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Abstract—This manual is an introduction to control systems based on GATE problems. Links to sample Python codes are available in the text.

Download python codes using

1 STABILITY

1.1 Second order System

2 ROUTH HURWITZ CRITERION

3 COMPENSATORS

4 NYQUIST PLOT

5 GAIN MARGIN

The figure below shows the Bode magnitude and phase plots of a stable transfer function:

$$G(s) = \frac{n_0}{s^3 + d_2 s^2 + d_1 s + d} \quad (5.0.1)$$

Consider the negative unity feedback configuration with gain k in the feed forward path. The closed loop is stable for . The maximum value of k_o is:

Solution:

$$K_g = \frac{1}{|G(j\omega)|} \quad (5.0.2)$$

K_g is the gain margin at the frequency at which phase angle is -180° .

In terms of decibels:

$$K_g \text{ dB} = -20 \log(|G(j\omega)|) \text{ dB} \quad (5.0.3)$$

1. For a stable system, Gain margin at the phase cross-over frequency $> 0 \text{ dB}$.

2. The phase crossover frequency is the frequency at which the phase angle first reaches -180° .

3. The gain margin refers to the amount of gain, which can be increased or decreased

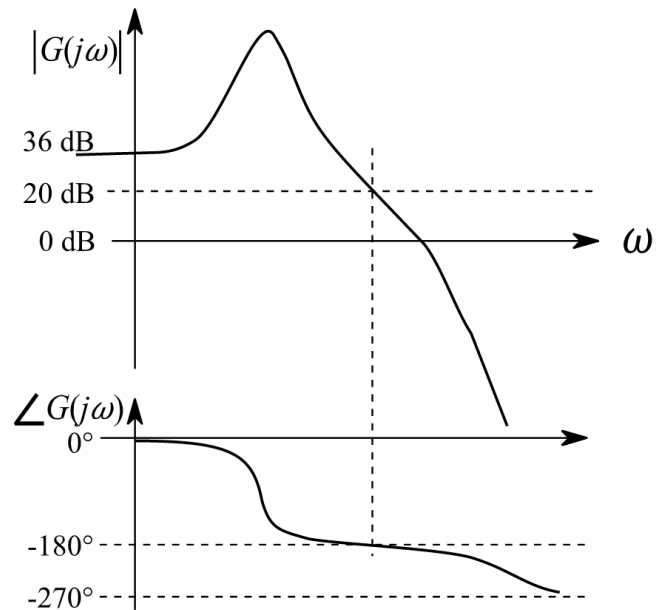


Fig. 5.0.1

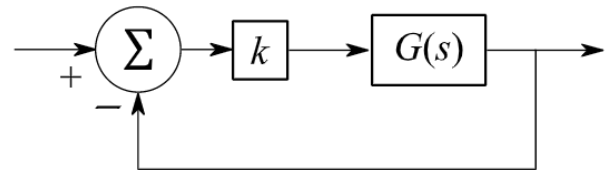


Fig. 5.0.2

without making the system unstable.

4. Gain margin is the factor by which the gain must be multiplied at the phase crossover to have the value 1.

5. The phase crossover frequency is the frequency at which the phase angle first reaches -180° and thus is the point where the Nyquist plot crosses the real axis.

For a stable system, Gain margin at the phase cross-over frequency > 1 .

$G(s)$ is cascaded with k , so,

$$G_1(s) = kG(s) \quad (5.0.4)$$

$$K_g = \frac{1}{|G_1(j\omega_{pc})|} > 1 \quad (5.0.5)$$

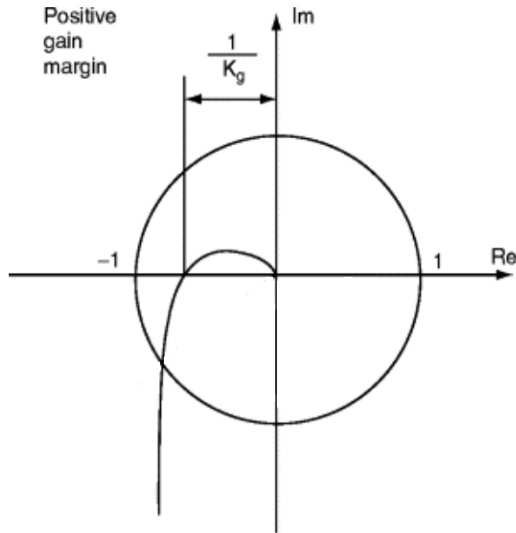


Fig. 5.0.3: nyquist plot of stable transfer function

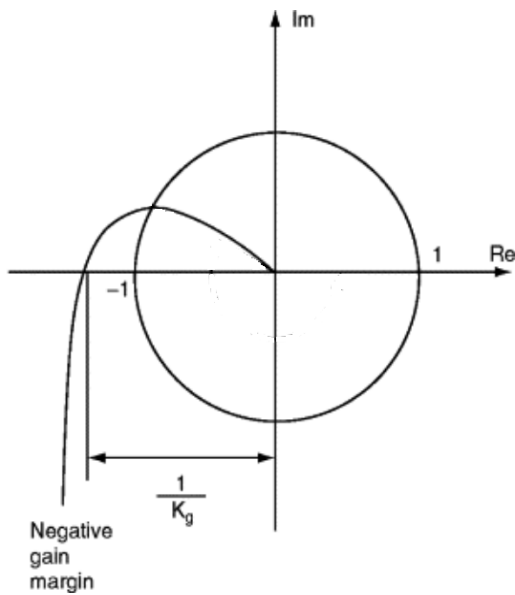


Fig. 5.0.4: nyquist plot of unstable transfer function

$$\Rightarrow K_{g(dB)} = -20\log(|G_1(j\omega_{pc})|) > 0dB \quad (5.0.6)$$

$$\Rightarrow -20\log(|G(j\omega_{pc})k|) > 0dB \quad (5.0.7)$$

$$\Rightarrow -20 - 20\log(|k|) > 0dB \quad (5.0.8)$$

$$\Rightarrow 20\log(k) < -20 \quad (5.0.9)$$

$$\Rightarrow k < 10^{-1} \quad (5.0.10)$$

$$\Rightarrow k_{max} = 0.1 \quad (5.0.11)$$

$$\therefore k_o = 0.1$$