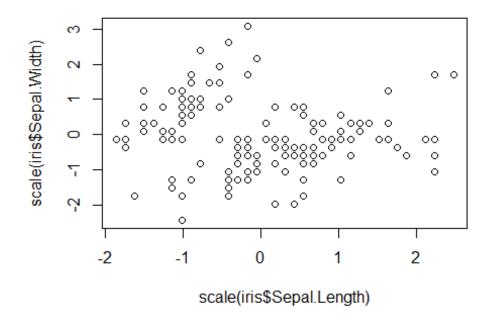
# **Clustering Flower Species and Principle Component Analysis**

### **Load and Explore Data**

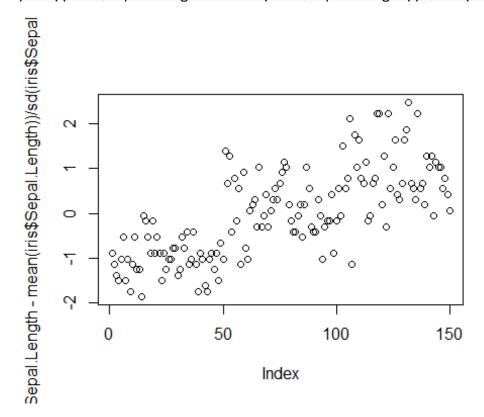
```
data(iris)
head(iris, 30)
      Sepal.Length Sepal.Width Petal.Length Petal.Width Species
## 1
                5.1
                            3.5
                                          1.4
                                                       0.2 setosa
                                                      0.2 setosa
## 2
                4.9
                            3.0
                                          1.4
## 3
                            3.2
                                          1.3
                4.7
                                                       0.2 setosa
## 4
                            3.1
                                          1.5
                                                       0.2 setosa
                4.6
                                                      0.2 setosa
## 5
                5.0
                            3.6
                                          1.4
## 6
                5.4
                            3.9
                                          1.7
                                                      0.4 setosa
## 7
                4.6
                            3.4
                                          1.4
                                                      0.3 setosa
## 8
                5.0
                            3.4
                                          1.5
                                                      0.2 setosa
## 9
                4.4
                            2.9
                                          1.4
                                                       0.2 setosa
                                                      0.1 setosa
## 10
                4.9
                                          1.5
                            3.1
## 11
                5.4
                                          1.5
                                                      0.2 setosa
                            3.7
## 12
                4.8
                                          1.6
                                                       0.2 setosa
                            3.4
## 13
                4.8
                            3.0
                                          1.4
                                                      0.1 setosa
                                                      0.1 setosa
## 14
                4.3
                            3.0
                                          1.1
                5.8
                                                      0.2 setosa
## 15
                            4.0
                                          1.2
                                          1.5
## 16
                5.7
                            4.4
                                                       0.4 setosa
## 17
                5.4
                            3.9
                                          1.3
                                                       0.4 setosa
## 18
                5.1
                            3.5
                                          1.4
                                                       0.3 setosa
                                          1.7
## 19
                5.7
                            3.8
                                                       0.3 setosa
## 20
                5.1
                            3.8
                                          1.5
                                                      0.3 setosa
                                          1.7
                                                       0.2 setosa
## 21
                5.4
                            3.4
                                                       0.4 setosa
## 22
                5.1
                            3.7
                                          1.5
## 23
                4.6
                            3.6
                                          1.0
                                                       0.2 setosa
## 24
                            3.3
                                          1.7
                                                      0.5 setosa
                5.1
## 25
                4.8
                            3.4
                                          1.9
                                                      0.2 setosa
## 26
                5.0
                            3.0
                                          1.6
                                                       0.2 setosa
## 27
                5.0
                            3.4
                                          1.6
                                                       0.4 setosa
                                                      0.2 setosa
## 28
                5.2
                            3.5
                                          1.5
## 29
                5.2
                            3.4
                                          1.4
                                                      0.2 setosa
## 30
               4.7
                            3.2
                                          1.6
                                                       0.2 setosa
```

