

Journal of Statistical Software

MMMMMM YYYY, Volume VV, Issue II.

doi: 10.18637/jss.v000.i00

ggenealogy: An R Package for Visualizing Genealogical Data

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Abstract

This paper introduces **ggenealogy** (Rutter *et al.* 2015), a developing R package that provides tools for searching through genealogical data, generating basic statistics on their graphical structures using parent and child connections, and displaying the results. It is possible to draw the genealogy in relation to variables related to the nodes, and to determine and display the shortest path distances between genetic lines. Production of pairwise distance matrices and genealogical diagrams constrained on generation are also available in the visualization toolkit. The software is being tested on datasets with milestone cultivars of soybean (Hymowitz *et al.* 1977) and barley varieties [2], as well as on data from the Mathematics Genealogy Project, a database of the academic genealogy of mathematicians. It is currently available on the Comprehensive R Archive Network.

Keywords: genealogy, data visualization, statistical graphics, exploratory data analysis, interactive, R.

1. Introduction

Genealogy is the study of the parent-child relationships. By tracing through lineages of groups of individuals, the history of features that have been modified over time can be studied. Comparative geneticists, computational biologists, and bioinformaticians commonly use these tools to better understand the historical changes that caused novel and desirable traits to arise in lineages. For example, in crops, desirable modifications could include an increase in protein yield or an increase in disease resistance. However, there are also times when lineages of detrimental traits are analyzed, such as to determine the origin of hazardous traits in rapidly-evolving viruses.

Furthermore, genealogical relationships can be applied outside of a strict biological sense, an example being the Mathematics Genealogy Project, which maintains the family lineage

of academic mathematicians, with documentation of doctoral advisors, doctoral students, and graduation years of all mathematicians in academia. Such family lineages allow us to understand the position of one member in the larger historical picture, and to accurately preserve past relationships for the knowledge of future generations.

In all these examples, the data structures containing the genealogical relationships can be represented visually. Access to various types of visual plots and diagrams of the lineage can allow scientists and others to more efficiently and accurately explore an otherwise complicated data structure. We introduce here a developing visualization toolkit that is intended to assist users in their exploration and analysis of genealogical relationships. In this paper, we will demonstrate some of the main features of this software package, and summarize any novelty that such features may provide users, using an example lineage dataset of soybean cultivars (Hymowitz et al. 1977).

2. Available Software

Publishing in the open source R statistical programming language allows for tools to be distributed and modified at ease, encourages cross-platform collaboration, and provides a foundation for effective and aesthetic data visualization from the grammar of graphics. There are several useful R packages that offer tools for analyzing and visualizing genealogical datasets. Here, we introduce these packages, and emphasize the new features that ggenealogy brings to this collection of work.

The R package pedigree is named after the standardized chart used by genealogists to study human family lines, and sometimes used to select breeding of animals, such as show dogs (Coster 2013). The package uses a similar data input type as ggenealogy, namely a data frame for parent and child labels. While it does provide tools to perform methods on the data set, such as rapidly determining the generation count for each member in the pedigree, it does not provide any visualization tools.

Another R package called kinship2 does produce basic pedigree charts, one from the package vignette of which is provided as an example in Figure 1 (Therneau et al. 2015). This pedigree chart adheres to the standard notations used for visualizing genealogical structures. Even though doing so creates powerful charts that can be applied across many applications, it cannot provide unequivocal information in situations where inter-generational cross-breeding occurs, as is often the case in agronomical genealogical lineages. We demonstrate how the standardized pedigree charts in the kinship2 package generate ambiguous results in such scenarios by superimposing a hypothetical inter-generational cross-breeding case in Figure 1. We then later illustrate how new plotting tools in the ggenealogy package resolve this previously unaddressed area in Figure 6.

