Random Number Generators: Implementation and Statistical Analysis Using Dieharder

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Abstract—We implement in efficient C++ several kinds of different modern pseudo-random number generators, or PRNGs; a Linear Congruential Generator, a Lagged Fibonacci Generator, an Xorshift type generator, and a Mersenne Twister Generator. We discuss the challenges in testing these kinds of PRNGs, and discuss one of the more common frameworks for testing these random number generators. Finally, we compare our results to what we expect from these implementations, as well as comment on the suitability of these PRNGs for use in simulation of systems.

Index Terms—Random Number Generators, Psuedo Random Number Generators, PRNGs, Statistical Analysis, Dieharder

I. INTRODUCTION

The applications of randomness are far reaching. From statistics, to simulation, to gaming, to cryptography, there is a large need for random number generators. Often time, these random number have to be fast, and deterministic in some cases, like simulations that have to be reproducible and debuggable. Thus, the creation of pseudo random number generators, or PRNGs, has become an important research area in modeling, computer simulation, and mathematics communities.

In the field of analysis of computing systems, simulation is an extremely important part of the modeling process. Today's stochastic models become so complex that solving these models analytically becomes impossible. Simulations driven by randomness then become a far more viable way to study the behavior of systems. This is the sort of need that motivates this project: a study of the theory behind random number generators, how to test them, and their suitability for this purpose.

A. Kinds of Random Number Generators

For the purposes of this paper, there are two kinds of Random Number Generators, or RNGs: Hardware RNGs, and Software RNGs. Hardware RNGs are used not only to output a random bit stream faster than a multipurpose CPU might be able to [1], [2], but also in order to gather entropy in a more unpredictable way, such as measuring thermal noise, detecting air moisture, or using unpredictable user interactions, such as keystrokes and mouse motion, to name a few. Often hardware RNGs are used to seed software RNGs. Readers interested in the seeding of RNGs with external entropy are encouraged to read [3].

Software RNGs, unless they draw upon these sources of entropy from nature for seeds, are in fact PRNGs, because the software that generates these sequences must be deterministic. In this paper, the term RNG will refer to software PRNGs, unless otherwise indicated. These software RNGs use mathematical models to take a finite amount of state and turn this into a sequence of seemingly random output, suitable for use in a variety of purposes. Though special purpose hardware RNG cir-

cuits may be fast, software RNGs are usually faster than repeatedly polling a sensor to gain outside entropy. They are also far more convenient to use, as all is required is a computer, rather than special purpose hardware.

Finally, there are several classes of software RNG based on quality of output. The highest class is those which are suited for cryptography. Generally, this includes passing the next bit test: that if k bits of a random sequence are known, then no polynomial time complexity algorithm should be able to guess the next bit [4]. These cryptographically secure random number generators tend to be slow. They are not designed to be run more than a few times in cryptography, which makes them unsuitable for use in applications in which speed is necessary, like simulation.

This paper deals with RNGs which are not of cryptographic quality, but are nonetheless useful. These RNGs combine speed with memory complexity and quality of output.

B. This Project

In this project, we study and implement a few common random number generators in C++, from those which have been used historically, to those which are most commonly in use today. We test our generators using the Dieharder test suite [5]. Using Dieharder, we can push these RNGs to the point of failure, and therein see their flaws and sutability for various applications. We can also compare our results with the results of the RNGs built into the GNU Scientific Library, or GSL, and thus Dieharder. All of the software written for this project is available on Github [6].

In this paper, we first discuss the methods and challenges of testing random numbers in Section II. Then, we discussed the different classes of RNGs we study in Section III. Finally, we describe our software approach in Section IV and share our results in Section V.

II. TESTING RANDOM NUMBER GENERATORS

Testing random number generators can be tricky. An ideal random number generator can be considered to be independently, identically distributed samples of a uniform distribution U(0,1). However, the RNGs that we consider here are not truly random. So, the crux of the problem is how to determine what set of numbers appear random enough, such that they are suitable for use.

A. The Empirical Approach

Imagine flipping a coin 10 times and recording the number of heads and tails. For a fair coin, one would expect to get roughly the same number of heads and tails. If one got 10 heads, and only 1 tails, one might be inclined to suspect that this coin might not be a fair and truly random coin. However, this event has a distinct nonzero probability of this happening, described by the pdf of the binomial distribution:

$$\binom{10}{9} \frac{1}{2}^9 \frac{1}{2} = 0.00977$$

In other words, even for a fair coin, in 1000 trials of 10 coin flips, one would expect to get 9 heads and 1 tails 9 or 10 times. Similarly, imagine if one had a different coin, and ran this same test, but always got exactly 5 heads and 5 tails, for all 1000 trials. Though on average we expect to get about the same number of heads and tails, this coin is also suspect, because for all these repeated trials, we should expect them to follow the binomial distribution discussed above.

If we increased the number of flips per trial to a very large n, and increased the number of trials to a very large t, increasingly the distribution of what we expect to see is a normal distribution, with mean heads percentage of $\mu=0.5$. This is verified by the Central Limit Theorem [7].

So taking again our mystery coin, if we apply the test with reasonably sized n and t, and get a distribution of

our sample means, we expect it to resemble a normal distribution, but reasonable n and t it will be close, but not perfect. There is a certain probability, if we assume that the underlying RNG is perfect, that the result we got would occur; a number on the range (0,1). We shall call this our p-value. If this p-value is very, very small (on the order of 10^{-6}), we might say with a certain degree of confidence that our assumption that the RNG is good is incorrect. However, we could be more confident if we again repeated this process several times, and looked at the distribution of p-values. Then, we could again find the p-value associated with getting this distribution, which we expect to be uniform on the range U(0,1).

We can find the probability of getting our p-value distribution using a Kolmogorov-Smirnov test [], which quantifies the difference between the expected distribution and the p-valuedistribution we get. This test yields a second p-value: the probability that the resultant distribution would occur given that the underlying RNG is indeed indistinguishable from a perfect one.

If this second *p*-value is low, then we can safely decide that the RNG being tested is not good. If this value is high, then, rather than accept that the RNG is 'good', instead we conclude that we cannot reject our hypothesis that it is 'good'.

In fact, this process is exactly what the Dieharder test suite does, and interested readers are encouraged to see [8] for further information. Our implementations of RNGs are used to pipe random numbers to Dieharder, which does this sort of analysis for several different kinds of tests, which are discussed next in Section II-B

B. Dieharder

Dieharder's man page states that "[...]dieharder can eventually contain all rng tests that prove useful in one place[...]" [5]. It aims to be a one stop-shop for testing RNGs. It is the spiritual successor and improvement to George Marsagalia's Diehard testing tool, which in turn is a testing tool which took many tests from the famous

Donald Knuth [9]. Though it is not the only set of tests or testing suite of this kind [10], [9], [11], [12], it holds the distinction of being readily available in the Ubuntu package repository, and having good documentation [8].

Dieharder has many tests, listed in Table I. It is worth discussing a few of the tests available in Dieharder to give the reader an idea of what sort of things are tested, and furthermore, what failing one of these tests might indicated about the quality of an RNG. Further information about tests not discussed is available in the Dieharder man pages and help flags.

