

Redundant Array of Inexpensive Disks (RAID)

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Chapter 5 Tanenbaum's book

First Commercial Disk Drive



1956

IBM RAMDAC computer included the IBM Model 350 disk storage system

5M (7 bit) characters

50 x 24" platters

Access time = < 1 second

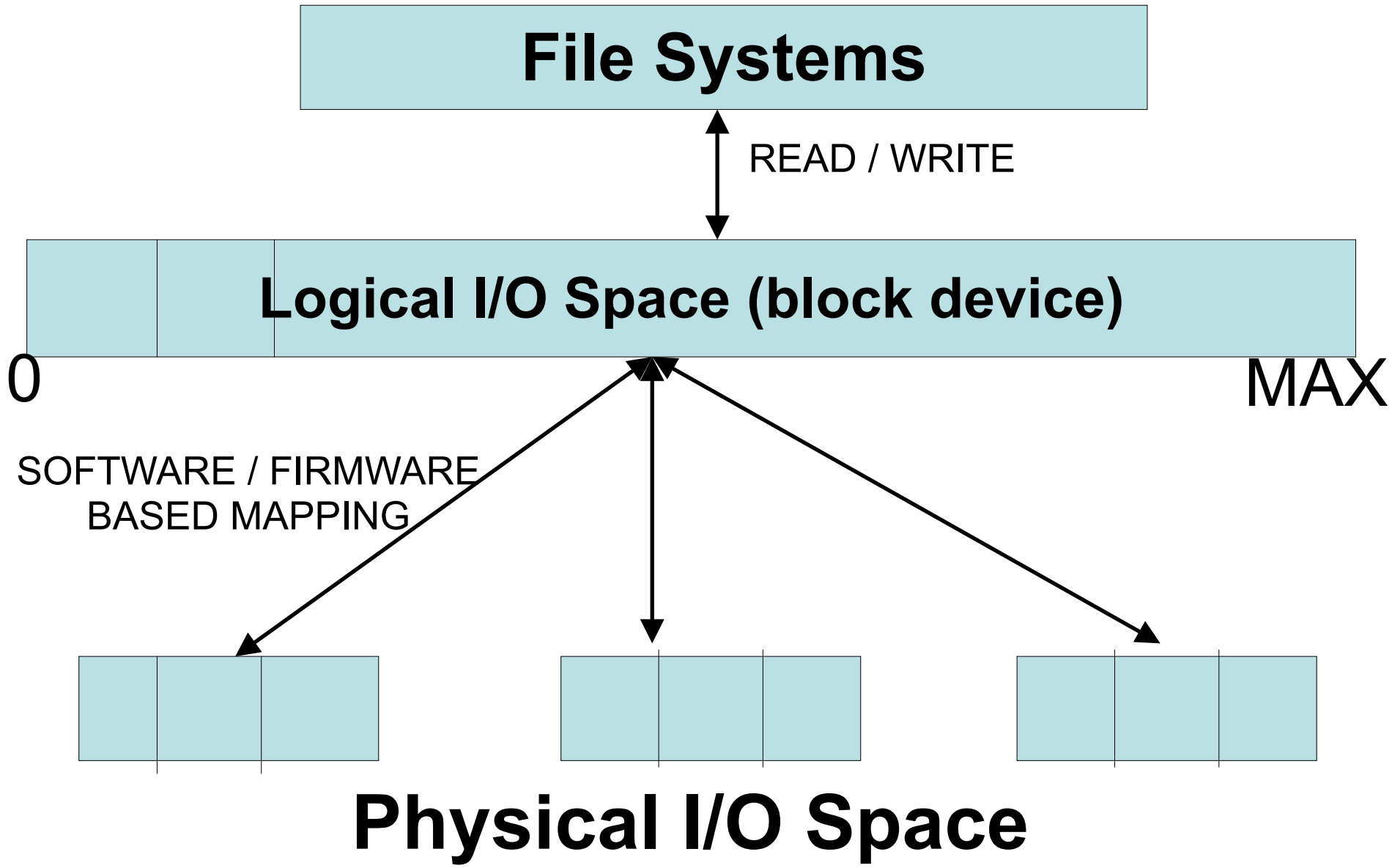
RAID — Original Motivation

- Replacing large and expensive mainframe hard drives (IBM 3310) by several cheaper Winchester disk drives
- Will work but introduces a data reliability problem:
 - Consider Mean Time To Failure (MTTF)
 - Assume MTTF of a disk drive is 30,000 hours
 - MTTF for a set of n drives is $30,000/n$
 - $n = 10$ means MTTF of 3,000 hours

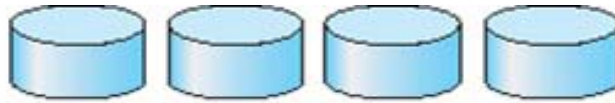
RAID — Today's Motivation

- “Cheap” hard drives are now big enough for most applications
- We use RAID today for
 - Increasing disk throughput by allowing parallel access
 - Eliminating the need to make disk backups
 - Disks are too big to be backed up efficiently

Logical-to-Physical I/O Address Space Mapping



Several Levels of RAID



(a) RAID 0: non-redundant striping.



