1)

a)

The error is the least for the case where cost=1 based on the 10 fold cross validation.

c)

POLYNOMIAL KERNEL:

```
Console C:/Users/Karthik/Desktop/Sem 1/ISEN 613/
> set.seed(1)
> tune.out <- tune(svm, gas_median \sim ., data = Auto, kernel = "polynomial", ranges = list(cost = c(0.01, 0.1, 1, 5, 10, 100), degree = c(2, 3, 4,5)))
> summary(tune.out)
Parameter tuning of 'svm':
- sampling method: 10-fold cross validation
- best parameters:
 cost degree
  100
- best performance: 0.3013462
- Detailed performance results:
                     error dispersion
    cost degree
               2 0.5611538 0.04344202
  1e-02
   1e-01
               2 0.5611538 0.04344202
3 1e+00
               2 0.5611538 0.04344202
               2 0.5611538 0.04344202
  5e+00
  1e+01
               2 0.5382051 0.05829238
6
  1e+02
               2 0.3013462 0.09040277
  1e-02
1e-01
               3 0.5611538 0.04344202
3 0.5611538 0.04344202
8
  1e+00
               3 0.5611538 0.04344202
10 5e+00
               3 0.5611538 0.04344202
               3 0.5611538 0.04344202
11 1e+01
               3 0.3322436 0.11140578
12 1e+02
13 1e-02
               4 0.5611538 0.04344202
14 1e-01
               4 0.5611538 0.04344202
```

```
Console C:/Users/Karthik/Desktop/Sem 1/ISEN 613/
I3 IE-UZ
               4 0.3011338 0.04344202
14 1e-01
               4 0.5611538 0.04344202
15 1e+00
               4 0.5611538 0.04344202
16 5e+00
              4 0.5611538 0.04344202
17 1e+01
              4 0.5611538 0.04344202
18 1e+02
               4 0.5611538 0.04344202
19 1e-02
               5 0.5611538 0.04344202
20 1e-01
               5 0.5611538 0.04344202
5 0.5611538 0.04344202
21 1e+00
               5 0.5611538 0.04344202
22 5e+00
23 1e+01
               5 0.5611538 0.04344202
24 1e+02
               5 0.5611538 0.04344202
```

cost=100, degree=2 has the best result according to the lowest cross validation error for the polynomial kernel.

RADIAL KERNEL:

```
Console C:/Users/Karthik/Desktop/Sem 1/ISEN 613/
                                                                                                                             > set.seed(1)
 tune.out <- tune(svm, gas_median \sim ., data = Auto, kernel = "radial", ranges = list(cost = c(0.01, 0.1, 1, 5, 10, 10
0), gamma = c(0.5,1,2,3,4))
> summary(tune.out)
Parameter tuning of 'svm':
- sampling method: 10-fold cross validation
- best parameters:
 cost gamma
- best performance: 0.04852564
- Detailed performance results:
    cost gamma
                     error dispersion
           0.5 0.56115385 0.04344202
0.5 0.07916667 0.05201159
   1e-02
   1e-01
   1e+00
           0.5 0.05365385 0.05470590
   5e+00
           0.5 0.04852564 0.04597747
   1e+01
           0.5 0.04852564 0.04597747
0.5 0.04852564 0.04597747
   1e+02
   1e-02
           1.0 0.56115385 0.04344202
   1e-01
           1.0 0.56115385 0.04344202
           1.0 0.06634615 0.06187383
   1e+00
10 5e+00
           1.0 0.06128205 0.06186124
           1.0 0.06128205 0.06186124
11 1e+01
           1.0 0.06128205 0.06186124
2.0 0.56115385 0.04344202
12 1e+02
13 1e-02
14 1e-01
            2.0 0.56115385 0.04344202
13 1e-02
          2.0 0.56115385 0.04344202
14 1e-01
           2.0 0.56115385 0.04344202
15 1e+00
           2.0 0.12756410 0.05916990
16 5e+00
           2.0 0.11730769 0.05277475
17 1e+01
           2.0 0.11730769 0.05277475
18 1e+02
           2.0 0.11730769 0.05277475
           3.0 0.56115385 0.04344202
19 1e-02
           3.0 0.56115385 0.04344202
20 1e-01
           3.0 0.37256410 0.14111555
21 1e+00
22 5e+00
           3.0 0.35205128 0.14165290
23 1e+01
           3.0 0.35205128 0.14165290
           3.0 0.35205128 0.14165290
24 1e+02
           4.0 0.56115385 0.04344202
25 1e-02
26 1e-01
           4.0 0.56115385 0.04344202
27 1e+00
           4.0 0.48198718 0.04342861
           4.0 0.47435897 0.05241275
28 5e+00
29 1e+01
           4.0 0.47435897 0.05241275
30 1e+02
           4.0 0.47435897 0.05241275
```

