```
In [52]: import os
         import numpy as np
         import torch as T
         import torch.nn as nn
         import torch.optim as optim
         from torch.distributions.normal import Normal
         import matplotlib.pyplot as plt
         import gym
In [53]: import a3_gym_env
         gym.make('Pendulum-v260')
Out[53]: <OrderEnforcing<PassiveEnvChecker<CustomPendulumEnv<Pendulum-v260>>>>
In [54]: class ReplayBuffer:
             def __init__(self):
                 self.states = []
                 self.probs = []
                 self.vals = []
                 self.actions = []
                 self.rewards = []
                 self.dones = []
             def store_memory(self, state, action, probs, vals, reward, done):
                 self.states.append(state)
                 self.actions.append(action)
                 self.probs.append(probs)
                 self.vals.append(vals)
                 self.rewards.append(reward)
                 self.dones.append(done)
In [88]: class ActorNetwork(nn.Module):
             def __init__(self, input_dims, output_dims, alpha,
                          hidden_layers = 2, hidden_dims=8, N=1):
                 super().__init__()
                 # actor network to estimate mean of the gaussian distribution
                 self.actor = nn.Sequential()
                 self.actor.append(nn.Linear(*input_dims, hidden_dims))
                 for i in range(hidden layers):
                     self.actor.append(nn.Linear(hidden_dims, hidden_dims))
                     self.actor.append(nn.ReLU())
                 self.actor.append(nn.Linear(hidden_dims, output_dims))
                 # use constant standard deviation
                 log_std = -0.9 * np.ones(output_dims, dtype=np.float32)
                 self.log_std = T.nn.Parameter(T.as_tensor(log_std))
                 self.optimizer = optim.Adam(self.parameters(), lr=alpha/N, eps=1e-05)
                   self.scheduler = optim.lr_scheduler.ReduceLROnPlateau(self.optimizer)
                 self.device = T.device('cuda:0' if T.cuda.is_available() else 'cpu')
                 self.to(self.device)
             def forward(self, state):
                 m = self.actor(state)
                 # return normal distribution
                 dist = Normal(m, T.exp(self.log_std))
                 return dist
```

```
def __init__(self, input_dims, alpha, hidden_layers = 2, hidden_dims=8, N=1):
                 super().__init__()
                 # crtic network for estimating value
                 self.critic = nn.Sequential()
                 self.critic.append(nn.Linear(*input_dims, hidden_dims))
                 for i in range(hidden_layers):
                     self.critic.append(nn.Linear(hidden_dims, hidden_dims))
                     self.critic.append(nn.ReLU())
                   self.critic.append(nn.Linear(hidden dims, 32))
         #
                   self.critic.append(nn.ReLU())
         #
                   self.critic.append(nn.Dropout())
         #
                   self.critic.append(nn.Linear(32, 64))
         #
                   self.critic.append(nn.ReLU())
         #
                   self.critic.append(nn.Dropout())
         #
                   self.critic.append(nn.Linear(64, 128))
         #
                   self.critic.append(nn.ReLU())
         #
                   self.critic.append(nn.Dropout())
                   self.critic.append(nn.Linear(128, 32))
         #
                   self.critic.append(nn.ReLU())
                   self.critic.append(nn.Dropout())
                 self.critic.append(nn.Linear(hidden_dims, 1))
                 self.optimizer = optim.Adam(self.parameters(), lr=alpha/N, eps=1e-05)
                   self.scheduler = optim.lr_scheduler.ReduceLROnPlateau(self.optimizer)
                 self.device = T.device('cuda:0' if T.cuda.is_available() else 'cpu')
                 self.to(self.device)
             def forward(self, state):
                 # return value
                 value = self.critic(state)
                 return value
In [57]: def choose_action_value(observation, actor, critic):
                 # convert state to tensor
                 state = T.tensor([observation], dtype=T.float).to(actor.device)
                 # get gaussian distribution for state
                 dist = actor(state)
                 # get value for current state
                 value = critic(state)
                 # sample action
                 action = dist.sample()
                 # get log prob for sampled action (to be used for ratio)
                 probs = T.squeeze(dist.log_prob(action)).item()
                 action = T.squeeze(action).item()
                 value = T.squeeze(value).item()
                 # return action, log prob for sampled action and value for current state
                 return action, probs, value
```