- 1) The STS Monobit Test: Taken from the NIST Statistical Test Suite [11], this test is exactly the test described above in Section II-A. The number of ones are counted in a bit stream generated by a random number generator, and the same analysis is done on it. It is not an extremely rigorous test; some bad RNGs will still pass it, this test is good at weeding out extremely poor RNGs.
- 2) The Diehard Birthdays Test: Taken from Diehard, the Birthdays Test is so named for the Birthday Paradox: That in some set of n randomly chosen people in a room, the probability that two of them share the same birthday becomes high astonishingly quickly, reaching 99.9% at n=70 [13]. If these birthdays are placed in a year then the distance between pairs birthdays should follow a Poisson distribution. The test in Dieharder places 512 birthdays in a 24 bit 'year' and determines if the the resultant distribution is in fact Poisson using the p-value analysis described above.
- 3) RGB Lagged Sums: Written by the main Dieharder author Robert G. Brown, this test is the only test in the Dieharder suite which tests for lagged correlations. Imagine that overall, an RNG's output seemed very random, but every seven bits, the same pattern emerged throughout the generation. This test tests for that, with several different lag numbers, when running all tests. The lagged bits are taken, used to create single precision numbers between 0 and 1, then t of these numbers are

 $\label{eq:table I} \mbox{TABLE I}$ Available tests in Dieharder version 3.31.1.

#	Test Name	Reliability
0	Diehard Birthdays	Good
1	Diehard OPERM5	Good
2	Diehard 32x32 Binary Rank	Good
3	Diehard 6x8 Binary Rank	Good
4	Diehard Bitstream	Good
5	Diehard OPSO	Suspect
6	Diehard OQSO	Suspect
7	Diehard DNA	Suspect
8	Diehard Count the 1s (stream)	Good
9	Diehard Count the 1s (byte)	Good
10	Diehard Parking Lot	Good
11	Diehard Minimum Distance (2d Circle)	Good
12	Diehard 3d Sphere (Minimum Distance)	Good
13	Diehard Squeeze	Good
14	Diehard Sums	Don't Use
15	Diehard Runs	Good
16	Diehard Craps	Good
17	Marsaglia and Tsang GCD	Good
100	STS Monobit	Good
101	STS Runs	Good
102	STS Serial (Generalize)	Good
200	RGB Bit Distribution	Good
201	RGB Generalized Minimum Distance	Good
202	RGB Permutations	Good
203	RGB Lagged Sum	Good
204	RGB Kolmogorov-Smirnov	Good
205	Byte Distribution	Good
206	DAB DCT	Good
207	DAB Fill Tree	Good
208	DAB Fill Tree 2	Good
209	DAB Monobit 2	Good

summed. A single trial should have a mean $\mu=0.5t$. Then, the p-values are determined from several trials of t sample sums. Interested readers are encouraged to see [8] for a more discussion.

C. Interpreting Dieharder Results

The authors of Dieharder are careful to avoid saying that Dieharder can verify that a random number generator appears truly random. Rather, Dieharder serves as a set of tests which can weed out poor RNGs, and say with certainty that they do not appear truly random under scrutiny. This is not to say that they are not useful; for instance, if one is simply creating a website which provides a virtual die for a user to roll, then the RNG powering the die need not necessarily pass every Dieharder test (perhaps only the Diehard Craps Test, which specifically tests using an RNG to power dice for a game), but rather pass a majority of them, and still fulfill the requirements. However, if one is running Monte Carlo simulations, an RNG of a higher quality may be desired, which passes more tests.

A system designer must take into account the trade offs between quality of RNG output, memory efficiency, speed, and complexity of implementation when choosing an RNG for a system. These days, with computer being as fast as they are, and many programming languages having already chosen a de facto RNG, this choice is hidden from most users, but is still relevant to those who work in large simulations, mathematicians, and those concerned with extremely high quality of randomness and speed.

What does failing a Dieharder test look like? We look back to the p-value analysis; This final p-value represents the probability that, given that the underlying PRNG resembles a true RNG, the series of our tests would yield the results that they did. The final p-value is a probability on the range (0,1). If this probability is extremely low or extremely high, then the result is considered to be a test failure.

In Dieharder specifically, if the p-value p is p > %99.95 or p < %0.05, then the test is regarded as failed, which is an extremely high threshold. If p > %99.5 or p < %0.5, then the test is marked as weak performance on the part of the RNG. In either the case of the failure or weakness result, it may be worth re-running the test using a different seed to see if this result is consistent. After all, there is some degree of randomness involved,

and finding an area of zero ambiguity is nigh impossible.

D. The Theoretical Approach

Apart from the empirical approach described above and used in Dieharder, there is also theoretical analysis that can be done with a priori knowledge of the RNG's implementation. For instance, the period of an RNG can be time consuming and memory inefficient to measure empirically, but with knowledge of the generating algorithm, can be deduced. Additionally some RNG algorithms (specifically the Linear Congruential Generator discussed in Section III-A) have a property where their output falls in planes which can be determined easily, if one knows where to look.

This sort of analysis exposes flaws of specific generator algorithms, but doesn't always provide an even footing on which to analyze the RNGs. The periods of the generators are discussed in each RNG class's section, along with other strengths and weaknesses, but the focus of our project is on the performance of these RNGs in Dieharder.

III. CLASSES OF RANDOM NUMBER GENERATORS

Here we describe a few different kinds of random number generators, the math that makes them work, give examples of each kind, and give their strengths and weaknesses.

A. Linear Congruential Generators

The Linear Congruential class of RNGs, or LCG for short, is a very old and relatively simple random number generator. They are based on the formula for a line, modulo another number. The following recurrence relation defines the LCG.

$$X_{n+1} = (aX_n + c) \mod m \tag{1}$$

TABLE II
TABLE OF COMMON LCG PARAMETERS.

Name	m	a	c
MINSTD	$2^{32}-1$	48271	0
glibc	2^{31}	1103515245	12345
RANDU	2^{31}	65539	0

Where the parameters are chosen with the following restraints:

$$m, \qquad 0 < m$$
 $a, \qquad 0 < a < m$
 $c, \qquad 0 \le c < m$
 $X_0, \qquad 0 \le X_0 < m$

If c = 0, this particular class of RNG is called a Lehmer, or Park-Miller RNG [14], [15].

The period of such generators depends heavily on the chosen parameters. It can be at most m, and as a result, m is often chosen to be the largest number which can fit in the number of bits of the output; usually 2^{32} or 2^{64} . Some common parameter sets in use include MINSTD, and glibc. A set of parameters notoriously deemed unfit for use is called RANDU, and is discussed below. Values for these parameters can be found in Table II.

- 1) Strengths: LCG generators are tiny. They store a single word of state, are easy to seed, and with proper parameter choosing can be quite effective RNGs. However, some of the flaws greatly outweigh the lightweight and speed benefits of LCGs for all but the most basic of platforms, discussed next.
- 2) Weaknesses: LCGs have a fatal flaw, that is amplified by bad parameter choosing: their outputs fall in easily identifiable planes, as proved by Marsaglia [16]. This is most easily demonstrated by viewing the output of a notoriously bad set of parameters: RANDU. In Figure 1, the output of RANDU is treated as (x, y, z) pairs as it is generated, then these points are plotted.

