

!! जय श्री राधे कृष्ण !! जय श्री विरराज श्री मन्दाज !! ①

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CHAPTER PROBABILITY: CLAS No: 4

Ques 1 A man is known to speak truth 3 out of 4 times.
He throws a die and reports that it is a Six.
Find the probability that it is actually a Six.

Solution

$A \rightarrow$ Man reports that it is a Six

$E_1 \rightarrow$ Six occurs

$E_2 \rightarrow$ Six doesn't occur

$$P(E_1) = 1/6$$

$$P(E_2) = 5/6$$

$$P(A|E_1) = 3/4$$

\uparrow 6 report
 \downarrow 6 occurs

$$P(A|E_2) = 1/4$$

\uparrow Man reports
 \downarrow 6 doesn't occur

By prob $P(E_1|A) =$

Bayes

$$\text{Ans} = 3/8$$

Ques 2 \rightarrow Of people having HIV, 90% of the test detect the disease but 10% go undetected. Of people free of HIV, 99% of the test are judged HIV -ve but 1% are diagnosed as ~~people~~ showing HIV +ve. From a large population of which only 0.1% have HIV, one person is selected at random, given the HIV test and the pathologist reports him/her as HIV +ve. What is the probability that the person actually has HIV?

(2)

Sol Mr A \rightarrow Pathologist reports HIV +ve

$E_1 \rightarrow$ Person has HIV +ve

$E_2 \rightarrow$ Person does not have HIV +ve

$$P(E_1) = 0.1\% = \frac{1}{1000}$$

$$P(E_2) = \frac{999}{1000}$$

HIV Report
 $P(A|E_1) = \frac{90}{100}$
HIV present

HIV Report
 $P(A|E_2) = \frac{1}{1000}$
HIV not present

$$P(E_1|A) = \text{value put}$$

$$\approx \underline{\underline{0.083}} \text{ approx}$$

Ques 3 Assume that the chances of a patient having a heart attack is 40%. It is also assumed that a meditation and yoga course reduce the risk of heart attack by 30% and prescription of certain drugs reduces its ~~chance~~ chance by 25%. At a time a patient can choose any one of the two options with equal probabilities. It is given that after going through one of the two options the patient selected at random "suffers a ~~heart~~ heart attack". Find the probability that the patient followed a course of meditation and yoga?

A → patent suffers hit attack

E_1 → He followed Meditation & Yoga

E_2 → He followed prescription of drug.

$$P(E_1) = P(E_2) = 1/2$$

$$P(A|E_1) = \frac{70}{100} \times \frac{40}{100} = \frac{28}{100}$$

$$P(A|E_2) = \frac{75}{100} \times \frac{40}{100} = \frac{30}{100}$$

$$P(E_1|A) = \text{value put}$$



Qn 4 → If a machine is correctly set up, it produces 90% acceptable items. If it is incorrectly set up, it produces only 40% acceptable items. Past experience shows that 80% of the set-ups are correctly done. If of the a certain set up, the machine produces 2 acceptable items, find the probability that the machine is correctly set-up.

Soln A → 2 acceptable items are produced

E_1 → Machine is correctly set up

E_2 → Machine is incorrectly set up

$$P(E_1) = 80/100 ; P(E_2) = 20/100$$

$$P(A|E_1) = \frac{90}{100} \times \frac{90}{100}$$

$$P(A|E_2) = \frac{40}{100} \times \frac{40}{100}$$

$$P(E_1|A) = ?$$

(4)

Topic Total law of probability

$A \rightarrow$ Required event

$E_1 \rightarrow$
 $E_2 \rightarrow$
 $E_3 \rightarrow$
 \vdots

Options
(atleast two)

$$P(E_1) + P(E_2) + \dots = 1$$

$P(A|E_1) =$ Meaning use

Formula

$$P(A) = P(E_1)P(A|E_1) + P(E_2)P(A|E_2) + P(E_3)P(A|E_3) + \dots$$

Ques 5 \rightarrow There are two bags. Bag I contains 3 Red & 4 green balls. Bag II contains 4 Red & 2 green balls. ~~A ball~~ ~~one~~ one of the bag is selected & from the selected bag a ball is drawn. what is the probability that it is Red.

$A \rightarrow$ ~~Red~~ Red ball is drawn (required)

$E_1 \rightarrow$ Bag I is selected

$E_2 \rightarrow$ Bag II is selected

$$P(E_1) = 1/2 \quad P(E_2) = 1/2$$

$$P(A|E_1) = 3/7 \quad P(A|E_2) = 4/6$$

Reqd. $P(A) =$ value put.

Q.6 → A person has undertaken a construction job.

The probabilities are 0.65 that there will be strike, 0.80 that the construction job will be completed on time if there is no strike and 0.32 that the construction job will be completed on time, if there is a strike. Determine the probability that the construction job will be completed on time.

Sol $A \rightarrow$ the construction job is completed on time

$E_1 \rightarrow$ there was a strike

$E_2 \rightarrow$ there was no strike

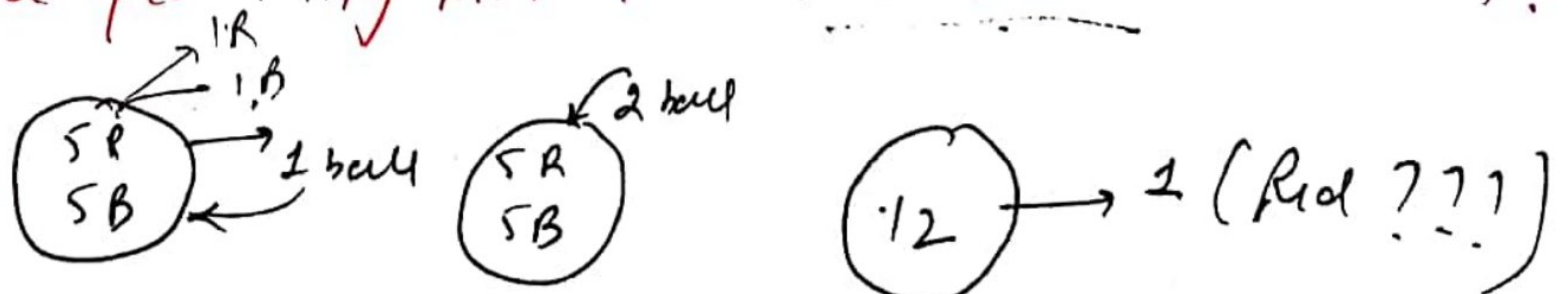
$$P(E_1) = 0.65 \quad P(E_2) = 1 - 0.65 = 0.35$$

$$P(A|E_1) = 0.32 \quad P(A|E_2) = 0.80$$

$$P(A) = \text{value put}$$

Q.7 An urn contains 5 red & 5 black balls.

A ball is drawn at random, its colour is noted and is returned to the urn. Moreover, 2 additional balls of the colour drawn are put in the urn and then a ball is drawn at random. What is the probability that the second ball is red?



Sol

(6)

$A \rightarrow$ the ball drawn (second ball) is Red

$E_1 \rightarrow$ the first ball was Red

$E_2 \rightarrow$ the first ball was Black

$$P(E_1) = \frac{5}{10} \quad P(E_2) = \frac{5}{10}$$

$$P(A|E_1) = \frac{7}{12}$$

2nd Red
1st ball

$$P(A|E_2) = \frac{5}{12}$$

2nd ball
1st black

$$P(A) = \text{value put}$$