

МИНОБРНАУКИ РОССИИ
САНКТ-ПЕТЕРБУРГСКИЙ ГОСУДАРСТВЕННЫЙ
ЭЛЕКТРОТЕХНИЧЕСКИЙ УНИВЕРСИТЕТ
«ЛЭТИ» ИМ. В.И. УЛЬЯНОВА (ЛЕНИНА)
Кафедра САПР

ОТЧЕТ
по лабораторной работе 3
по дисциплине «Алгоритмы и структуры данных»
Тема: нахождение кратчайшего пути по алгоритму Беллмана-Форда

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Задача: найти наиболее эффективный по стоимости перелет из города i в город j используя алгоритм Беллмана-Форда.

Описание алгоритмов:

Алгоритм позволяет найти кратчайший путь в ориентированном графе из исходной вершины до любой другой вершины этого графа.

Оценка временной сложности:

Ford_Bellman $O(n^4)$

Результат:

	St.Petersburg	Moscow	Khabarovsk	Vladivostok	Kasan
St.Petersburg	0	10	14	20	inf
Moscow	20	0	4	49	3
Khabarovsk	inf	3	0	8	inf
Vladivostok	inf	32	13	0	15
Kasan	20	inf	inf	37	0

After applying Bellman-Ford algorithm:

	St.Petersburg	Moscow	Khabarovsk	Vladivostok	Kasan
St.Petersburg	0	10	14	20	13
Moscow	20	0	4	12	3
Khabarovsk	23	3	0	8	6
Vladivostok	35	16	13	0	15
Kasan	20	30	34	37	0

D:\4_STUDY\АИСД\Lab_3\LR_3-1\Debug\LR_3-1.exe (процесс 19816) завершил работу с кодом 0.

Листинг:

Main.cpp

```
#include "FB.h"

int main()
{
    setlocale(LC_ALL, "Russian");

    AdjMatrix graph;
    ifstream fin;
    const char filename[] = "input.txt";

    fin.open(filename);
    if (fin.good()) fin >> graph;
    else return 5;

    cout << "Initial graph's adjacent matrix is\n" << graph << "\n";
    cout << "After applying Bellman-Ford algorithm:\n" << graph.FordBellman() << endl;

    fin.close();
    return 0;
}
```

FB.h

```
#include "linear.h"
#include <fstream>
#include <iomanip>

#define INF ((double)(1e300 * 1e300))

const string NOT_AVAILABLE = "N/A";

class AdjMatrix
{
    size_t size;
```

```

string* names;
double** values;

void outputline(ostream& stream, AdjMatrix& matrix, size_t maxwidth)
{
    stream << "--";
    for (size_t i = 0; i < maxwidth; i++) stream << '-';
    stream << "---";
    for (size_t i = 0; i < matrix.size; i++)
    {
        const size_t len = matrix.names[i].length();
        for (size_t j = 0; j < len; j++)
        {
            stream << '-';
        }
        stream << "--" << (i == matrix.size - 1 ? '\n' : '-');
    }
}

public:
AdjMatrix() : values(nullptr), names(nullptr), size(0) {}
AdjMatrix(size_t size, string* names, double** values) : values(values), names(names),
size(size) {}
~AdjMatrix()
{
    if (values != nullptr)
    {
        for (size_t i = 0; i < size; i++)
        {
            delete[] values[i];
        }
        delete[] values;
    }
}

friend bool operator==(AdjMatrix& gr1, AdjMatrix& gr2)
{
    if (gr1.size != gr2.size) return false;
    for (size_t i = 0; i < gr1.size; i++) if (gr1.names[i] != gr2.names[i]) return
false;
    for (size_t i = 0; i < gr1.size; i++)
    {
        for (size_t j = 0; j < gr1.size; j++)
        {
            if (gr1.values[i][j] != gr2.values[i][j]) return false;
        }
    }
    return true;
}

friend ifstream& operator>>(ifstream& stream, AdjMatrix& matrix)
{
    string name1_buffer, name2_buffer;
    double value1_buffer, value2_buffer;
    List<string> names;
    while (!stream.eof())
    {
        string temp;
        stream >> name1_buffer >> name2_buffer >> value1_buffer >> value2_buffer;
        if (names.Find(name1_buffer) < 0) names.PushBack(name1_buffer);
        if (names.Find(name2_buffer) < 0) names.PushBack(name2_buffer);
        if (value1_buffer == 0)
        {
            stream.clear();
            stream >> temp >> value2_buffer;
        }
        if (value2_buffer == 0)
        {
            stream.clear();