In addition, popular graph drawing software such as GraphViz and Cytoscape can be used to visualize genealogical structures, as is shown in Figure 2 (Gansner and North 2000, Shannon et al. 2003). These programs allow for visualizations of graphs, which are defined as objects with sets of nodes and edges, where nodes cannot be repeated. However, as is described in Figure 6, for certain genealogical datasets to be non-ambiguously displayed (as is described in), Hence, as is the case with the aforementioned R packages, these popular software also cannot

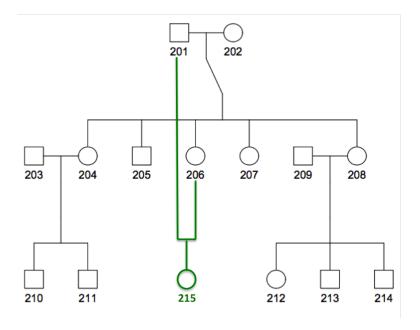


Figure 1: Example pedigree chart output from the kinship2 package. A standardized set of symbols are used to represent males with squares and females with circles. Parents are connected to each other by horizontal lines, and to their children by vertical lines. Siblings are connected by horizontal sibship lines. Each generation is defined by its position on the vertical axis, with the first generation containing individuals 201 and 202. We superimposed green-highlighted individual 215 and its corresponding connections onto the pedigree chart for explanatory purposes. Its parents are individuals 201 and 206, which are from generations one and two, respectively, and have a parent-child relationship themselves. As an offspring of a parent-child relationship, individual 215 is both a second generation and third generation individual. Hence, individual 215 should be displayed in both generational positions on the vertical axis. However, standard pedigree tools only allow for an individual to be displayed once. As a result, in cases where inter-generational cross-breading occurs, such as in agronomical applications, standardized tools for visualizing genealogical information cannot non-ambiguously portray the genealogical dataset.

3. Demonstration Dataset

The available data used in the current demonstration of the software is a data frame structure that contains 412 rows, each representing a direct parent-child relationship between a pair of soybean varieties. In total, there are 230 unique soybean varieties present. These data were collected from field trials, genetic studies, and United States Department of Agriculture (USDA) bulletins, and date as early as the first decade of the 1900s. They also contain information on the developmental years, as well as the copy number variants, single nucleotide polymorphisms, protein content, and yield, of each of the soybeans.

In this context, the software could ideally be used by bioinformaticians, geneticists, and agronomists who wish to study how soybean varieties are related. By referencing the visualization of the genealogical tree, these scientists may better understand genetic testing results in this particular dataset, in terms of copy number variants, single nucleotide polymorphisms,

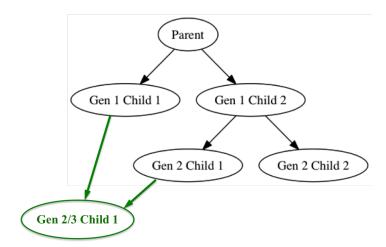


Figure 2: Example genealogical display using popular software like GraphViz and Cytoscape. The generation count of an individual node is constrained by its position on the vertical axis. As was shown in Figure 1, here too we superimpose a green node that has parents from the first and second generations. As an offspring of parents from two different generations, this green node is both a second generation and third generation individual of the original parent. Hence, it should be displayed in both corresponding generation positions on the vertical axis. However, standard graph visualization tools only allow for a given ode to be displayed once. As a result, this green node must be ambiguously positioned as either a second or third generation individual; here, it is positioned as a third generation individual.

protein content, and yield - and use that knowledge in future breeding sessions.

4. Generating a Graphical Object

Most functions in the software package require an input parameter of a graph structure. Therefore, as a preprocessing step, we must first convert our original data frame structure into a graph structure. Below, we read in the R data file sbGeneal that is included in the package as a sample data set of soybean genealogy.

```
R> library("ggenealogy")
R> data(sbGeneal)
R> str(sbGeneal)
'data.frame':
                     412 obs. of 5 variables:
 $ child
                      "5601T" "Adams" "A.K." "A.K. (Harrow)" ...
               : chr
 $ year
               : num
                      1981 1948 1910 1912 1968 ...
               : int
                      NA 2734 NA 2665 NA 2981 2887 2817 NA NA ...
                       TRUE FALSE TRUE FALSE FALSE FALSE ...
 $ year.imputed: logi
 $ parent
               : chr
                      "Hutcheson" "Dunfield" NA "A.K." ...
```

