

Relation & Functions

Qns 1 $\rightarrow A = \{-1, 0, 2, 4\}$

$$f(x) = x^2 + 1$$

$$f(-1) = 1 + 1 = 2$$

$$f(0) = 0 + 1 = 1$$

$$f(2) = 4 + 1 = 5$$

$$f(4) = 16 + 1 = 17$$

$$\therefore \text{Range of } f = \{2, 1, 5, 17\}$$

$$f = \{(-1, 2), (0, 1), (2, 5), (4, 17)\}$$

for preimage of 3 put $f(x) = 3$

$$\Rightarrow x^2 + 1 = 3$$

$$\Rightarrow x^2 = 2$$

$$\Rightarrow x = \pm\sqrt{2} \notin A$$

\therefore there is no preimage of 3 Ans

Qns 2 \rightarrow Given $f(x) = g(x)$

$$\Rightarrow 2x^2 - 1 = 1 - 3x$$

$$\Rightarrow 2x^2 + 3x - 2 = 0$$

$$\Rightarrow 2x^2 + 4x - x - 2 = 0$$

$$\Rightarrow 2x(x+2) - 1(x+2) = 0$$

$$\Rightarrow (2x-1)(x+2) = 0$$

$$\Rightarrow x = \frac{1}{2} ; x = -2$$

\therefore Required domain is $\{\frac{1}{2}, -2\}$ Ans

Qns 3 $\rightarrow f(x) = x^2 - 1$ and $g(x) = 2x + 3$

(1) $(f+g)(x) = f(x) + g(x) = x^2 - 1 + 2x + 3 \Rightarrow x^2 + 2x + 2$

(2) $(f-g)(x) = f(x) - g(x) = x^2 - 1 - 2x - 3 = x^2 - 2x - 4$

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$$(3) (fg)(x) = f(x)g(x) = (x^2-1)(2x+3) = 2x^3 + 3x^2 - 2x - 3$$

$$(4) \left(\frac{f}{g}\right)(x) = \frac{f(x)}{g(x)} = \frac{x^2-1}{2x+3} ; x \neq -\frac{3}{2}$$

Ques 4 $\rightarrow g = \{(3,5), (2,3), (1,1), (4,7)\}$

$$g(x) = \alpha x + \beta$$

$$(3,5) \in g$$

here $x=3$ and $g(x)=5$

$$\therefore 5 = 3\alpha + \beta \quad \dots (1)$$

$$(2,3) \in g$$

here $x=2$ and $g(x)=3$

$$\therefore 3 = 2\alpha + \beta \quad \dots (2)$$

$$(1) - (2)$$

$$2 = \alpha \Rightarrow 5 = 6 + \beta \Rightarrow \beta = -1$$

$$\therefore g(x) = 2x - 1 \quad \underline{\text{Ans}}$$

Ques 5 \rightarrow (i) $\{(x,y) : y = 3x ; x \in \{1,2,3\} , y \in \{3,6,9,12\}\}$

$$R = \{(1,3), (2,6), (3,9)\}$$

It is a function because every element in domain has unique image in codomain.

(ii) $\{(x,y) : y > x+1 ; x = 1, 2 \text{ and } y \in \{2,4,6\}\}$

$$R = \{(1,4), (1,6), (2,4), (2,6)\}$$

It is not a function because element 1 has two different images 4 & 6

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(iii) $\{(x, y) : x + y = 3 ; x, y \in \{0, 1, 2, 3\}\}$

$R = \{(0, 3) (3, 0) (1, 2) (2, 1)\}$

It is a function because every element in domain has unique image in codomain. Ans

Qn. 6 $\rightarrow A = \{12, 13, 14, 15, 16, 17\}$

$f(x) =$ highest prime factor of x

$f(12) =$ highest prime factor of $12 = 3$

$f(13) =$ " " " " $13 = 13$

$f(14) =$ " " " " $14 = 7$

$f(15) =$ " " " " $15 = 5$

$f(16) =$ " " " " $16 = 2$

$f(17) =$ " " " " $17 = 17$

\therefore Range of $f = \{3, 13, 7, 5, 2, 17\}$ Ans

Qn. 7 $\rightarrow f(x) = x^2$

$f(1.1) = (1.1)^2 = 1.21$

$f(1) = (1)^2 = 1$

Now $\frac{f(1.1) - f(1)}{1.1 - 1} = \frac{1.21 - 1}{0.1} = \frac{0.21}{0.1} = 2.1$ Ans

