

## 1) a) Aggregate method

- ① First insertion taken  $O(1)$  time
- ② Second one taken  $O(1)$  time
- ③ Third one taken  $O(2)$  time
- ④  $k^{\text{th}}$  one taken  $O(2^{k-1})$  time
- ⑤  $n^{\text{th}}$  one taken  $O(2^{k-1})$  time

$$T = O(1) + O(1) + O(2) + O(n) + \dots + O(2^{k-1})$$

$$T = O(2^0) + O(2^1) + O(2^2) + O(2^3) + \dots + O(2^{k-1})$$

$$T = O(n)$$

## b) Accounting method

$O(1) \rightarrow$  for insertion

$O(n) \rightarrow$  for resizing

$$T = n \times O(1) + \frac{n}{2} \times O(n)$$

$$T = O(n) + O\left(\frac{n^2}{2}\right) = O(n^2)$$

$$T_a = \frac{T}{n} = O(n)$$