



# **Advanced Topics in Machine Learning**

**Winter Semester 2024/2025**

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Prof. Dr.-Ing. Christian Bergler | OTH Amberg-Weiden

### Topics of Today: Advanced Deep Learning Strategies – Part III

- Self-Supervised Learning
- Active Learning

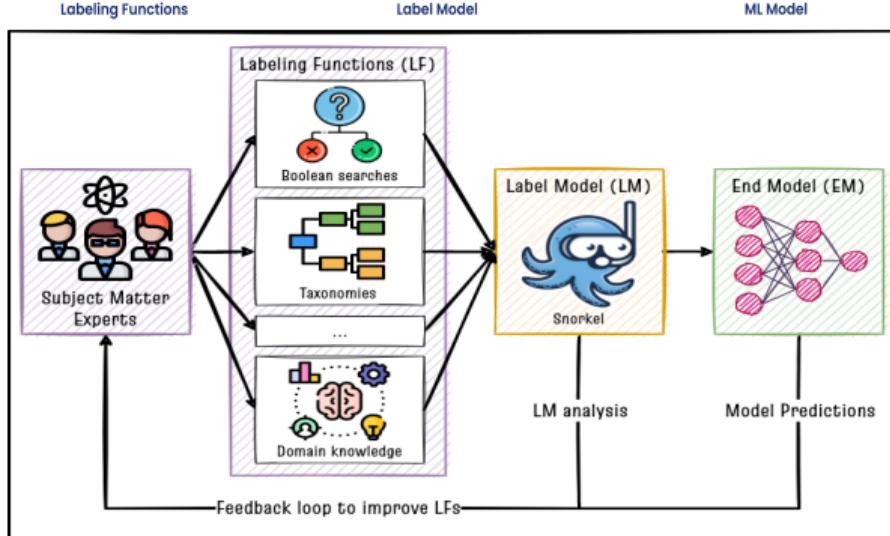
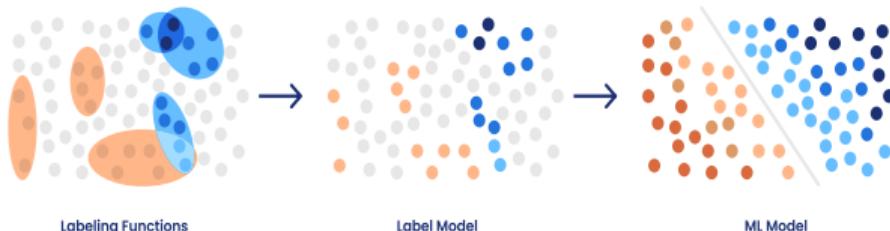
### Topics of Today: Advanced Deep Learning Strategies – Part III

- Weak Supervision
- N-Shot Learning
- Causal Learning

# Deep Learning Strategies – Part III

## Weak Supervision

- Goal: How to transfer an unsupervised to a (weakly) supervised task!



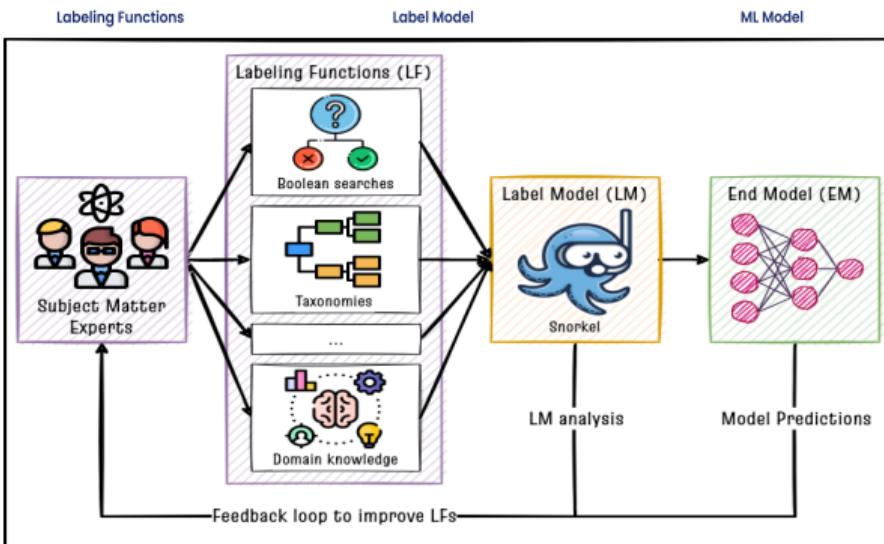
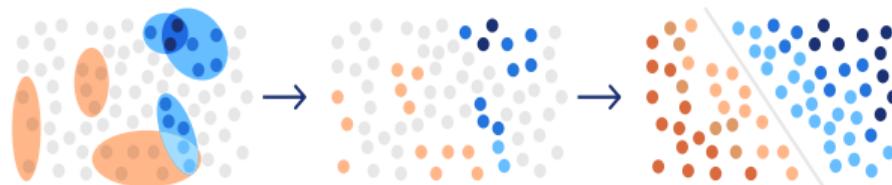
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# Deep Learning Strategies – Part III

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- Interpret & categorize high-level, scalable, and potentially noisy signal sources by applying multiple sources of supervision



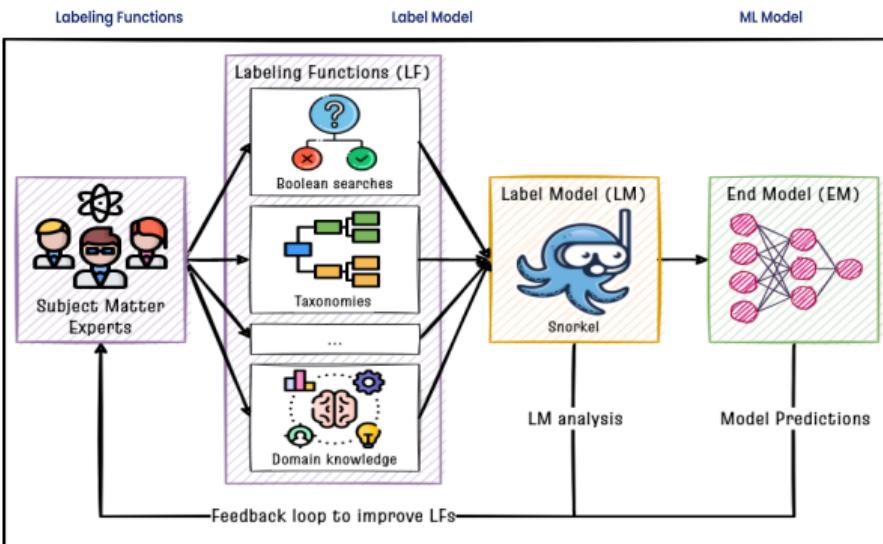
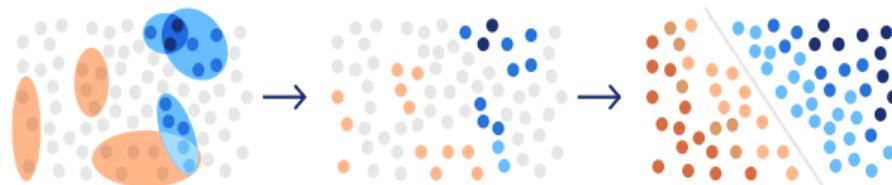
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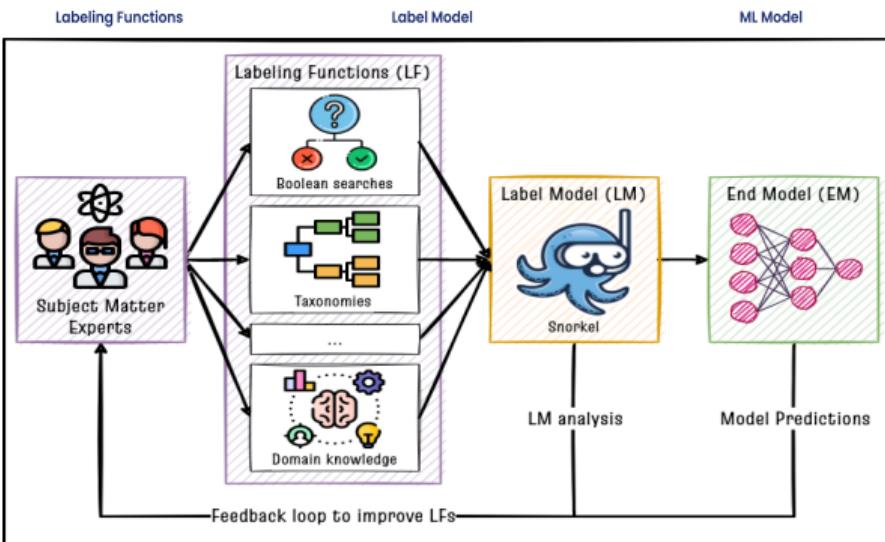
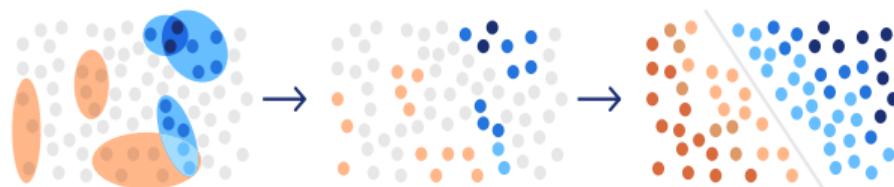
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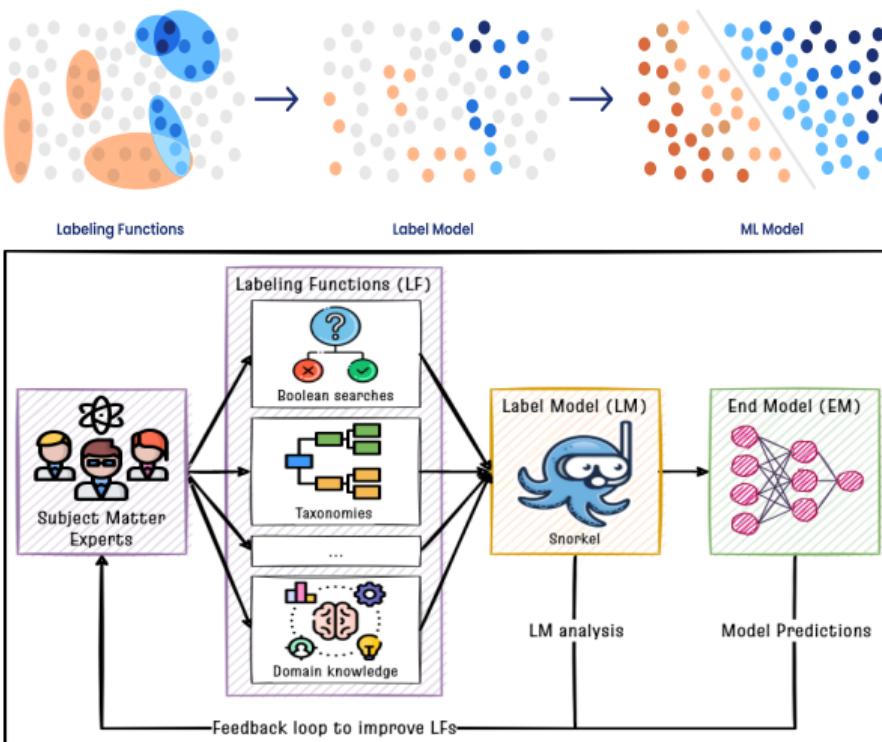
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- Weak supervision training on incomplete, partially (machine-)labeled data
- Lack of precision: completely labeled, but often not precisely enough to recognize subtle differences



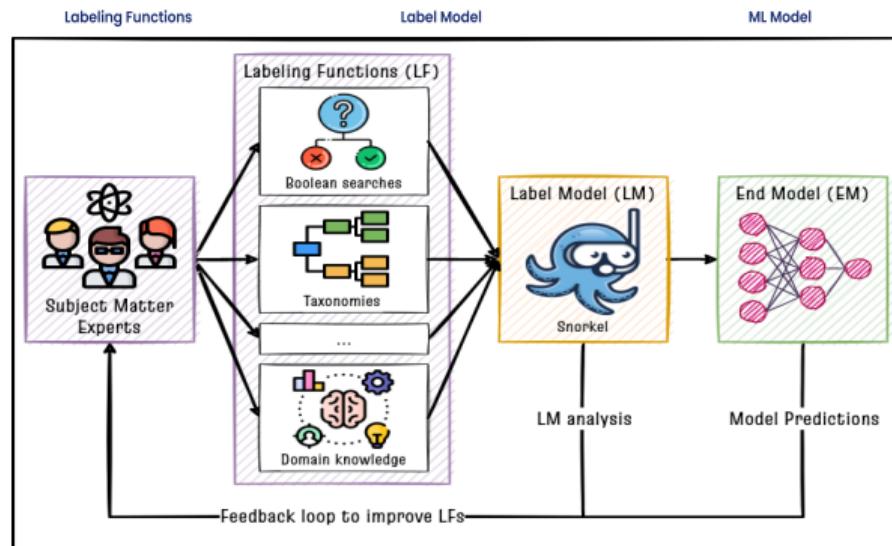
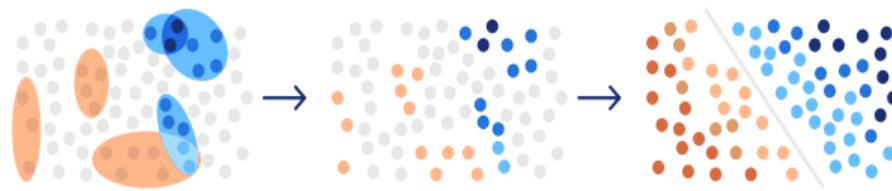
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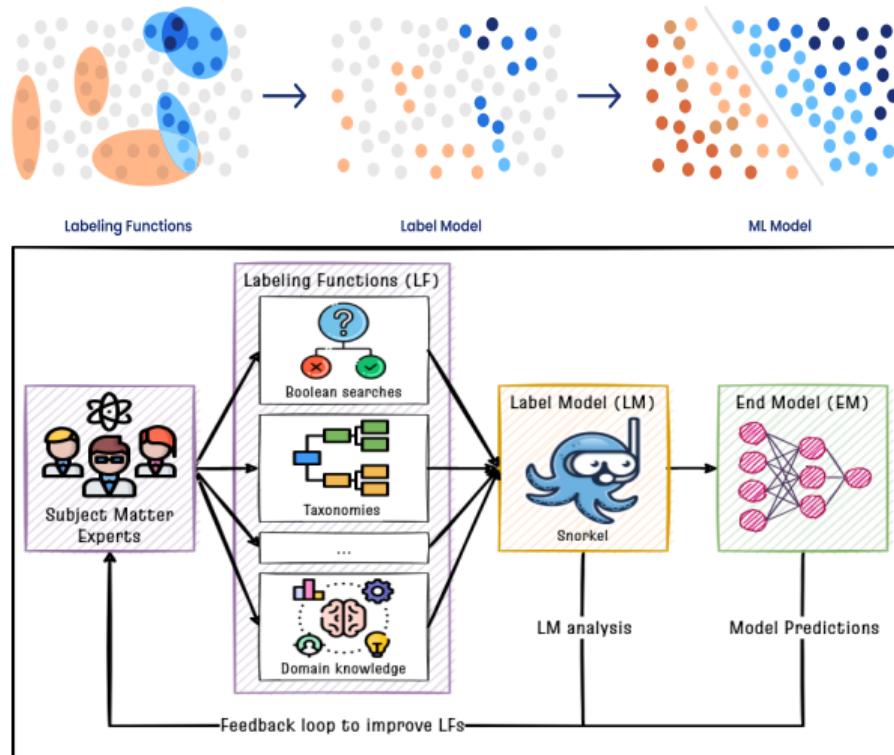