```

```

        if (temp == NOT_AVAILABLE) throw invalid_argument("Wrong input");
        stream >> temp;
    }
}
matrix.size = names.GetSize();
matrix.names = new string[matrix.size];
matrix.values = new double* [matrix.size];
for (size_t i = 0; i < matrix.size; i++)
{
    matrix.names[i] = names.GetData();
    names.PopFront();
    matrix.values[i] = new double[matrix.size];
    for (size_t j = 0; j < matrix.size; j++)
    {
        matrix.values[i][j] = (i == j ? 0 : INF);
    }
}

stream.seekg(ios::beg);
while (!stream.eof())
{
    string temp;
    stream >> name1_buffer >> name2_buffer >> value1_buffer >> value2_buffer;
    if (value1_buffer == 0)
    {
        stream.clear();
        stream >> temp >> value2_buffer;
        value1_buffer = INF;
    }
    if (value2_buffer == 0)
    {
        stream.clear();
        stream >> temp;
        value2_buffer = INF;
    }

    size_t i = 0, j = 0, k;
    for (k = 0; k < matrix.size; k++)
    {
        if (matrix.names[k] == name1_buffer) i = k;
        if (matrix.names[k] == name2_buffer) j = k;
    }
    matrix.values[i][j] = value1_buffer;
    matrix.values[j][i] = value2_buffer;
}
return stream;
}

friend ostream& operator<<(ostream& stream, AdjMatrix& matrix)
{
    size_t maxwidth = 0;
    for (size_t i = 0; i < matrix.size; i++)
    {
        if (matrix.names[i].length() > maxwidth) maxwidth =
matrix.names[i].length();
    }
    matrix.outputline(stream, matrix, maxwidth);
    stream << "| ";
    for (size_t i = 0; i < maxwidth; i++)
    {
        stream << ' ';
    }
    stream << " | ";
    for (size_t i = 0; i < matrix.size; i++)
    {
        stream << setw(matrix.names[i].length()) << left << matrix.names[i] << "
| ";
    }
    stream << "\n";
}

```

```

        matrix.outputline(stream, matrix, maxwidth);
        for (size_t i = 0; i < matrix.size; i++)
        {
            stream << " | " << setw(maxwidth) << right << matrix.names[i] << " | ";
            for (size_t j = 0; j < matrix.size; j++)
            {
                stream << setw(matrix.names[j].length()) << left <<
matrix.values[i][j] << " | ";
            }
            stream << "\n";
        }
        matrix.outputline(stream, matrix, maxwidth);
        return stream;
    }

    AdjMatrix& FordBellman()
    {
        if (size == 0) throw logic_error("Adjacent matrix does not have a graph yet");
        AdjMatrix* newMatrix = new AdjMatrix();
        newMatrix->size = size;
        newMatrix->names = names;
        newMatrix->values = new double* [size];

        // Choosing the vertex to calculate from
        for (size_t vertex = 0; vertex < size; vertex++)
        {
            // Initializing array with 0 on a current vertex and +INF on other
            double* distances = new double[size];
            for (size_t i = 0; i < size; i++)
            {
                distances[i] = (i == vertex ? 0 : INF);
            }

            // Repeating algorithm [vertex count - 1] times (enough)
            for (size_t step = 0; step < size; step++)
            {
                // Relaxing edges
                for (size_t i = 0; i < size; i++)
                {
                    for (size_t j = 0; j < size; j++)
                    {
                        if (i != j && values[i][j] < INF && distances[i] +
values[i][j] < distances[j])
                        {
                            if (step == size - 1) throw
logic_error("Graph has negative cycles");
                            else distances[j] = distances[i] +
values[i][j];
                        }
                    }
                }
                newMatrix->values[vertex] = distances;
            }

            return *newMatrix;
        }

        inline double** GetValues() { return values; }
    };