(b) RAID 1: mirrored disks.



(c) RAID 2: memory-style error-correcting codes.



(d) RAID 3: bit-interleaved parity.



(e) RAID 4: block-interleaved parity.



(f) RAID 5: block-interleaved distributed parity.

RAID 0

- Striping
 - Spread the data over multiple disk drives
- No fault tolerance
- But, much better I/O throughput
 - Number of I/O operations per second

DISK 0	DISK 1	DISK 2	DISK 3
BLOCK 0	BLOCK 1	BLOCK 2	BLOCK 3
BLOCK 4	BLOCK 5	BLOCK 6	BLOCK 7
BLOCK 8	BLOCK 9	BLOCK 10	BLOCK 11
BLOCK 12	BLOCK 13	BLOCK 14	BLOCK 15

RAID 1

- Mirroring
 - Two copies of each disk block
- Advantage
 - Simple to implement
 - Fault-tolerant
- Disadvantage
 - Requires twice the disk capacity

DISK 0	DISK 1	MIRROR 0	MIRROR 1
BLOCK 0	BLOCK 1	BLOCK 0	BLOCK 1
BLOCK 2	BLOCK 3	BLOCK 2	BLOCK 3
BLOCK 4	BLOCK 5	BLOCK 4	BLOCK 5
BLOCK 6	BLOCK 7	BLOCK 6	BLOCK 7

RAID 2

- Use an **error (detection + correction)** code instead of duplicating the data blocks
- Meant for disks that don't have built-in error detection.
- Modern disks support built-in error detection, so this level is mostly unused.

DISK 0	DISK 1	DISK 2	PARITY 1	PARITY 2
BLOCK 0	BLOCK 1	BLOCK 2	F(0,1,2)	
BLOCK 3	BLOCK 4	BLOCK 5	F(3,4,5)	
BLOCK 6	BLOCK 7	BLOCK 8	F(6,7,8)	
BLOCK 9	BLOCK 10	BLOCK 11	F(9,10,11)	

F = FUNCTION FOR ERROR DETECTION + CORRECTION

XOR Primer

- Truth Table
 - $0 \text{ XOR } 0 = 0$
 - $0 \text{ XOR } 1 = 1$
 - $1 \text{ XOR } 0 = 1$
 - $1 \text{ XOR } 1 = 0$
- Associative and commutative
- Lost any one bit? XOR the rest to recover.
 - If $1 \text{ XOR (lost bit)} = 0$
 - then lost bit = $1 \text{ XOR } 0 = 1$
- Extends to any number of data bits
 - If $1 \text{ XOR (lost bit) XOR } 1 = 0$
 - then lost bit = $1 \text{ XOR } 1 \text{ XOR } 0 = 0$

RAID 3

- N+1 disk drives: N data drives + 1 parity drive
- Data Block $b[k]$ partitioned into N fragments $b[k,1]$, $b[k,2]$, ... $b[k,N]$
- Parity drive contains **XOR (exclusive or)** of these N fragments
 - $p[k] = b[k,1] \text{ XOR } b[k,2] \text{ XOR } \dots \text{ XOR } b[k,N]$
- Upon a failure, reconstruct the lost fragments by XOR of corresponding fragments from remaining drives.
 - $b[k,i] = p[k] \text{ XOR } b[k,1] \text{ XOR } \dots \text{ XOR } b[k,i-1] \text{ XOR } b[k,i+1] \dots \text{ XOR } b[k,N]$
- Simple to implement in firmware/software
- Permits only one I/O operation at a time over entire array

DISK 0	DISK 1	DISK 2	PARITY
BLOCK [0,1]	BLOCK [0,2]	BLOCK [0,3]	PARITY 0
BLOCK [1,1]	BLOCK [1,2]	BLOCK [1,3]	PARITY 1
BLOCK [2,1]	BLOCK [2,2]	BLOCK [2,3]	PARITY 2
BLOCK [3,1]	BLOCK [3,2]	BLOCK [3,3]	PARITY 3

RAID 4

- Requires N+1 disk drives (as in RAID 3)
 - N data drives + 1 Parity drive
- Data striped at block granularity (as in RAID 0)
 - Disk 1 has block 1, disk 2 has block 2, and so on.
- Parity drive contains **exclusive or** of the N blocks in stripe
 - $p[k] = b[Nk] \text{ XOR } b[Nk+1] \text{ XOR } \dots \text{ XOR } b[Nk+N-1]$
- Multiple Read I/O operations can be processed in parallel
- But how about parallel writes I/O operations?

