

Introduction to Large Language Models

Week-2 Assignment

Number of questions: 8

Total mark: $6 \times 1 + 2 \times 2 = 10$

Question 1:

Which of the following does **not** directly affect perplexity?

- a. Vocabulary size
- b. Sentence probability
- c. Number of tokens
- d. Sentence length

Answer: a

Question 2:

What is the goal of a probabilistic language model?

- a. Translate sentences
- b. Predict the next word in a sequence
- c. Classify documents
- d. Summarize text

Answer: b

Question 3:

Which equation expresses the chain rule for a 4-word sentence?

- a. $P(w_1, w_2, w_3, w_4) = P(w_1) + P(w_2|w_1) + P(w_3|w_2) + P(w_4|w_3)$
- b. $P(w_1, w_2, w_3, w_4) = P(w_1) \times P(w_2|w_1) \times P(w_3|w_1, w_2) \times P(w_4|w_1, w_2, w_3)$
- c. $P(w_1, w_2, w_3, w_4) = P(w_1) \times P(w_2|w_1) \times P(w_3|w_2) \times P(w_4|w_3)$
- d. $P(w_1, w_2, w_3, w_4) = P(w_4|w_3) \times P(w_3|w_2) \times P(w_2|w_1) \times P(w_1)$

Answer: b

Question 4:

Which assumption allows n-gram models to reduce computation?

- a. Bayes Assumption
- b. Chain Rule
- c. Independence Assumption
- d. Markov Assumption

Answer: d

Question 5:

In a trigram language model, which of the following is a correct example of linear interpolation?

- a. $P(w_i|w_{i-2}, w_{i-1}) = \lambda_1 P(w_i|w_{i-2}, w_{i-1})$
- b. $P(w_i|w_{i-2}, w_{i-1}) = \lambda_1 P(w_i|w_{i-2}, w_{i-1}) + \lambda_2 P(w_i|w_{i-1}) + \lambda_3 P(w_i)$
- c. $P(w_i|w_{i-2}, w_{i-1}) = \max(P(w_i|w_{i-2}, w_{i-1}), P(w_i|w_{i-1}))$
- d. $P(w_i|w_{i-2}, w_{i-1}) = P(w_i)P(w_{i-1})/P(w_{i-2})$

Answer: b

Question 5:

A trigram model is equivalent to which order Markov model?

- a. 3
- b. 2
- c. 1
- d. 4

Answer: b

Question 6:

Which smoothing technique leverages the number of unique contexts a word appears in?

- a. Good-Turing
- b. Add-k
- c. Kneser-Ney
- d. Absolute Discounting

Correct Answer: c

Explanation: Kneser-Ney uses continuation probability which counts the number of unique left contexts.

For Question 4 to 5, consider the following corpus:

<s> the sky is blue </s>

<s> birds fly in the sky </s>

<s> the blue birds sing </s>

QUESTION 4:

Assuming a bi-gram language model, calculate the probability of the sentence:

<s> birds fly in the blue sky </s>

Ignore the unigram probability of $P(<s>)$ in your calculation.

a. $2/37$

b. $1/27$

c. 0

d. $1/36$

Correct Answer: c

Solution:

$P(<s> \text{ birds fly in the blue sky } </s>) =$

$P(<s>) \times P(\text{birds} \mid <s>) \times P(\text{fly} \mid \text{birds}) \times P(\text{in} \mid \text{fly}) \times P(\text{the} \mid \text{in}) \times P(\text{blue} \mid \text{the}) \times P(\text{sky} \mid \text{blue})$
 $\times P(</s> \mid \text{sky})$

From the corpus:

$P(\text{birds} \mid <s>) = \text{Count}(<s> \text{ birds}) / \text{Count}(<s>) = 1 / 3$

$P(\text{fly} \mid \text{birds}) = \text{Count}(\text{birds fly}) / \text{Count}(\text{birds}) = 1 / 2$

$P(\text{in} \mid \text{fly}) = \text{Count}(\text{fly in}) / \text{Count}(\text{fly}) = 1 / 1$

$P(\text{the} \mid \text{in}) = \text{Count}(\text{in the}) / \text{Count}(\text{in}) = 1 / 1$

$P(\text{blue} \mid \text{the}) = \text{Count}(\text{the blue}) / \text{Count}(\text{the}) = 1 / 3$

$P(\text{sky} \mid \text{blue}) = \text{Count}(\text{blue sky}) = 0$

$P(<s> \text{ birds fly in the blue sky } </s>) = 0$

QUESTION 5:

Assuming a bi-gram language model, calculate the perplexity of the sentence:

<s> birds fly in the blue sky </s>

Please do not consider <s> and </s> as words of the sentence.

a. $271/4$

b. $271/5$

c. $91/6$

d. None of these

Correct Answer: d

Solution:

As calculated in the previous question,

$P(<s> \text{ birds fly in the blue sky } </s>) = 0$

Thus, Perplexity = undefined