We now convert it into an **igraph** object (Csardi and Nepusz 2006) ig using the function dfToIG().

```
R> ig <- dfToIG(sbGeneal)</pre>
R> ig
IGRAPH UNW- 230 340 --
+ attr: name (v/c), weight (e/n)
+ edges (vertex names):
 [1] 5601T
              --Hutcheson
                                   Adams
                                            --Dunfield
 [3] A.K.
              --A.K. (Harrow)
                                   Altona
                                            --Flambeau
 [5] Amcor
              --Amsoy 71
                                   Adams
                                            --Amsoy
 [7] Amsoy 71 --C1253
                                   Anderson --Lincoln
 [9] Bay
              --York
                                  Bedford --Forrest
[11] Beeson
              --Kent
                                  Blackhawk--Richland
[13] Bonus
              --C1266R
                                  Bradley --J74-39
[15] Bragg
              --Jackson
                                            --Bragg x D60-7965
                                  Bragg
+ ... omitted several edges
```

There are many statistics about the sbGeneal genealogical dataset that we may wish to know that cannot easily be obtained through images and tables. The package function getBasicStatistics() can be called, using the ig object as input. This will return a list of common graph theoretical measurements regarding the genealogical graph structure. For instance, is the whole structure connected? If not, how many separated components does it contain? In addition to these statistics, the getBasicStatistics() function will also return the number of nodes, the number of edges, the average path length, the graph diameter, and other graph theoretical information.

```
R> getBasicStatistics(ig)
```

```
$isConnected [1] FALSE
```

\$numComponents

[1] 11

\$avePathLength

[1] 5.333746

\$graphDiameter

[1] 13

\$numNodes

[1] 230

\$numEdges

[1] 340

\$logN

[1] 5.438079

5. Plotting a Shortest Path

As this data set deals with soy bean lineages, it may be useful for agronomists to track how two varieties are related to each other via parent-child relationships. Then, any dramatic changes in protein yield, SNP varieties, and other measures of interest between the two varieties can be traced across their genetic timeline, and pinpointed to certain varieties within their historical lineage. The **ggenealogy** software allows users to select two varieties of interest, and determine the shortest pathway of parent-child relationships between them, using the **getPath()** function. This will return a list path that contains the variety names and their years in the path.

```
R> pathTN <- getPath("Tokyo", "Narow", ig, sbGeneal)
R> pathTN

$pathVertices
[1] "Tokyo" "Volstate" "Jackson" "R66-873" "Narow"

$yearVertices
[1] "1907" "1942" "1954.5" "1971.5" "1985"
```

The returned path object can then be plotted using the plotPath() function, as demonstrated below.

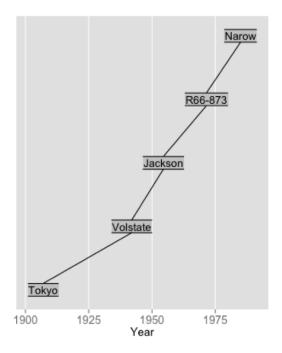
```
R> plotPath(pathTN)
```

This produces a visual that informs users of all the varieties involved in the shortest path between the two varieties of interest, see left half of Figure 3. In this plot, the years of all varieties involved in the path are indicated on the horizontal axis, while the vertical axis has no meaning other than to simply to display the labels evenly spaced vertically. The shortest path between varieties Tokyo and Narow is composed of a unidirectional series of parent-child relationships, with Tokyo as the starting ancestor in the early 1900s, Narow as the most recent descendent in the mid 1980s, and three varieties in between.

Next, we can run the same set of functions on a different pair of varieties. First, a call to the **ggenealogy** function **getYear()** indicates that variety **Bedford** was developed in 1978 and variety **Zane** in 1985.

```
R> getYear("Bedford", sbGeneal)
[1] 1978
R> getYear("Zane", sbGeneal)
[1] 1985
```

We can then create a plot showing the shortest path between these two varieties of interest.