In [89]: class CriticNetwork(nn.Module):

```
num_steps = len(rewards)
             if use gae:
                 advantages = np.zeros_like(rewards)
                  last gae lam = 0
                 for t in reversed(range(num_steps)):
                      if t == num_steps - 1:
                          next non terminal = 1.0 - next done
                          next_values = next_value
                      else:
                          next_non_terminal = 1.0 - dones[t + 1]
                          next_values = values[t + 1]
                      delta = rewards[t] + gamma * next_values * next_non_terminal - values[t]
                      advantages[t] = last gae lam = delta + gamma * lmbda * next non terminal * last ga
                  returns = advantages + values
             else:
                 returns = np.zeros like(rewards)
                 for t in reversed(range(num_steps)):
                      if t == num_steps - 1:
                          next non terminal = 1.0 - next done
                          next_return = next_value
                      else:
                          next_non_terminal = 1.0 - dones[t + 1]
                          next_return = returns[t + 1]
                      returns[t] = rewards[t] + gamma * next_non_terminal * next_return
                  advantages = returns - values
             return returns, advantages
In [58]: def combine_trajectories(trajectories):
             c_states = []
             c_actions = []
             c_rewards = []
             c_logprobs = []
             c_values = []
             c_dones = []
             c_returns = []
             c_advantages = []
             for k, v in trajectories.items():
                 buf, ret, adv = v
                 c_states.extend(buf.states)
                 c_actions.extend(buf.actions)
                 c_rewards.extend(buf.rewards)
                 c_logprobs.extend(buf.probs)
                  c_values.extend(buf.vals)
                  c_dones.extend(buf.dones)
                 c_returns.extend(ret)
                 c_advantages.extend(adv)
                  'states': c_states,
                  'actions': c_actions,
                  'rewards': c_rewards,
                  'logprobs': c_logprobs,
                  'values': c_values,
                  'dones': c_dones,
                  'returns': c_returns,
                  'advantages': c_advantages,
              }
```

