

Question:

Given an array representing profit or loss from a stock over a period of days, write a function that calculates total profit or loss for a given range of days.

Example:

	0	1	2	3	4	5	6	7	8	9
SP[] :	-5	10	20	40	50	-10	80	-90	-20	-10
C :	-5	5	25	65	115	105	185	95	75	65

Queries

<u>S</u>	<u>E</u>	<u>Net</u>		Q queries.
0	9	65	N	
1	4	120	N	
0	0	-5	N	
7	9	-120	N	
2	7	90	N	

$O(QN)$

```
int [][] queries = new int [Q][2];
```

queries[i] → ith query.

queries[i][0] → s for ith query.

queries[i][1] → e for ith query.

```

void printQuerySum (int[] A, int[][] Q)
{
    for (i=0; i < Q.length; i++)
    {
        int[] query = Q[i];
        int s = query[0];
        int e = query[1];
        int sum = 0;
        for (j=s; j <= e; j++)
        {
            sum = sum + A[j];
        }
        print (sum);
    }
}

```

TC: $O(N * Q)$

SC: $O(1)$

Question:

Given N elements and Q queries.
For each query, calculate sum of all elements from L to R .

Eg: $A: \overset{0}{-3} \overset{1}{6} \overset{2}{2} \overset{3}{4} \overset{4}{5} \overset{5}{2} \overset{6}{8} \overset{7}{-9} \overset{8}{3} \overset{9}{1}$

<u>L</u>	<u>R</u>	<u>Sum</u>
4	8	9
3	7	10
1	3	12
0	4	14
7	7	-9

Given the scores of the 1st 10 overs of a cricket match

2	6	6	15	2	18	16	14	9	9
<u>1</u>	<u>2</u>	<u>3</u>	<u>4</u>	<u>5</u>	<u>6</u>	<u>7</u>	<u>8</u>	<u>9</u>	<u>10</u>
2	8	14	29	31	49	65	79	88	97

a. Runs scored in 7th over = $T(7) - T(6)$

$$= 65 - 49 = \underline{\underline{16}}$$

<u>s</u>	<u>e</u>	<u>Runs</u>
3	6	$T(6) - T(2)$

b. Runs scored from 6th to 10th over

$$S(6-10) : T(10) - T(5)$$

4	9	$T(9) - T(3)$
---	---	---------------

c. Runs scored in the 10th over:

$$S(10) - T(10) - T(9)$$

$$\begin{array}{cc} s & e \\ T(e) - T(s-1) \end{array}$$

Prefix Sum Array:

	0	1	2	3	4
A:	2	5	-1	7	1
PF:	2	7	6	13	14

	0	1	2	3	4	5
A:	10	32	6	12	20	1
PF:	10	42	48	60	80	81

	0	1	2	3	4	5	6	7	8	9
A :	-3	6	2	4	5	2	8	-9	3	1

<u>L</u>	<u>R</u>	<u>Sum</u>
4	8	
3	7	
1	3	
0	4	
7	7	

Create a prefix array:

SP[] : ⁰ ¹ ² ³ ⁴ ⁵ ⁶ ⁷ ⁸ ⁹
 -5 10 20 40 50 -10 80 -90 -20 -10

```
long[] getPrefixSum(int[] A)
```

```
{  
    long[] psa = new long[A.length];  
    psa[0] = A[0];  
    for (i=1; i < A.length; i++)  
    {  
        psa[i] = psa[i-1] + A[i];  
    }  
    return psa;  
}
```

Using prefix array to answer queries:

```
void printQuerySum (int[] A, int[][] Q)
{
    long[] pa = getPrefixSum(A);
    for (i=0; i < Q.length; i++)
    {
        int[] query = Q[i];
        int s = query[0];
        int e = query[1];
        if (s==0)
        { print ps[e]; }
        else
        { print (pa[e] - pa[s-1]); }
    }
}
```

TC: $O(N+Q)$

SC: $O(N)$

Break : 10:52 PM

Question:

Given an array of size N and Q queries with start and end index. For each query return the sum of all even indexed elements from s to e .

Brute Force $O(N*Q)$

	*		*		*	
	0	1	2	3	4	5
A :	2	3	1	6	4	5
pse :	2	2	3	3	7	7
<u>s</u>	<u>e</u>		<u>sum</u>	<u>$P[E] - P[S-1]$</u>		
1	3		1	$P(3) - P(0) = 1$		
2	5		5	$P(5) - P(1) = 5$		
0	4		7	$P(4) = 7$		
3	3		0	$P(3) - P(2) = 0$		

```
long[] getPrefixSumEv (int[] A)
```

```
{  
    long[] psa = new long[A.length];
```

```
    psa[0] = A[0];
```

```
    for (i=1; i < A.length; i++)
```

```
    { if (i % 2 == 0)
```

```
        { psa[i] = psa[i-1] + A[i]; }
```

```
        else
```

```
        { psa[i] = psa[i-1]; }
```

```
    }
```

```
    return psa;
```

```
}
```

HW for odd

Special Index:

Given A, calculate the no. of special indices.

	0	1	2	3	4	5
A:	4	3	2	7	6	-2
S_o :	8	8	9	9	10	10
S_E :	8	9	9	4	4	12

	0	1	2	3	4	5
A:	4	3	2	7	6	-2
pse:	4	4	6	6	12	12
ps0:	0	3	3	10	10	8

HW

$S_o(3)$: Sum of all odd index [0-2] +
Sum of all even index [4-5]

$S_E(3)$: Sum of all even index [0-2] +
Sum of all odd index [4-5]

0	1	2	3	4	5	6	7	8	9
2	3	1	4	0	-1	2	-2	10	8

Carry Fwd
Subarrays.


```
int countSpecial (int[] A)
```

```
{
```

```
    int count = 0;
```

```
    int[] pse = getPrefixSumEv(A);
```

```
    int[] pso = getPrefixSumOdd(A);
```

```
    int N = A.length;
```

```
    for (i=0; i < A.length; i++)
```

```
    { int so = 0; int se = 0;
```

```
        if (i == 0)
```

```
        {
```

```
            so = pse[N-1]
                - pse[0];
```

// Sum of even index
elements from
1 → N-1

```
            se = pso[N-1]
                - pso[0];
```

```
        }
```

```
    else
```

```
    {
```

```
        so = pso[i-1] +
            pse[n-1] - pse[i];
```

// so [0 → (i-1)]

// + se [i+1 → n-1]

```
        se = pse[i-1] +
            pso[n-1] - pso[i];
```

// se [0 → (i-1)]

// + so [i+1 → n-1]

```
    }
```

```
    if (so == se)
```

```
    { count++; }
```

```
}
```

```
return count;
```

Doubts:

0	4	2	3	1
2	4	5	6	—

Q[] [] \rightarrow fun()