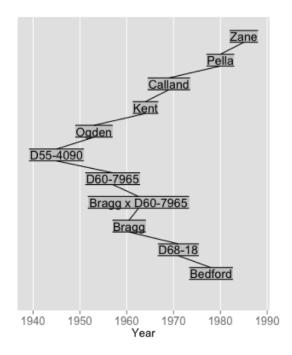


Figure 3: Left: The shortest path between varieties Tokyo and Narow is strictly composed of a unidirectional sequence of parent-child relationships. Right: The shortest path between varieties Zane and Bedford is not strictly composed of unidirectional parent-child relationships, but have a cousin-like relationship.

R> pathZB <- getPath("Zane", "Bedford", ig, sbGeneal)
R> plotPath(pathZB)

The resulting plot (right half of Figure 3) allows us to quickly determine that Bedford is not a parent, grandparent, or any great grandparent of Zane. Instead, we see that these two varieties are not related through a unidirectional parent-child lineage, but have a cousin-like relationship. The oldest common ancestor between Zane and Bedford is the variety D55-4090, which was developed in the mid 1940s.

Furthermore, as determined by the figure, for both Zane and Bedford, there are four varieties of unidirectional parent-child relationships between each of them and their common ancestor D55-4090. Hence, any parameter of interest that differentiates Zane and Bedford (protein yield, disease resistance, etc.) can also be examined across these two separate lineage histories.

6. Superimposing Shortest Path on Tree

Now that we can create path objects, we may wish to know how those paths are positioned in comparison to the genealogical lineage of the entire data structure. For instance, of the documented soybean cultivar lineage varieties, where does the shortest path between two varieties of interest exist? Are these two varieties comparatively older compared to the overall data structure? Are they newer? Or, do they span the entire structure, and represent two extreme ends of documented time points?

There is a function available in the **ggenealogy** package plotPathOnAll() that can allow users to quickly visualize their path of interest superimposed over all varieties and edges present in the whole data structure. Here we will produce a plot of the previously-determined shortest path between varieties Tokyo and Narow across the entire dataset:

```
R> plotAllImage <- plotPathOnAll(pathTN, sbGeneal, ig, binVector = 1:3,
   pathColor = "red")
R> plotAllImage + ggplot2::theme(axis.text = element_text(size = 20),
   axis.title = element_text(size = 20))
R> plotAllImage <- plotPathOnAll(path = path, geneal = sbGeneal, ig = ig,
   binVector = sample(1:3), edgeCol = "gray84", pathEdgeCol = "blue", nodeSize
   = 1, pathNodeSize = 3)</pre>
```

While the first three explicit parameters to the function plotPathOnAll() have been introduced earlier in this paper, the fourth parameter (binVector) requires some explanation. The motivation of the plotPathOnAll() is to write variety text labels on a plot, with the center of each variety label constricted on the horizontal axis to its developmental year. As is the case for the plots before, the vertical axis has no meaning other than providing a plotting area in which to draw the text labels. Unfortunately, for large datasets, this motivation can be a difficult task because the text labels of the varieties can overlap if they are assigned a similar y coordinate, have a similar year (x coordinate), and have labels with large numbers of characters (width of x coordinate).

For each variety, the x coordinate (year) and width of the x coordinate (text label width) cannot be altered, as they provide useful information. However, for each variety, the y coordinate is arbitrary. Hence, in an attempt to mitigate text overlapping, the plotPathOnAll() does not randomly assign the y coordinate. Instead, it allows users to partially control the y coordinates with a user-determined number of bins (binVector).

If the user determines to produce a plot using three bins, as in the example code above, then the varieties are all grouped into three bins based on their years of development. In other words, there will be bin 1 (the "oldest bin") which includes one-third of the total number of varieties all with the oldest developmental years, bin 2 (the "middle bin"), and bin 3 (the "youngest bin").