In [7]: def get_advantages(gamma, lmbda, values, dones, rewards,

next_value, next_done, use_gae):

```
In [102...] def ppo(N = 1, M = 50, max_trajectory_len = 200, batch_size = 25,
                  alpha = 0.0001, hidden_layers = 2, hidden_dims = 8, gamma = 0.99,
                  lmbda = 0.95, clip_value = 0.2, use_gae=True, use_clip=True):
              \# N = 1 \# number of times to collect new trajectories and update actor
              # M = 50 # num of trajectories
              # max_trajectory_len = 200 # trajectory length
              # batch_size = 25 # size for minibatch
              # n_epochs = 30 # number of epochs to optimize loss
              # alpha = 0.00005
              # hidden_layers = 3
              # hidden dims = 10
              \# gamma = 0.8
              # Lmbda = 0.95
              # clip_value = 0.2
              # use gae = True
              # use clip = True
              env = gym.make('Pendulum-v260')
              input_dim = env.observation_space.shape
              actor = ActorNetwork(input_dims=input_dim, output_dims=1, alpha=alpha,
                                  hidden_layers=hidden_layers, hidden_dims=hidden_dims)
              critic = CriticNetwork(input_dims=input_dim, alpha=alpha,
                                  hidden_layers=hidden_layers, hidden_dims=hidden_dims)
              trajectories = {}
              total_loss_list = []
              loss_list = []
              reward_list = []
              observation list = []
              for n in range(N):
                  # collect M trajectories, their returns, and activations
                  for i in range(M):
                      curr_trajectory = ReplayBuffer()
                      observation = env.reset()
                      done = False
                      steps = 0
                      while steps < max_trajectory_len:</pre>
                          action, prob, val = choose_action_value(
                               observation, actor, critic)
                          next observation, reward, done, info = env.step([action])
                          steps +=1
                          curr_trajectory.store_memory(
                              observation, action, prob, val, reward, done)
                          observation = next_observation
                          if done:
                              break
                      # get GAE advantage
                      # get value of next_observation
                      next_value = critic(T.tensor(observation).to(actor.device))
                      # calculate return and advantage
                      returns, advantages = get_advantages(
                          gamma, lmbda, curr_trajectory.vals, curr_trajectory.dones,
                          curr_trajectory.rewards, next_value, done, use_gae)
                      trajectories[i] = (curr_trajectory, returns, advantages)
                  # combine_trajectories
                  c_trajectories = combine_trajectories(trajectories)
                  total_steps_taken = len(c_trajectories['states'])
                  indicies = np.arange(total_steps_taken)
                  np.random.shuffle(indicies)
                  # optimize loss
                  for epoch in range(n_epochs):
                      # get batches
                      for start in range(0, total_steps_taken, batch_size):
                          end = start + batch size
```

```
# batch indicies
                b_indicies = indicies[start:end]
                states = T.tensor(
                    np.array(c_trajectories['states'])[b_indicies],
                    dtype=T.float).to(actor.device)
                new_value = critic(states)
                distr = actor(states)
                old_log_prob = T.tensor(
                    np.array(c_trajectories['logprobs'])[b_indicies]).to(actor.device)
                actions = T.tensor(
                    np.array(c_trajectories['actions'])[b_indicies],
                    dtype=T.float).to(actor.device)
                new_log_prob = distr.log_prob(actions)
                # Probability ratio
                log_ratio = new_log_prob - old_log_prob
                ratio = log_ratio.exp()
                b_returns = T.tensor(
                    np.array(c_trajectories['returns'])[b_indicies]).to(actor.device)
                b_advantages = T.tensor(
                    np.array(c_trajectories['advantages'])[b_indicies]).to(actor.device)
                  b_advantages = (b_advantages - b_advantages.mean())/(b_advantages.std()+1e-8)
                # Clipping
                weighted_probs = b_advantages * ratio
                if use_clip:
                    weighted_clipped_probs = T.clamp(ratio, 1-clip_value,
                            1+clip_value)*b_advantages
                    actor_loss = -T.min(
                        weighted_probs, weighted_clipped_probs).mean()
                else:
                    weighted_probs = b_advantages * ratio
                    actor_loss = -(weighted_probs).mean()
                critic_loss = (b_returns-new_value)**2
                critic_loss = critic_loss.mean()
                total_loss = actor_loss + 0.5*critic_loss
                print("n: {}, epoch: {}, minibatch no.: {},".format(
                    n, epoch, start//batch_size))
                print("total_loss: {}, actor_loss: {}, critic_loss: {}".format(
                    total_loss, actor_loss, critic_loss))
                total_loss_list.append(total_loss)
                actor.optimizer.zero grad()
                critic.optimizer.zero_grad()
                total_loss.backward()
                actor.optimizer.step()
               critic.optimizer.step()
             actor.scheduler.step(actor_loss)
#
             critic.scheduler.step(critic_loss)
       # get a single trajectory from actor for plotting
       loss_list.append(total_loss)
       reward_list.append(b_returns.mean())
       observation = env.reset()
       done = False
       steps = 0
       while steps < 200:
            action, prob, val = choose_action_value(
                observation, actor, critic)
            next_observation, reward, done, info = env.step([action])
            observation_list.append(observation)
            observation = next_observation
```

```
if done:
    break

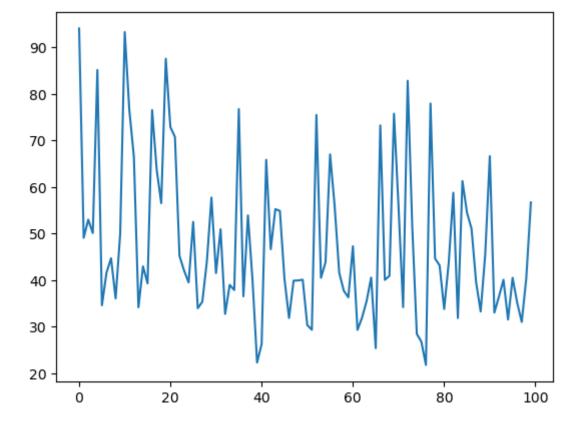
return total_loss_list, observation_list, loss_list, reward_list
```

