

← ULTIMATE MATHEMATICS → ①

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TRIGONOMETRY:

X : ① $\sin(90^\circ - \theta) = \cos \theta$; $\cos(90^\circ - \theta) = \sin \theta$
 $\tan(90^\circ - \theta) = \cot \theta$; $\cot(90^\circ - \theta) = \tan \theta$
 $\sec(90^\circ - \theta) = \csc \theta$; $\csc(90^\circ - \theta) = \sec \theta$

② $\csc \theta = \frac{1}{\sin \theta}$; $\sin \theta = \frac{1}{\csc \theta}$ change

$\cot \theta = \frac{1}{\tan \theta}$; $\tan \theta = \frac{1}{\cot \theta}$

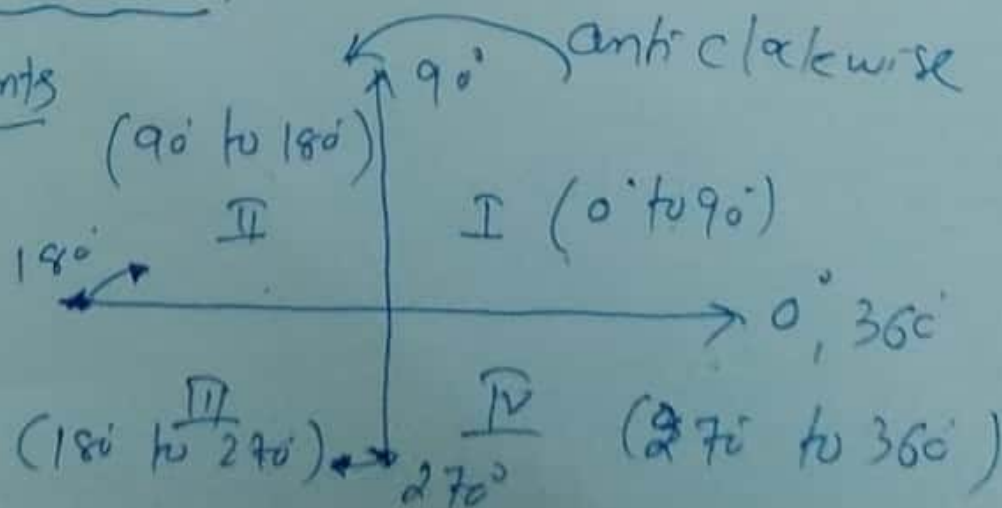
$\sec \theta = \frac{1}{\cos \theta}$, $\cos \theta = \frac{1}{\sec \theta}$ Reciprocal

③ trig table

	0°	30°	45°	60°	90°
$\sin \theta$	0	$\frac{1}{2}$	$\frac{1}{\sqrt{2}}$	$\frac{\sqrt{3}}{2}$	1
$\cos \theta$	1	$\frac{\sqrt{3}}{2}$	$\frac{1}{\sqrt{2}}$	$\frac{1}{2}$	0
$\tan \theta$	0	$\frac{1}{\sqrt{3}}$	1	$\sqrt{3}$	∞ (∞)

XI Trigonometry

(1) Quadrants
four

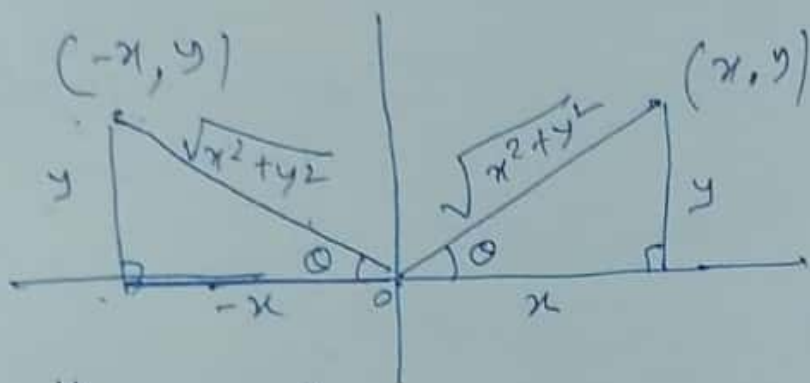


← ULTIMATE MATHEMATICS → 2

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(2) I	II	III	IV	
Add	Sugar	To	Coffee	
↓	↓	↓	↓	
All (+ve)	sin θ, cosec θ (+ve)	tand, cot θ (+ve)	cos θ, sec θ (+ve)	2, 1/2