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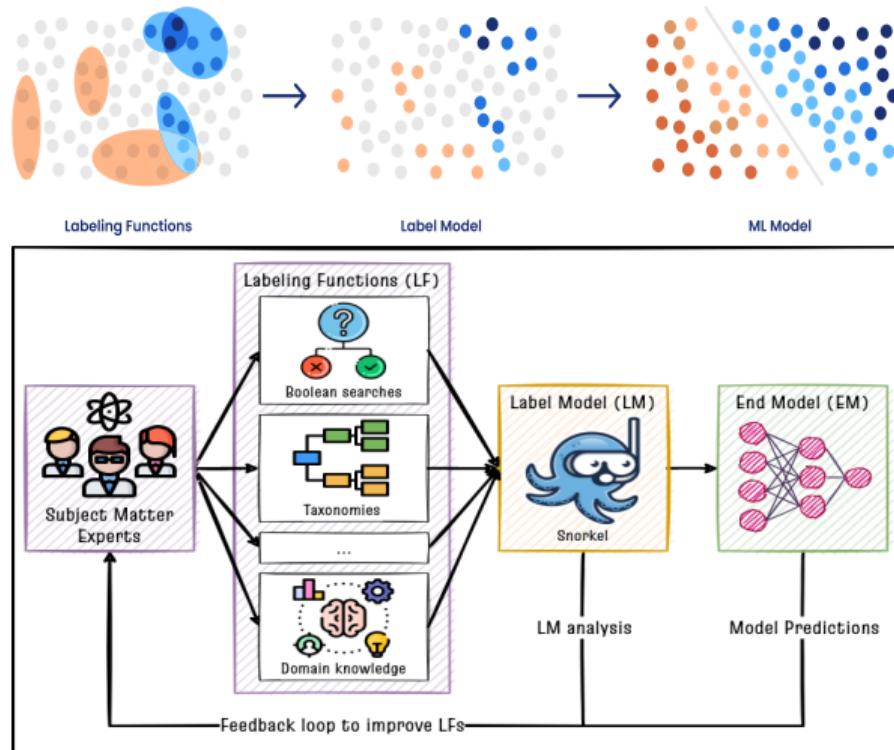
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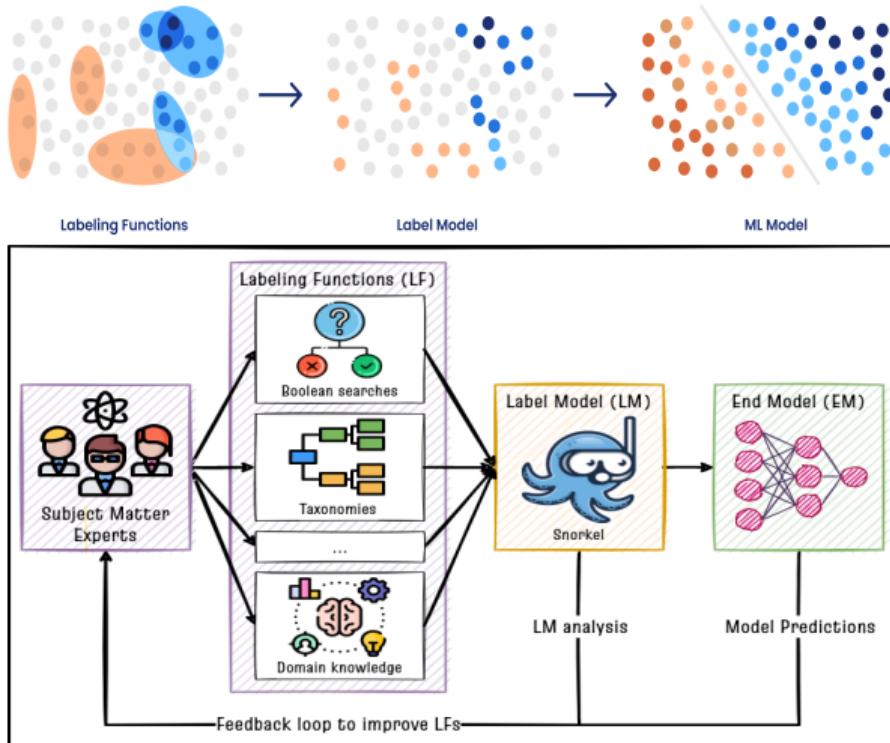


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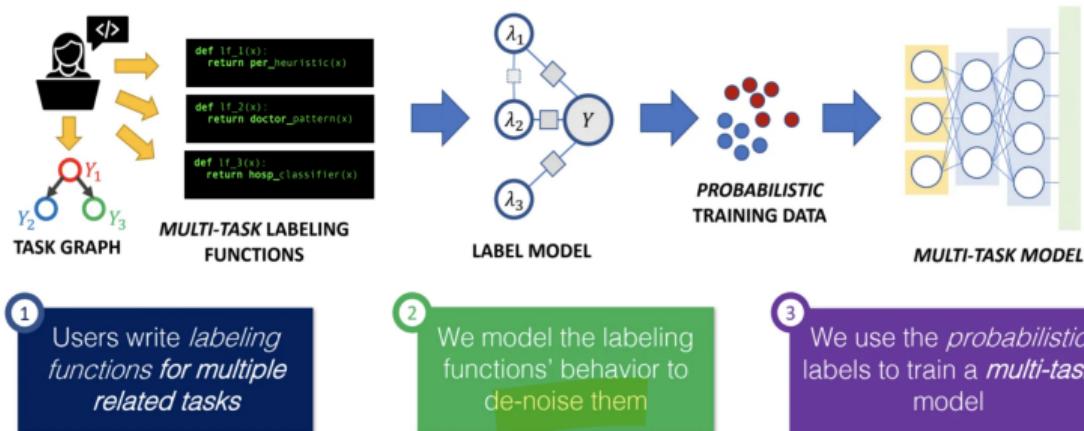
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- Idea: trade-off 100,000 pretty good vs. 100 perfect data labels



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# Labeling in Snorkel

## Snorkel Framework



- Labeling functions  $\lambda_N$  (simple functions/rules), providing multiple inconsistent or overlapping labels (commercialized version available here: [Snorkel](#))
- Combine noisy weak labels in a labeling model to generate a consensus more accurate final label
- Label model learns dependencies/reliabilities of the labeling functions, weighting each function according to its accuracy and overlap with others
- Probabilistic labels for each sample, allow to build a (weakly) supervised training set

Source: [Link to Image](#)

### Smart Labeling

- Labeling involves using automated or semi-automated techniques to label data intelligently (see pseudo-labeling, self-supervised approaches)

Source: Image from OTH-AW, Electrical Engineering, Media and Computer Science, Thomas Nierhoff – Vorlesung Advanced Topics in ML

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- Active Learning: label only the most uncertain or informative data points, making the labeling process more efficient

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## Weak Supervision

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### Application: Cut-In Prediction Autonomous Vehicle

- Refers to predicting when another vehicle in adjacent lanes will “cut in” or merge into the lane occupied by the autonomous vehicle (critical for safe driving!)

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# Deep Learning Strategies – Part III

## Weak Supervision

every potential event has to be taken into account

here pattern recognition is important

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- Sensor fusion: combining data from multiple sensors (e.g., LIDAR, radar, cameras) to create an accurate model that can predict “cut-in” even when labeling data is limited
- Unlabeled data: process large amounts of unlabeled driving data with weakly supervised trained models that learn to identify “cut-in” scenarios indirectly

Source: Image from OTH-AW, Electrical Engineering, Mechanical Engineering, Source: Thomas Mischler, Advanced Topics in ML  
train model on weakly supervised data sets.  
from sensor data, heuristics etc and unlabeled

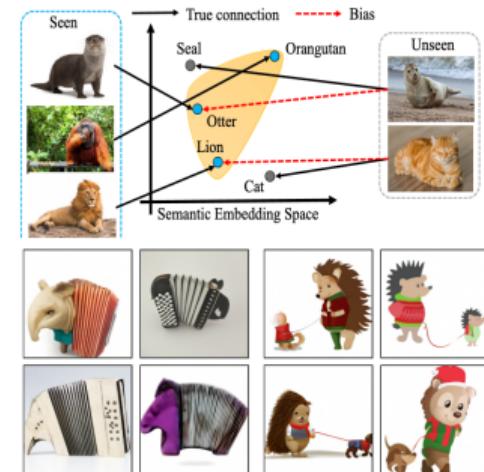
# Deep Learning Strategies – Part III

## N-Shot Learning

### N-Shot Learning – Zero-Shot, Single-Shot & Few-Shot Learning

**Idea:** Zero-shot, single/one-shot, and few-shot learning are learning paradigms where models identify/categorize or generate new categories with very few or even no labeled examples

- **Zero-Shot Learning:** identify new categories never seen in training by leveraging auxiliary semantic knowledge based on feature similarity via textual/visual embeddings!



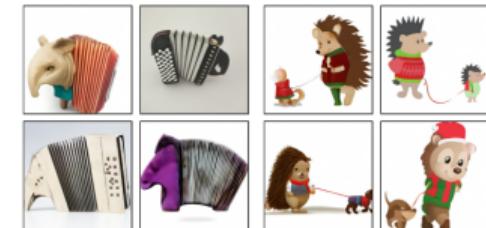
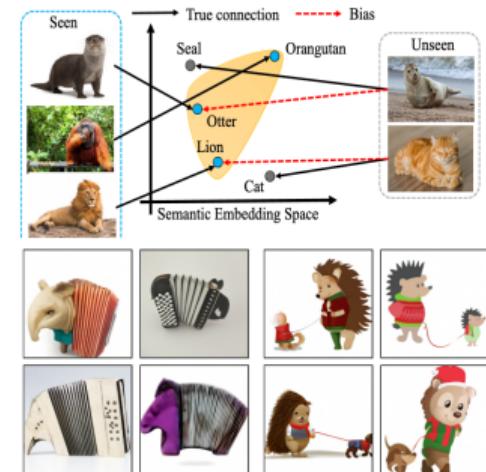
Source: <https://medium.com/@vireshj/zero-shot-learning-understanding-machines-that-learn-like-humans-e670f83186b8>  
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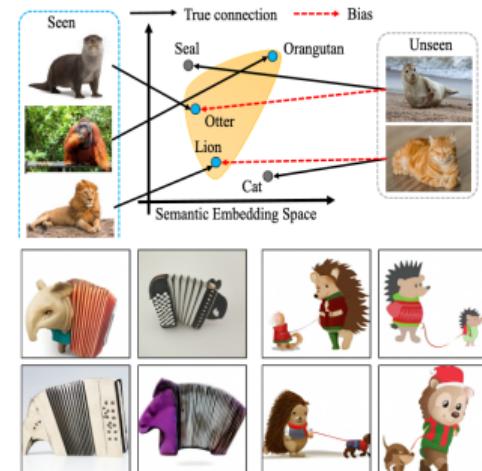
## N-Shot Learning

zero shot for first time seeing few shot is for few times seeing

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- Non-static set of classes, while unseen events will be stored in the high-dimensional feature space either near (related to “Knowns”) or far-apart (unrelated to “Knowns”)
- Class assignment for a first-time appearance of a new category requires pre-existing knowledge (embeddings, e.g. single-shot) describing the new class



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- Comparison of new data points w.r.t. the given single sample using similarity measures or embeddings in a latent space (deep metric learning!)
- These networks learn to measure similarity between data samples, enabling classification with just a single instance
- Class assignment is based on distance-related outcome (“close enough”) of an unseen sample w.r.t. the “single shot data point”



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## N-Shot Learning

- **Few-Shot Learning:** model learns from a small number of labeled examples, with more than zero/one images to compare against

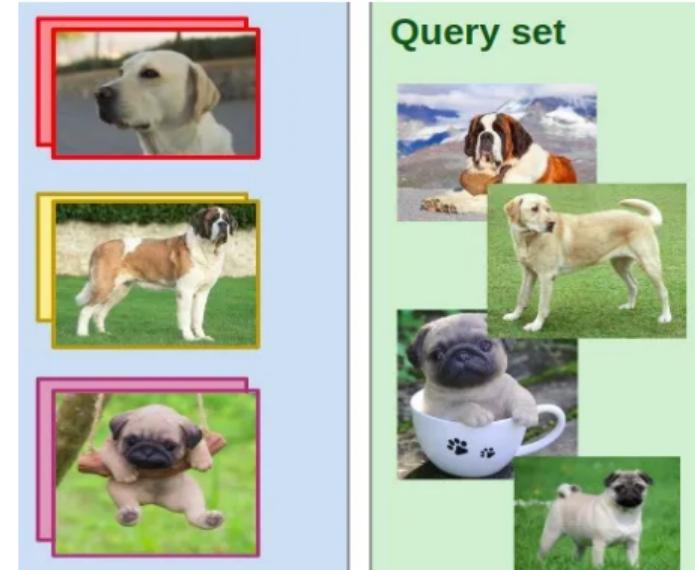


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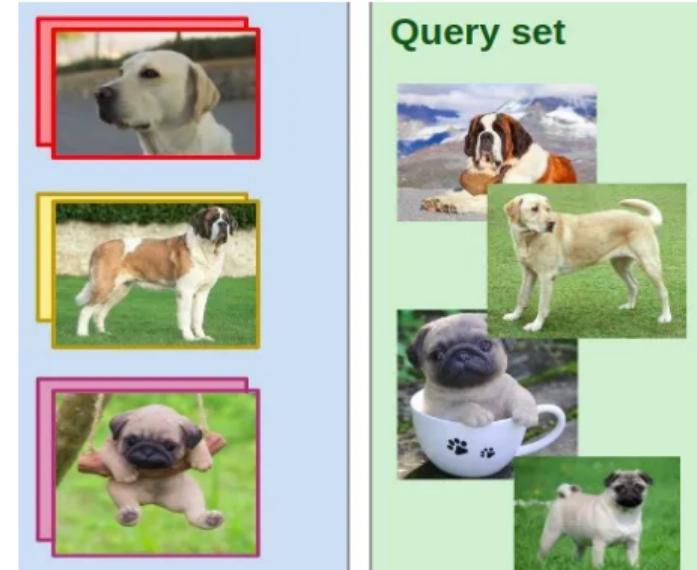


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causal learning home work

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- Classify  $Q$  query images among the  $K$  classes, with  $K \times N$  samples in the training set are the only representatives

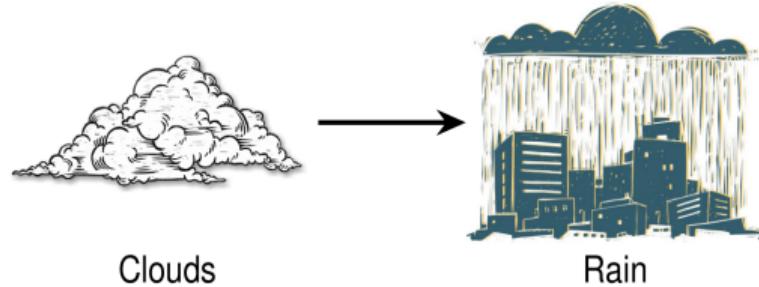


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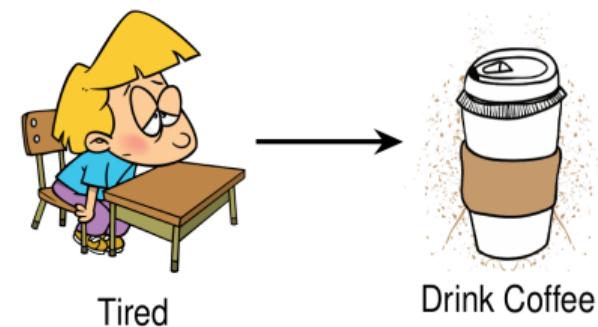
## Causal Learning

- Implies a direct cause-and-effect relationship (“explain the cause of an effect”) between two variables (change one variable will directly impact the other in a predictable way)



Clouds

Rain



Tired

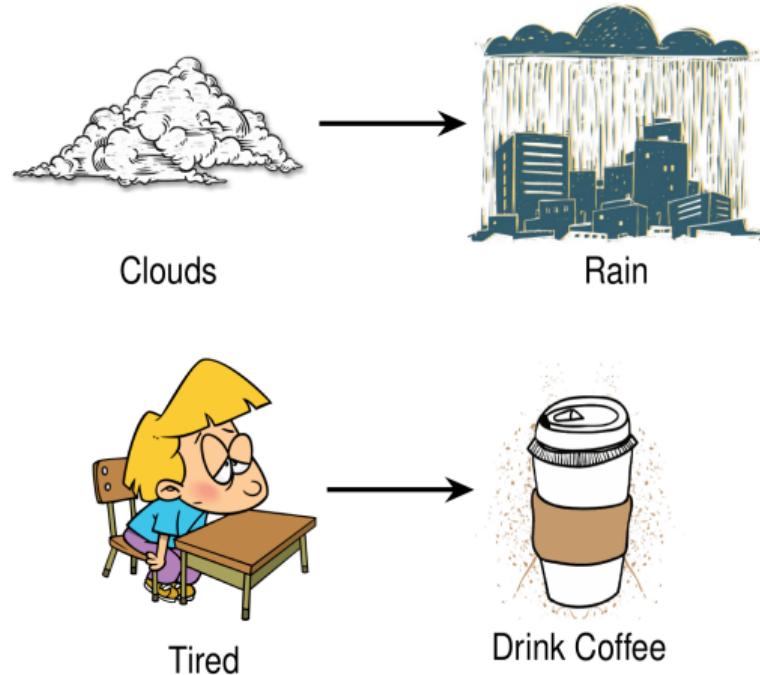
Drink Coffee

Source: FAU Erlangen-Nuremberg, Pattern Recognition Lab, K.Breininger, V. Christlein, Advanced Deep Learning – Interpretable/Causal Deep Learning