# **Relation between Sepal Length and Sepal Width**

plot(scale(iris\$Sepal.Length), scale(iris\$Sepal.Width))



plot((iris\$Sepal.Length - mean(iris\$Sepal.Length)) / sd(iris\$Sepal.Length))



#### **Applying Pricipal Component Analysis (PCA) on Independent Variables**

```
iris x \leftarrow iris[,1:4]
iris.pca.rawdata <- prcomp(iris_x, scale = FALSE, center= FALSE)</pre>
iris.pca.rawdata
## Standard deviations (1, .., p=4):
## [1] 7.8613425 1.4550406 0.2835305 0.1544110
## Rotation (n \times k) = (4 \times 4):
                                              PC3
                                                          PC4
                       PC1
                                  PC2
## Sepal.Length -0.7511082 0.2841749 0.50215472 0.3208143
## Sepal.Width -0.3800862 0.5467445 -0.67524332 -0.3172561
## Petal.Length -0.5130089 -0.7086646 -0.05916621 -0.4807451
## Petal.Width -0.1679075 -0.3436708 -0.53701625 0.7518717
summary(iris.pca.rawdata)
## Importance of components:
                                     PC2
                                             PC3
                                                      PC4
##
                             PC1
## Standard deviation
                          7.8613 1.45504 0.28353 0.15441
## Proportion of Variance 0.9653 0.03307 0.00126 0.00037
## Cumulative Proportion 0.9653 0.99837 0.99963 1.00000
str(iris.pca.rawdata)
## List of 5
## $ sdev : num [1:4] 7.861 1.455 0.284 0.154
## $ rotation: num [1:4, 1:4] -0.751 -0.38 -0.513 -0.168 0.284 ...
     ... attr(*, "dimnames")=List of 2
     ....$ : chr [1:4] "Sepal.Length" "Sepal.Width" "Petal.Length"
"Petal.Width"
    .. ..$ : chr [1:4] "PC1" "PC2" "PC3" "PC4"
## $ center : logi FALSE
## $ scale : logi FALSE
              : num [1:150, 1:4] -5.91 -5.57 -5.45 -5.44 -5.88 ...
## $ x
    ... attr(*, "dimnames")=List of 2
##
    .. ..$ : NULL
## ....$ : chr [1:4] "PC1" "PC2" "PC3" "PC4"
## - attr(*, "class")= chr "prcomp"
```

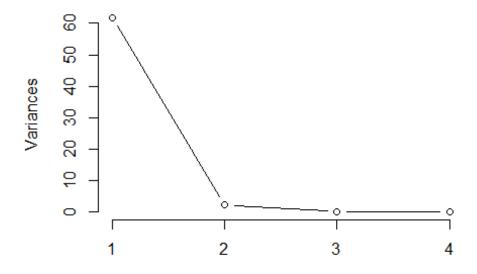
#### Normalize the Data

```
iris.pca.normaldata <- prcomp(iris_x, scale = TRUE, center= TRUE)</pre>
iris.pca.normaldata
## Standard deviations (1, .., p=4):
## [1] 1.7083611 0.9560494 0.3830886 0.1439265
##
## Rotation (n \times k) = (4 \times 4):
                                              PC3
##
                       PC1
                                   PC2
## Sepal.Length 0.5210659 -0.37741762 0.7195664 0.2612863
## Sepal.Width -0.2693474 -0.92329566 -0.2443818 -0.1235096
## Petal.Length 0.5804131 -0.02449161 -0.1421264 -0.8014492
                0.5648565 -0.06694199 -0.6342727 0.5235971
## Petal.Width
summary(iris.pca.normaldata)
## Importance of components:
                             PC1
                                    PC2
                                            PC3
                                                    PC4
## Standard deviation
                          1.7084 0.9560 0.38309 0.14393
## Proportion of Variance 0.7296 0.2285 0.03669 0.00518
## Cumulative Proportion 0.7296 0.9581 0.99482 1.00000
str(iris.pca.normaldata)
## List of 5
## $ sdev
            : num [1:4] 1.708 0.956 0.383 0.144
## $ rotation: num [1:4, 1:4] 0.521 -0.269 0.58 0.565 -0.377 ...
     ... attr(*, "dimnames")=List of 2
##
     ....$ : chr [1:4] "Sepal.Length" "Sepal.Width" "Petal.Length"
"Petal.Width"
   ....$ : chr [1:4] "PC1" "PC2" "PC3" "PC4"
   $ center : Named num [1:4] 5.84 3.06 3.76 1.2
## ..- attr(*, "names")= chr [1:4] "Sepal.Length" "Sepal.Width"
"Petal.Length" "Petal.Width"
            : Named num [1:4] 0.828 0.436 1.765 0.762
## $ scale
     ... attr(*, "names")= chr [1:4] "Sepal.Length" "Sepal.Width"
"Petal.Length" "Petal.Width"
## $ x
            : num [1:150, 1:4] -2.26 -2.07 -2.36 -2.29 -2.38 ...
   ... attr(*, "dimnames")=List of 2
##
    .. ..$ : NULL
## ....$ : chr [1:4] "PC1" "PC2" "PC3" "PC4"
## - attr(*, "class")= chr "prcomp"
```