Reason



$$\sqrt{4} = 2$$

$$\sin \theta = \frac{y}{\sqrt{x^2 + y^2}}$$

$$\tan \theta = \frac{y}{x}$$

$$\sin \theta = \frac{y}{\sqrt{x^2 + y^2}} \quad (+ve)$$

$$\tan \theta = \frac{y}{-x} \quad (-ve)$$

$$\cos \theta = \frac{-x}{\sqrt{x^2 + y^2}} \quad (-ve)$$

(3) (1 × 90°) (3 × 90°)
 90°, 270° → change (odd multiple of 90°)

180°, 360° → no change
 (2 × 90°) (4 × 90°) (even multiple of 90°)

← ULTIMATE MATHEMATICS → 3

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(1) $\sin(180^\circ - \theta) = \sin \theta$

\downarrow \downarrow
left acute

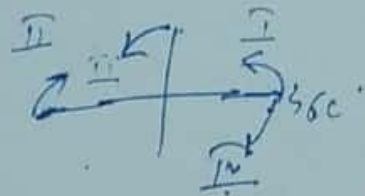
Check

(2) $\tan(270^\circ + \theta) = -\cot \theta$

\downarrow
left

(3) $\sec(270^\circ - \theta) = -\csc \theta$

\downarrow
left



(4) $\sin(120^\circ) = \sin(90^\circ + 30^\circ) = \cos(30^\circ) = \frac{\sqrt{3}}{2}$

$= \sin(180^\circ - 60^\circ) = \sin(60^\circ) = \frac{\sqrt{3}}{2}$

(5) $\cot(315^\circ) = \cot(360^\circ - 45^\circ) = -\cot(45^\circ)$

$= -1$

(6) $\csc(420^\circ) = \csc(360^\circ + 60^\circ) = \csc(60^\circ)$

$= \frac{2}{\sqrt{3}}$

← ULTIMATE MATHEMATICS →

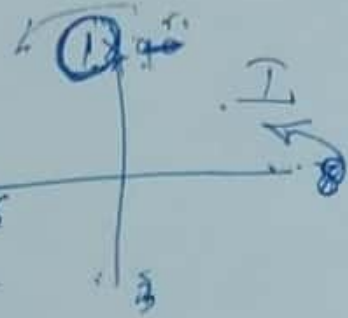
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4

(i) $\sin(765^\circ)$

$$\begin{aligned} &= \sin(8 \times 90^\circ + 45^\circ) \\ &= \sin(45^\circ) = \frac{1}{\sqrt{2}} \end{aligned}$$

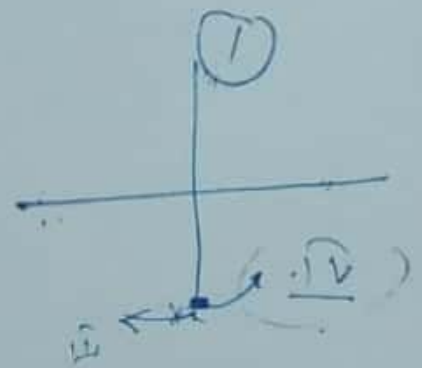
$$\begin{array}{r} 8 \\ 90^\circ \overline{) 765^\circ} \\ \underline{720} \\ 45 \end{array}$$



(ii) $\cot(1410^\circ)$

$$\begin{aligned} &= \cot(15 \times 90^\circ + 60^\circ) \\ &= -\tan(60^\circ) \\ &= -\sqrt{3} \end{aligned}$$

$$\begin{array}{r} 15 \\ 90^\circ \overline{) 1410} \\ \underline{90} \\ 510 \\ \underline{450} \\ 60 \end{array}$$