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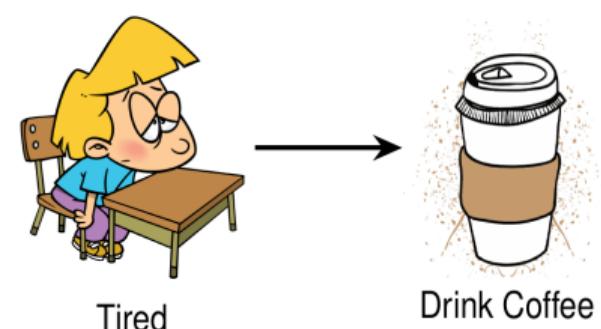
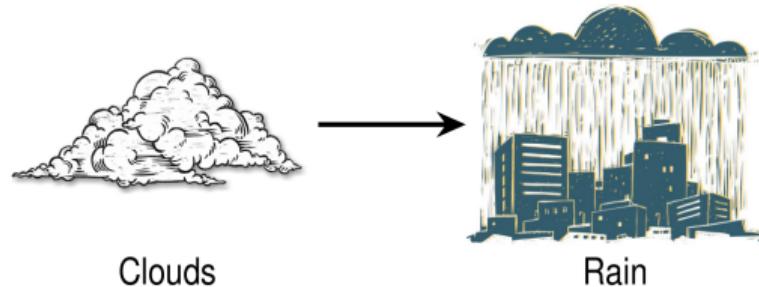


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- **Careful:** correlation describes a statistical association between two variables and indicates a simultaneous change (trend!) → However, not necessarily causing the other!
- Causal inference often uses statistical methods to identify relationships that are not simply correlations but have a directional influence



Source: FAU Erlangen-Nuremberg, Pattern Recognition Lab, K.Breininger, V. Christlein, Advanced Deep Learning – Interpretable/Causal Deep Learning

## Causal Learning

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### Types of Causal Relationships

- **Direct Causal Relationships:** One variable directly affects another (e.g., smoking directly causes an increased risk of lung cancer)
- **Indirect Causal Relationships:** The effect of one variable on another is mediated through a third variable (e.g., education may lead to higher income, and higher income might then lead to better health outcomes)
- **Bidirectional Causality:** Some relationships may involve mutual causality, where two variables affect each other (e.g., diet and exercise can both affect each other over time)

Source: FAU Erlangen-Nuremberg, Pattern Recognition Lab, K.Breininger, V. Christlein, Advanced Deep Learning – Interpretable/Causal Deep Learning

# Deep Learning Strategies – Part III

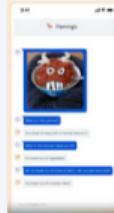
## Causal Learning

### Deep Learning

Representation Learning

Continuous Optimization

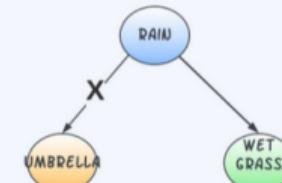
Handling Large Quantities of Data



### Causality

Model Cause and Effect

Answer Interventional Questions



Source: Image from Nan Rosemary Ke, Stefan Bauer, "Causality and Deep Learning: Synergies, Challenges and the Future", Slide 29

# Deep Learning Strategies – Part III

## Causal Learning

Correlation is NOT Causation!



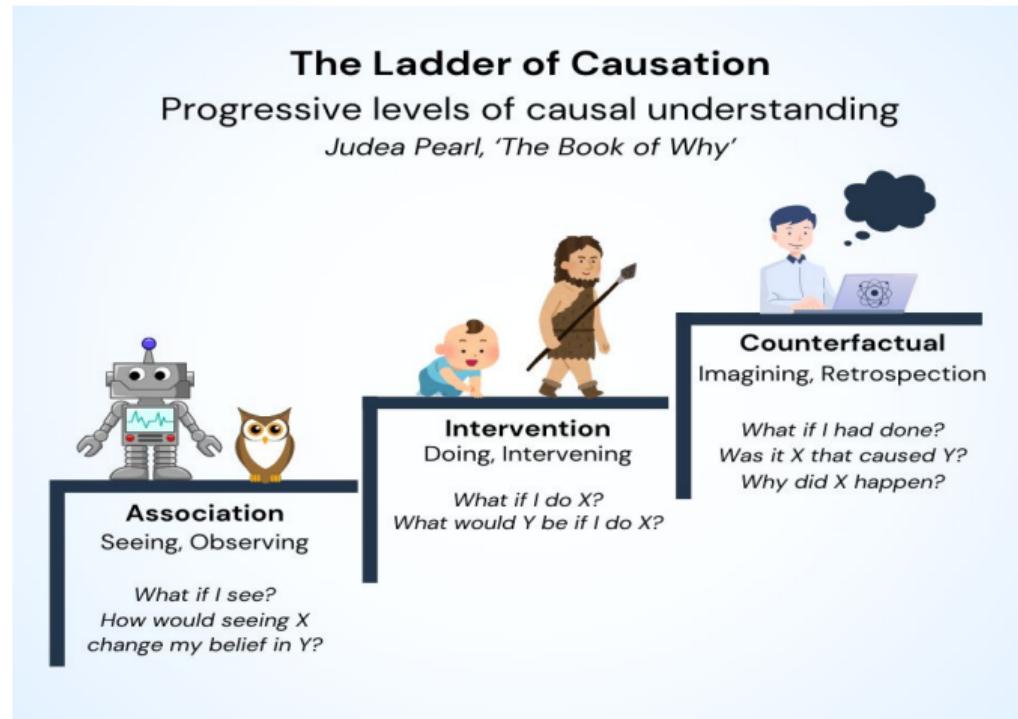
© marketoonist.com

Source: Image from <https://censemaking.com/2022/08/03/the-fear-and-folly-of-data/>

# Deep Learning Strategies – Part III

## Causal Learning

### Ladder of Causation



- Organizes causal reasons into three hierarchical levels: association, intervention, counterfactuals
- From simply observing data to fully understanding & reasoning about causal mechanisms

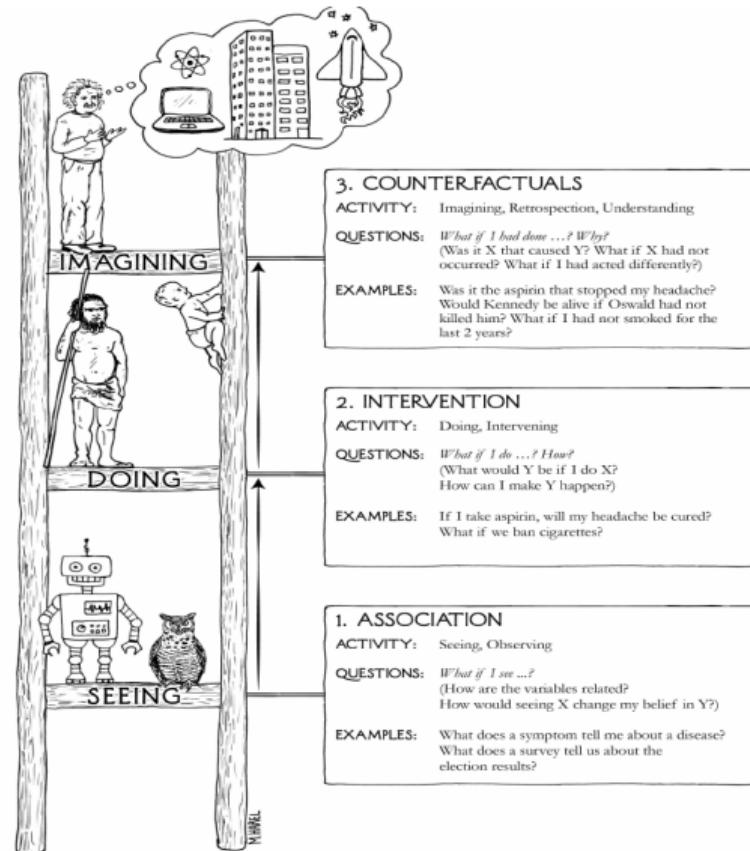
Source: Image from [https://www.linkedin.com/posts/causal-bv\\_ladderofcausation-causalai-decisionmaking-activity-7177992092458057729-hiP9](https://www.linkedin.com/posts/causal-bv_ladderofcausation-causalai-decisionmaking-activity-7177992092458057729-hiP9)

# Deep Learning Strategies – Part III

## Causal Learning

### Association

- Observing correlations/dependencies of variables:  
“What happens if we change this variable?”



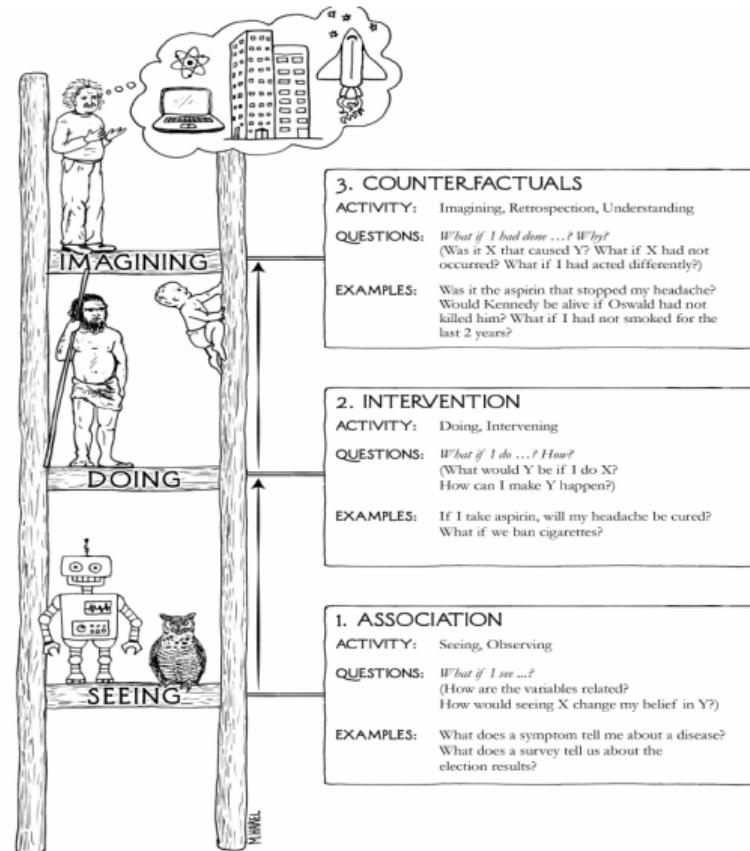
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# Deep Learning Strategies – Part III

## Causal Learning

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- However, no explanation why one thing happens because of another (purely observational!)



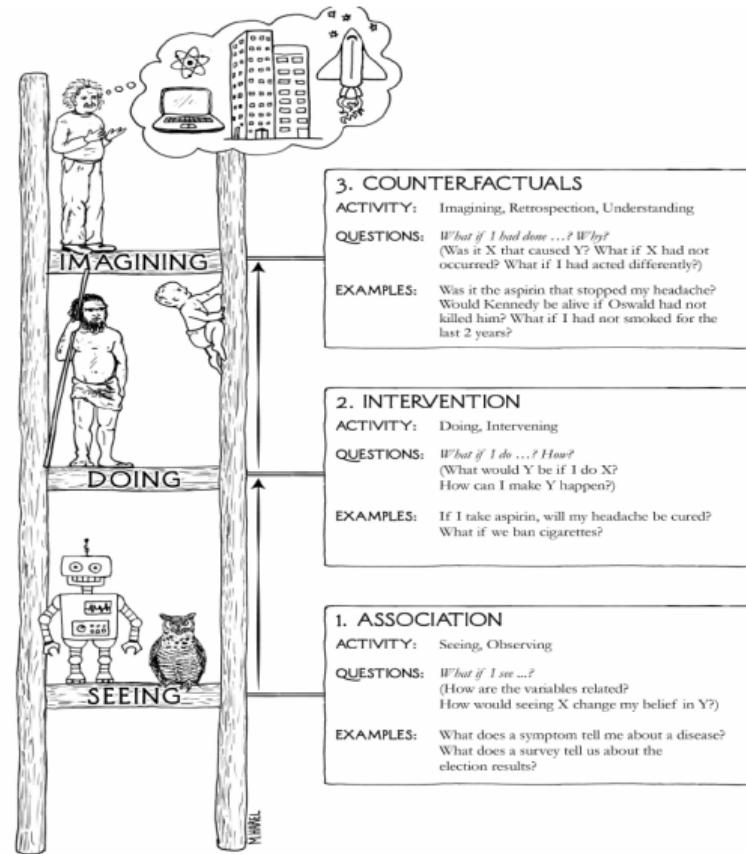
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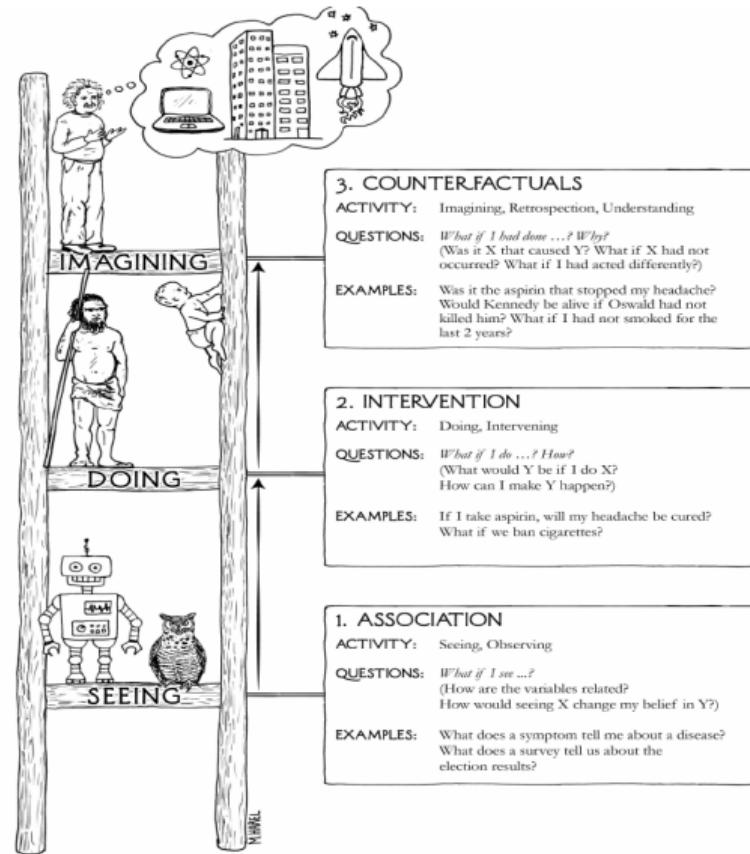
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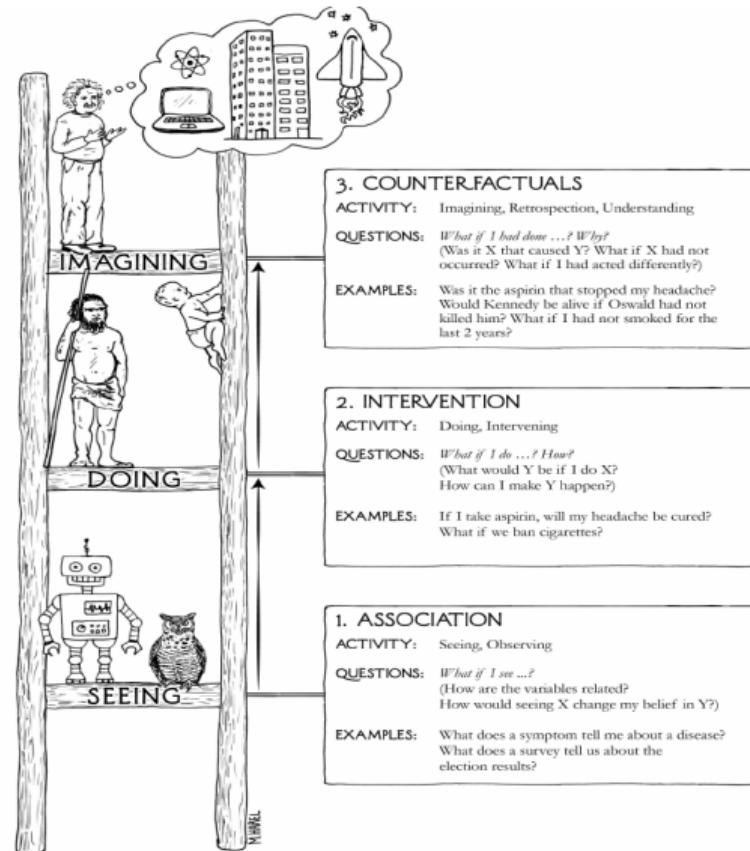
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- Association alone do not determine if a relationship is causal (correlation between ice cream sales and drowning incidents does not imply that buying ice cream causes drowning)



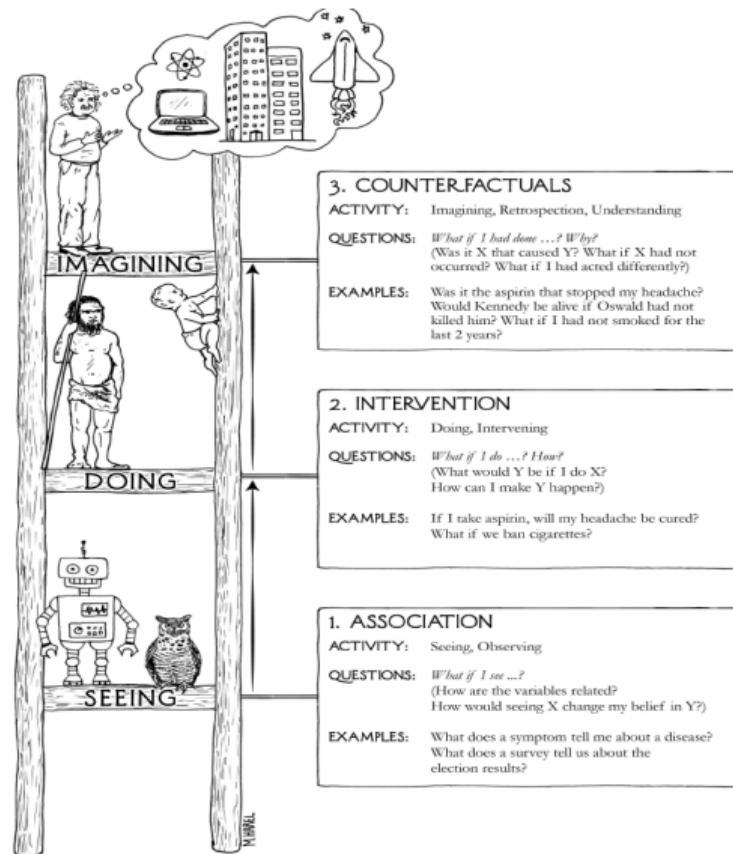
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# Deep Learning Strategies – Part III

## Causal Learning

### Intervention

- Moving beyond observation by introducing actions to change the system and observing the results: “What if I do this?”