Then, in order to decrease text overlap, the consecutively increasing y-axis coordinates are alternatively assigned to the three bins (For example: bin 1, then bin 2, then bin 3, then bin 1, then bin 2, then bin 3, ...) repeatedly until all varieties are accounted for. This algorithm means that for any pair of varieties within a given bin constrained to those years on the horizontal axis, there are exactly two other varieties placed between them vertically on the y-axis that come from the two other bins 1 constrained to a different set of year values on the horizontal axis.

Hence, in the code above, the user selected a binVector value of three, and a plotColor of red, which produces the plot in Figure 4. We see that edges not on the path of interest are thin and gray by default, whereas edges on the path of interest are bolded and red. We also see that varieties in the path of interest are boldfaced by default.

The plot presents useful information: We immediately gather that the path of interest between does span most of the years of the data structure. In fact, Tokyo appears to be the oldest variety present in the dataset, and Narow appears to be one of the youngest varieties. We can

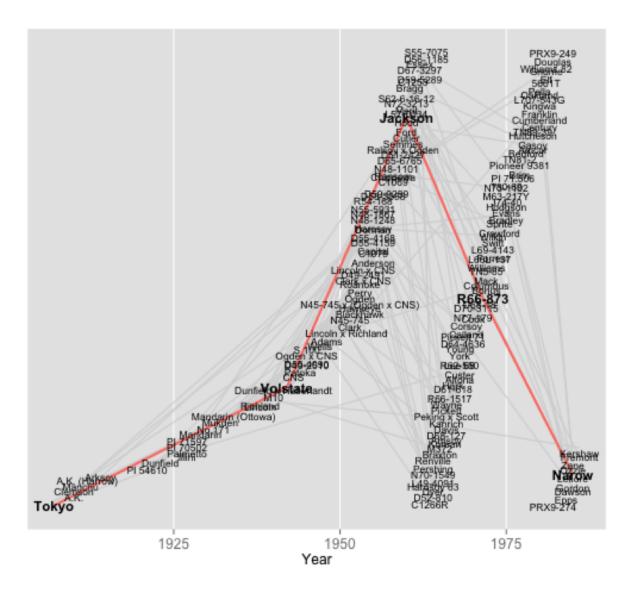


Figure 4: The shortest path between Tokyo and Narow, superimposed over the data structure, using a bin size of 3.

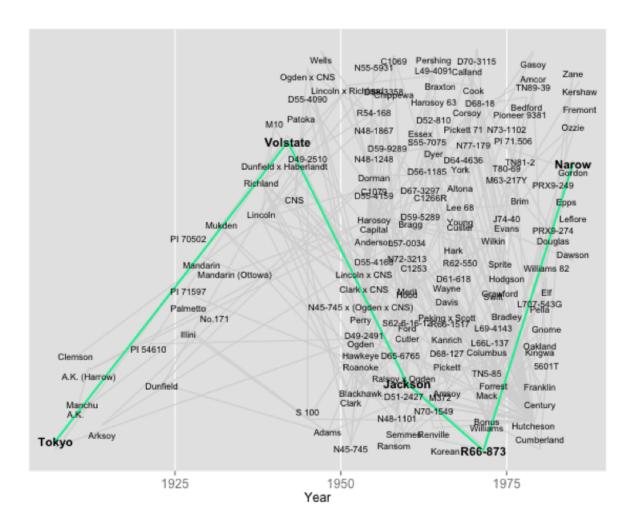


Figure 5: The shortest path between Tokyo and Narow, superimposed over the data structure, using a bin size of 6.

also determine that the vast majority of varieties appear to have development years between 1950 and 1970.