(iii) $\cos(720^\circ) \cos(270^\circ)$

$$\checkmark \cos(270^\circ + 0^\circ) = +\sin 0^\circ = 0$$

$$\checkmark \cos(270^\circ - 0^\circ) = -\sin 0^\circ = 0$$

$$\lambda = 180^\circ$$

$$x = \frac{\pi}{2} \cdot \sin\left(\frac{\pi}{2}\right) = \frac{22}{7} \times 1 = \frac{22}{7}$$

$$\frac{\pi}{2} = 90^\circ$$

$$\frac{\pi}{3} = 60^\circ$$

$$\frac{\pi}{6} = 30^\circ$$

$$\frac{\pi}{4} = 45^\circ$$

$$\lambda = 180^\circ$$

Qns 1 → Show that $\cos(510^\circ) \cdot \cos(330^\circ) + \sin(390^\circ) \cos(120^\circ) = -1$

Qns 2 → Show that $\cos(660^\circ) \sin(330^\circ) - \sin(420^\circ) \cos(390^\circ) = -1$

Qns 3 → Show that $\tan(225^\circ) \cot(405^\circ) + \tan(765^\circ) \cot(675^\circ) = 0$

Qns 4 → Show that $\tan(720^\circ) - \cos(270^\circ) - \sin(150^\circ) \cdot \cos(120^\circ) = \frac{1}{4}$

Qns 5 → Show that $2\sin^2\left(\frac{\pi}{6}\right) + \operatorname{cosec}^2\left(\frac{7\pi}{6}\right) \cdot \cos^2\left(\frac{\pi}{3}\right) = \frac{3}{2}$

Qns 6 → Show that $\tan\left(\frac{11\pi}{3}\right) - 2\sin\left(\frac{4\pi}{6}\right) - \frac{3}{4} \operatorname{cosec}^2\left(\frac{\pi}{4}\right) + 4\cos^2\left(\frac{17\pi}{8}\right) = \frac{3-4\sqrt{3}}{2}$

Qns 7 → Show that $\frac{\cos(\pi+x) \cos x}{\sin(\pi-x) \cos\left(\frac{\pi}{2}+x\right)} = \cot^2 x$

Qns 8 → Show that $\frac{\cos(2\pi+\theta) \cdot \operatorname{cosec}(2\pi+\theta) \tan\left(\frac{\pi}{2}+\theta\right)}{\sec\left(\frac{\pi}{2}+\theta\right) \cos\theta \cot(\pi+\theta)} = 1$

Qns 9 → Show that $\frac{\sin(180^\circ+\theta) \cdot \cos(90^\circ+\theta) \tan(270^\circ-\theta) \cot(360^\circ-\theta)}{\sin(360^\circ-\theta) \cdot \cos(360^\circ+\theta) \operatorname{cosec}\theta \cdot \cot(360^\circ-\theta)} = 1$

Qns 10 → Show that $\cos\left(\frac{3\pi}{2}+x\right) \cdot \cos(2\pi+x) \left[\cot\left(\frac{3\pi}{2}+x\right) + \cot(2\pi+x) \right] = 1$

Qns 11 → Find x from the equation

$$\operatorname{cosec}(90^\circ+\theta) + x \cot\theta \cot(90^\circ+\theta) = \sin(90^\circ+\theta)$$

Ans $x = \tan\theta$

Qns 12 → Find x from the equation

$$x \cot(90^\circ+\theta) + \tan(90^\circ+\theta) \cdot \sin\theta + \operatorname{cosec}(90^\circ+\theta) = 0$$

Ans $x = \sin\theta$

Qns 13 → If A, B, C, D be the angles of a cyclic quadrilateral

Show that $\cos(180^\circ-A) + \cos(180^\circ+B) + \cos(180^\circ+C)$

$\rightarrow x \rightarrow$

$-\sin(90^\circ+D) = 0$