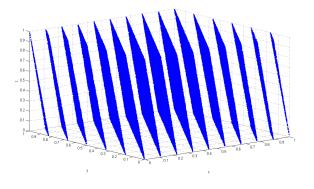


Fig. 1. The problem with LCGs demonstrated by RANDU; a MATLAB plot of consecutive outputs from RANDU used as (x,y,z) points and plotted [18].

It is obvious that all of the output falls in the same set of planes, and is not even an approximation of a truly random number generator. Better parameter choices alleviate this phenomenon by adding the number of planes that would come up in a test like this, and making them closer together, but the basic problem is unavoidable.

Another issue is the period length; at most the period length is m, which cannot be easily increased without increasing the number of bits in the word being operated on, which is not practical on modern architectures. In fact, experts recommend not even considering generators with periods $< 2^{50}$ for anything but the most trivial uses [17].

Due to these problems, most LCGs pass some tests in Dieharder, but do not stand up to more intense scrutiny, like the lagged sums tests. RANDU's performance is patently awful, and stands up to its infamy. MINSTD fares better, but still does not pass as many tests as more sophisticated generators.

Despite these flaws, these extremely small and fast RNGs may still be suited to small embedded architectures and applications where speed is significantly more important than quality.

B. Xorshift Generators

A far more attractive choice than LCGs for those trying to implement RNGs with a lot of memory constraints, speed requirements, or a combination of the two on an embedded platform, is the Xorshift generator. Discovered and described by George Marsaglia [19], they are significantly more adept at creating sufficiently long periods for more applications.

Xorshift RNGs work by keeping a small amount of state (in many example implementations, four numbers), then repeatedly XORing these numbers with shifted versions of themselves. By doing this, the period of the generation can be $2^{32*4} = 2^{128}$ with very little code. The following is a short example for how easily Xorshift generators can be implemented. Let t, x, y, and w be seed values. Then, let a, b, and c be the parameters of the RNG. Then, the C style code is as simple as the following:

```
// Random seed numbers
uint32_t t, x, y, w;
// Fixed constants for shifting
const uint32_t a, b, c;
uint32_t get_rand(void) {
    t = x ^ (x << a);
    x = y;
    y = z;
    z = w;
    w = w ^ (x >> b) ^ t ^ t( >> c);
    return w;
}
```

Picking parameters for the directions and amounts to shift each state variable by is also relatively easy, and is discussed in [19], along with every set of appropriate parameters a, b, and c for 32 bit and 64 bit words.

1) Strengths: Xorshift RNGs are very fast on modern architectures, and use very little state. They have longer periods than LCGs, and are easier to choose parameters

for. These RNGs also do far better on the Dieharder tests than LCGs, and pass the majority of them rather convincingly.

2) Weaknesses: However, the periods of Xorshift generators are not as large as some other generators. They are suitable for most uses, but in large simulations and Monte Carlo analysis, which both use massive amounts of random numbers, the relatively small period could affect results.

C. Lagged Fibonacci Generators

Lagged Fibonacci Generators, or LFGs, owe their name to the general form of the recurrence relation that defines them, which is reminiscent of the Fibonacci recurrence relation:

$$X_n \equiv (X_{n-r} \star X_{n-s}) \mod m, \quad 0 < r < s$$
 (2)

Here, \star can be any operation, usually addition, subtraction, or logical XOR, and m is a modulus which ensures the output is in a proper range. Usually, $m=2^{32}-1$, to give maximum period and avoid correlation issues that can arise when $m=2^32$. The generator stores the past s items of state, then uses the recurrence relation above in Equation 2 to generate the next output. The two lag constants r and s are specially chosen to avoid correlations.

For example, in a popular implementation called R250, \star is defined as XOR, r=147, and s=250 [20]. Another popular implementation is RANLUX, which adds a few wrinkles to a simpler recurrence style generator, called Subtract with Carry [21], [22]:

$$X_n \equiv (X_{n-r} - X_{n-s} - c_{n-1}) \mod m \tag{3}$$

Here, r and s are the usual lag constants where 0 < r < s, and c is defined as:

$$c_n = 1$$
 if $X_{n-r} - X_{n-s} - c_{n-1} \ge 0$, $c_n = 0$ otherwise.

RANLUX takes this generator and adds skipping element parameter p, designed to remove unwanted correlations at the expense of speed. After 24 random numbers are generated, p-24 random numbers are thrown away [23], [24]. The default C++11 parameters for the RANLUX 24 bit engine are r=10, s=24, p=24, which results in no numbers being thrown away, increasing speed, but reducing effectiveness.

- 1) Strengths: Lagged Fibonacci generators can store a wide range of amount of state, but their flexibility results in many generators of this type being created and seeing common use. The operations are relatively fast, and have larger periods when a few different twist like the subtract with carry has been applied [22]. As a result, good implementations generally do well on the Dieharder tests, passing most, and only getting weak on a some, sporadically.
- 2) Weaknesses: LFGs have a wrinkle in understanding their simplicity; they are difficult to seed properly, and require special initialization to make sure that there are no linear correlations in the initial seed data, lest the entire generator become extremely predictable [25]. They are in general, slower and require more state than Xorshift generators, and do not have periods as large as Xorshift or Multiply with Carry Generators, discussed next.

D. Multiply With Carry Generators

- 1) Strengths:
- 2) Weaknesses:

E. Mersenne Twister Generators

This section will describe the Mersenne Twister class of generators.

- 1) Strengths:
- 2) Weaknesses: http://en.wikipedia.org/wiki/ Mersenne_twister

IV. SOFTWARE IMPLEMENTATION

For this project, we use the Dieharder binary on Ubuntu in its raw input mode. This allows us to use a shell pipe to send raw random numbers from an arbitrary generator into Dieharder for analysis.

There are two major components included in our code: C++ source to build an RNG binary, and a small Python script to call the RNG binary and pipe it into Dieharder appropriately. We chose C++ because these tests can take a long time if the generator is slow, and C++ is a good compromise between its ability to allow for modular code and its speed.

The specific RNG algorithms implemented are as follows:

- Mersenne Twister
- RANDU
- MINSTD
- R250
- RANLUX
- Xorshift
- CMWC

Each RNG algorithm inherits from a common base class, which allows for the RNG binary to choose the RNG in use via a command line argument. Random 32 bit numbers are written to stdout in raw binary, which is in turned piped to Dieharder for analysis. Finally, the output of Dieharder can be optionally piped to file.

All code for this project is available on Github [6], with some selected source files in Appendix B.The project was tested using Ubuntu 14.04, gcc version 4.9.1, and Python version 3.4.2. Note that Dieharder is required to run examples, and can be installed via your package manager if available, or built from source [5].

V. RESULTS AND ANALYSIS

Describe the results of the dieharder tests for our implementations. Discuss speed, and suitability for simulation.

VI. CONCLUSION

Talk about the generators.

[26] Marsaglia giving a better MCCSFWCW gen than twister.

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APPENDIX A

RESULTS FROM DIEHARDER

This section includes the raw results outputs from a run of Dieharder for some of our implemented RNGs. Plaintext files with these results, and the full results for the rest of the RNGs, can be found in the Github repository [6].