## **Variances of Components (Both Raw vs Normalized)**

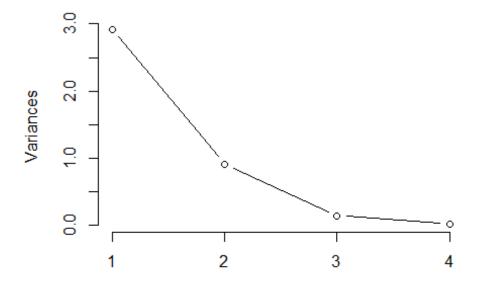
plot(iris.pca.rawdata, type = "l", main='with data normalization')

### with data normalization



plot(iris.pca.normaldata, type = "l", main='with data normalization')

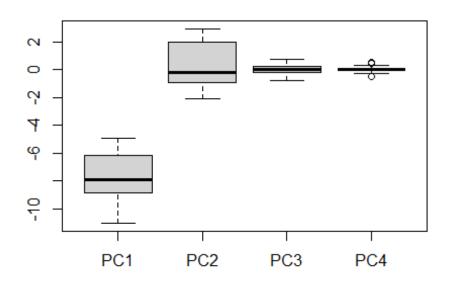
### with data normalization



# **Comparing Boxplots of Raw vs Normal Datasets**

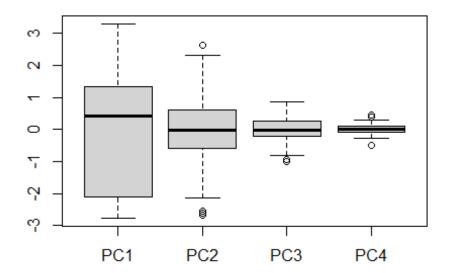
boxplot(iris.pca.rawdata\$x, main='Raw Data Transformation')

### **Raw Data Transformation**



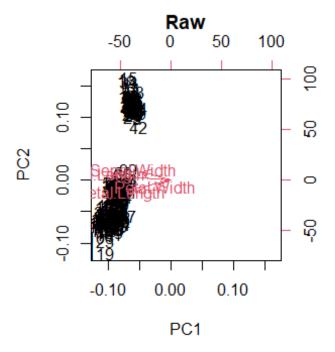
boxplot(iris.pca.normaldata\$x, main='Normal Data Transformation')

### **Normal Data Transformation**

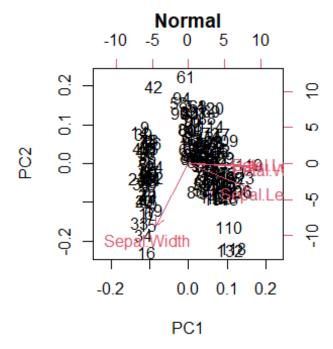


# **2-D Graph of PCA Components**

biplot(iris.pca.rawdata, choices = 1:2, main='Raw')



biplot(iris.pca.normaldata, choices = 1:2, main='Normal')



