

SSN College of Engineering  
Department of Computer Science and Engineering  
CS1504 — Artificial Intelligence  
2021 – 2022

**Assignment — 04 (Additional)**  
**( State Space Search — Genetic Algorithm )**

September 11, 2021

**Problem Statement**

Solve 8-queens problem. Place 8 queens on a chessboard so that no queen is under attack from any other queen. Implement the Genetic Algorithm to find any one such safe configuration

**Response ( [Link to repl.it implementation repository](#) )**

**State Space Formulation**

State: An arrangement of all 8 queens on the board, one per column

State Representation: An 8-element tuple. Each value represents the row index of the queen's position in that column

Initial State: Randomly generated arrangement of 8 queens, one per column

Actions: Move a queen from one row to another within its column

Heuristic / Cost: No. of pairs of attacking queens

Goal State: No attacking pairs of queens

**Sample Case**

No. of Non-Attacking Pairs shown for each successor state

```
[ '25', '23', '25', '26', '28', '26', '25', '25' ]  
[ 'Q ', '24', '23', '25', '25', '25', '24', '24' ]  
[ '25', '24', '24', 'Q ', '25', '24', '24', '24' ]  
[ '24', '24', '22', '23', 'Q ', 'Q ', '22', '24' ]  
[ '24', '24', '24', '24', '25', '23', '24', 'Q ' ]  
[ '23', 'Q ', '24', '25', '25', '25', '22', '23' ]  
[ '24', '23', '23', '25', '27', '24', 'Q ', '23' ]  
[ '24', '24', 'Q ', '25', '26', '25', '24', '24' ]
```

## Python Program Code

1. StateFormulation.py - Script to formulate the state space and instantiate a problem case

```
import numpy.random as random
from copy import deepcopy

NUM_QUEENS = 8
MAX_POSSIBLE_ATTACKS = ( NUM_QUEENS * (NUM_QUEENS-1) ) // 2 # i.e nC2
MIN_POSSIBLE_ATTACKS = 0

def generate_random_state():
    state = [
        random.randint(0, NUM_QUEENS)
        for x in range(NUM_QUEENS)
    ]
    return state

def count_attacks(state):
    num_attacks = 0
    # Count for each queen
    for column in range(NUM_QUEENS):
        # Count queens in same row. Exclude self
        num_attacks += state.count(state[column])-1
        # Try right and left diagonals. Exclude self
        num_attacks -= 2
        diag_sum = column + state[column]
        diag_diff = column - state[column]
        for i in range(NUM_QUEENS):
            if i+state[i]==diag_sum:
                num_attacks += 1
            if i-state[i]==diag_diff:
                num_attacks += 1
    # Each pair-attack was counted twice. Hence, return result/2
    return num_attacks//2
```

```

def count_non_attacks(state):
    return MAX_POSSIBLE_ATTACKS - count_attacks(state)

# Find the next states
def get_next_states(state):
    moves = list()
    attacks = list()
    disp_arr = [[None for x in range(NUM_QUEENS)] for y in
range(NUM_QUEENS) ]
    # Try moving each queen to every other position in its column
    for column in range(NUM_QUEENS):
        for row in range(NUM_QUEENS):
            if row == state[column]:
                # If moving again to same row, skip
                disp_arr[row][column] = 'Q '
                continue
            else:
                temp_state = deepcopy(state)
                temp_state[column] = row
                disp_arr[row][column] =
str(count_non_attacks(temp_state)).ljust(2)
        for i in disp_arr:
            print(i)
    return moves, attacks

def is_goal_reached(state):
    return count_attacks(state)==0

# Display the state, visually
def display_state(state):
    disp_array = [
        [ 'Q' if state[col]==row else '-' for row in
range(NUM_QUEENS) ]
        for col in range(NUM_QUEENS)
    ]
    for disp_row in disp_array:
        print(disp_row)

```

```

"""
# Testing state generation
sample_state = [4, 5, 6, 3, 4, 5, 6, 5]
sample_state = [1, 5, 7, 2, 3, 3, 6, 4]
print(get_next_states(sample_state))
"""

```

## 2. GeneticAlgorithm.py - Script to perform genetic algorithm search

```

from copy import copy
from StateFormulation import *
import numpy as np

def sample_population(population):
    num_draws = len(population)
    # Create array with elements as per probability of choice
    population_fitness = [ count_non_attacks(state)
                           for state in population ]

    # Create a population sample
    population_sample = []
    for idx, state in enumerate(population):
        population_sample.extend([
            state for k in range(population_fitness[idx])
        ])

    np.random.shuffle(population_sample)
    # Select parents and pair them up
    population_idx = [ x for x in range(len(population_sample)) ]
    parent_pairs_idx = np.random.choice(population_idx, num_draws)
    parent_pairs = [ population_sample[idx] for idx in
parent_pairs_idx ]
    parent_pairs = [ (parent_pairs[i], parent_pairs[i+1])
                      for i in range(num_draws//2) ]
    return parent_pairs

def crossover_pair(pair, population_size):
    crossover_idx = np.random.randint(1, population_size-1)
    result = []
    parent_1, parent_2 = pair

```

```

        result.append(parent_1[:crossover_idx] +
parent_2[crossover_idx:])
        result.append(parent_2[:crossover_idx] +
parent_1[crossover_idx:])
        return tuple(result)

def mutate_state(state):
    mutation_idx = np.random.randint(0, len(state)+1)
    if mutation_idx == len(state):
        # No mutation
        pass
    else:
        mutated_state = np.random.randint(0, NUM_QUEENS)
        state[mutation_idx] = mutated_state
    return state

def search(population_size=8):

    # Check if the population has a goal state
    def scan_goal_state(population):
        for state in population:
            if is_goal_reached(state):
                return True, state
        return False, None

    # Generate random population
    population = [ generate_random_state() for k in
range(population_size) ]

    # Get parents, crossover and mutate till goal is generated
    num_generations = 0
    has_goal_state, goal_state = scan_goal_state(population)
    while not has_goal_state:
        num_generations += 1
        # Select parent-pairs from population as per probability of
selection
        parent_pairs = sample_population(population)
        # Generate descendant population
        population_next = list()

```

```

        for pair in parent_pairs:
            population_next.extend(list(map(mutate_state,
            crossover_pair(pair, population_size))))
            population = copy(population_next)
            has_goal_state, goal_state = scan_goal_state(population)

    return goal_state, num_generations

```

### 3. main.py - Driver program to implement and summarize the search technique

```

from GeneticAlgorithm import search as GA_search
from StateFormulation import display_state

population_size = 8
print("Running Genetic Algorithm...")
goal_state, num_generations =
GA_search(population_size=population_size)
print("\nGOAL STATE REACHED:", goal_state)
print()
display_state(goal_state)
print("\nPopulation Size:", population_size)
print("Number of Generations:", num_generations)

```

## Sample Output

```
Running Genetic Algorithm...  
GOAL STATE REACHED: [7, 2, 0, 5, 1, 4, 6, 3]  
  
['-', '-', '-', '-', '-', '-', '-', 'Q']  
['-', '-', 'Q', '-', '-', '-', '-', '-']  
['Q', '-', '-', '-', '-', '-', '-', '-']  
['-', '-', '-', '-', '-', 'Q', '-', '-']  
['-', 'Q', '-', '-', '-', '-', '-', '-']  
['-', '-', '-', '-', 'Q', '-', '-', '-']  
['-', '-', '-', '-', '-', '-', 'Q', '-']  
['-', '-', '-', 'Q', '-', '-', '-', '-']  
  
Population Size: 8  
Number of Generations: 4449
```