A. Mersenne Twister

```
dieharder version 3.31.1 Copyright 2003 Robert G. Brown
#-----
            |rands/second|
                          Seed
  rng name
stdin_input_raw| 3.69e+06 | 334501002|
#-----#
      test_name | ntup| tsamples | psamples| p-value | Assessment
#-----
  diehard_birthdays| 0| 100| 100|0.94658958| PASSED
    diehard_operm5| 0| 1000000| 100|0.96198385| PASSED
 diehard_rank_32x32| 0| 40000| 100|0.24240504| PASSED diehard_rank_6x8| 0| 100000| 100|0.56033672| PASSED
  diehard_bitstream|
                       2097152|
                                   100|0.36069880| PASSED
                   0.1
                   0| 2097152|
                                100|0.40862193| PASSED
      diehard_opso|
      diehard_oqso|
                    0| 2097152| 100|0.45443937| PASSED
       diehard_dna|
                   0| 2097152|
                                100|0.06000922| PASSED
                       256000|
diehard_count_1s_str|
                                100|0.17495967| PASSED
                   0 1
                       256000|
diehard_count_1s_byt|
                   0 |
                                   100|0.79645250| PASSED
                   0| 12000| 100|0.43824831| PASSED
diehard_parking_lot|
   diehard_2dsphere|
                   2 |
                        8000| 100|0.17246784| PASSED
                   3|
   diehard_3dsphere|
                         4000| 100|0.16472438| PASSED
   diehard_squeeze|
                    0 |
                        100000|
                                  100|0.60317887| PASSED
      diehard_sums|
                   0 |
                        100|
                                   100|0.02682330| PASSED
                   0| 100000|
      diehard_runs|
                                100|0.60254832| PASSED
      diehard_runs|
                   0| 100000|
                                100|0.46677063| PASSED
                   0| 200000|
     diehard_craps|
                                 100|0.32427347| PASSED
     diehard_craps|
                   0 |
                       200000|
                                  100|0.27961217| PASSED
marsaglia_tsang_gcd|
                   0| 10000000|
                                   100|0.23485073| PASSED
                   0| 10000000|
                                  100|0.82596264| PASSED
marsaglia_tsang_gcd|
       sts_monobit|
                   1| 100000| 100|0.85246403| PASSED
                   2| 100000|
                                100|0.35817371| PASSED
         sts_runs|
        sts_serial|
                   1 |
                       100000|
                                   100|0.74162598| PASSED
                   2| 100000|
                                   100|0.16597190| PASSED
        sts_serial|
        sts_serial|
                   3| 100000|
                                100|0.91870927| PASSED
        sts_serial|
                   3| 100000|
                                 100|0.60604836| PASSED
                   4 | 100000 |
                                  100|0.49807683| PASSED
        sts_serial|
                       100000|
        sts_serial|
                                   100|0.73416252| PASSED
                   4 |
        sts_serial| 5| 100000|
                                   10010.995005831
                                                 WEAK
        sts_serial| 5| 100000|
                                100|0.82089520| PASSED
        sts_serial| 6| 100000|
                                100|0.69150250| PASSED
                    6| 100000|
                                   100|0.90675682| PASSED
        sts_serial|
                   7 |
        sts_serial|
                        100000|
                                   100|0.50223133| PASSED
                                   100|0.25121204| PASSED
        sts_serial|
                   7| 100000|
                   8 | 100000 |
                                 100|0.79597609| PASSED
        sts_serial|
                   8 | 100000 |
                                 100|0.74387173| PASSED
        sts serial|
                       100000|
                                   100|0.48188135| PASSED
        sts_serial|
                    9|
                                   100|0.32245638| PASSED
        sts_serial|
                    9|
                         100000|
```

```
100000|
                                             100|0.85675457|
          sts_serial|
          sts_serial|
                        101
                                100000|
                                             100|0.58565755|
                                                               PASSED
          sts_serial|
                                100000|
                                             100|0.27398289|
                                                               PASSED
                        111
          sts_serial|
                        11|
                                100000|
                                             100|0.96699373|
                                                               PASSED
          sts_serial|
                        12 I
                                100000|
                                             100|0.99571085|
                                                                WEAK
                                             100|0.99998250|
          sts_serial|
                        12|
                                100000|
                                                                WEAK
          sts_serial|
                        13 I
                                100000|
                                             100|0.83769749|
                                                               PASSED
          sts_serial|
                                100000|
                                             100|0.70406949|
                                                               PASSED
                        13 I
          sts_serial|
                        14|
                                100000|
                                             100|0.33108799|
                                                               PASSED
                                1000001
                                             100|0.33874542|
          sts_serial|
                        141
                                                               PASSED
                                             100|0.62491377|
          sts_serial|
                        15 I
                                100000|
                                                               PASSED
          sts_serial|
                        15|
                                100000|
                                             100|0.97355969|
                                                               PASSED
          sts_serial|
                        161
                                100000|
                                             100|0.52289877|
                                                               PASSED
          sts_serial|
                        161
                                100000|
                                             100|0.91101554|
                                                               PASSED
                                1000001
                                             100|0.71168623|
         rgb_bitdist|
                         1 |
                                                               PASSED
         rgb_bitdist|
                         21
                                100000|
                                             100|0.50192972|
                                                               PASSED
         rgb_bitdist|
                         31
                                1000001
                                             100|0.98142915|
                                                               PASSED
                                100000|
                                             100|0.77984554|
         rgb_bitdist|
                         4 |
                                                               PASSED
                                             100|0.66101093|
         rgb_bitdist|
                         5|
                                100000|
                                                               PASSED
         rgb_bitdist|
                                100000|
                                             100|0.91816382|
                         6|
                                                               PASSED
         rgb_bitdist|
                         7 |
                                100000|
                                             100|0.80046681|
                                                               PASSED
         rgb_bitdist|
                                100000|
                                             100|0.79769030|
                                                               PASSED
                         81
         rgb_bitdist|
                         9 |
                                100000|
                                             100|0.39761538|
                                                               PASSED
         rgb_bitdist|
                        10|
                                100000|
                                             100|0.72563831|
                                                               PASSED
         rgb_bitdist|
                                100000|
                                             100|0.94635747|
                        111
                                                               PASSED
                                100000|
                                             100|0.00790713|
         rgb_bitdist|
                        12|
                                                               PASSED
rgb_minimum_distance|
                                 10000|
                                            1000|0.66619425|
                                                               PASSED
                         21
rgb_minimum_distance|
                                 10000|
                                            1000|0.29126310|
                                                               PASSED
                         31
rgb_minimum_distance|
                                 10000|
                                            1000|0.61539740|
                                                               PASSED
                         4 |
                                            1000|0.69380013|
rgb_minimum_distance|
                         5|
                                 100001
                                                               PASSED
                                             100|0.54292104|
    rgb_permutations|
                         21
                                100000|
                                                               PASSED
                                100000|
                                                               PASSED
    rgb_permutations|
                         31
                                             100|0.84339338|
    rgb_permutations|
                         4 1
                                100000|
                                             100|0.65721535|
                                                               PASSED
    rgb_permutations|
                         5 I
                                1000001
                                             100|0.63741550|
                                                               PASSED
                                             100|0.91499091|
      rgb_lagged_sum|
                         01
                               1000000|
                                                               PASSED
      rgb_lagged_sum|
                         1 |
                               1000000|
                                             100|0.58803936|
                                                               PASSED
                               1000000|
                                             100|0.45161465|
                                                               PASSED
      rgb_lagged_sum|
                         2 |
                               1000000|
                                             100|0.19256312|
      rgb_lagged_sum|
                         3 I
                                                               PASSED
                               1000000|
                                             100|0.78964801|
                                                               PASSED
      rgb_lagged_sum |
                         4 |
      rgb_lagged_sum|
                         5 |
                               1000000|
                                             100|0.99999945|
                                                               FAILED
      rgb_lagged_sum |
                         61
                               10000001
                                             100|0.92564798|
                                                               PASSED
      rgb_lagged_sum|
                         7 |
                               1000000|
                                             100|0.42382792|
                                                               PASSED
      rgb_lagged_sum|
                         8 |
                               1000000|
                                             100|0.86728057|
                                                               PASSED
                               1000000|
                                             100|0.94533364|
      rgb_lagged_sum|
                         91
                                                               PASSED
                        10|
                               1000000|
                                             100|0.86319260|
                                                               PASSED
      rgb_lagged_sum|
                               1000000|
                                             100|0.67230198|
                                                               PASSED
      rgb_lagged_sum|
                        11 I
                               1000000|
                                             100|0.60087872|
      rgb_lagged_sum|
                        12|
                                                               PASSED
                               1000000|
      rgb_lagged_sum|
                        13|
                                             100|0.53686765|
                                                               PASSED
                                             100|0.59498101|
      rgb_lagged_sum|
                        14|
                               1000000|
                                                               PASSED
      rgb_lagged_sum|
                        15|
                               10000001
                                             100|0.25928645|
                                                               PASSED
      rgb_lagged_sum|
                        161
                               1000000|
                                             100|0.99649444|
                                                                WEAK
                        17|
                               1000000|
                                             100|0.57762461|
                                                               PASSED
      rgb_lagged_sum|
                        18|
                               1000000|
                                             100|0.61051907|
                                                               PASSED
      rgb_lagged_sum|
                               1000000|
                                             100|0.99642829|
      rgb_lagged_sum|
                        19|
                                                                WEAK
                               1000000|
                                             100|0.70037387|
      rgb_lagged_sum|
                        201
                                                               PASSED
                               1000000|
                                             100|0.48495808|
                                                               PASSED
      rgb_lagged_sum|
                        21|
      rgb_lagged_sum|
                        22 |
                               1000000|
                                             100|0.95914643|
                                                               PASSED
```