Clipped and GAE

```
In [11]: N = 100 # number of times to collect new trajectories and update actor
         M = 1 # num of trajectories
         max_trajectory_len = 200 # trajectory Length
         batch_size = 25 # size for minibatch
         n_epochs = 30 # number of epochs to optimize loss
         alpha = 0.0001
         hidden_layers = 2
         hidden_dims = 8
         gamma = 0.7
         lmbda = 0.9
         clip_value = 0.1
         use_gae = True
         use_clip = True
         total_losses, observations, loss_list, reward_list = ppo(
             N, M, max_trajectory_len, batch_size, alpha, hidden_layers, hidden_dims,
             gamma, lmbda, clip_value, use_gae, use_clip)
```

```
In [12]: tmp = [x for x in range(100)]
In [13]: plt.plot(tmp, np.array([l.cpu().detach() for l in loss_list]))
```

Out[13]: [<matplotlib.lines.Line2D at 0x214e98362c0>]



```
In [14]: plt.plot(tmp, np.array([1.cpu().detach() for 1 in reward_list]))
```

Out[14]: [<matplotlib.lines.Line2D at 0x214f3874f10>]

```
-10.0 -
-12.5 -
-15.0 -
-17.5 -
-20.0 -
-22.5 -
-25.0 -
-27.5 -
```

```
In [15]: o = []
    for i in range(N):
        o.append(observations[200*(i+1)-200:200*(i+1)])

In [16]: o_old = o.copy()
    o = [j for i, j in enumerate(o) if i%10==0]

In [17]: o = o_old[-10:]

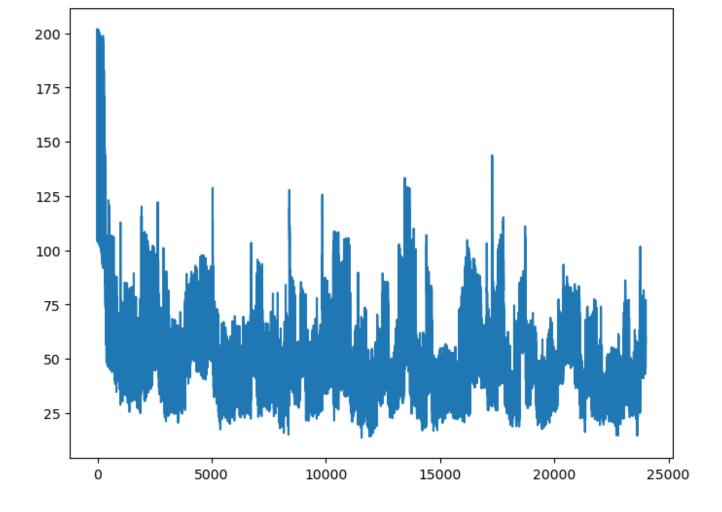
In [18]: x_ = [i+1 for i in range(200)]

In [19]: np.array(o).shape

Out[19]: (10, 200, 3)
```

```
In [20]: N = 10
          plt.figure(1, figsize=(20, 12))
          for i in range(N):
              obs = o[i]
              # print(obs)
              theta_ = []
              x_list = []
              y_list = []
              for x,y,v in obs:
                  # print(x, y)
                  theta_.append(v)
                  x_list.append(x)
                  y_list.append(y)
              plt.subplot(N, 3, 3*i+1)
              plt.plot(x_, x_list)
              plt.xlabel('time')
              plt.ylabel('x')
              plt.subplot(N, 3, 3*i+2)
              plt.plot(x_, y_list)
              plt.xlabel('time')
              plt.ylabel('y')
              plt.subplot(N, 3, 3*i+3)
              plt.plot(x_, theta_)
              plt.xlabel('time')
              plt.ylabel('.theta')
                                             0.25
           -0.95
                                            > 0.00
                                             0.0
                                                                               0.0
                                                                                0
                                                                                0
                                                                                0
                                              -1 -
                                              0.5
                                                                                5
                                                                                              100 125 150
time
                              125 150
                                    175
In [21]: len(total_losses)
Out[21]: 24000
In [22]: x = np.arange(len(total_losses))
          y = [float(x) for x in total_losses]
          plt.figure(figsize=(8, 6))
          plt.plot(x, y)
```