For the considered values of cost and gamma, gamma=0.5 and cost=5 gives the least cross validation error for the radial kernel.

2)

a)

```
Console C:/Users/Karthik/Desktop/Sem 1/ISEN 613/ 
> attach(OJ)
> train=sample(1:nrow(OJ),800)
> |
```

b)

Number of support vectors in this case is high = 622, out of which 312 belong to CH and 310 belong to MM in the 800 training values of 'purchase'.

c)

Training error=1-0.6825=0.3175

Test error=1-0.68=0.311

d)

Optimal cost=0.3163,

e)

Training error0=1-0.8375=0.1625

Test error=1-0.833=0.167

f)

Number of support vectors in this case is high = 624, out of which 314 belong to CH and 310 belong to MM in the 800 training values of 'purchase'.

Training error=1-0.6125=0.3875

Test error=1-0.604=0.396

```
Console C:/Users/Karthik/Desktop/Sem 1/ISEN 613/Project/ 🙈
                                                                                                                        elo/i was putit under k version 5.4.2
> attach(0))
> train=sample(1:nrow(0J),800)
> train.03=03[train.]
> tune.out=tune(svm,Purchase~.,data=train.0],kernel="radial",ranges=list(cost=10^seq(-2, 1, by = 0.5),gamma=c(0.1,0.5,
> summary(tune.out)
Parameter tuning of 'svm':
- sampling method: 10-fold cross validation
- best parameters:
cost gamma
       0.1
- best performance: 0.1775
- Detailed performance results:
    cost gamma error dispersion 0.01000000 0.1 0.42000 0.05177400
                 0.1 0.29500 0.07910085
    0.03162278
                 0.1 0.19250 0.03917553
    0.10000000
    0.31622777
                 0.1 0.18375 0.04041881
   1.00000000
                 0.1 0.17750 0.03162278
6
    3.16227766
                 0.1 0.18625 0.03972562
   10.00000000
                 0.1 0.19250 0.04456581
                 0.5 0.42000 0.05177408
   0.01000000
    0.03162278
                 0.5 0.42000 0.05177408
10 0.10000000
                 0.5 0.28375 0.05744865
11 0.31622777
                 0.5 0.20375 0.05952649
    1.00000000
12
                 0.5 0.20125 0.05318012
   3.16227766
                 0.5 0.22125 0.04489571
14 10.00000000
                 0.5 0.23125 0.04050463
                                                                                                                        Console C:/Users/Karthik/Desktop/Sem 1/ISEN 613/Project/
12 1.00000000 0.5 0.20125 0.05318012
   3.16227766
                 0.5 0.22125 0.04489571
                0.5 0.23125 0.04050463
14 10.00000000
15 0.01000000
                 1.0 0.42000 0.05177408
16
   0.03162278
                 1.0 0.42000 0.05177408
17
   0.10000000
                 1.0 0.32375 0.06440163
18
   0.31622777
                 1.0 0.22625 0.05185785
   1.00000000
                 1.0 0.21625 0.05070681
19
                 1.0 0.23125 0.04093101
20
   3.16227766
21 10.00000000
                 1.0 0.24000 0.04440971
   0.01000000
                 2.0 0.42000 0.05177408
22
                 2.0 0.42000 0.05177408
23
   0.03162278
   0.10000000
                 2.0 0.37875 0.05894029
25
   0.31622777
                 2.0 0.25125 0.05876330
   1.00000000
                 2.0 0.24500 0.04937104
26
   3.16227766
                 2.0 0.25000 0.03996526
28 10.00000000
                 2.0 0.26875 0.04340139
29
   0.01000000
                 3.0 0.42000 0.05177408
                 3.0 0.42000 0.05177408
30
   0.03162278
                 3.0 0.39750 0.05974483
31
   0.10000000
32
   0.31622777
                 3.0 0.27750 0.06942222
33
   1.00000000
                 3.0 0.24875 0.05318012
3.0 0.25000 0.05103104
   3.16227766
34
35 10.00000000
                 3.0 0.26125 0.05152197
36
   0.01000000
                 4.0 0.42000 0.05177408
   0.03162278
                 4.0 0.42000 0.05177408
37
38 0.10000000
                 4.0 0.41375 0.05604128
                 4.0 0.28375 0.06536489
   0.31622777
40 1.00000000
                 4.0 0.25250 0.05230785
```