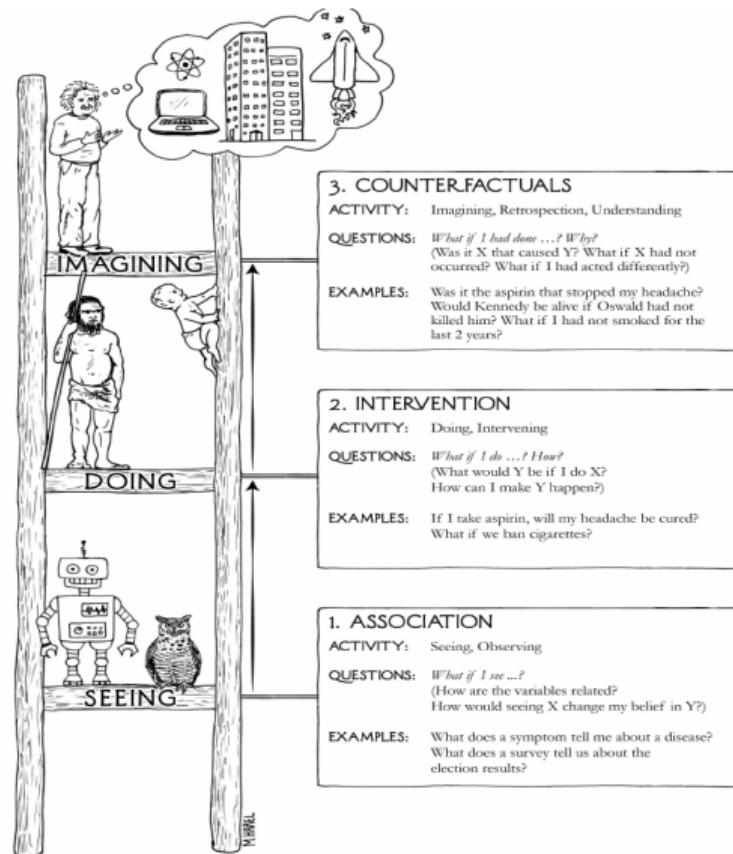


# Deep Learning Strategies – Part III

## Causal Learning

### Intervention

- Moving beyond observation by introducing actions to change the system and observing the results: “What if I do this?”
- Represent causal relationship by showing how changes in one variable affect another



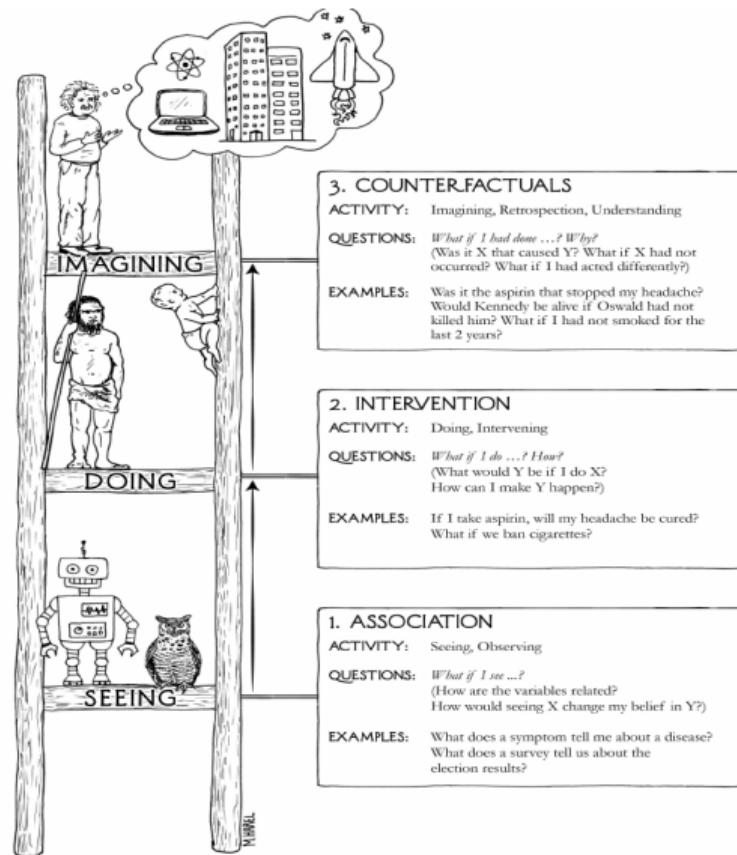
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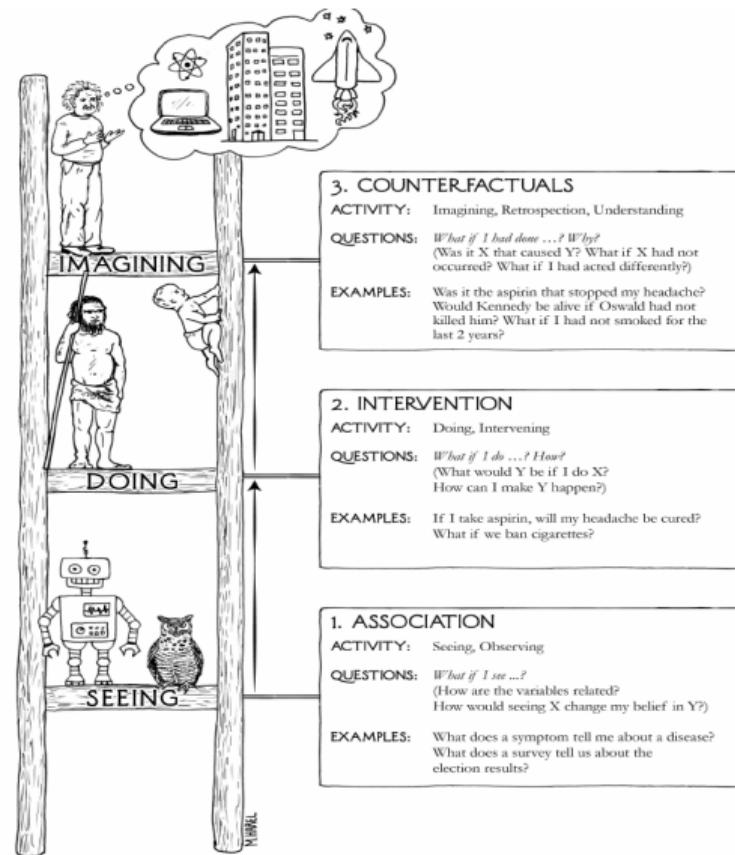
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- Represent causal relationship by showing how changes in one variable affect another
- Question: “What will happen to  $Y$  if I change  $X$ ? ”
- Methods: randomized controlled trials, where the experimenter manipulates the independent variable  $P(Y|do(X))$  (e.g. giving patients a treatment placebo) to observe the effect on a dependent variable (like recovery rates)



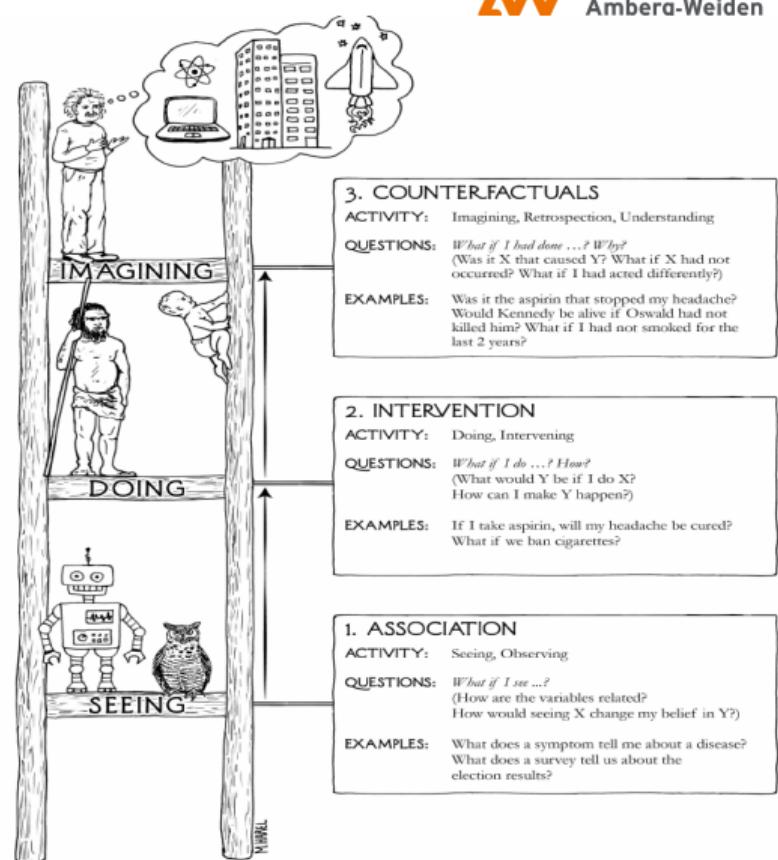
Source: FAU Erlangen-Nuremberg, Pattern Recognition Lab, K.Breininger, V. Christlein, Advanced Deep Learning – Interpretable/Causal Deep Learning

# Deep Learning Strategies – Part III

## Causal Learning

### Counterfactuals

- Asking about hypothetical alternatives to what actually happened, what would have happened “if”



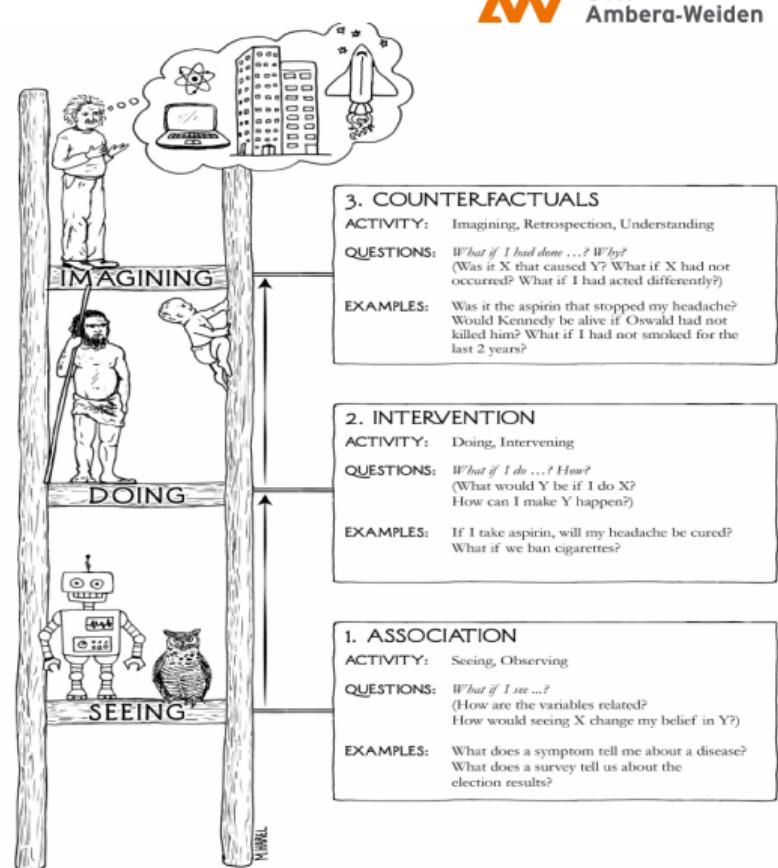
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# Deep Learning Strategies – Part III

## Causal Learning

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- Asking about hypothetical alternatives to what actually happened, what would have happened “if”
- Alternative realities by imagining what the outcome would have been if a different action or condition had been in place



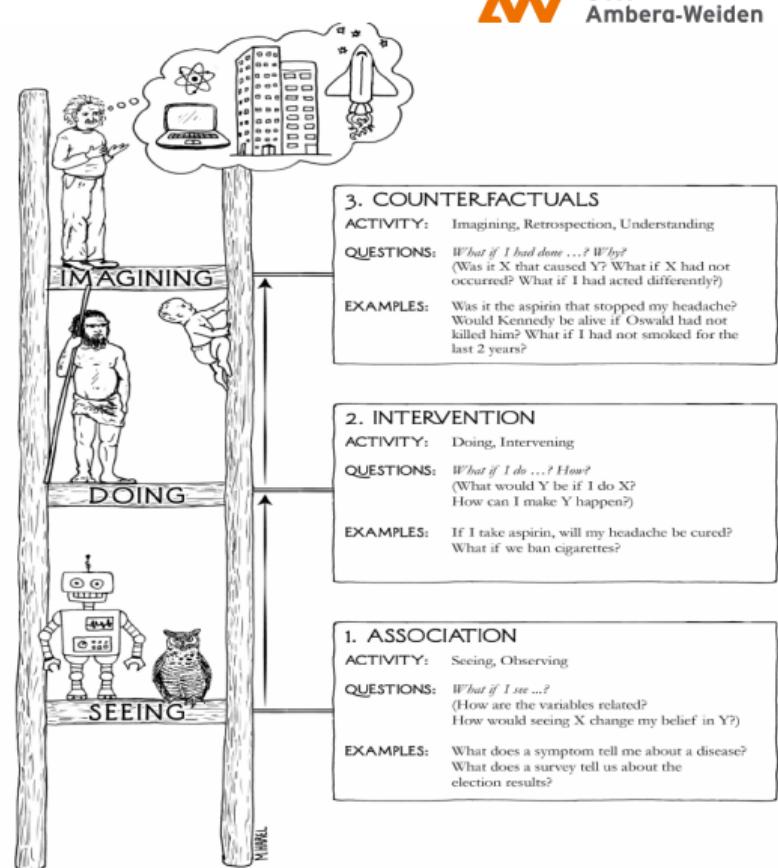
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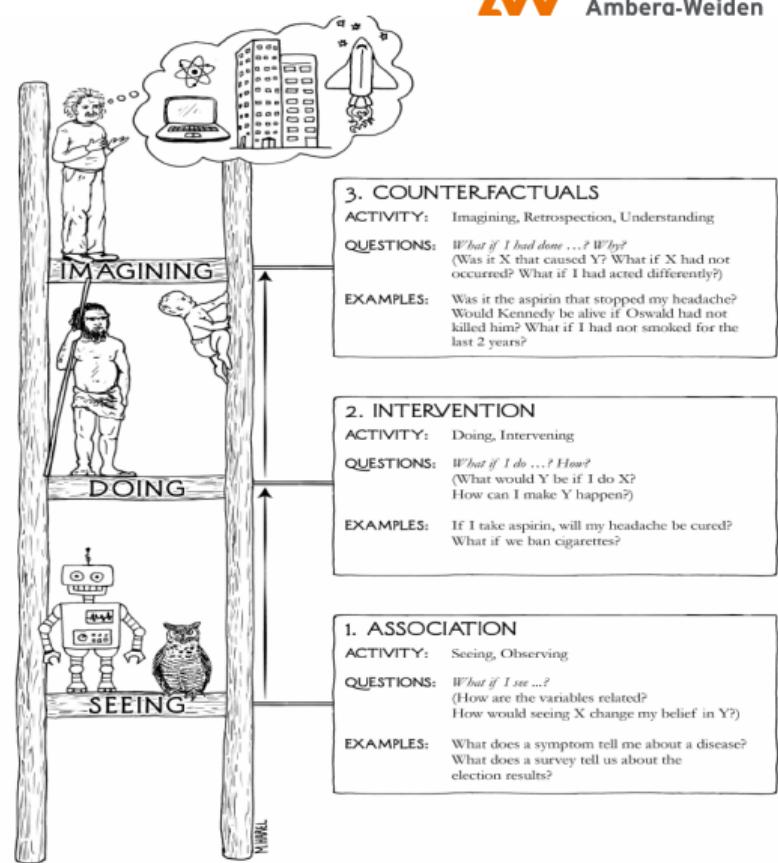
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# Deep Learning Strategies – Part III