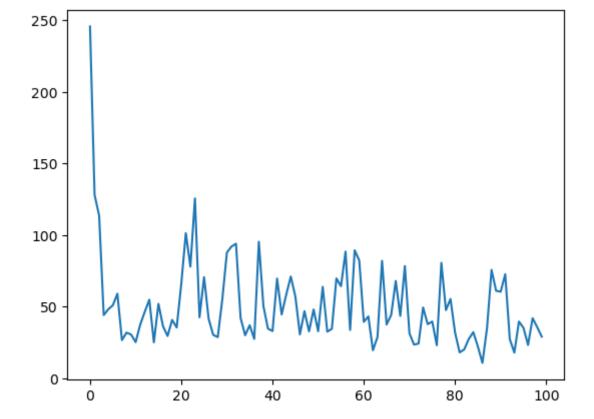
```
Out[22]: [<matplotlib.lines.Line2D at 0x214f4ef67a0>]
```



Clipped and No GAE

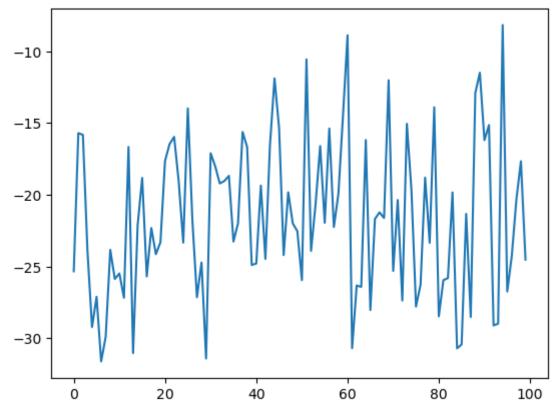
```
In [23]: N = 100 # number of times to collect new trajectories and update actor
         M = 1 # num of trajectories
         max_trajectory_len = 200 # trajectory Length
         batch_size = 25 # size for minibatch
         n_epochs = 30 # number of epochs to optimize loss
         alpha = 0.0001
         hidden_layers = 2
         hidden_dims = 8
         gamma = 0.7
         lmbda = 0.9
         clip_value = 0.1
         use_gae = False
         use_clip = True
         total_losses, observations, loss_list, reward_list = ppo(
             N, M, max_trajectory_len, batch_size, alpha, hidden_layers, hidden_dims,
             gamma, lmbda, clip_value, use_gae, use_clip)
```

```
In [24]: tmp = [x for x in range(100)]
In [25]: plt.plot(tmp, np.array([1.cpu().detach() for 1 in loss_list]))
Out[25]: [<matplotlib.lines.Line2D at 0x214f5b084f0>]
```



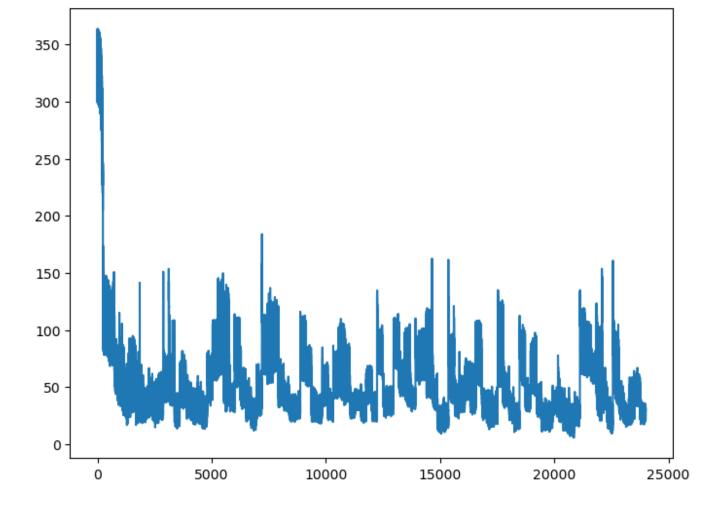
In [26]: plt.plot(tmp, np.array([1.cpu().detach() for 1 in reward_list]))