#### **Clustering the Species in Groups**

```
iris.pca.normaldata$x
##
                                            PC3
                                                         PC4
                  PC1
                               PC2
##
     [1,] -2.25714118 -0.478423832 0.127279624
                                                 0.024087508
##
     [2,] -2.07401302
                       0.671882687
                                    0.233825517
                                                 0.102662845
##
                       0.340766425 -0.044053900
     [3,] -2.35633511
                                                 0.028282305
##
     [4,] -2.29170679
                       0.595399863 -0.090985297 -0.065735340
##
     [5,] -2.38186270 -0.644675659 -0.015685647 -0.035802870
##
     [6,] -2.06870061 -1.484205297 -0.026878250 0.006586116
##
     [7,] -2.43586845 -0.047485118 -0.334350297 -0.036652767
##
     [8,] -2.22539189 -0.222403002 0.088399352 -0.024529919
     [9,] -2.32684533 1.111603700 -0.144592465 -0.026769540
##
##
    [10,] -2.17703491  0.467447569  0.252918268  -0.039766068
    [11,] -2.15907699 -1.040205867
                                    0.267784001 0.016675503
##
    [12,] -2.31836413 -0.132633999 -0.093446191 -0.133037725
##
##
    [13,] -2.21104370 0.726243183 0.230140246 0.002416941
##
    [14,] -2.62430902  0.958296347 -0.180192423 -0.019151375
##
    [15,] -2.19139921 -1.853846555 0.471322025
                                                 0.194081578
##
    [16,] -2.25466121 -2.677315230 -0.030424684
                                                 0.050365010
##
    [17,] -2.20021676 -1.478655729 0.005326251
                                                 0.188186988
##
    [18,] -2.18303613 -0.487206131 0.044067686
                                                 0.092779618
                                    0.373093377
##
    [19,] -1.89223284 -1.400327567
                                                 0.060891973
##
    [20,] -2.33554476 -1.124083597 -0.132187626 -0.037630354
##
    [21,] -1.90793125 -0.407490576
                                   0.419885937
                                                 0.010884821
##
    [22,] -2.19964383 -0.921035871 -0.159331502
                                                 0.059398340
    [23,] -2.76508142 -0.456813301 -0.331069982
##
                                                 0.019582826
##
    [24,] -1.81259716 -0.085272854 -0.034373442
                                                 0.150636353
##
    [25,] -2.21972701 -0.136796175 -0.117599566 -0.269238379
##
                                   0.304620475
    [26,] -1.94532930 0.623529705
                                                 0.043416203
##
    [27,] -2.04430277 -0.241354991 -0.086075649
                                                 0.067454082
##
    [28,] -2.16133650 -0.525389422 0.206125707
                                                 0.010241084
##
    [29,] -2.13241965 -0.312172005
                                    0.270244895
                                                 0.083977887
##
    [30,] -2.25769799  0.336604248  -0.068207276  -0.107918349
##
    [31,] -2.13297647  0.502856075  0.074757996  -0.048027970
##
    [32,] -1.82547925 -0.422280389 0.269564311
                                                0.239069476
##
    [33,] -2.60621687 -1.787587272 -0.047070727 -0.228470534
    [34,] -2.43800983 -2.143546796
##
                                   0.082392024 -0.048053409
##
    [35,] -2.10292986 0.458665270
                                   0.169706329
                                                 0.028926042
##
    [36,] -2.20043723 0.205419224 0.224688852
                                                 0.168343905
##
    [37,] -2.03831765 -0.659349230
                                    0.482919584
                                                 0.195702902
##
    [38,] -2.51889339 -0.590315163 -0.019370918 -0.136048774
##
    [39,] -2.42152026  0.901161067  -0.192609402  -0.009705907
##
    [40,] -2.16246625 -0.267981199 0.175296561 0.007023875
##
    [41,] -2.27884081 -0.440240541 -0.034778398
                                                 0.106626042
##
    [42,] -1.85191836 2.329610745 0.203552303
                                                 0.288896090
##
    [43,] -2.54511203  0.477501017 -0.304745527 -0.066379077
    [44,] -1.95788857 -0.470749613 -0.308567588 0.176501717
   [45,] -2.12992356 -1.138415464 -0.247604064 -0.150539117
##
  [46,] -2.06283361 0.708678586 0.063716370 0.139801160
```

```
##
    [47,] -2.37677076 -1.116688691 -0.057026813 -0.151722682
##
    [48,] -2.38638171  0.384957230  -0.139002234  -0.048671707
##
    [49,] -2.22200263 -0.994627669
                                     0.180886792 -0.014878291
##
    [50,] -2.19647504 -0.009185585
                                     0.152518539
                                                   0.049206884
    [51,]
##
           1.09810244 -0.860091033
                                     0.682300393
                                                   0.034717469
##
    [52,]
           0.72889556 -0.592629362
                                     0.093807452
                                                   0.004887251
##
    [53,]
           1.23683580 -0.614239894
                                     0.552157058
                                                   0.009391933