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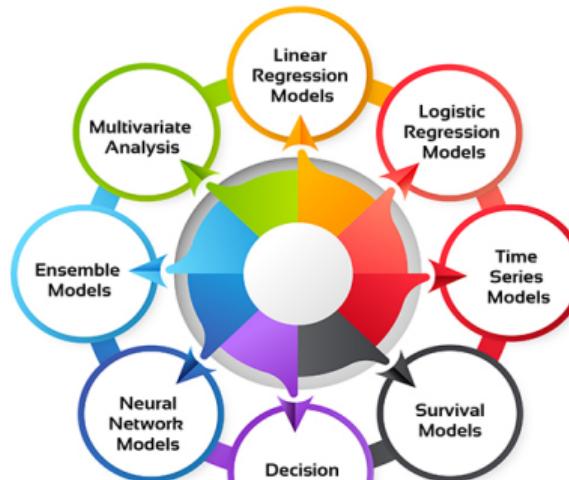
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- Alternative realities by imagining what the outcome would have been if a different action or condition had been in place
- Question: “What would have happened to  $Y$  if  $X$  had been different?”
- Methods: **structural causal models (SCMs)**, provide a framework for understanding causal relationships at a deeper level by specifying equations reflecting mechanisms of causation



Source: FAU Erlangen-Nuremberg, Pattern Recognition Lab, K.Breininger, V. Christlein, Advanced Deep Learning – Interpretable/Causal Deep Learning

# Types of Statistical Models

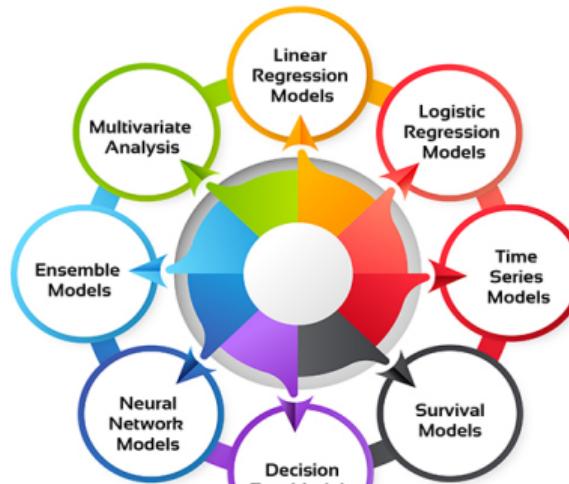


- Current ML-Models or statistical models can only do “Association”

Source: <https://www.dasca.org/world-of-data-science/article/what-is-statistical-modeling-in-data-science>

Source: FAU Erlangen-Nuremberg, Pattern Recognition Lab, K.Breininger, V. Christlein, Advanced Deep Learning – Interpretable/Causal Deep Learning

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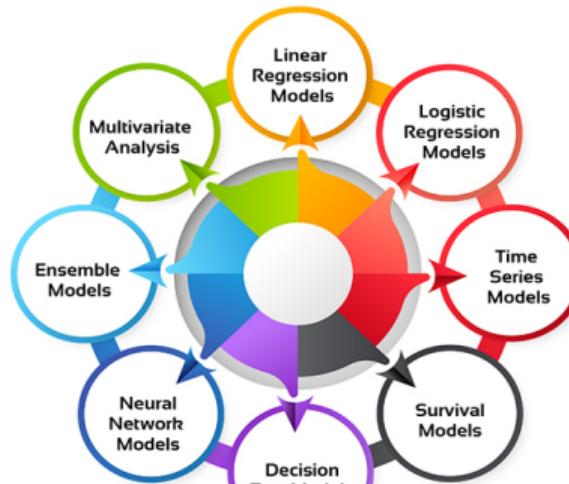


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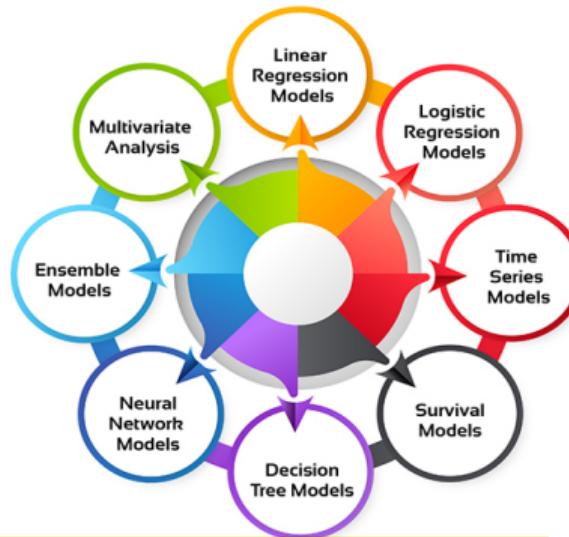


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# Types of Statistical Models



here we have assosiations only because of current ml modles

- Current ML-Models or statistical models can only do “Association”
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- No Causal Inference → Yes: Fire causes Smoke, No: Smoke causes Fire reality
- Successful because: massive amount of data, high number of parameters, strong computational power, independent and identically distributed (i.i.d.) assumption

Source: https://www.datascience.org/world-of-data-science/article/what-is-statistical-modeling-in-data-science  
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# Deep Learning Strategies – Part III

## Causal Learning

- **Independent:** each data sample is collected independently of others, one sample does not influence/depend on another



$$\begin{matrix} \text{x} \\ \text{"panda"} \\ 57.7\% \text{ confidence} \end{matrix} + .007 \times \begin{matrix} \text{sign}(\nabla_x J(\theta, x, y)) \\ \text{"nematode"} \\ 8.2\% \text{ confidence} \end{matrix} = \begin{matrix} \text{x} + \text{esign}(\nabla_x J(\theta, x, y)) \\ \text{"gibbon"} \\ 99.3 \% \text{ confidence} \end{matrix}$$

Source: Szegedy et al., Intriguing properties of neural networks, Figure 5

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# Deep Learning Strategies – Part III

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- **Introducing an unexpected distribution change?**



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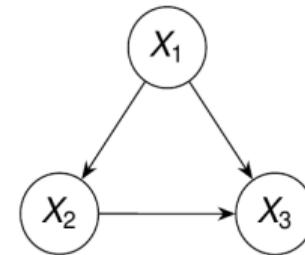
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- If  $Z$  is not observed (hidden), it is a confounding variable, affecting both the cause and the effect, making it difficult to establish a true causal relationship
- Example: exercise frequency ( $Z$ ), body weight ( $X$ ), cholesterol levels ( $Y$ )  $\rightarrow$  without considering  $Z$ , it might appear that body weight directly affects cholesterol, however, exercise impacts both independently

Source: FAU Erlangen-Nuremberg, Pattern Recognition Lab, K.Breininger, V. Christlein, Advanced Deep Learning – Interpretable/Causal Deep Learning

## Causal Learning

### Causal Graphical Models (CGMs)

- Directed Acyclic Graphs (DAGs) or Bayesian Networks  
("acyclic" part → no loops, flow in one direction without cycling back)



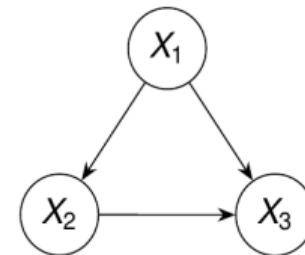
$$p(X_1, X_2, X_3) = p(X_1) p(X_2 | X_1) p(X_3 | X_1, X_2)$$

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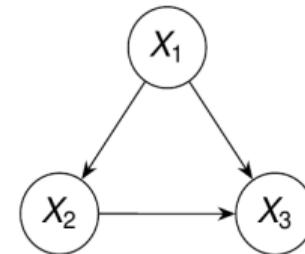
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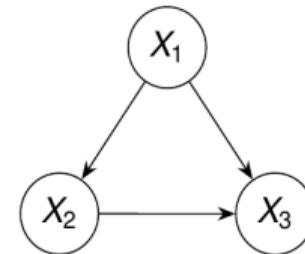
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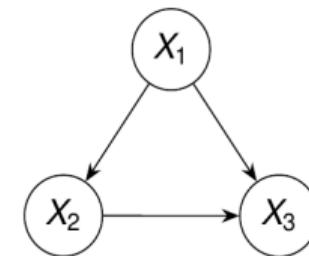
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- Variables  $X$  (observations) as nodes and causal relationships between them as directed edges
- Causal Markov condition (Causal Independence!):  
 $P(X_1, \dots, X_n) = \prod_{i=1}^n P(X_i | PA_i)$ , with  $PA_i$  as the parents of  $X_i$ , having a direct causal link (e.g.  $X_1 \rightarrow X_2$ )



$$p(X_1, X_2, X_3) = p(X_1) p(X_2 | X_1) p(X_3 | X_1, X_2)$$

check it out again markov assumption

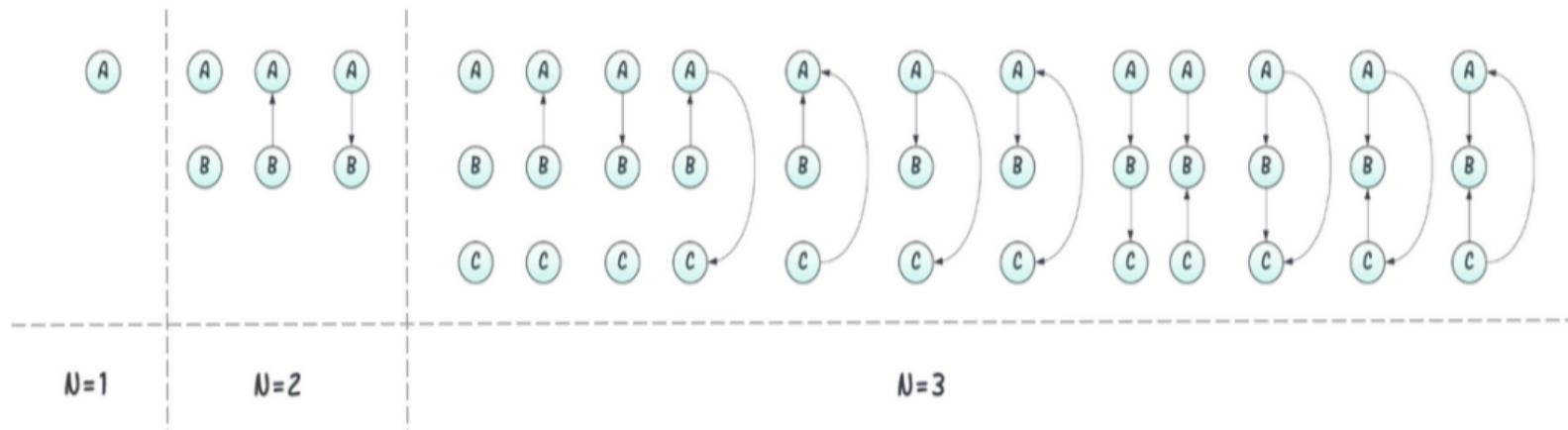
Source: FAU Erlangen-Nuremberg, Pattern Recognition Lab, K.Breininger, V. Christlein, Advanced Deep Learning – Interpretable/Causal Deep Learning

# Deep Learning Strategies – Part III

## Causal Learning

Space of causal graphs (i.e. DAGs) grows **super-exponentially**.

combination of all the directions



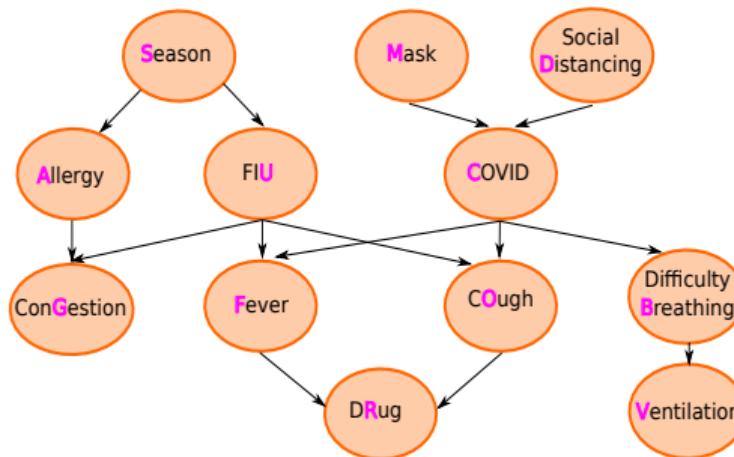
Source: Image from Nan Rosemary Ke, Stefan Bauer, "Causality and Deep Learning: Synergies, Challenges and the Future", Slide 26

# Deep Learning Strategies – Part III

## Causal Learning

### Bayesian Network

#	COVID	Mask	Soc. Distance	FIU	Cough	Fever	Ventilate	Season	ConGestion	Difficulty Breath	Drug	Allergy
1	1	0	1	0	1	0	1	Spring	0	0	1	0
2	0	1	0	1	0	1	0	Summer	1	1	0	0
3	1	1	1	0	0	0	1	Fall	1	0	1	1
4	0	0	1	1	1	0	0	Winter	0	1	0	0
...	...	...	...	...	...	...	...	...	...	...	...	...
500	0	1	1	1	0	0	0	Summer	0	0	1	1

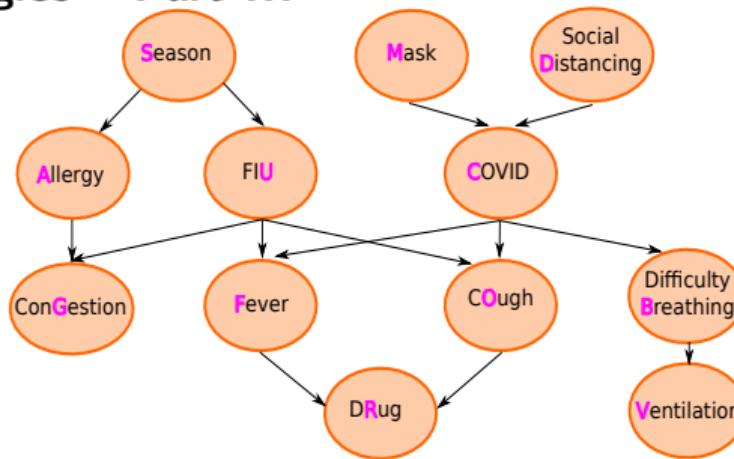


Source: YouTube – easy learning – Causality 1: Bayesian networks are not causal, [Link](#)

# Deep Learning Strategies – Part III

## Causal Learning

### Bayesian Network



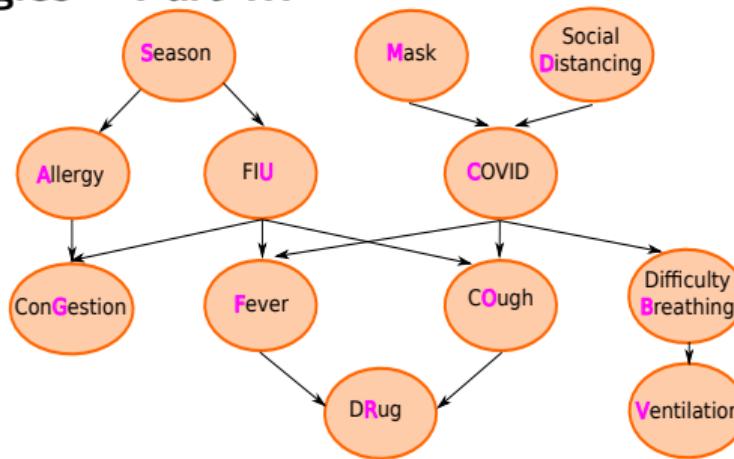
- Random (dependent/independent) variables, e.g. Fever/COVID and Allergy/Cough

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# Deep Learning Strategies – Part III