Out[26]: [<matplotlib.lines.Line2D at 0x214f5a8e7d0>]



```
In [31]: np.array(o).shape
Out[31]: (10, 200, 3)
In [32]: N = 10
          plt.figure(1, figsize=(20, 12))
          for i in range(N):
              obs = o[i]
              # print(obs)
              theta_ = []
              x_list = []
              y_list = []
              for x,y,v in obs:
                   # print(x, y)
                   theta_.append(v)
                   x_list.append(x)
                   y_list.append(y)
              plt.subplot(N, 3, 3*i+1)
              plt.plot(x_, x_list)
              plt.xlabel('time')
              plt.ylabel('x')
              plt.subplot(N, 3, 3*i+2)
              plt.plot(x_, y_list)
              plt.xlabel('time')
              plt.ylabel('y')
              plt.subplot(N, 3, 3*i+3)
              plt.plot(x_, theta_)
              plt.xlabel('time')
              plt.ylabel('.theta')
                                                                                 . theta
. o
                                                                                −2.5
−5.0
−7.5
                                              > 0
            -0.9
                                               0.25
                                              -0.25
                                               0.1
                                              > 0
                                                                                   0
            -1.0
                                                                                  0.0
          × -0.95
           -1.00
                                                                                 theta
o o
                                                                                 theta
0
                                              > 0
In [33]: len(total_losses)
Out[33]: 24000
In [34]: x = np.arange(len(total_losses))
          y = [float(x) for x in total_losses]
          plt.figure(figsize=(8, 6))
          plt.plot(x, y)
```

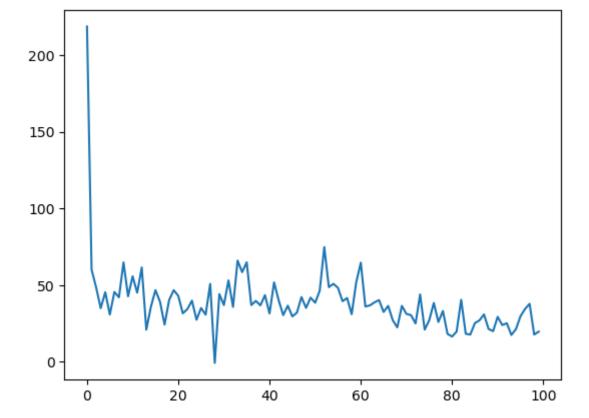
Out[34]: [<matplotlib.lines.Line2D at 0x214f3a59b40>]



No Clipping and GAE

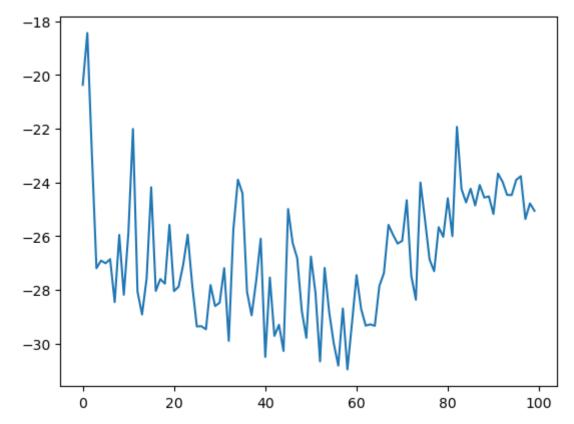
```
In [35]: N = 100 # number of times to collect new trajectories and update actor
         M = 1 # num of trajectories
         max_trajectory_len = 200 # trajectory Length
         batch_size = 25 # size for minibatch
         n_epochs = 30 # number of epochs to optimize loss
         alpha = 0.0001
         hidden_layers = 2
         hidden dims = 8
         gamma = 0.7
         lmbda = 0.9
         clip_value = 0.1
         use_gae = True
         use_clip = False
         total_losses, observations, loss_list, reward_list = ppo(
             N, M, max_trajectory_len, batch_size, alpha, hidden_layers, hidden_dims,
             gamma, lmbda, clip_value, use_gae, use_clip)
```

```
In [36]: tmp = [x for x in range(100)]
In [37]: plt.plot(tmp, np.array([l.cpu().detach() for l in loss_list]))
Out[37]: [<matplotlib.lines.Line2D at 0x214f3a44c70>]
```