10 I

PASSED

```
1000000|
                                       100|0.30312748| PASSED
     rgb_lagged_sum| 23|
     rgb_lagged_sum| 24| 1000000|
                                     100|0.26160988| PASSED
                                     100|0.13145792| PASSED
     rgb_lagged_sum| 25|
                         1000000|
     rgb_lagged_sum| 26|
                          1000000|
                                       100|0.84738587| PASSED
     rgb_lagged_sum| 27|
                          1000000|
                                       100|0.16458415| PASSED
                          1000000|
                                     100|0.12698620| PASSED
     rgb_lagged_sum| 28|
     rgb_lagged_sum| 29|
                          1000000|
                                     100|0.96405239| PASSED
     rgb_lagged_sum| 30|
                          1000000|
                                       100|0.67856463| PASSED
     rgb_lagged_sum| 31|
                          1000000|
                                       100|0.24194016| PASSED
     rgb_lagged_sum| 32|
                         1000000|
                                      100|0.37704298| PASSED
    rgb_kstest_test| 0| 10000| 1000|0.65808472| PASSED
    dab_bytedistrib| 0| 51200000|
                                       1|0.63940335| PASSED
                                         1|0.31841243| PASSED
            dab_dct| 256|
                            500001
Preparing to run test 207. ntuple = 0
       dab_filltree| 32| 15000000|
                                        1|0.88641557| PASSED
       dab_filltree| 32| 15000000|
                                        1|0.89984663| PASSED
Preparing to run test 208. ntuple = 0
      dab_filltree2| 0|
                         5000000|
                                         1|0.61511593| PASSED
      dab_filltree2| 1|
                         5000000|
                                        1|0.50735769| PASSED
Preparing to run test 209. ntuple = 0
       dab_monobit2| 12| 65000000|
                                       1|0.27042876| PASSED
```