## Causal Learning

### Bayesian Network



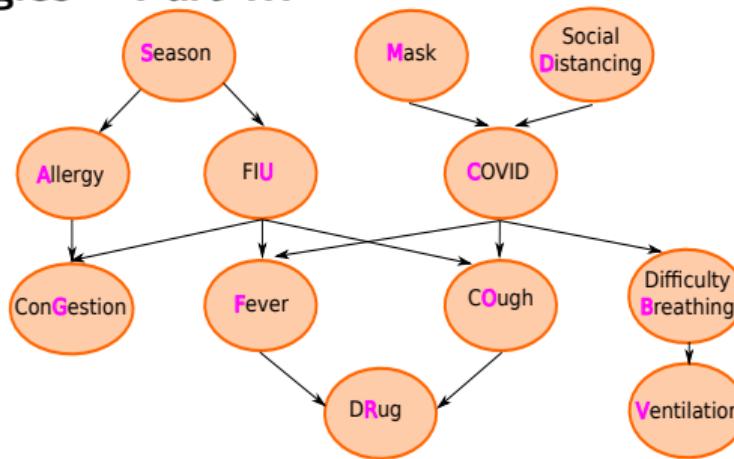
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# Deep Learning Strategies – Part III

## Causal Learning

### Bayesian Network



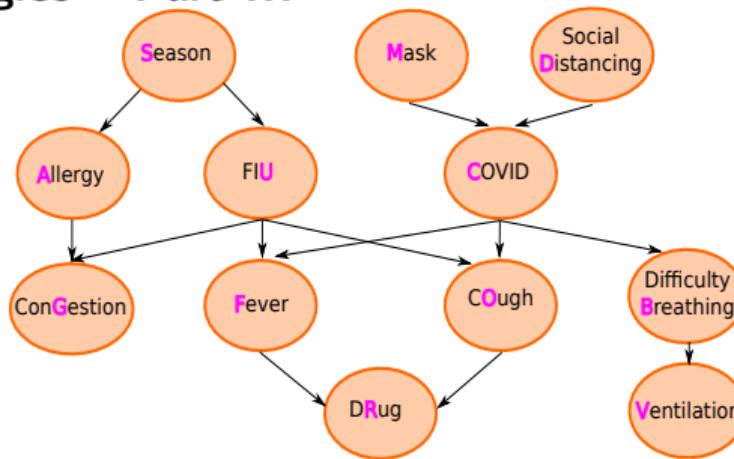
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Source: YouTube – easy learning – Causality 1: Bayesian networks are not causal, [Link](#)

# Deep Learning Strategies – Part III

## Causal Learning

### Bayesian Network



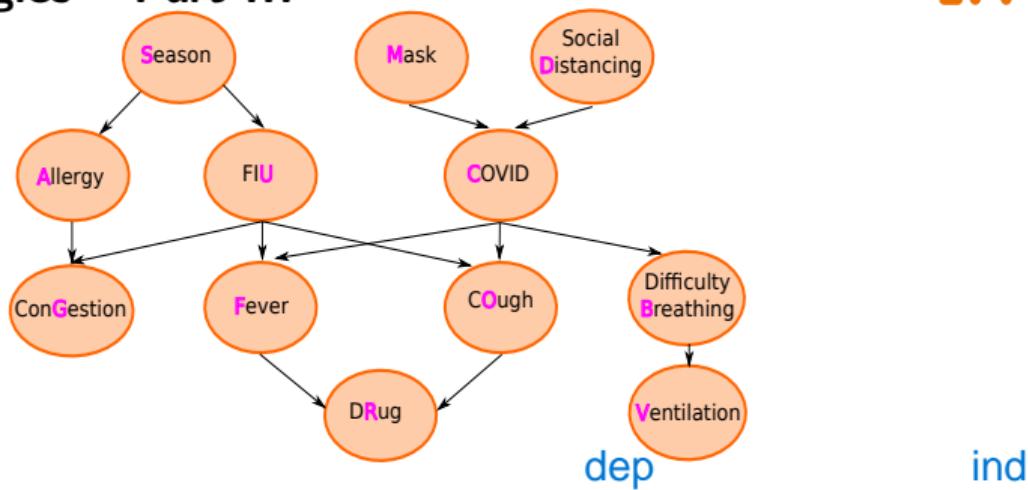
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# Deep Learning Strategies – Part III

## Causal Learning

### Bayesian Network



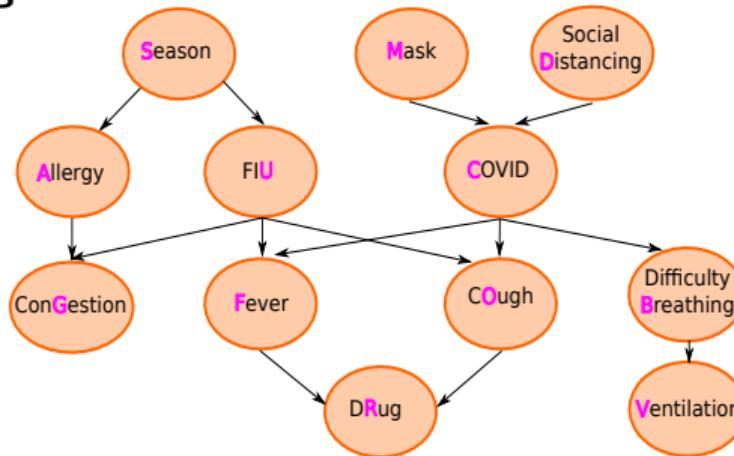
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- Causality (single direction!) would mean either  $F$  is causing  $C$  or  $C$  is causing  $F$
- How to read statistical dependence as causal dependence?

Source: YouTube – easy learning – Causality 1: Bayesian networks are not causal, [Link](#)

# Deep Learning Strategies – Part III

## Causal Learning

### Bayesian Network



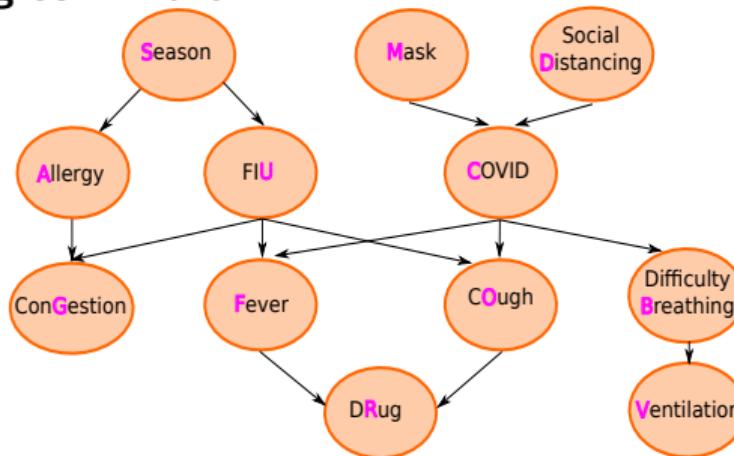
- In general: read a conditional probability  $P(X|Y_1, \dots, Y_n) \neq P(X)$ , as  $X$  is “caused” by  $Y_1, \dots, Y_n$

Source: YouTube – easy learning – Causality 1: Bayesian networks are not causal, [Link](#)

# Deep Learning Strategies – Part III

## Causal Learning

### Bayesian Network



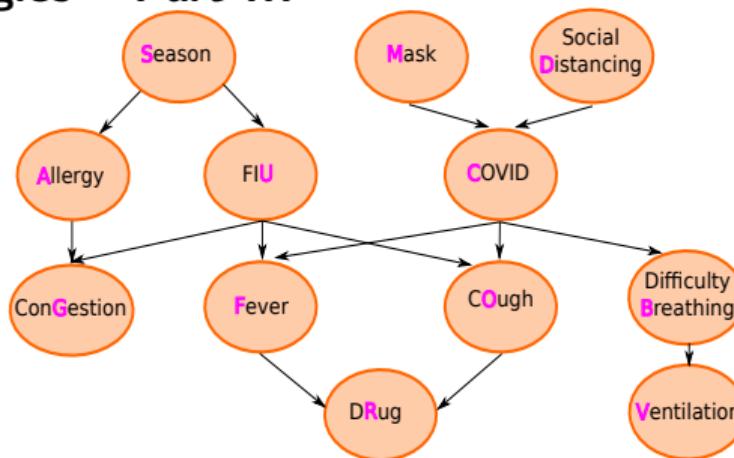
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- However: above relation just indicates **association**, meaning how  $X$  is associated with  $Y_1, \dots, Y_n$ , also possible:  $P(Y_1, \dots, Y_n|X) \neq P(Y_1, \dots, Y_n)$

Source: YouTube – easy learning – Causality 1: Bayesian networks are not causal, [Link](#)

# Deep Learning Strategies – Part III

## Causal Learning

### Bayesian Network



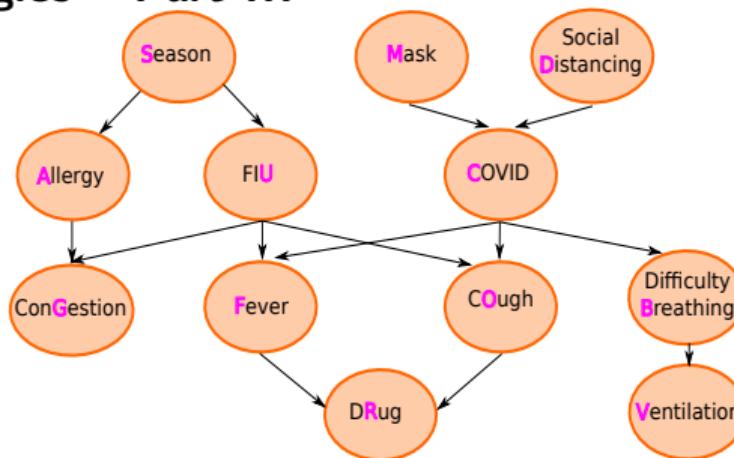
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Source: YouTube – easy learning – Causality 1: Bayesian networks are not causal, [Link](#)

# Deep Learning Strategies – Part III

## Causal Learning

### Bayesian Network



- In general: read a conditional probability  $P(X|Y_1, \dots, Y_n) \neq P(X)$ , as  $X$  is “caused” by  $Y_1, \dots, Y_n$
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- Still: No Causality!
- Goal: Given data  $D$ , what is causing what (the other)?

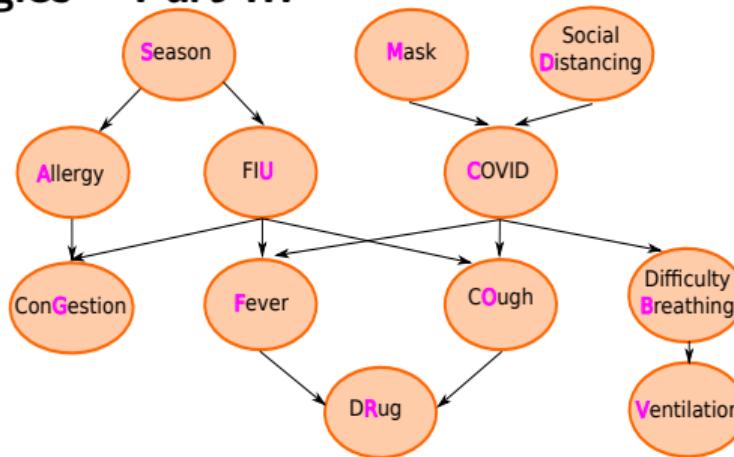
if we put  $p(x)=1$  it means  
 $x$  does not have anything  
to do with the effect

Source: YouTube – easy learning – Causality 10: Bayesian networks are not causal, [Link](#)

# Deep Learning Strategies – Part III

## Causal Learning

### Bayesian Network



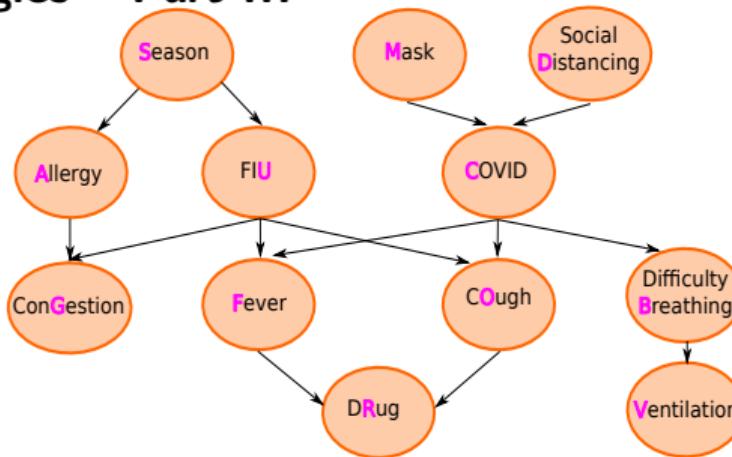
- Consider binary variables  $\text{COVID} \in \{\text{COVID}, \neg\text{COVID}\}$  and  $\text{Fever} \in \{\text{Fever}, \neg\text{Fever}\}$

Source: YouTube – easy learning – Causality 2: Intervention, [Link](#)

# Deep Learning Strategies – Part III

## Causal Learning

### Bayesian Network



- Consider binary variables  $\text{COVID} \in \{\text{COVID}, \neg\text{COVID}\}$  and  $\text{Fever} \in \{\text{Fever}, \neg\text{Fever}\}$
- $\text{COVID}$  is detected by a test,  $\text{Fever}$  by temperature, while observations result in:

$$P(\text{Fever}|\text{COVID}) > P(\text{Fever}|\neg\text{COVID})$$

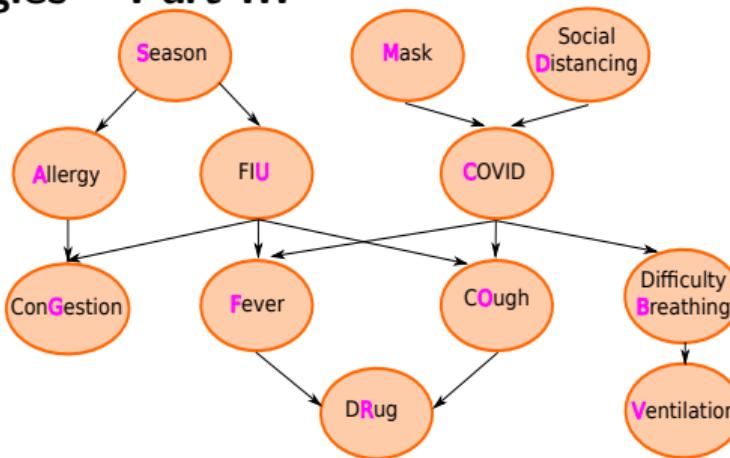
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# Deep Learning Strategies – Part III

## Causal Learning

### Bayesian Network



here we know there is some corelation but we dont know what is the corelation

- Consider binary variables  $\text{COVID} \in \{\text{COVID}, \neg\text{COVID}\}$  and  $\text{Fever} \in \{\text{Fever}, \neg\text{Fever}\}$
- $\text{COVID}$  is detected by a test,  $\text{Fever}$  by temperature, while observations result in:
$$P(\text{Fever}|\text{COVID}) > P(\text{Fever}|\neg\text{COVID})$$
$$P(\text{COVID}|\text{Fever}) > P(\text{COVID}|\neg\text{Fever})$$
- Observing one of them, increases probability of the other! → Statistical dependence (correlation!) – Which one causes the other, how to figure it out – more data?

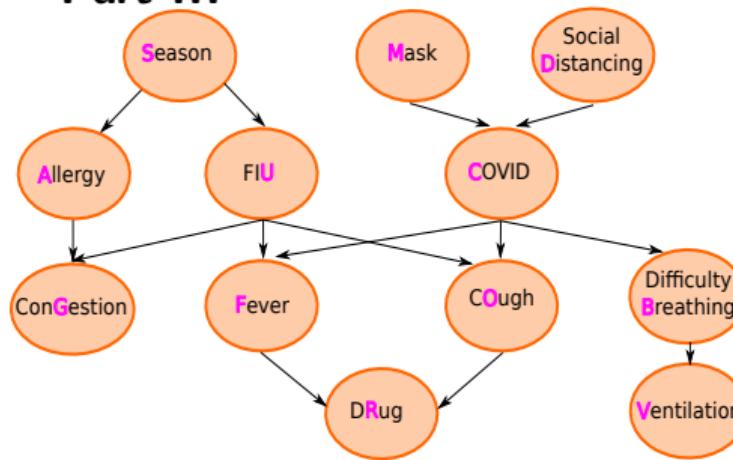
if we add more data it is still in observing mode we have to intervene to check what causes what

Source: YouTube – easy learning – Causality 2: Intervention, [Link](#)

# Deep Learning Strategies – Part III

## Causal Learning

### Observation vs. Intervention



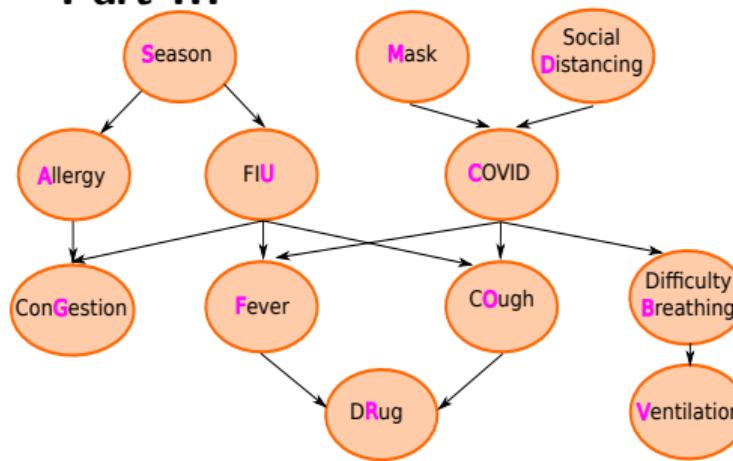
- Just by observing, it is not possible to determine what is causality!