DISK 0	DISK 1	DISK 2	PARITY
BLOCK 0	BLOCK 1	BLOCK 2	PARITY 0
BLOCK 3	BLOCK 4	BLOCK 5	PARITY 1
BLOCK 6	BLOCK 7	BLOCK 8	PARITY 2
BLOCK 9	BLOCK 10	BLOCK 11	PARITY 3

RAID 5

- Single parity drive of RAID-4 is involved in every write
 - Will limit write parallelism
 - Exercises one parity disk more than others
- Solution in RAID-5
 - Distribute the parity blocks among all $N+1$ drives
- Up to $N/2$ parallel writes

DISK 0	DISK 1	DISK 2	DISK 3
BLOCK 0	BLOCK 1	BLOCK 2	PARITY 0
BLOCK 3	BLOCK 4	PARITY 1	BLOCK 5
BLOCK 6	PARITY 2	BLOCK 7	BLOCK 8
PARITY 3	BLOCK 9	BLOCK 10	BLOCK 11

The write problem

- What happens when we want to update a single block?
 - Block belongs to a stripe
- Problem: How do we compute the new parity?

The write problem

- Every time a block is updated, the parity must be updated as well.
- Assume we want to update the k th block $b_{k_{old}}$ to $b_{k_{new}}$
- Before writing $b_{k_{new}}$
 - $p_{old} = b_{0_{old}} \mathbf{XOR} b_{1_{old}} \mathbf{XOR} \dots b_{k_{old}} \dots \mathbf{XOR} b_{N_{old}}$
- After writing $b_{k_{new}}$, we can naively recompute p_{new} as follows
 - $p_{new} = b_{0_{old}} \mathbf{XOR} b_{1_{old}} \mathbf{XOR} \dots b_{k_{new}} \dots \mathbf{XOR} b_{N_{old}}$
- Naive solution incurs high overhead
 - N-1 reads
 - Read all old data blocks except the block being written ($b_{k_{new}}$)
 - 2 writes
 - $b_{k_{new}}$ and p_{new}

Second (smarter) solution

- Assume we want to update the kth block bk_{old} to bk_{new}
- Before writing bk_{new}

$$(A) \text{ } p_{old} = b0_{old} \text{ XOR } b1_{old} \text{ XOR } \dots \text{ } bk_{old} \text{ XOR } \dots \text{ XOR } bN_{old}$$

- Moving bk_{old} to left hand side

$$(B) p_{old} \text{ XOR } bk_{old} = b0_{old} \text{ XOR } b1_{old} \text{ XOR } \dots \text{ XOR } bN_{old}$$

- Naive solution to compute p_{new}

$$(C) p_{new} = b0_{old} \text{ XOR } b1_{old} \text{ XOR } \dots \text{ } bk_{new} \text{ XOR } \dots \text{ XOR } bN_{old}$$

- Moving bk_{new} to left hand side

$$(D) p_{new} \text{ XOR } bk_{new} = b0_{old} \text{ XOR } b1_{old} \text{ XOR } \dots \text{ XOR } bN_{old}$$

- Combining (B) and (D)

$$(E) p_{new} \text{ XOR } bk_{new} = p_{old} \text{ XOR } bk_{old}$$

- Smarter solution: moving bk_{new} to right hand side

- $p_{new} = bk_{new} \text{ XOR } p_{old} \text{ XOR } bk_{old}$

- Smarter Solution requires

- 2 reads
 - bk_{old} and p_{old}
 - Or just one read of p_{old} if bk_{old} was read into memory earlier
- 2 writes
 - bk_{new} and p_{new}

Comparison

	RAID 0 (N disks)	RAID 1 (N disks)	RAID 2 (N+1) disks	RAID 3 (N+1) disks	RAID 4 (N+1) disks	RAID 5 (N+1) disks
Fault-tolerance	None	All 1-disk and most 2-disk failures	1-disk failure with error detection and correction	1-disk failure with Error Correction	1-disk failure with Error Correction	1-disk failure with Error Correction
Max. READ Parallelism	N	N	N	1 (none)	N	N+1
Max. WRITE Parallelism	N	N/2	1 (none)	1 (none)	1 (none)	(N+1)/2
Space Overhead	0%	100%	$(k/N) \times 100\%$ for K parity disks	$(1/N) \times 100\%$	$(1/N) \times 100\%$	$(1/N) \times 100\%$

Conclusion

- RAID original purpose was to take advantage of commodity drives that were smaller and cheaper than conventional disk drives
 - Replace a single large drive by an array of smaller drives
- Nobody does that anymore!
- Today: Main purpose of RAID is to build **fault-tolerant** storage systems that do not need backups and deliver **high throughput**.
- Low cost of disk drives makes RAID-1 attractive for small installations
 - We have now very cheap RAID controllers
- Otherwise prefer
 - RAID-3 for simplicity
 - RAID-5 for higher parallelism
- Often combined with NVRAM to improve write performance