##
    [54,]
           0.40612251
                       1.748546197
                                     0.023024633
                                                   0.065549239
##
    [55,]
           1.07188379
                        0.207725147
                                     0.396925784
                                                   0.104387166
    [56,]
                        0.591302717 -0.123776885 -0.240027187
##
           0.38738955
##
    [57,]
           0.74403715 -0.770438272 -0.148472007 -0.077111455
##
    [58,] -0.48569562
                       1.846243998 -0.248432992 -0.040384912
##
                                     0.594178807 -0.029779844
    [59,]
           0.92480346 -0.032118478
##
    [60,]
           0.01138804
                        1.030565784 -0.537100055 -0.028366154
                        2.645211115
                                     0.046634215
                                                   0.013714785
##
    [61,] -0.10982834
##
           0.43922201
                        0.063083852 -0.204389093
                                                   0.039992104
    [62,]
##
    [63,]
           0.56023148
                        1.758832129
                                     0.763214554
                                                   0.045578465
##
    [64,]
           0.71715934
                        0.185602819
                                     0.068429700 -0.164256922
##
    [65,]
          -0.03324333
                        0.437537419 -0.194282030
                                                  0.108684396
##
           0.87248429 -0.507364239
                                     0.501830204
                                                   0.104593326
    [66,]
                        0.195656268 -0.489234095 -0.190869932
##
    [67,]
           0.34908221
##
           0.15827980
                        0.789451008
                                     0.301028700 -0.204612265
    [68,]
##
    [69,]
           1.22100316
                        1.616827281
                                     0.480693656 0.225145511
##
                        1.298259939
                                     0.172260719 -0.051554138
    [70,]
           0.16436725
##
           0.73521959 -0.395247446 -0.614467782 -0.083006045
    [71,]
##
    [72,]
           0.47469691
                        0.415926887
                                     0.264067576
                                                  0.113189079
##
                        0.930209441
    [73,]
           1.23005729
                                     0.367182178 -0.009911322
##
    [74,]
           0.63074514
                        0.414997441
                                     0.290921638 -0.273304557
##
    [75,]
                        0.063200094
                                     0.444537765
                                                   0.043313222
           0.70031506
                                     0.471001057
##
           0.87135454 - 0.249956017
                                                   0.101376117
    [76,]
##
    [77,]
           1.25231375
                        0.076998069
                                     0.724727099
                                                   0.039556002
##
    [78,]
           1.35386953 -0.330205463
                                     0.259955701
                                                   0.066604931
##
    [79,]
           0.66258066
                        0.225173502 -0.085577197 -0.036318171
##
    [80,] -0.04012419
                        1.055183583
                                     0.318506304 0.064571834
##
    [81,]
           0.13035846
                        1.557055553
                                     0.149482697 -0.009371129
##
    [82,]
           0.02337438
                        1.567225244
                                     0.240745761 -0.032663020
##
    [83,]
           0.24073180
                        0.774661195
                                     0.150707074 0.023572390
                        0.631726901 -0.104959762 -0.183354200
##
    [84,]
           1.05755171
##
    [85,]
           0.22323093
                        0.286812663 -0.663028512 -0.253977520
##
    [86,]
           0.42770626 -0.842758920 -0.449129446 -0.109308985
##
           1.04522645 -0.520308714
                                     0.394464890 0.037084781
    [87,]
##
    [88,]
           1.04104379
                        1.378371048
                                     0.685997804
                                                   0.136378719
##
    [89,]
           0.06935597
                        0.218770433 -0.290605718 -0.146653279
##
    [90,]
           0.28253073
                        1.324886147 -0.089111491 0.008876070
##
    [91,]
           0.27814596
                        1.116288852 -0.094172116 -0.269753497
##
    [92,]
           0.62248441 -0.024839814
                                     0.020412763 -0.147193289
##
                        0.985103828
                                     0.198724011 0.006508757
    [93,]
           0.33540673
                        2.012495825 -0.105467721 0.019505467
##
    [94,] -0.36097409
##
    [95,]
           0.28762268
                        0.852873116 -0.130452657 -0.107043742
    [96,] 0.09105561
                       0.180587142 -0.128547696 -0.229191812
```