Source: YouTube – easy learning – Causality 2: Intervention, [Link](#)

# Deep Learning Strategies – Part III

## Causal Learning

### Observation vs. Intervention



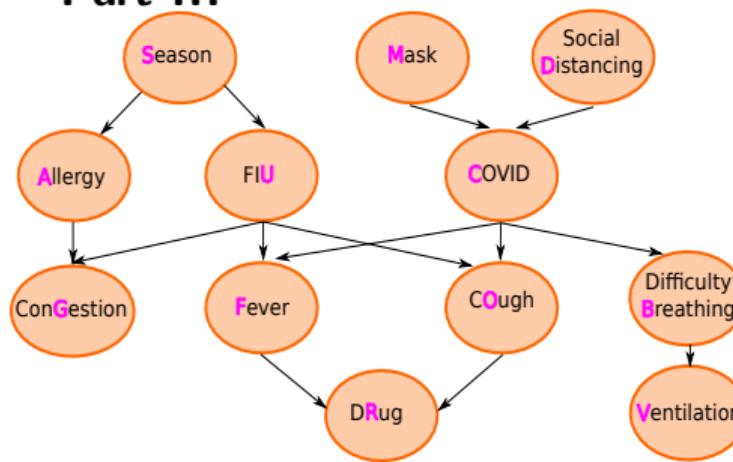
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- Why??? – How do we know that COVID is causing ( $\rightarrow$ ) Fever and not vice versa?

Source: YouTube – easy learning – Causality 2: Intervention, [Link](#)

# Deep Learning Strategies – Part III

## Causal Learning

### Observation vs. Intervention



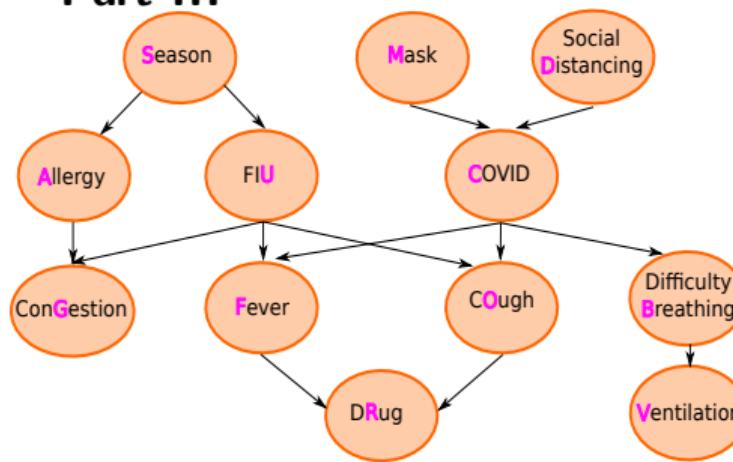
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- Intervene via experimental verification!!! (by observing people with COVID, it is likely to observe Fever; observing Fever, is very often not COVID-related, e.g. fire/smoke)

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# Deep Learning Strategies – Part III

## Causal Learning

### Observation vs. Intervention



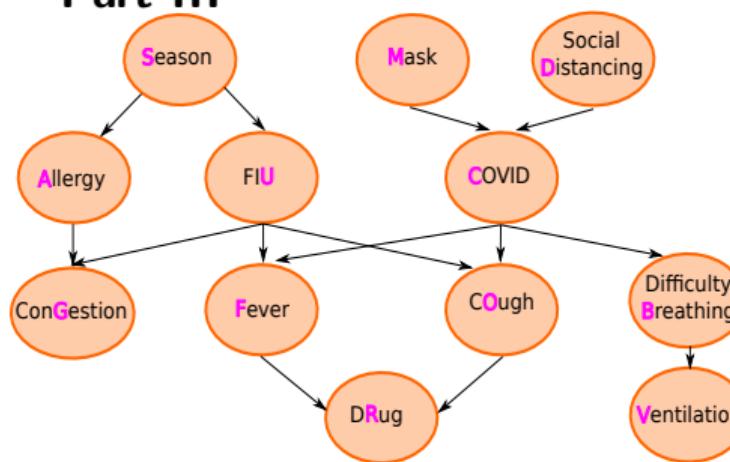
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Source: YouTube – easy learning – Causality 2: Intervention, [Link](#)

# Deep Learning Strategies – Part III

## Causal Learning

### Observation vs. Intervention



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- Force variables to certain values and check changes in the other variable
- Intervention  $\rightarrow$  Causality!!! (...Find causal relationships)

Source: YouTube – easy learning – Causality 2: Intervention, [Link](#)

## Causal Learning

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### Intervention – Do-Operator

- Definition “Intervention”: an ideal intervention on a given random variable  $Z$  is described by forcing its value to  $z$ , denoted  $\text{do}(Z := z)$  or  $\text{do}(z)$

Source: YouTube – easy learning – Causality 2: Intervention, [Link](#)

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- Constraint: when intervening on one variable, no other variable should be intervened

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- $P(Y|\text{do}(Z := z)) \rightarrow$  Probability of  $Y$ , given that  $Z$  is set/forced to  $z$       when  $z=z$   
 $P(Y|Z = z) \rightarrow$  Probability of  $Y$ , given that  $Z$  is seen/observed equals to  $z$       observation
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- $\text{do}(\text{COVID} := 1)$  or  $\text{do}(\text{COVID} := 0) \rightarrow$  Expectation: affect the likelihood of Fever, because COVID is a cause of fever (being the effect/symptom of COVID)
- $\text{do}(\text{Fever} := 1)$  or  $\text{do}(\text{Fever} := 0) \rightarrow$  Expectation: does not affect the likelihood of COVID, because Fever is NOT a cause of COVID (not a symptom of Fever)

Source: YouTube – easy learning – Causality 2: Intervention, [Link](#)

## Causal Learning

- Intervene on Fever (induce/remove fever) and observe COVID (person has/has not COVID), should not result in any probability difference of seeing/causing COVID:

$$P(\text{COVID}|\text{do}(\text{Fever})) = P(\text{COVID}|\text{do}(-\text{Fever}))$$

indicating that Fever does not cause COVID!

$$P(\text{COVID}|\text{see}(\text{Fever})) > P(\text{COVID}|\text{see}(-\text{Fever}))$$

Different from the observational relation!

## Causal Learning

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$$P(\text{COVID}|\text{see}(\text{Fever})) > P(\text{COVID}|\text{see}(-\text{Fever}))$$

see is  
observation

Different from the observational relation!

- However: intervene on COVID and observe Fever, lead to:

$$P(\text{Fever}|\text{do}(\text{COVID})) > P(\text{Fever}|\text{do}(-\text{COVID}))$$

COVID causes Fever!

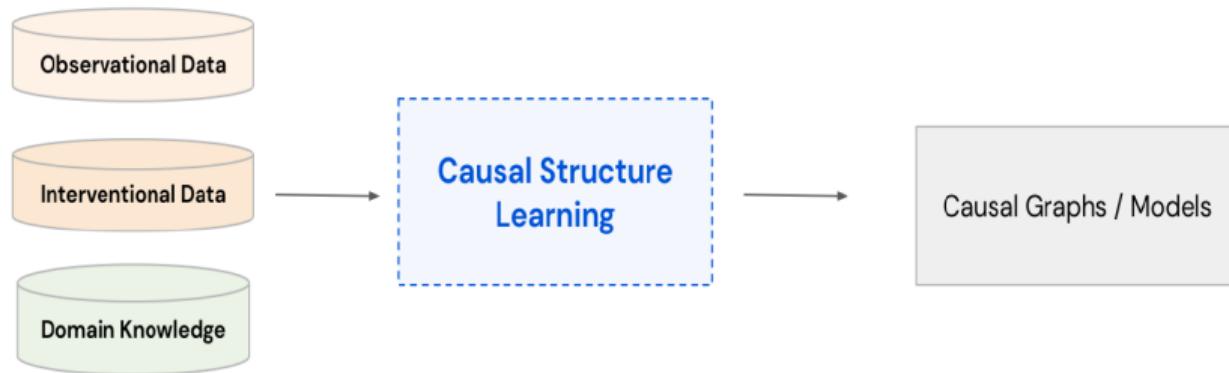
$$P(\text{Fever}|\text{COVID}) > P(\text{Fever}|-\text{COVID})$$

Interventional and observational relation is in line!

here the  
samples are iid  
and that is why  
we have  
relation  
between covid  
and fever

# Deep Learning Strategies – Part III

## Causal Learning

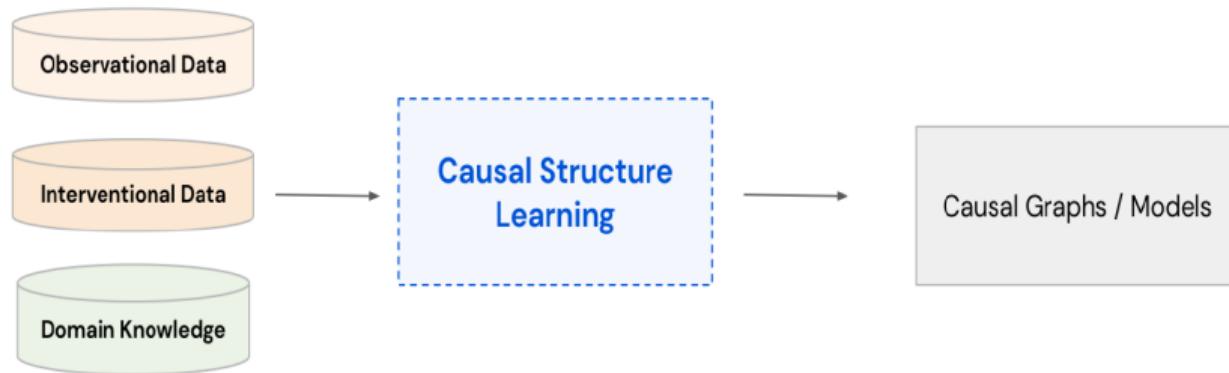


- **Observational Data:** collected without actively manipulating variables, just observing the natural state of the system (correlations/associations)

Source: FAU Erlangen-Nuremberg, Pattern Recognition Lab, K.Breininger, V. Christlein, Advanced Deep Learning – Interpretable/Causal Deep Learning

# Deep Learning Strategies – Part III

## Causal Learning

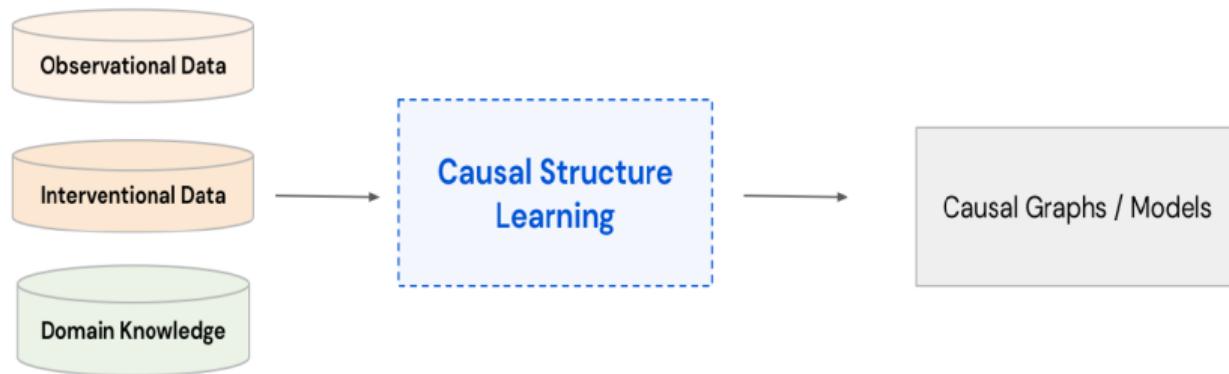


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- **Interventional Data:** collected by actively changing or intervening on specific variables, to reveal causal relationships

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# Deep Learning Strategies – Part III

## Causal Learning



- **Observational Data:** collected without actively manipulating variables, just observing the natural state of the system (correlations/associations)
- **Interventional Data:** collected by actively changing or intervening on specific variables, to reveal causal relationships
- **Domain Knowledge:** includes expert understanding, assumptions, or prior information about the system being studied, to help guiding the interpretation of observational data and the design of meaningful interventions

Source: FAU Erlangen-Nuremberg, Pattern Recognition Lab, K.Breininger, V. Christlein, Advanced Deep Learning – Interpretable/Causal Deep Learning

## Causality

- **Average Causal Effect (ACE):** Binary variable  $Z \in \{0, 1\}$ , causes variable  $Y$ , if the average causal effect (ACE) of  $Z$  on  $Y = y$  is defined as:

$$ACE(Z \rightarrow Y_y) = P(Y = y | do(Z := 1)) - P(Y = y | do(Z := 0))$$

is non-zero!

Source: YouTube – easy learning – Causality 3: Defining causality: Structural causal models (SCM), [Link](#)

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is non-zero!      if it is zero then there is no causal effect      interpret with previous slides

- **Causality:** A variable  $Z$  **causes** variable  $Y$  if there exist two interventional events  $z_0$  and  $z_1$  changing the distribution  $Y$ :

$$P(Y | do(z_0)) \neq P(Y | do(z_1))$$

- However: Let  $Y = X \oplus Z$  be the XOR-Function of  $X$  and  $Z$ , then:

$$P(Y | do(X = 0)) = P(Y | do(X = 1)) = P(Y)$$

check this formula

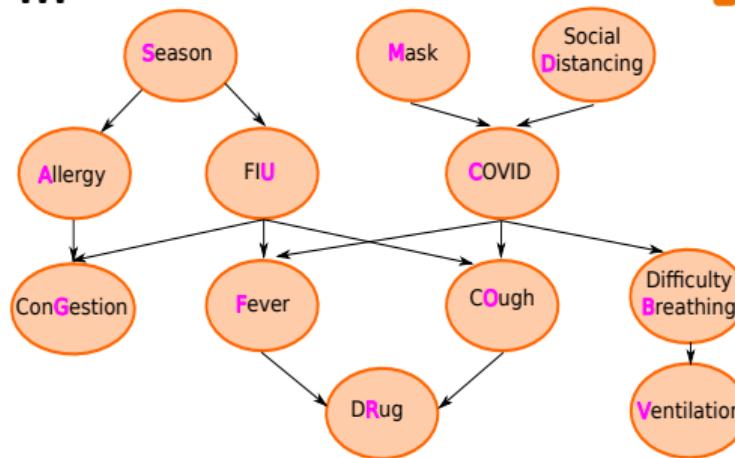
→ Better Definition as Deterministic Function!

Source: YouTube – easy learning – Causality 3: Defining causality: Structural causal models (SCM), [Link](#)

# Deep Learning Strategies – Part III

## Causal Learning

Causality as Deterministic Function!



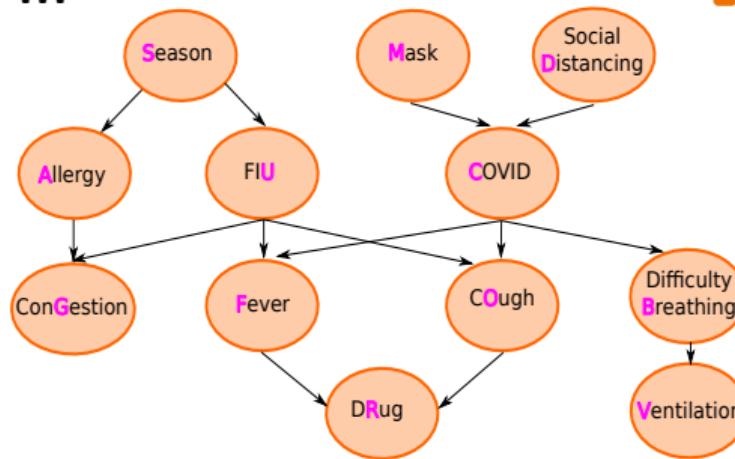
- COVID is the cause of Cough and Cough is the cause of Drug → More factors, however not being explicitly modeled and represented as single **exogenous** (latent variable)  $U_x$

Source: YouTube – easy learning – Causality 3: Defining causality: Structural causal models (SCM), [Link](#)

# Deep Learning Strategies – Part III

## Causal Learning

Causality as Deterministic Function!