```

Linear.h

```

#ifndef LINEAR_STRUCT
#define LINEAR_STRUCT
#include <iostream>
using namespace std;

```

```

template <class T>
class List
{
protected:
    struct ListElement
    {
        ListElement* previous, * next;
        T data;

        ListElement(T& data, ListElement* next = nullptr, ListElement* previous =
nullptr) : data(data), previous(previous), next(next) {}
        ~ListElement() {}
    };

public:
    ListElement* head, * tail;

    List() : head(nullptr), tail(nullptr) {}

    List(const size_t size, T* arr) : head(nullptr), tail(nullptr)
    {
        for (size_t i = 0; i < size; i++) this->PushBack(arr[i]);
    }

    List(List<T>& ref) : head(nullptr), tail(nullptr)
    {
        const size_t size = ref.GetSize();
        for (size_t i = 0; i < size; i++)
        {
            T newElem = ref.GetData(i);
            this->PushBack(newElem);
        }
    }

    template <typename... Args> List(Args... list) : head(nullptr), tail(nullptr) { this-
>PushBack(list...); }

    template <typename... Args>
    void PushBack(T first, Args&... rest)
    {
        this->PushBack(first);
        this->PushBack(rest...);
    }

    ~List()
    {
        if (head != nullptr) Clear();
    }

    List<T>& operator+(List<T>& l)
    {
        List<T>* newList = new List<T>();
        for (size_t i = 0; i < GetSize(); i++) newList->PushBack(GetData(i));
        for (size_t i = 0; i < l.GetSize(); i++) newList->PushBack(l.GetData(i));
        return *newList;
    }

    void operator+=(List<T>& l)
    {
        *this = *this + l;
    }

    friend bool operator==(List<T>& list1, List<T>& list2)
    {
        ListElement* current1 = list1.head;
        ListElement* current2 = list2.head;
        while (current1 != nullptr)
        {
            if (current2 != nullptr)

```

```

        {
            if (current1->data != current2->data) return false;
        }
        else return false;
        current1 = current1->next;
        current2 = current2->next;
    }
    if (current2 != nullptr) return false;
    return true;
}

friend ostream& operator<<(ostream& stream, List<T>& list)
{
    ListElement* current = list.head;
    stream << "[";
    while (current != nullptr)
    {
        stream << current->data;
        if (current->next != nullptr) stream << " ";
        current = current->next;
    }
    stream << "]";
    return stream;
}

void Clear()
{
    if (head == nullptr) throw logic_error("List is already empty");
    while (head != nullptr)
    {
        if (head->next == nullptr) break;
        head = head->next;
        delete head->previous;
    }
    delete head;
}

size_t GetSize()
{
    int size = 0;
    ListElement* current = head;
    while (current != nullptr)
    {
        size++;
        current = current->next;
    }
    return size;
}

int Find(T element)
{
    ListElement* current = head;
    int index = 0;
    while (current != nullptr)
    {
        if (current->data == element) return index;
        current = current->next;
        index++;
    }
    return -1;
}

virtual void PushFront(T element)
{
    ListElement* newElement = new ListElement(element, head);
    if (head == nullptr)
    {
        head = newElement;
        tail = head;
    }
}

