

Solution

WORKSHEET No: 2

(STATS)

(1)

Ques-1 Given $n=8$

Mean = 9 & Variance = 9.25

Let the remaining two observations are x & y

\therefore data : 6, 7, 10, 12, 12, 13, x , y

Now Mean = $\frac{\sum x}{n}$

$$\Rightarrow 9 = \frac{6+7+10+12+12+13+x+y}{8}$$

$$\Rightarrow 72 = 60 + x + y$$

$$\Rightarrow \boxed{x+y=12} \text{ --- (1)}$$

Now, Variance = $\frac{1}{n} \sum x^2 - (\text{Mean})^2$

$$9.25 = \frac{1}{8} (36 + 49 + 100 + 144 + 144 + 169 + x^2 + y^2) - 81$$

$$\Rightarrow 9.25 + 81 = \frac{1}{8} (642 + x^2 + y^2)$$

$$\Rightarrow (90.25) \times 8 = 642 + x^2 + y^2$$

$$\Rightarrow 722 = 642 + x^2 + y^2$$

$$\Rightarrow \boxed{x^2 + y^2 = 80} \text{ --- (2)}$$

Solving (1) & (2)

$$x=8 \text{ \& } y=4$$

\therefore other two observations are 8 & 4 Ans

Q. No. 2 → Given $n=6$

Mean = 8 & S.D = 4

$$\text{variance} = (S.D)^2 = (4)^2 = 16$$

$$\therefore \text{old Mean} = 8 \Rightarrow 8 = \frac{\sum x}{6}$$

$$\text{old } S.D = 4$$

$$\text{old variance} = 16 \Rightarrow 16 = \frac{1}{6} \sum (x-8)^2$$

old observations: $x = x_1, x_2, x_3, x_4, x_5, x_6$

New observation

$$y = y_1, y_2, \dots, y_6$$

$$y = 3x_1, 3x_2, 3x_3, \dots, 3x_6$$

$$\text{new Mean } \bar{y} = \frac{\sum y}{n}$$

$$\bar{y} = \frac{\sum (3x)}{6}$$

$$\Rightarrow \bar{y} = 3 \frac{\sum x}{6}$$

$$\Rightarrow \bar{y} = 3 \times 8 \quad \dots \dots \dots \left\{ \because \text{old Mean } \frac{\sum x}{6} = 8 \right\}$$

$$\text{new Mean } \boxed{\bar{y} = 24}$$

$$\text{new variance} = \frac{1}{n} \sum (y - \bar{y})^2$$

$$= \frac{1}{6} \sum (3x - 24)^2$$

take 3 common

$$= \frac{1}{6} \times 9 \sum (x - 8)^2$$

$$= 9 \times \frac{1}{6} \sum (x - 8)^2$$

$$= 9 \times 16 \quad \dots \dots \dots \left\{ \text{old variance} = \frac{1}{6} \sum (x - 8)^2 = 16 \right\}$$

$$\boxed{\text{new } S.D = \sqrt{144} = 12} \text{ Ans}$$

Q. 3 → Given

3

$$C.V_1 = 60$$

$$C.V_2 = 70$$

$$S.D_1 (\sigma_1) = 21$$

$$S.D_2 (\sigma_2) = 16$$

to find: \bar{X}_1

2 \bar{X}_2

$$C.V_1 = \frac{\sigma_1}{\bar{X}_1} \times 100$$

$$C.V_2 = \frac{\sigma_2}{\bar{X}_2} \times 100$$

$$60 = \frac{21}{\bar{X}_1} \times 100$$

$$70 = \frac{16}{\bar{X}_2} \times 100$$

$$\bar{X}_1 = \frac{2100}{60}$$

$$\bar{X}_2 = \frac{1600}{70}$$

$$\boxed{\bar{X}_1 = 35} \text{ Ans}$$

$$\boxed{\bar{X}_2 = 22.85} \text{ Ans}$$

Q. 4 → (A) $n_1 = 586$

$$\bar{X}_1 = 5253$$

$$\text{variance} = 100$$

$$\therefore \sigma_1 = \sqrt{100} = 10$$

(B) $n_2 = 648$

$$\bar{X}_2 = 5253$$

$$\text{variance} = 121$$

$$\sigma_2 = \sqrt{121} = 11$$

(i) From A pays = Rs 586 x 5253 as monthly wages

From B pays = Rs 648 x 5253 as monthly wages

Clearly from B pays larger amount as monthly wages

(2) $C.V_A = \frac{\sigma_1}{\bar{x}_1} \times 100$

$$C.V_A = \frac{10}{5253} \times 100$$

$$C.V_A = 0.19$$

$C.V_B = \frac{\sigma_2}{\bar{x}_2} \times 100$

$$C.V_B = \frac{11}{5253} \times 100$$

$$C.V_B = 0.209$$

clearly $C.V_B > C.V_A$

\therefore from B shows greater variability Ans
→ X ←