In [38]: plt.plot(tmp, np.array([1.cpu().detach() for 1 in reward_list]))

Out[38]: [<matplotlib.lines.Line2D at 0x214f3abddb0>]

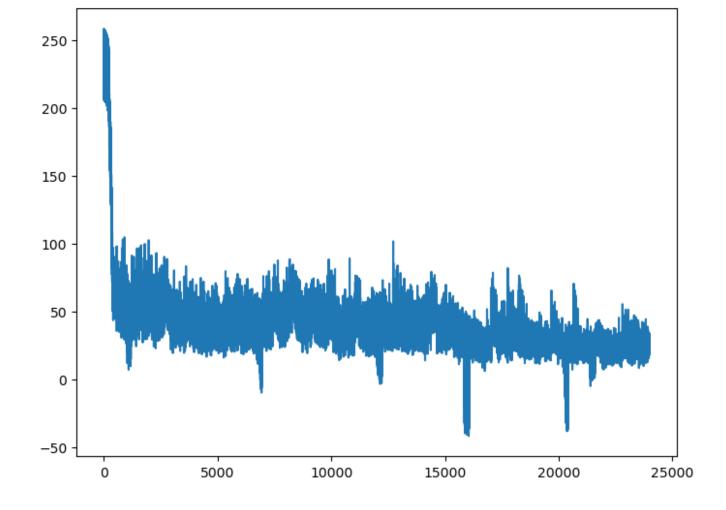


```
In [41]: o = o_old[-10:]
```

```
In [42]: x_ = [i+1 \text{ for } i \text{ in } range(200)]
```

```
In [43]: np.array(o).shape
Out[43]: (10, 200, 3)
In [44]: N = 10
          plt.figure(1, figsize=(20, 12))
          for i in range(N):
               obs = o[i]
               # print(obs)
               theta_ = []
               x_list = []
               y_list = []
               for x,y,v in obs:
                   # print(x, y)
                   theta_.append(v)
                   x_list.append(x)
                   y_list.append(y)
               plt.subplot(N, 3, 3*i+1)
               plt.plot(x_, x_list)
               plt.xlabel('time')
               plt.ylabel('x')
               plt.subplot(N, 3, 3*i+2)
               plt.plot(x_, y_list)
               plt.xlabel('time')
               plt.ylabel('y')
               plt.subplot(N, 3, 3*i+3)
               plt.plot(x_, theta_)
               plt.xlabel('time')
               plt.ylabel('.theta')
            × 0
                                                                                  theta
                                               > 0
                                                                                  0.25
0.00
          × -0.90
                                              > -0.4
                                               -0.5
                                                                                  o.0 theta
          × −0.75
          × -0.90
                                                                                  o.o
            -0.95
                                                                                  theta.
            × 0
                                                               100 125 150 175 200
time
                                                                                                   100 125 150
time
In [45]: len(total_losses)
Out[45]: 24000
In [46]: x = np.arange(len(total_losses))
          y = [float(x) for x in total_losses]
          plt.figure(figsize=(8, 6))
          plt.plot(x, y)
```