```

```

    }
    else
    {
        head->previous = newElement;
        head = head->previous;
    }
    return;
}

virtual void PushBack(T element)
{
    ListElement* newElement = new ListElement(element, nullptr, tail);
    if (tail == nullptr)
    {
        tail = newElement;
        head = tail;
    }
    else
    {
        tail->next = newElement;
        tail = tail->next;
    }
    return;
}

virtual void Push(T element)
{
    throw logic_error("Push is undefinable, use PushFront/PushBack/PushIndex");
}

virtual void PushIndex(int index, T element)
{
    const size_t lastIndex = GetSize() - 1;
    if (index == 0) PushFront(element);
    else if (index == lastIndex + 1) PushBack(element);
    else if (index > lastIndex + 1 || index < 0) throw out_of_range("Stated index is
invalid");
    else
    {
        int currentIndex = 1;
        ListElement* current = head->next;
        while (currentIndex != index)
        {
            current = current->next;
            currentIndex++;
        }
        ListElement* newElement = new ListElement(element, current, current-
>previous);
        current->previous->next = newElement;
        current->previous = newElement;
    }
}

virtual void PopFront()
{
    if (head == nullptr) throw logic_error("List is already empty");
    if (head->next == nullptr)
    {
        delete head;
        head = nullptr;
        tail = nullptr;
    }
    else
    {
        head = head->next;
        delete head->previous;
        head->previous = nullptr;
    }
    return;
}

```



```

    }

    virtual void PopBack()
    {
        if (tail == nullptr) throw logic_error("List is already empty");
        if (tail->previous == nullptr)
        {
            delete tail;
            head = nullptr;
            tail = nullptr;
        }
        else
        {
            tail = tail->previous;
            delete tail->next;
            tail->next = nullptr;
        }
        return;
    }

    virtual void PopIndex(int index)
    {
        const size_t lastIndex = GetSize() - 1;
        if (index == 0) PopFront();
        else if (index == lastIndex) PopBack();
        else if (index > lastIndex || index < 0) throw out_of_range("Stated index is
invalid");
        else
        {
            int currentIndex = 1;
            ListElement* current = head->next;
            while (currentIndex != index)
            {
                current = current->next;
                currentIndex++;
            }
            ListElement* next = current->next, * previous = current->previous;
            delete current;
            next->previous = previous;
            previous->next = next;
        }
    }

    virtual void Pop()
    {
        throw logic_error("Push is undefinable, use PopFront/PopBack/PopIndex");
    }

    T& GetData(size_t index = 0)
    {
        ListElement* current = head;
        size_t i = 0;
        while (current != nullptr)
        {
            if (i == index) return current->data;
            i++;
            current = current->next;
        }
        throw out_of_range("Index is incorrect");
    }

    inline void PrintData() { cout << *this; }
};

template <typename T>
class Queue : public List<T>
{
public:
    List<T>::Clear;

```

```

List<T>::GetSize;

void PushFront(T element) override
{
    throw logic_error("Queue structure has no access to execute PushFront");
}

List<T>::PushBack;

void PushIndex(int index, T element) override
{
    if (index == GetSize()) PushBack(element);
    else throw logic_error("In queue structure pushing index can only be the last
one");
    return;
}

void Push(T element) override
{
    PushBack(element);
    return;
}

List<T>::PopFront;

void PopBack() override
{
    throw logic_error("Queue structure has no access to execute PopBack");
}

void PopIndex(int index) override
{
    if (index == 0) PopFront();
    else throw logic_error("In queue structure popping index can only be zero");
    return;
}

void Pop() override
{
    PopFront();
    return;
}

List<T>::GetData;

List<T>::PrintData;
};

template <typename T>
class Stack : public List<T>
{
public:
    List<T>::Clear;

    List<T>::GetSize;

    List<T>::PushFront;

    void PushBack(T element) override
    {
        throw logic_error("Stack structure has no access to execute PushFront");
    }

    void PushIndex(int index, T element) override
    {
        if (index == 0) PushFront(element);
        else throw logic_error("In stack structure pushing index can only be zero");
        return;
    }

```

```

    }

    void Push(T element) override
    {
        PushFront(element);
        return;
    }

    List<T>::PopFront;

    void PopBack() override
    {
        throw logic_error("Stack structure has no access to execute PopBack");
    }

    void PopIndex(int index) override
    {
        if (index == 0) PopFront();
        else throw logic_error("In stack structure popping index can only be zero");
        return;
    }

    void Pop() override
    {
        PopFront();
        return;
    }

    List<T>::GetData;

    List<T>::PrintData;
};
#endif // LINEAR_STRUCT

```