However, this plot has significant empty spaces between the noticeably distinct bins, whereas almost all text labels are overlapping, thereby decreasing their readability. To force some variety text labels into these spaces, the user may consider using a larger number of bins. Hence, we next examine a bin size of 6:

```
R> plotAllImage <- plotPathOnAll(pathTN, sbGeneal, ig, binVector = 1:6,
   pathEdgeCol = "seagreen2", nodeSize = 1, pathNodeSize = 3)</pre>
```

This similar code now outputs the plot shown in Figure 5. We can immediately see that this plot more successfully mitigates text variety label overlap than the previous plot in 4. We can also confirm what we saw in the previous plot that indeed most varieties have development years between 1950 and 1970, and any textual overlap is confined to this range of years.

7. Future Directions: Fine-tuning Superimposition

This visualization tool is suitable as part of a data exploration phase, but not for any users seeking publication quality plots due to the remaining textual overlap. We continue to work towards further reducing this textual overlap, although it is impossible to guarantee no textual overlap, especially with larger datasets with dense subgroups of varieties having similar years.

As such, we plan to add a feature to the **ggenealogy** package that allows users to manually finetune the plot they deem best after examining various bin sizes. For example, after comparing several bin sizes (1-12) on the current soy bean data set, we determined that the bin size of 6 produced minimal textual overlap, as seen in Figure 4.

However, there still remained one dozen cases of partial textual overlap. As an example, the labels of Crawford (1974) and Swift (1973) overlap at just below the vertical midpoint of the plot. The proposed function would allow users to hardcode the label of either variety and manually assign it to a new vertical coordinate. For instance, a user might select Swift and slightly decrease its vertical coordinate so that it is drawn halfway between Crawford and Bradley.

If the user sequentially fine-tuned the vertical positions of overlapping text labels for the small fraction of labels that remained overlapped after the automated function, and if they monitored the progress by visually inspecting updated plots until there were no more overlaps, then the plot could be used in presentations and publications.

8. Plotting Ancestors and Descendants by Generation

The most novel visual tool in **ggenealogy**, plotAncDes(), allows users to view the ancestors and descendants of a given variety. The inputted variety is highlighted in the center of the plot, ancestors are displayed to the left of the center, and descendants to the right of the center. The further from the center, the larger the number of generations that particular ancestor/descendant is from the centered variety of interest.

This particular **ggenealogy** tool is unique because most available graphical software only consider simple graphs, with no repeated nodes. However, in some genealogical lineage datasets, some varieties must be repeated if they are to be visualized by generation counts. This was found to be the case in the soy bean dataset.

As an example, we will create a plot of the ancestors and descendants of the variety Lee. We specify that the maximum number of ancestor and descendant generations are both 6, and that the text of the variety of interest is highlighted in blue:

```
R> plotAncDes("Lee", sbGeneal, mAnc = 6, mDes = 6, vCol = "blue")
```

This generates the plot we see in the left side of Figure 6. We notice that Lee has 3 generations of ancestors and 5 generations of descendants. However, we also notice that some varieties are repeated in the plot. For example, the variety 5601T is represented four times - once as a third generation descendant of Lee, once as a fourth generation descendant of Lee, and twice as a fifth generation descendant of Lee.

This happens because there are various paths between Lee and 5601T (see the right side of Figure 6). Hence, if we are to present all ancestors and descendants of Lee - while constricting

