## Review-7

## On Variational Bounds of Mutual Information

A number of machine learning problems make use of Mutual Information (MI) as a metric for estimating the relationship between variables. However, bounding MI is a challenging task. Variational bounds allow tractabe objectives which are scalable to high dimensional tasks. The work presents a unified framework for variational bounds which consists of existing lower and upper bounds on MI. The bounds exhibit high bias or variance when MI is large. To that end, the framework is improved by providing a continuum on lower bounds which trades off bias and variance. Suitability of bounds is assessed on high dimensional control problems and representation learning.

Variational bounds provide tractability of objectives and improved approximations in the case f parameterized distributions. The work reviews existing bounds in literature by accumulating variational objectives in a unified framework. The framework consists of bounds which maximize or minimize MI pertaining to the auxiliary objective. In order to improve the performance of bounds with large values of MI, a continuum of multi-sample bounds is proposed which reduces variance by sample dependence. The multi-sample unnormalized setup consists of samples from  $p(x_1)p(y|x_1)$  and access to K-1 additional samples which are used to estimate MI I(X;Y). The bounds proposed in the work make use of an interpolation scheme which is upper bounded by  $\log(\frac{K}{\alpha})$  where  $\alpha$  is a hyperparameter which allows in the trade off between bias and variance. The multi-sample InfoNCE bound is obtained as a lower bound the MI I(X;Y). Validation of the bound is carried out on 2 correlated Gaussian problems with the multi-sample bound demonstrating lower variance.

The multi-sample InfoNCE bound trades off variance with bias for the correlated Gaussian problem. Additionally, the utility of bounds for representation learning is highlighte din the case of position and scale on the dSpirtes dataset. However, the bound presents two shortcomings. Firstly, InfoNCE is