Qn. 8 (i) $f(x) = \frac{x-1}{x+2}$

$f(x)$ is real for all values of x such that

$x+2 \neq 0 \Rightarrow x \neq -2 \therefore$ Domain $= \mathbb{R} - \{-2\}$ Ans

$$(ii) f(x) = \frac{x^2 + 3x + 5}{x^2 - 5x + 4}$$

$f(x)$ is real for all values of x such that

$$x^2 - 5x + 4 \neq 0$$

$$(x-4)(x-1) \neq 0$$

$$x \neq 4 ; x \neq 1$$

$$\therefore \text{Domain} = \mathbb{R} - \{1, 4\} \quad \underline{\text{Ans}}$$

$$(iii) f(x) = \frac{3x-1}{x^2-2}$$

$f(x)$ is real for all values of x such that

$$x^2 - 2 \neq 0$$

$$(x+\sqrt{2})(x-\sqrt{2}) \neq 0$$

$$x \neq -\sqrt{2} ; x \neq \sqrt{2}$$

$$\therefore \text{Domain} = \mathbb{R} - \{-\sqrt{2}, \sqrt{2}\} \quad \underline{\text{Ans}}$$

$$(iv) f(x) = \frac{1}{x^2+2}$$

$f(x)$ is real for all values of x such that

$$x^2 + 2 \neq 0$$

$$\therefore \text{Domain} = \mathbb{R} \quad \underline{\text{Ans}} \quad \left\{ \begin{array}{l} \text{there is no value of } x \\ \text{for which } x^2 + 2 = 0 \end{array} \right.$$

$$(v) f(x) = \sqrt{4x-3}$$

$f(x)$ is real for all values of x such that

$$4x-3 \geq 0$$

$$x \geq 3/4$$

$$\therefore \text{Domain } x \in \left[\frac{3}{4}, \infty \right) \quad \underline{\text{Ans}}$$

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$$(6) \quad f(x) = \frac{1}{\sqrt{3x-2}}$$

$f(x)$ is real for all values of x such that

$$3x-2 > 0$$

$$\Rightarrow x > 2/3$$

$$\therefore \text{Domain } x \in \left(\frac{2}{3}, \infty\right) \quad \underline{\text{AM}}$$

$$(7) \quad f(x) = \frac{1}{\sqrt{3-2x}}$$

$f(x)$ is real for all values of x such that

$$3-2x > 0$$

$$2x-3 < 0$$

$$x < 3/2$$

$$\therefore \text{Domain } x \in (-\infty, 3/2) \quad \underline{\text{AM}}$$

$$(8) \quad f(x) = \sqrt{1-\sin(3x)}$$

$f(x)$ is real for all values of x such that

$$1-\sin(3x) \geq 0$$

$$\sin(3x) - 1 \leq 0$$

$$\sin(3x) \leq 1 \quad \text{which is always true}$$

$$\text{Since } -1 \leq \sin \theta \leq 1$$

$$\therefore \text{Domain} = \mathbb{R} \quad \underline{\text{AM}}$$

$$(9) \quad f(x) = |x-2|$$

$f(x)$ is real for all values of x such that
 $x \in \mathbb{R}$ Since there is no value of x
 for which $f(x)$ does not exist

$$\therefore \text{Domain} = \mathbb{R} \quad \underline{\text{AM}}$$

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(6)

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(10) $f(x) = \frac{1}{|x-3|}$

$f(x)$ is real for all values of x such that
that $x-3 \neq 0$
 $x \neq 3$

$\therefore \text{Domain} = R - \{3\}$ Ans

(11) $f(x) = \frac{1}{|x|-2}$

$f(x)$ is real for all values of x such that

$$|x|-2 \neq 0$$

$$|x| \neq 2$$

$$x \neq \pm 2$$

$$\left\{ \begin{array}{l} \text{Since } |2| = 2 \\ |-2| = 2 \end{array} \right\}$$

$\therefore \text{Domain} = R - \{-2, 2\}$ Ans

(12) $f(x) = \frac{1}{1-2\sin x}$

$f(x)$ is real for all values of x such that
 $1-2\sin x \neq 0$

$$\sin x \neq \frac{1}{2}$$

$$x \neq \pi/6$$

$\therefore \text{Domain} = R - \{\pi/6\}$ Ans

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