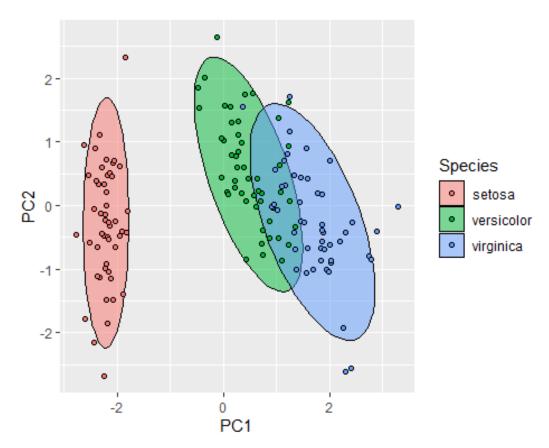
```
##
    [97,]
           0.22695654
                       0.383634868 -0.155691572 -0.132163118
##
    [98,]
           0.57446378
                       0.154356489 0.270743347 -0.019794366
   [99,] -0.44617230
                       1.538637456 -0.189765199 0.199278855
##
## [100,]
           0.25587339
                       0.596852285 -0.091572385 -0.058426315
## [101,]
           1.83841002 -0.867515056 -1.002044077 -0.049085303
## [102,]
           1.15401555
                       0.696536401 -0.528389994 -0.040385459
## [103,]
           2.19790361 -0.560133976 0.202236658 0.058986583
## [104,]
           1.43534213
                      0.046830701 -0.163083761 -0.234982858
## [105,]
           1.86157577 -0.294059697 -0.394307408 -0.016243853
## [106,]
           2.74268509 -0.797736709
                                   0.580364827 -0.101045973
## [107,]
           0.36579225
                      1.556289178 -0.983598122 -0.132679346
## [108,]
           2.29475181 -0.418663020
                                    0.649530452 -0.237246445
                                   0.392675073 -0.086221779
                       0.709063226
## [109,]
           1.99998633
## [110,]
           2.25223216 -1.914596301 -0.396224508
                                                 0.104488870
           1.35962064 -0.690443405 -0.283661780
## [111,]
                                                 0.107500284
                                                 0.058136869
           1.59732747
                       0.420292431 -0.023108991
## [112,]
## [113,]
           1.87761053 -0.417849815 -0.026250468
                                                 0.145926073
## [114,]
           1.25590769
                      1.158379741 -0.578311891
                                                 0.098826244
## [115,]
           1.46274487 0.440794883 -1.000517746
                                                 0.274738504
## [116,]
           1.58476820 -0.673986887 -0.636297054
                                                 0.191222383
## [117,]
           1.46651849 -0.254768327 -0.037306280 -0.154811637
## [118,]
           2.41822770 -2.548124795
                                    0.127454475 -0.272892966
## [119,]
           3.29964148 -0.017721580
                                    0.700957033
                                                0.045037725
## [120,]
           1.25954707
                                    0.266643612 -0.064963167
                      1.701046715
## [121,]
           2.03091256 -0.907427443 -0.234015510
                                                 0.167390481
## [122,]
           0.97471535
                      0.569855257 -0.825362161 0.027662914
           2.88797650 -0.412259950
## [123,]
                                    0.854558973 -0.126911337
## [124,]
           1.32878064 0.480202496
                                    0.005410239 0.139491837
