

# Assignment - 4

Date. \_\_\_\_\_  
Page No. \_\_\_\_\_

Q → What is MST ? applications.

- A spanning tree which visits all the nodes
- The sum of the weights is as minimum as possible plus it should not form cycles
- 8. ~~no. of edges = no. of nodes - 1.~~

## Applications:

1. Design Local area network
2. In constructing highways or railways
3. laying pipelines
4. Telecommunication network

Q2.

Kruskal

$$O(V^2) \text{ if } E \gg V$$

Prim

$$O(V^2)$$

Dijkstra's

$$O(V+E)$$

Bellman-Ford.

$$O(VE)$$

T.C

S.C

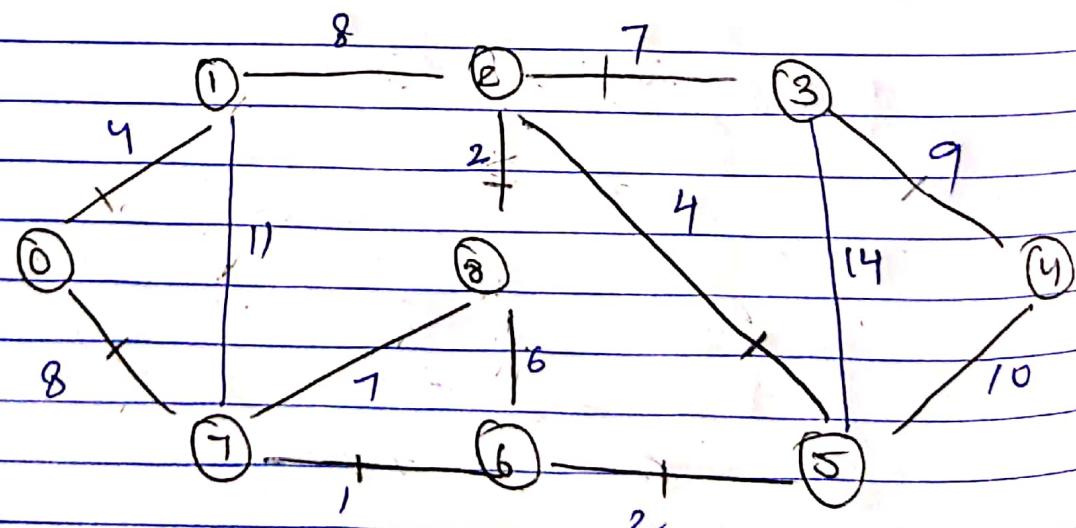
~~$O(V \log E)$~~

~~$O(E \log V + E)$~~

$O(V+E)$

$O(V)$

Q3.)



8 edges

edges cut

(7, 6)

1.

6, 5

2.

2, 8

2.

0, 1

4

2, 5

4

6, 8

6 x

2, 3

7

7, 8

7 x

1, 2

8

7, 0

8 x

3, 4

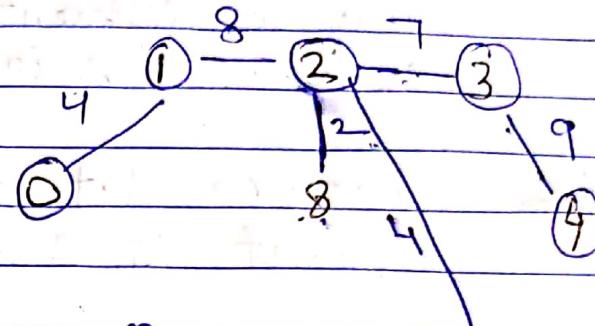
9

5, 4

16 x

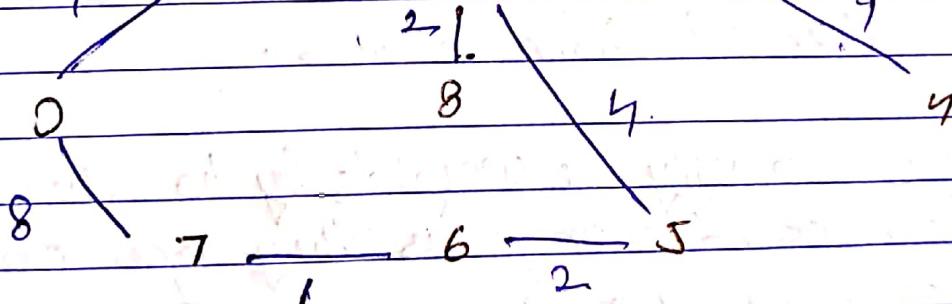
3, 5

14 x



37

Points - 4 1 2 3



31

In Prims we take a minimum cost edge then always select minimum cost edge which is connected to already connected vertices.

Q4.) The shortest path may change bcoz there may be different no. of edges in different paths from s to t.

For ex: let shortest path ~~may~~ be of weight 15 & has 5 edges.

let another path with 2 edges and total weight = 25.

After increasing weights by 10.

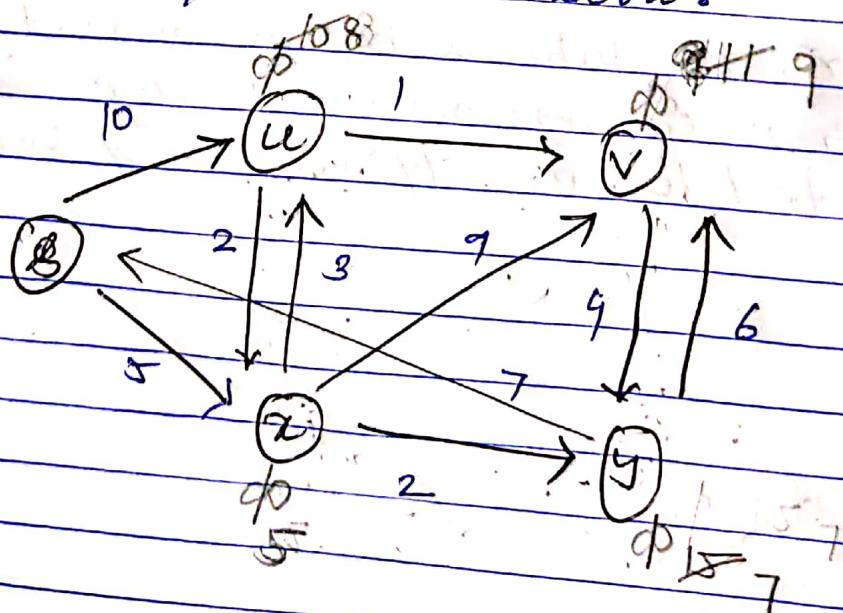
for 1st option weight becomes  $15 + (5 \times 10)$   
 $= 65$

for 2nd weight becomes  $25 + (2 \times 10)$   
 $= 45$

∴ the shortest path changes as weight got changed. from previous.

i) If we multiply the weights by 10, the shortest path doesn't change as they are multiplied or increased in same amount.

Q5.)



Dijkstra's node shortest path from src node

u	8
x	5
v	9
y	7

Bellman-Ford  
edges

(s, u) (s, x) (u, v) (v, y) (x, y) (~~(x, u)~~) (~~(x, v)~~)

u	8	Answer same -
x	5	
v	9	
y	7	