B. RANDU

```
#______#
        dieharder version 3.31.1 Copyright 2003 Robert G. Brown
#-----#
  rng_name |rands/second| Seed
stdin_input_raw| 7.88e+06 |3038070828|
#-----#
     test_name |ntup| tsamples |psamples| p-value |Assessment
#-----#
  diehard_birthdays|
                 0| 100|
                                100|0.00000000| FAILED
    diehard_operm5| 0| 1000000|
                              100|0.00000000| FAILED
 diehard_rank_32x32| 0| 40000|
                              100|0.00000000| FAILED
  diehard_rank_6x8| 0| 100000|
                              100|0.00000000| FAILED
                  0| 2097152|
                              100|0.00000000| FAILED
  diehard_bitstream|
                             100|0.00000000| FAILED
     diehard_opso| 0| 2097152|
     diehard_oqso| 0| 2097152| 100|0.00000000| FAILED
      diehard_dna| 0| 2097152| 100|0.00000000| FAILED
                             100|0.00000000| FAILED
diehard_count_1s_str|
                  0| 256000|
diehard_count_1s_byt|
                     256000|
                                100|0.00000000| FAILED
                  01
                     12000|
                                100|0.00000000| FAILED
diehard_parking_lot|
                  0.1
  diehard_2dsphere|
                  2 |
                      80001
                              100|0.00000000| FAILED
  diehard_3dsphere|
                  3|
                       4000|
                               100|0.00000000| FAILED
                                100|0.00000000| FAILED
                     100000|
                  0 |
   diehard_squeeze|
      diehard_sums|
                       1001
                                100|0.00000000| FAILED
                  0 [
                  0| 100000|
                                100|0.00581517| PASSED
     diehard_runs|
     diehard_runs|
                  0| 100000|
                                100|0.00088099| WEAK
     diehard_craps|
                  0| 200000|
                                100|0.00000000| FAILED
                  0| 200000|
                                100|0.00000000| FAILED
     diehard_craps|
                  0| 10000000|
marsaglia_tsang_gcd|
                                100|0.00000000| FAILED
                  0| 10000000|
marsaglia_tsang_gcd|
                                100|0.00000000| FAILED
                  1 | 100000|
                                100|0.00132032| WEAK
      sts_monobit|
                     100000|
                                100|0.05116931| PASSED
        sts_runs|
                  21
                                100|0.04426849| PASSED
                     100000|
       sts_serial|
                  1 |
                                100|0.00000000| FAILED
       sts_serial|
                  21
                      100000|
```

```
100|0.00000000|
          sts_serial|
                         31
                               100000|
                                                             FAILED
          sts_serial|
                               100000|
                                            100|0.00000000|
                                                             FAILED
                         4 |
          sts_serial|
                         4 |
                               100000|
                                            100|0.00000000|
                                                              FAILED
          sts_serial|
                         5 I
                               100000|
                                            100|0.00000000|
                                                             FAILED
                                            100|0.00000000| FAILED
          sts_serial|
                         5 I
                               100000|
          sts_serial|
                         6 I
                               100000|
                                            100|0.00000000|
                                                             FAILED
                               100000|
          sts_serial|
                                            100|0.00000000|
                                                             FATLED
                         61
          sts_serial|
                               100000|
                                            100|0.00000000|
                                                             FAILED
                         7 I
                               1000001
                                            100|0.00000000|
          sts_serial|
                         7 I
                                                             FATLED
                               100000|
                                            100|0.00000000| FAILED
          sts_serial|
                         81
          sts_serial|
                         8 |
                               100000|
                                            100|0.00000000|
                                                             FAILED
          sts_serial|
                         91
                               100000|
                                            100|0.00000000|
                                                             FAILED
          sts_serial|
                         91
                               100000|
                                            100|0.00000000|
                                                             FAILED
                               1000001
                                            100|0.00000000| FAILED
          sts_serial|
                       101
          sts_serial|
                        10|
                               100000|
                                            100|0.00000000| FAILED
          sts_serial|
                       111
                               1000001
                                            100|0.00000000| FAILED
                               100000|
                                            100|0.00000000| FAILED
          sts_serial|
                        111
                                            100|0.00000000|
          sts_serial|
                       12|
                               100000|
                                                             FAILED
          sts_serial|
                               100000|
                                            100|0.00000000| FAILED
                       12 I
          sts_serial|
                       13|
                               100000|
                                            100|0.00000000| FAILED
          sts_serial|
                               100000|
                                            100|0.00000000|
                                                             FAILED
                       13 I
          sts_serial|
                        141
                               100000|
                                            100|0.00000000|
                                                             FAILED
          sts_serial|
                        141
                               100000|
                                            100|0.00000000|
                                                             FAILED
          sts_serial|
                               100000|
                                            100|0.00000000| FAILED
                       15 I
                               100000|
                                            100|0.00000000| FAILED
          sts_serial|
                       15|
          sts_serial|
                               100000|
                                            100|0.00000000| FAILED
                       161
          sts_serial|
                        16|
                               100000|
                                            100|0.00000000|
                                                             FAILED
         rgb_bitdist|
                               100000|
                                            100|0.00000000|
                                                             FAILED
                         11
                               100000|
                                            100|0.00000000| FAILED
         rgb_bitdist|
                         2 |
                               100000|
                                            100|0.00000000| FAILED
         rgb_bitdist|
                         3 I
                               100000|
                                                             FAILED
         rgb_bitdist|
                         4 |
                                            100|0.00000000|
         rgb_bitdist|
                               100000|
                                            100|0.00000000|
                                                             FAILED
         rgb_bitdist|
                         61
                               1000001
                                            100|0.00000000|
                                                             FAILED
                                            100|0.00000000| FAILED
         rgb_bitdist|
                         7 I
                               100000|
         rgb_bitdist|
                         8 |
                               100000|
                                            100|0.00000000| FAILED
         rgb_bitdist|
                               100000|
                                            100|0.00000000| FAILED
                         91
         rgb_bitdist|
                               100000|
                                            100|0.00000000|
                        10 I
                                                             FAILED
         rgb_bitdist|
                               1000001
                                            100|0.00000000| FAILED
                       111
         rgb_bitdist|
                        12|
                               100000|
                                            100|0.00000000| FAILED
rgb_minimum_distance|
                         2.1
                                100001
                                           1000|0.00000000|
                                                             FAILED
                                10000|
rgb_minimum_distance|
                         3 I
                                           1000|0.00000000|
                                                             FAILED
rgb_minimum_distance|
                         4 |
                                10000|
                                           1000|0.00000000|
                                                             FAILED
                                10000|
                                           1000|0.00000000|
                                                             FAILED
rgb_minimum_distance|
                         5 I
    rgb_permutations|
                               100000|
                                            100|0.97069761|
                                                             PASSED
    rgb_permutations|
                               100000|
                                            100|0.28310835|
                                                             PASSED
                         3 I
                               100000|
                                            100|0.66914232|
    rgb_permutations|
                         4 |
                                                             PASSED
                               100000|
                                            100|0.00000705|
    rgb_permutations|
                         5 I
                                                               WEAK
                              1000000|
                                            100|0.00000000| FAILED
      rgb_lagged_sum|
                         01
      rgb_lagged_sum|
                         11
                              10000001
                                            100|0.00000000|
                                                             FATLED
      rgb_lagged_sum|
                         21
                              1000000|
                                            100|0.00000000|
                                                             FATLED
      rgb_lagged_sum|
                              1000000|
                                            100|0.00000000|
                                                             FAILED
                         31
                              1000000|
                                            100|0.00000000|
                                                             FAILED
      rgb_lagged_sum|
                         4 1
                                            100|0.00000000| FAILED
                              1000000|
      rgb_lagged_sum|
                         5|
                              1000000|
                                            100|0.00000000| FAILED
      rgb_lagged_sum|
                         61
                         7 |
                              10000001
                                            100|0.00000000| FAILED
      rgb_lagged_sum|
      rgb_lagged_sum|
                              1000000|
                                            100|0.00000000| FAILED
```

100000|

3 I

sts_serial|

100|0.00000000| FAILED

```
rgb_lagged_sum| 9| 1000000|
                                    100|0.00000000| FAILED
     rgb_lagged_sum| 10| 1000000| 100|0.00000000| FAILED
     rgb_lagged_sum| 11| 1000000| 100|0.00000000| FAILED
                                      100|0.00000000| FAILED
     rgb_lagged_sum| 12|
                          1000000|
                                   100|0.00000000| FAILED
     rgb_lagged_sum| 13| 1000000|
     rgb_lagged_sum| 14| 1000000| 100|0.00000000| FAILED
     rgb_lagged_sum| 15| 1000000| 100|0.00000000| FAILED
     rgb_lagged_sum| 16| 1000000|
                                   100|0.00000000| FAILED
     rgb_lagged_sum| 17|
                          1000000|
                                      100|0.00000000| FAILED
     rgb_lagged_sum| 18| 1000000| 100|0.00000000| FAILED
     rgb_lagged_sum| 19| 1000000| 100|0.00000000| FAILED
     rgb_lagged_sum| 20| 1000000| 100|0.00000000| FAILED
                         1000000| 100|0.00000000| FAILED
1000000| 100|0.00000000| FAILED
     rgb_lagged_sum| 21|
     rgb_lagged_sum| 22|
     rgb_lagged_sum| 23| 1000000| 100|0.00000000| FAILED
     rgb_lagged_sum| 24| 1000000| 100|0.00000000| FAILED
     rgb_lagged_sum| 25| 1000000| 100|0.00000000| FAILED
     rgb_lagged_sum| 26|
                         1000000| 100|0.00000000| FAILED
1000000| 100|0.00000000| FAILED
     rgb_lagged_sum| 27|
     rgb_lagged_sum| 28| 1000000| 100|0.00000000| FAILED
     rgb_lagged_sum| 29| 1000000| 100|0.00000000| FAILED
     rgb_lagged_sum| 30| 1000000| 100|0.00000000| FAILED
     rgb_lagged_sum| 31| 1000000|
                                   100|0.00000000| FAILED
     rgb_lagged_sum| 32| 1000000|
                                     100|0.00000000| FAILED
    rgb_kstest_test| 0| 10000| 1000|0.00000000| FAILED
    dab_bytedistrib| 0| 51200000|
                                      1|0.00000000| FAILED
          dab_dct| 256| 50000|
                                        1|0.00000000| FAILED
Preparing to run test 207. ntuple = 0
       dab_filltree| 32| 15000000|
                                        1|0.00000000| FAILED
       dab_filltree| 32| 15000000|
                                       1|0.00000000| FAILED
Preparing to run test 208. ntuple = 0
                                    1|0.00000000| FAILED
      dab_filltree2| 0| 5000000|
      dab_filltree2| 1| 5000000|
                                        1|0.00000000| FAILED
Preparing to run test 209. ntuple = 0
       dab_monobit2| 12| 65000000|
                                     1|1.00000000| FAILED
```

