')
points(8,ovr_ffs_model_summary$bic[8],col="red",cex=2,pch=20)
```