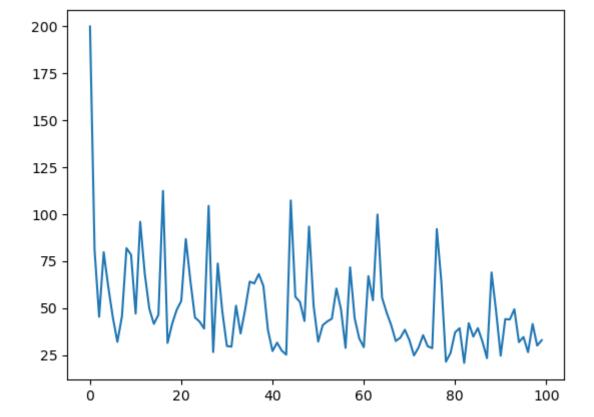
Out[46]: [<matplotlib.lines.Line2D at 0x214f501ec50>]



No Clipping and No GAE

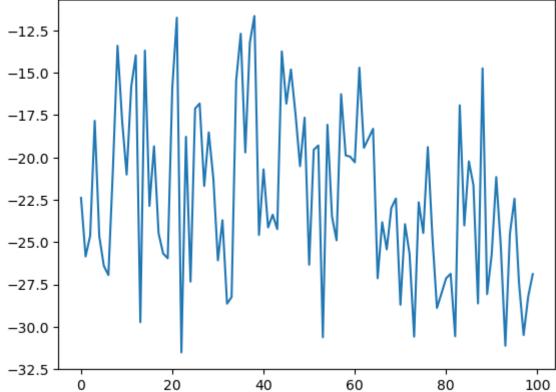
```
In [47]: N = 100 # number of times to collect new trajectories and update actor
         M = 1 # num of trajectories
         max_trajectory_len = 200 # trajectory Length
         batch_size = 25 # size for minibatch
         n_epochs = 30 # number of epochs to optimize loss
         alpha = 0.0001
         hidden_layers = 2
         hidden_dims = 8
         gamma = 0.7
         lmbda = 0.9
         clip_value = 0.1
         use_gae = False
         use_clip = False
         total_losses, observations, loss_list, reward_list = ppo(
             N, M, max_trajectory_len, batch_size, alpha, hidden_layers, hidden_dims,
             gamma, lmbda, clip_value, use_gae, use_clip)
```

```
In [48]: tmp = [x for x in range(100)]
In [49]: plt.plot(tmp, np.array([l.cpu().detach() for l in loss_list]))
Out[49]: [<matplotlib.lines.Line2D at 0x214f60b82b0>]
```



```
In [50]: plt.plot(tmp, np.array([1.cpu().detach() for 1 in reward_list]))
```

Out[50]: [<matplotlib.lines.Line2D at 0x214f6121fc0>]



```
In [55]: np.array(o).shape
Out[55]: (10, 200, 3)
In [56]: N = 10
          plt.figure(1, figsize=(20, 12))
          for i in range(N):
              obs = o[i]
              # print(obs)
              theta_ = []
              x_list = []
              y_list = []
              for x,y,v in obs:
                   # print(x, y)
                   theta_.append(v)
                   x_list.append(x)
                   y_list.append(y)
              plt.subplot(N, 3, 3*i+1)
              plt.plot(x_, x_list)
              plt.xlabel('time')
              plt.ylabel('x')
              plt.subplot(N, 3, 3*i+2)
              plt.plot(x_, y_list)
              plt.xlabel('time')
              plt.ylabel('y')
              plt.subplot(N, 3, 3*i+3)
              plt.plot(x_, theta_)
              plt.xlabel('time')
               plt.ylabel('.theta')
                                              > 0
                                                                                -2.5 -
           -0.5
          × -0.9
                                              > 0.0
                                                                                 theta
o
                                               0
                                                                                   0 -
                                                                                0.0
-2.5
                                              0.5
                                              -0.5
                                                                                 -2.5
                           100
time
                               125 150
                                     175
                                                               100
time
                                                                  125 150 175 200
                                                                                                  100
time
                                                                                                     125 150 175
In [57]: len(total_losses)
Out[57]: 24000
In [58]: x = np.arange(len(total_losses))
          y = [float(x) for x in total_losses]
          plt.figure(figsize=(8, 6))
          plt.plot(x, y)
```

Out[58]: [<matplotlib.lines.Line2D at 0x214f59cf760>]