C. Xorshift

```
dieharder version 3.31.1 Copyright 2003 Robert G. Brown
#-----#
  rng_name |rands/second| Seed |
stdin_input_raw| 7.18e+06 |1616344042|
test_name | ntup| tsamples | psamples| p-value | Assessment
#-----#
 diehard_birthdays| 0|
                            100|0.49902432| PASSED
   ehard_birthdays| 0| 100| 100|0.49902432| PASSED diehard_operm5| 0| 1000000| 100|0.25474793| PASSED
                     1001
 diehard_rank_32x32| 0| 40000| 100|0.03165397| PASSED
  diehard_rank_6x8| 0| 100000| 100|0.25767730| PASSED
 diehard_bitstream| 0| 2097152| 100|0.20672267| PASSED
     diehard_opso| 0| 2097152| 100|0.25133362| PASSED
     diehard_oqso| 0| 2097152| 100|0.66694775| PASSED
     diehard_dna| 0| 2097152| 100|0.75118125| PASSED
diehard_count_1s_str| 0| 256000| 100|0.64648928| PASSED
                   256000|
                          100|0.11279025| PASSED
diehard_count_1s_byt|
                0 |
                           100|0.41532341| PASSED
diehard_parking_lot|
                0 |
                    12000|
```

diehard_2dsphere	2	8000	100 0.65294377	PASSED
diehard_3dsphere		4000	100 0.41726522	PASSED
diehard_squeeze	0	100000	100 0.88235090	PASSED
diehard_sums	0	100	100 0.30287804	PASSED
diehard_runs	0	100000	100 0.61241815	PASSED
diehard_runs	0	100000	100 0.93971074	PASSED
diehard_craps	0	200000	100 0.94690900	PASSED
diehard_craps	0	200000	100 0.88014864	PASSED
marsaglia_tsang_gcd	0	10000000	100 0.66822887	PASSED
marsaglia_tsang_gcd	0	10000000	100 0.23714996	PASSED
sts_monobit	1	100000	100 0.07263718	PASSED
sts_runs	2	100000	100 0.59150620	PASSED
sts_serial	1	100000	100 0.98865452	PASSED
sts_serial	2	100000	100 0.67923671	PASSED
sts_serial	3	100000	100 0.40038667	PASSED
sts_serial	3	100000	100 0.74590304	PASSED
sts_serial	4	100000	100 0.76395907	PASSED
sts_serial	4	100000	100 0.45655805	PASSED
sts_serial	5	100000	100 0.72571182	PASSED
sts_serial		100000	100 0.48061111	PASSED
sts_serial		100000	100 0.81233938	PASSED
sts_serial		100000	100 0.65075997	PASSED
sts_serial		100000	100 0.78242940	PASSED
sts_serial		100000	100 0.54454691	PASSED
sts_serial		100000	100 0.69263905	PASSED
sts_serial		100000	100 0.71216880	PASSED
sts_serial		100000	100 0.71210000	PASSED
		100000	100 0.25173033	PASSED
sts_serial				
sts_serial		100000	100 0.35354245	PASSED
sts_serial		100000	100 0.12568077	PASSED
sts_serial		100000	100 0.99890521	WEAK
sts_serial		100000	100 0.59350010	PASSED
sts_serial		100000	100 0.81969952	PASSED
sts_serial		100000	100 0.98941712	PASSED
sts_serial		100000	100 0.99975291	WEAK
sts_serial		100000	100 0.71872451	PASSED
sts_serial		100000	100 0.99917709	WEAK
sts_serial		100000	100 0.99773009	WEAK
sts_serial	15	100000	100 0.96041847	PASSED
sts_serial	15	100000	100 0.90680839	PASSED
sts_serial	16	100000	100 0.55058080	PASSED
sts_serial	16	100000	100 0.22192587	PASSED
rgb_bitdist	1	100000	100 0.95111713	PASSED
rgb_bitdist	2	100000	100 0.46876584	PASSED
rgb_bitdist	3	100000	100 0.07937752	PASSED
rgb_bitdist	4	100000	100 0.31077302	PASSED
rgb_bitdist	5	100000	100 0.23549435	PASSED
rgb_bitdist	6	100000	100 0.37517346	PASSED
rgb_bitdist	7	100000	100 0.90181028	PASSED
rgb_bitdist	8	100000	100 0.71075597	PASSED
rgb_bitdist	9	100000	100 0.42126443	PASSED
rgb_bitdist	10	100000	100 0.17021069	PASSED
rgb_bitdist	11	100000	100 0.10316838	PASSED
rgb_bitdist		100000	100 0.42217482	PASSED
rgb_minimum_distance		10000	1000 0.24582710	PASSED
rgb_minimum_distance		10000	1000 0.51767092	PASSED
rgb_minimum_distance		10000	1000 0.96320260	PASSED
· · ·				

rgb_minimum_distance	5	10000	1000 0.33004027	PASSED
rgb_permutations	2	100000	100 0.85682126	PASSED
rgb_permutations	3	100000	100 0.97107041	PASSED
rgb_permutations	4	100000	100 0.46006773	PASSED
rgb_permutations	5	100000	100 0.00182706	WEAK
rgb_lagged_sum	0	1000000	100 0.03326173	PASSED
rgb_lagged_sum	1	1000000	100 0.05387456	PASSED
rgb_lagged_sum	2	1000000	100 0.93556085	PASSED
rgb_lagged_sum	3	1000000	100 0.56177954	PASSED
rgb_lagged_sum	4	1000000	100 0.53075714	PASSED
rgb_lagged_sum	5	1000000	100 0.97957264	PASSED
rgb_lagged_sum	6	1000000	100 0.99626119	WEAK
rgb_lagged_sum	7	1000000	100 0.84475689	PASSED
rgb_lagged_sum	8	1000000	100 0.20696248	PASSED
rgb_lagged_sum	9	1000000	100 0.86572183	PASSED
rgb_lagged_sum	10	1000000	100 0.77684529	PASSED
rgb_lagged_sum	11	1000000	100 0.80172300	PASSED
rgb_lagged_sum	12	1000000	100 0.16379969	PASSED
rgb_lagged_sum	13	1000000	100 0.07773692	PASSED
rgb_lagged_sum	14	1000000	100 0.52496663	PASSED
rgb_lagged_sum	15	1000000	100 0.79522715	PASSED
rgb_lagged_sum	16	1000000	100 0.48450975	PASSED
rgb_lagged_sum	17	1000000	100 0.01868482	PASSED
rgb_lagged_sum	18	1000000	100 0.98448891	PASSED
rgb_lagged_sum	19	1000000	100 0.34024310	PASSED
rgb_lagged_sum	20	1000000	100 0.97691977	PASSED
rgb_lagged_sum	21	1000000	100 0.33271752	PASSED
rgb_lagged_sum	22	1000000	100 0.99307319	PASSED
rgb_lagged_sum	23	1000000	100 0.36269171	PASSED
rgb_lagged_sum	24	1000000	100 0.07769534	PASSED
rgb_lagged_sum	25	1000000	100 0.06889774	PASSED
rgb_lagged_sum	26	1000000	100 0.95699166	PASSED
rgb_lagged_sum	27	1000000	100 0.69000388	PASSED
rgb_lagged_sum	28	1000000	100 0.48259760	PASSED
rgb_lagged_sum	29	1000000	100 0.25775601	PASSED
rgb_lagged_sum	30	1000000	100 0.95312206	PASSED
rgb_lagged_sum	31	1000000	100 0.80795102	PASSED
rgb_lagged_sum	32	1000000	100 0.75798961	PASSED
rgb_kstest_test	0	10000	1000 0.77393295	PASSED
dab_bytedistrib	0	51200000	1 0.42869597	PASSED
dab_dct	256	50000	1 0.29261724	PASSED
Preparing to run test	207.	ntuple = 0		
dab_filltree	32	15000000	1 0.90526013	PASSED
dab_filltree	32	15000000	1 0.88055907	PASSED
Preparing to run test		ntuple = 0		
dab_filltree2	0	5000000	1 0.74399501	PASSED
dab_filltree2	1	5000000	1 0.70764739	PASSED
Preparing to run test	209.	ntuple = 0		
dab_monobit2	12	65000000	1 0.99626005	WEAK

