

COM Design and Analysis of Algorithms Assignment-1

Note: All assignments involve a team of size 5 or 6. Due: 18/Jan

1. Given an integer array, write an algorithm to find max and min. Calculate its step count. Express the step count (time complexity) interms of $O, \Omega, \theta, o, \omega$.
2. Write a recursive algorithm to search an element in an integer array. Calculate its step count. Express the step count (time complexity) interms of $O, \Omega, \theta, o, \omega$.
3. Algorithm A performs $10 n^2$ basic operations, and algorithm B performs $300 \log n$ basic operations. For what value of n does algorithm B start to show its better performance.
4. In each of the following situations, indicate whether $f = O(g)$ or $f = \Omega(g)$ or both (in which case $f = \theta(g)$)

$f(n)$	$g(n)$
(a) $n-100$	$n-200$
(b) $100n + \log n$	$n + (\log n)^2$
(c) $\log 2n$	$\log 3n$
(d) $n^{1.01}$	$n \log^2 n$
(e) $n2^n$	3^n
(f) $n!$	2^n

5. Arrange the following functions in order. $7, \frac{1}{n^2}, 2^{n \cdot \log n}, 4^{\log n}, n^{\log 7}, n!, (\frac{n}{e})^n$
6. For each of the above function, express the function (time complexity) using little-oh and little-omega.
7. Fill-in the following table with a tick if the asymptotic notation satisfies the property. Justify any three.

Notation	Reflectivity	Symmetric	Transitive	Antisymmetric
θ				
O				
Ω				
o				
ω				