Optimal cost=1

3.16227766 42 10.00000000

41

> |

4.0 0.26250 0.05237419

4.0 0.25875 0.05497790

```
Console C:/Users/Karthik/Desktop/Sem 1/ISEN 613/Project/ 🖒
> bestmod=tune.out$best.model
> summary(bestmod)
best.tune(method = svm, train.x = Purchase ~ ., data = train.OJ, ranges = list(cost = 10^seq(-2, 1, by = 0.5), gamma = c(0.1, 0.5, 1, 2, 3, 4)), kernel = "radial")
 SVM-Type: C-classification
SVM-Kernel: radial
cost: 1
          gamma: 0.1
Number of Support Vectors: 381
 (195 186)
Number of Classes: 2
Levels:
 CH MM
> |
Console C:/Users/Karthik/Desktop/Sem 1/ISEN 613/Project/ 🖒
> pred=predict(bestmod,newdata=0J[train,])
> train_purchase=Purchase[train]
> table(pred,train_purchase)
train_purchase
pred CH MM
CH 415 64
MM 49 272
> pred=predict(bestmod,newdata=0][-train,])
> test_purchase=Purchase[-train]
> table(pred,test_purchase)
test_purchase
pred CH MM
CH 164 27
MM 25 54
```

Training error=1-0.859=0.1413

Test error=1-0.807=0.193

g)

```
Console C:/Users/Karthik/Desktop/Sem 1/ISEN 613/ 
> svm.fit=svm(Purchase~.,data=OJ,subset=train,kernel="polynomial",cost=0.01) #deafault gamma value used
> summary(svm.fit)

call:
svm(formula = Purchase ~ ., data = OJ, kernel = "polynomial", cost = 0.01, subset = train)

Parameters:
sVM-Type: C-classification
sVM-Kernel: polynomial
cost: 0.01
degree: 3
gamma: 0.05555556
coef.0: 0

Number of Support Vectors: 611
( 308 303 )

Number of Classes: 2

Levels:
CH MM
```

Number of support vectors in this case is high = 611, out of which 308 belong to CH and 303 belong to MM in the 800 training values of 'purchase'.

Training error=1-0.6375=0.3625

Test error=1-0.611=0.389

```
Console C:/Users/Karthik/Desktop/Sem 1/ISEN 613/ 🙈
> train.0J=0J[train,]
> tune.out=tune(svm,Purchase~.,data=train.OJ,kernel="polynomial",ranges=list(cost=10^seq(-2, 1, by = 0.5)),degree=2)
> summary(tune.out)
Parameter tuning of 'svm':
- sampling method: 10-fold cross validation
- best parameters:
cost
   10
- best performance: 0.185
- Detailed performance results:
                  error dispersion
           cost
   0.01000000 0.38750 0.06346478
2 0.03162278 0.35375 0.06375136
3 0.10000000 0.32875 0.05981743
4 0.31622777 0.22000 0.06043821
  1.00000000 0.20125 0.05756940
6 3.16227766 0.19375 0.05987545
7 10.00000000 0.18500 0.07041543
```

Optimal cost=10

Training Error rate= 1-[(457+223)/(453+87+37+223)=0.154

Test error=1-0.837=0.163

h)

	TRAINNIG ERROR	TEST ERROR
Linear Kernel	0.1625	0.167
Polynomial Kernel	0.154	0.163
Radial Kernel	0.1413	0.193

According to the test errors, Polynomial Kernel gives the best results and seems to be the most accurate in classifying the 'Purchase' followed closely by the Linear kernel and radial kernel.