## [125,]
           1.69505530 -1.010536476 -0.297454114 -0.061437911
## [126,]
           1.94780139 -1.004412720
                                    0.418582432 -0.217609339
## [127,]
           1.17118007 0.315338060 -0.129503907 0.125001677
## [128,]
           1.01754169 -0.064131184 -0.336588365 -0.008625505
## [129,]
           1.78237879 0.186735633 -0.269754304 0.030983849
## [130,]
           1.85742501 -0.560413289
                                   0.713244682 -0.207519953
## [131,]
           2.42782030 -0.258418706
                                    0.725386035 -0.017863520
## [132,]
           2.29723178 -2.617554417
                                    0.491826144 -0.210968943
## [133,]
           1.85648383
                       0.177953334 -0.352966242 0.099675959
## [134,]
           1.11042770
                       0.291944582
                                    0.182875741 -0.185721512
## [135,]
           1.19845835 0.808606364
                                    0.164173760 -0.487849130
## [136,]
           2.78942561 -0.853942542
                                   0.541093785
                                                 0.294893130
## [137,]
           1.57099294 -1.065013214 -0.942695700
                                                 0.035486875
## [138,]
           1.34179696 -0.421020154 -0.180271551 -0.214702016
## [139,]
           0.92173701 -0.017165594 -0.415434449
                                                 0.005220919
## [140,]
           1.84586124 -0.673870645 0.012629804
                                                 0.194543500
## [141,]
           2.00808316 -0.611835930 -0.426902678
                                                 0.246711805
## [142,]
           1.89543421 -0.687273065 -0.129640697
                                                 0.468128374
## [143,]
           1.15401555 0.696536401 -0.528389994 -0.040385459
## [144,]
           2.03374499 -0.864624030 -0.337014969
                                                 0.045036251
## [145,]
           1.99147547 -1.045665670 -0.630301866
                                                 0.213330527
## [146,] 1.86425786 -0.385674038 -0.255418178 0.387957152
```

```
## [147,] 1.55935649 0.893692855 0.026283300 0.219456899
## [148,] 1.51609145 -0.268170747 -0.179576781 0.118773236
## [149,] 1.36820418 -1.007877934 -0.930278721 0.026041407
## [150,] 0.95744849 0.024250427 -0.526485033 -0.162533529

iris2 <- cbind(iris, iris.pca.normaldata$x)

library(ggplot2)

ggplot(iris2, aes(PC1, PC2, col = Species, fill = Species)) +
    stat_ellipse(geom = "polygon", col = "black", alpha = 0.5) +
    geom_point(shape = 21, col = "black")</pre>
```



#### **PCA Coefficients**

```
cor(iris[, 1:4], iris2[, 6:9])

## PC1 PC2 PC3 PC4

## Sepal.Length 0.8901688 -0.36082989 0.27565767 0.03760602

## Sepal.Width -0.4601427 -0.88271627 -0.09361987 -0.01777631

## Petal.Length 0.9915552 -0.02341519 -0.05444699 -0.11534978

## Petal.Width 0.9649790 -0.06399985 -0.24298265 0.07535950
```