APPENDIX B

SELECTED SOURCE FILES

This section includes some source files from the code base. Interested readers are encouraged to view the Github Repository for all code [6].

The first file included is rng.h in Section B-A. This header file defines the interfaces for all the implemented RNGs. The next included sources are xorshift.h and xorshift.cpp, in Sections B-B and B-C, respectively. This should give the reader a feel for what the internals of the generators look like. Finally, the Python calling script, rngs.py in Section B-D, which demonstrates hooking up the produced RNG binary to Dieharder, is included as well.

A. rng.h

The source for rng.h, the basic skeleton of all implemented generators.

```
* rngs
 * ECE 541 Project 2
 * Kashev Dalmia - dalmia3
 * David Huang - huang157
 */
#ifndef RNG_H
#define RNG_H
#include <cstdint> // for fixed width integer types.
 * Convenience typedef for the integer type being used.
typedef uint32_t fuint;
namespace rng
    class RandomNumberGenerator {
    public:
        RandomNumberGenerator() { };
        virtual ~RandomNumberGenerator(){};
        virtual void seed(fuint seed_num) = 0;
        virtual fuint operator()() = 0;
    } ;
#endif /* RNG_H */
```

B. xorshift.h

The source for xorshift.h, an example generator implementation.

```
* rngs
 * ECE 541 Project 2
 * Kashev Dalmia - dalmia3
 * David Huang - huang157
 */
#ifndef XORSHIFT_H
#define XORSHIFT_H
#include "rng.h"
namespace rng
    class Xorshift : public RandomNumberGenerator {
       Xorshift();
       void seed(fuint seed_num);
        fuint operator()();
    private:
        fuint x, y, z, w;
    } ;
}
#endif /* XORSHIFT_H */
```

C. xorshift.cpp

The source for xorshift.cpp, an example generator implementation.

```
* rngs
 * ECE 541 Project 2
 * Kashev Dalmia - dalmia3
 * David Huang - huang157
 */
#include "xorshift.h"
namespace rng
    Xorshift::Xorshift() :
            RandomNumberGenerator(),
            x(0),
            y(0),
            z(0),
            w(0)
    { }
    void Xorshift::seed(fuint seed_num) {
        static constexpr uint64_t g = 48271;
        static constexpr uint64_t n = (1UL << 31UL) - 1UL; // 2^32 - 1
        x = seed_num;
        /*
         * Use MINSTD to finish populating state.
        y = static_cast<fuint>((static_cast<uint64_t>(x) * g) % n);
        z = static_cast<fuint>((static_cast<uint64_t>(y) * g) % n);
        w = static_cast<fuint>((static_cast<uint64_t>(z) * q) % n);
    }
    fuint Xorshift::operator()() {
        fuint t = x ^ (x << 11);
        x = y;
       y = z;
        z = w;
        w = w ^ (w >> 19) ^ t ^ (t >> 8);
        return w;
    }
}
```

D. rngs.py

The source for rngs.py, the main code for the RNG binary.

```
#!/usr/bin/env python3
# rngs
# ECE 541 Project 2
# Kashev Dalmia - dalmia3
# David Huang - huang157
"""_The_called_script_for_this_project._Wraps_the_C++_based_RNG,_passes
____necessary_options_to_it,_and_then_pipes_the_output_to_dieharder._Note_that
____this_script_requires_Python3.
import argparse
import enum
import os
import subprocess
@enum.unique
class Generator(enum.Enum):
    \mathbf{all} = -1
    stl = 0
   mt19937 = 1
    randu = 2
    minstd = 3
   r250 = 4
    ranlux = 5
    xorshift = 6
    cmwc = 7
    # Add more generator types here! Remember to update main.cpp.
def check_generator_type(value):
    try:
        ival = int(value)
        for gen in Generator:
            if gen.value == ival:
                return gen
    except ValueError:
        for gen in Generator:
            if gen.name == value:
                return gen
    raise argparse.ArgumentTypeError(
        "{}_is_an_invalid_generator_type.".format(value))
```

```
def main():
    """_Parse_command_line_arguments,_pass_appropriate_ones_to_the_RNG,
_____and_pipe_to_dieharder.
# Change to script directory
   abspath = os.path.abspath(__file__)
   dname = os.path.dirname(abspath)
   os.chdir(dname)
   parser = argparse.ArgumentParser(
        description="Wrapper_script_for_RNGs._Sets_up_C++_RNG_and_pipes_to"
                    "dieharder_for_analysis.",
        formatter_class=argparse.RawTextHelpFormatter)
   helpstring = "The_generator_can_be_any_specified_number_or_name:\n"
    for gen in Generator:
        helpstring += "{}_|_{{}}\n".format(gen.value, gen.name)
   parser.add_argument("generator", type=check_generator_type,
                        help=helpstring)
   parser.add_argument("--file", action='store_true',
                        help="Output_to_file_or_not.")
   parser.add_argument('args', nargs=argparse.REMAINDER)
   args = parser.parse_args()
    # Create Results Directory if it doesn't exist, if the file option is
    # turned on
   directory = "results"
    if args.file and not os.path.exists(directory):
        os.makedirs(directory)
    # Check for running all generators.
    if args.generator == Generator.all:
        print("Using_all_generators...")
        for gen in Generator:
            if gen != Generator.all:
                if args.file:
                    pipestring = "_>_results/{}.txt".format(gen.name)
                else:
                    pipestring = ""
                print("Running_generator_{{}}...".format(gen.name))
                subprocess.call("./bin/rngs_{}_|_dieharder_-g_200_{}}{}"
                                .format (gen.value,
                                        "_".join(args.args),
                                        pipestring),
                                shell=True)
```

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