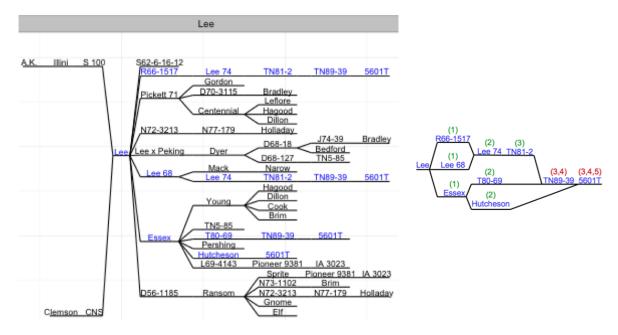


Figure 6: Left: All varieties within three generations of ancestors and five generations of descendants of the variety Lee are shown. The generation distance from the center variety is neatly displayed in this graph; the larger the generation distance from the center variety, the further left (for ancestors) or right (for descendants). For explanation purposes, all paths between Lee and 5601T are highlighted in blue. We see that 5601T appears four times in the plot, which is a unique and novel requirement provided by ggenealogy. Right: The paths that are highlighted in blue in the left plot from genealogy are shown here again, only now nodes cannot be repeated. We unsuccessfully try to constrain the horizontal position of the nodes by generation count, as was accomplished by the genealogy plot, without repeating nodes. The parenthetical number above each node represents the set of generation counts that node is away from the center node Lee; green ones indicate that the node could be successfully placed in one horizontal position, but red ones indicate that the node could not be successfully placed in only one horizontal position. Hence, without allowing nodes to repeat, this data information cannot be presented as it is in the genealogy graph on the left, and this is a current limitation in other currently-available graphical software that ggenealogy can now provide.

the horizontal axis to generational distance from Lee - then varieties like 5601T must occur more than once in the plot.

One of the main motivations in developing the plotAncDes() function was an inability to find other similar software (Claude et al. 2003) that could produce such a plot, where repeated nodes were permitted, see right side of Figure 6 for additional explanation. The plotAncDes() function generates plots that have increased readability, as it is relatively easy to compare how far varieties are from the center to obtain an idea of generational distance.

9. Plotting Distance Matrix

It may also be of interest to generate matrices where the colors indicates a variable (such as the degree of the shortest path) between all pairwise combinations of inputted varieties. The package **ggenealogy** also provides a function **plotDegMatrix()** for that purpose.

Here we generate a distance matrix for a set of 10 varieties, setting the x-label and y-label as "Variety" and the legend label as "Degree". Syntax from the **ggplot2** package (Wickham 2009) can be appended to the **plotDegMatrix()** function. In this example, we add **ggplot2** functionality to specify that pairs with small degrees are white, while those with large degrees are dark green, as well as to specify the label size of the legend title and text:

```
>R varieties <- c("Brim", "Bedford", "Calland", "Dillon", "Hood", "Narow",
    "Pella", "Tokyo", "Young", "Zane")
>R plotDegMatrix(varieties, ig, sbGeneal, "Variety", "Variety", "Degree") +
    ggplot2::scale_fill_continuous(low = "white", high = "darkgreen") +
    ggplot2::theme(legend.title = ggplot2::element_text(size = 15),
    legend.text = ggplot2::element_text(size = 15))
```

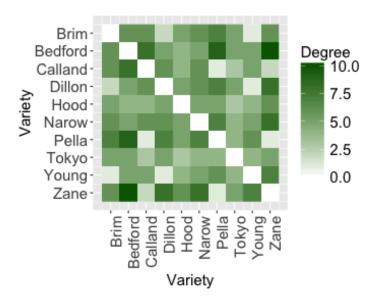


Figure 7: The shortest path degree matrix between ten varieties of interest.

This creates the plot in Figure 7. We see that the degree of the shortest path between varieties Bedford and Zane is 10, which is consistent with what we saw earlier in Figure 3. However, we now also see that 10 may be a comparatively large degree in this same dataset.

10. Conclusions

The **ggenealogy** package offers various plotting tools that can assist those studying genealogical lineages in the data exploration phases, as well as in preparing publication-suitable images. As each plot comes with its pros and cons, we recommended for users to explore several visualization tools. If users are simultaneously using similar packages, we in particular recommend using the plotAncDes() function. This plot allows users to view generation counts of a variety of interest in a manner that is not as readily available in similar software packages (Claude *et al.* 2003).

11. Future Avenues

Incorporation of the Shiny application (RStudio 2014) would allow users to examine **ggenealogy** tools in a more interactive way. The reactive programming would save them the time of using command-line for each change of input as well as the inefficiency of rerunning code. We also look forward to testing this package on additional genealogical data sets (Mathematics Genealogy Project). Exploring several datasets with our software will allow us to fix remaining bugs, and provide us further insight into how to make our tools available for a flexible set of data inputs.

Acknowledgments

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Submitted: yyyy-mm-dd

Accepted: yyyy-mm-dd