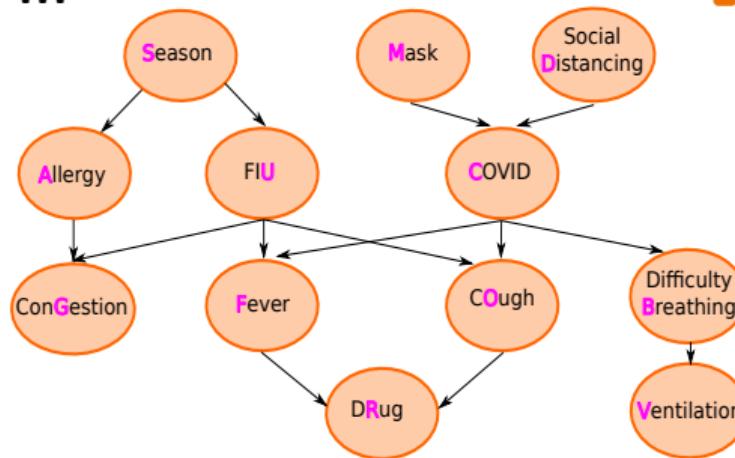
- COVID is the cause of Cough and Cough is the cause of Drug → More factors, however not being explicitly modeled and represented as single **exogenous** (latent variable)  $U_X$
- Each Variable  $X$  (here: C, O, R – referred to as **endogenous**) have such **exogenous** (here:  $U_C, U_O, U_R$ ) variables, used together with a **deterministic function** of is **endogenous** and **exogenous** parents

Source: YouTube – easy learning – Causality 3: Defining causality: Structural causal models (SCM), [Link](#)

# Deep Learning Strategies – Part III

## Causal Learning

Causality as Deterministic Function!



- COVID is the cause of Cough and Cough is the cause of Drug → More factors, however not being explicitly modeled and represented as single **exogenous** (latent variable)  $U_X$
- Each Variable  $X$  (here: C, O, R – referred to as **endogenous**) have such **exogenous** (here:  $U_C, U_O, U_R$ ) variables, used together with a **deterministic function** of its **endogenous** and **exogenous** parents
- $C := f_C(U_C) = U_C, O := f_O(C, U_O), R := f_R(O, U_R)$   
→ **Structural Causal Model (SCM)**

Source: YouTube – easy learning – Causality 3: Defining causality: Structural causal models (SCM), [Link](#)

# Deep Learning Strategies – Part III

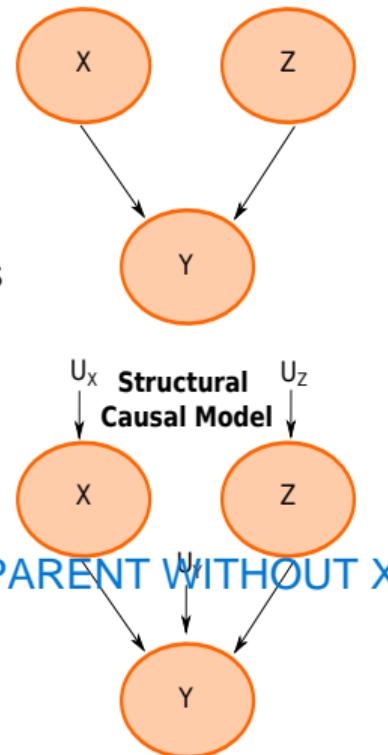
## Causal Learning

### Structural Causal Models (SCMs)

- SCM defined as a tuple  $\langle V, U, P_U, F \rangle$  with:
  1.  $V$  as the set of **endogenous** random variables
  2.  $U = \{U_X | X \in V\}$  as set of **exogenous/latent/noise** random variables
  3.  $P_U$  is the joint distribution over  $U$  satisfying  $P_U(U) = \prod_X P_U(U_X)$
  4.  $F$  set of functions  $f_X$ , how values are assigned to each variable  $X \in V$ , based on a subset of endogenous variables  $Pa_X \subset V \setminus \{X\}$  (**parents**), with a parent exogenous variable  $U_X \subset U$ , leading to:

$$X := f_X(Pa_X, U_X)$$

PAX IS PARENT WITHOUT X



Source: YouTube – easy learning – Causality 3: Defining causality: Structural causal models (SCM), [Link](#)

# Deep Learning Strategies – Part III

## Causal Learning

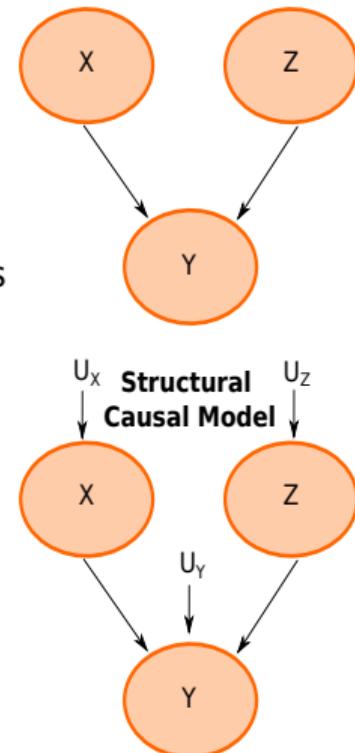
### Structural Causal Models (SCMs)

- SCM defined as a tuple  $\langle V, U, P_U, F \rangle$  with:
  1.  $V$  as the set of **endogenous** random variables
  2.  $U = \{U_X | X \in V\}$  as set of **exogenous/latent/noise** random variables
  3.  $P_U$  is the joint distribution over  $U$  satisfying  $P_U(U) = \prod_X P_U(U_X)$
  4.  $F$  set of functions  $f_X$ , how values are assigned to each variable  $X \in V$ , based on a subset of endogenous variables  $P_{AX} \subset V \setminus \{X\}$  (**parents**), with a parent exogenous variable  $U_X \subset U$ , leading to:

$$X := f_X(P_{AX}, U_X)$$

- **Causal graph (network)** over nodes  $V$ , where the parents of each node are linked to it (assume the graph as DAG)

Causal Network



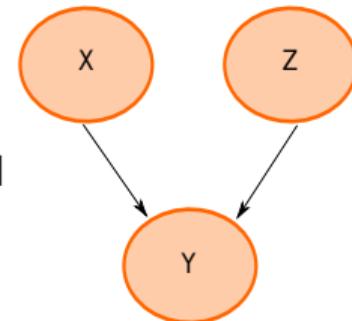
# Deep Learning Strategies – Part III

## Causal Learning

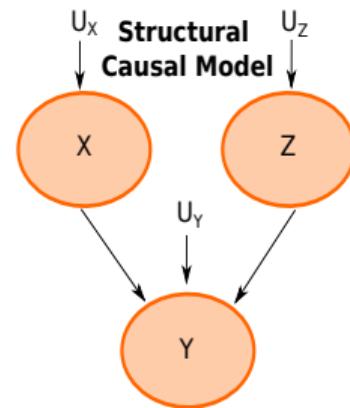
### Structural Causal Models (SCMs)

- Parents of a variable  $V$  are also called **direct causes** (one hierarchy level above), while the ancestors are known as **indirect causes** (multiple previous hierarchy levels)

#### Causal Network



#### Structural Causal Model



Source: YouTube – easy learning – Causality 3: Defining causality: Structural causal models (SCM), [Link](#)

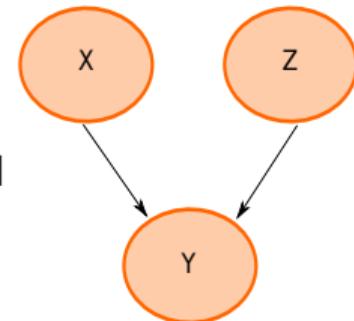
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## Causal Learning

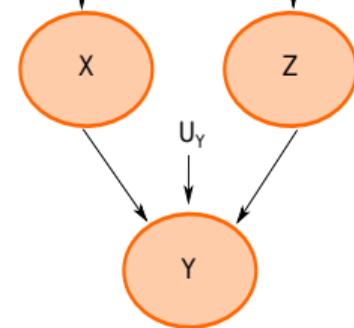
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Causal Network



Structural Causal Model



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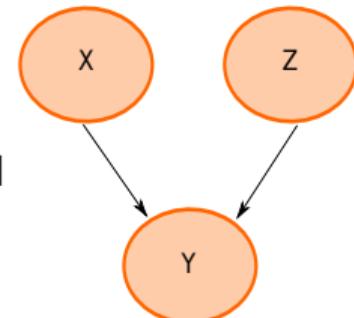
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## Causal Learning

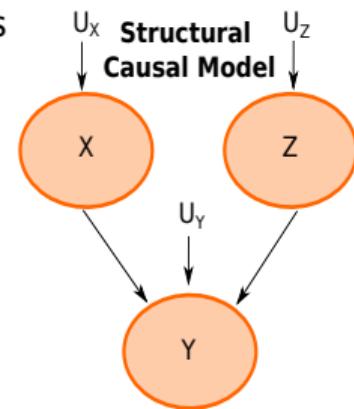
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- The variable  $X = f_X(Pax, U_X)$  (e.g.  $Y$ ) depends only on endogenous parents (e.g  $X, Z$ ), together with the exogenous variable (e.g  $U_Y$ )

Causal Network



Structural Causal Model



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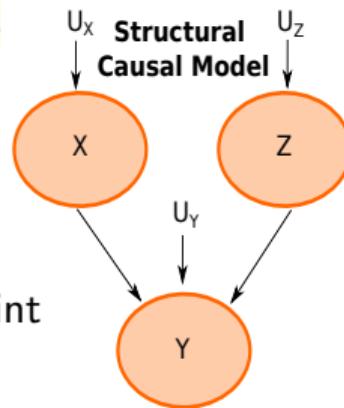
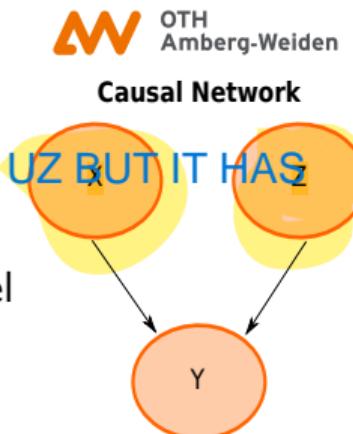
# Deep Learning Strategies – Part III

## Causal Learning

### Structural Causal Models (SCMs)

Y DOENT CARE ABOUT UX AND UZ BUT IT HAS EFFECTED BY UY

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- The variable  $X = f_X(Pax, U_X)$  (e.g.  $Y$ ) depends only on endogenous parents (e.g  $X, Z$ ), together with the exogenous variable (e.g  $U_Y$ )
- Observational distribution of all endogenous variables  $V$  refers to the joint probability distribution  $P(V) = \prod_X P(X|Pax)$



Source: YouTube – easy learning – Causality 3: Defining causality: Structural causal models (SCM), [Link](#)

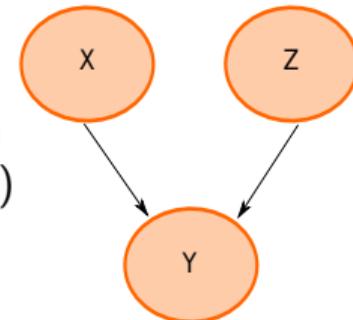
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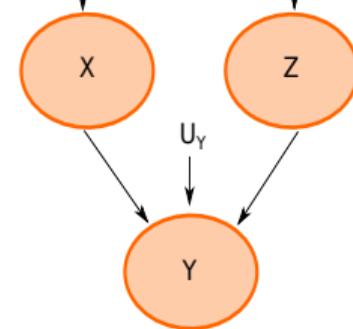
### Structural Causal Models (SCMs)

- The causal network  $\mathcal{G}$  is an I-Map for  $P(V) = \prod_X P(X|Pax)$  (**Bayesian Network Factorization**) with  $P(X|Pax)$  obtained from  $X = f_X(Pax, U_X)$

Causal Network



Structural Causal Model



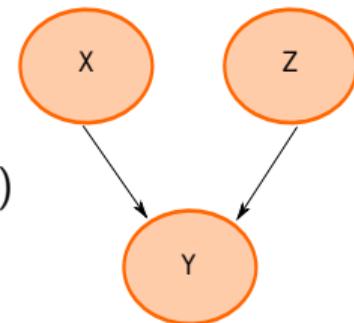
# Deep Learning Strategies – Part III

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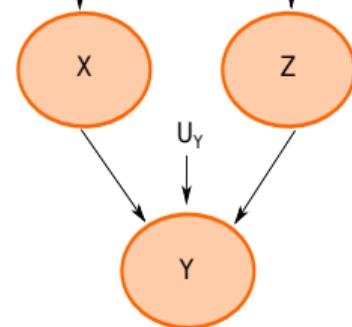
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#### Causal Network



#### Structural Causal Model



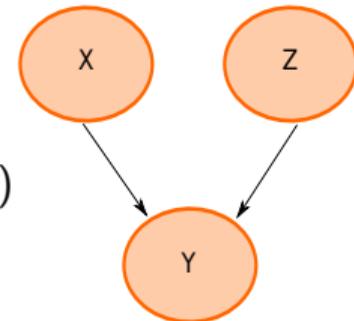
# Deep Learning Strategies – Part III

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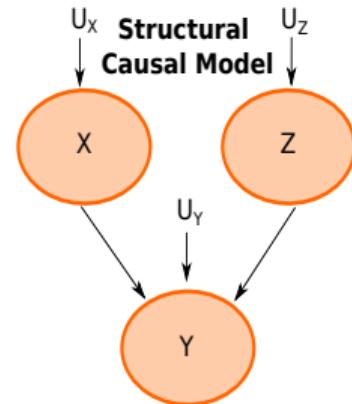
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Causal Network



Structural Causal Model



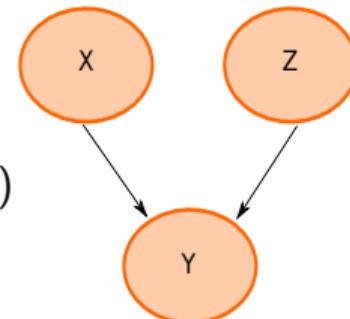
# Deep Learning Strategies – Part III

## Causal Learning

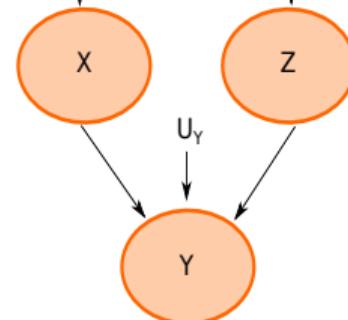
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- **Example I-MAP Graph:**  $X \rightarrow Y \rightarrow Z$  – with  $X$  = Having Disease,  $Y$  = Taking Medication,  $Z$  = Observing Side Effects

Causal Network



U<sub>X</sub>      **Structural Causal Model**      U<sub>Z</sub>



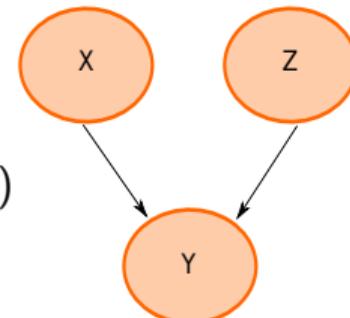
# Deep Learning Strategies – Part III

## Causal Learning

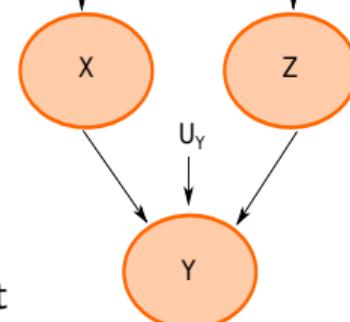
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$$P(X, Z|Y) = P(X|Y)P(Z|Y)$$
- Example I-MAP Graph:**  $X \rightarrow Y \rightarrow Z$  – with  $X$  = Having Disease,  $Y$  = Taking Medication,  $Z$  = Observing Side Effects
- Captures **direct dependencies** ( $X \rightarrow Y$ ,  $Y \rightarrow Z$ ) and **conditional independencies** ( $X$  and  $Z$  are independent given  $Y$ , disease  $X$  alone not directly lead to side effects  $Z$ , only through the medication  $Y$  – parents!!!)

Causal Network



Structural Causal Model



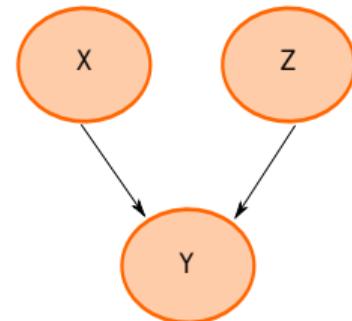
# Deep Learning Strategies – Part III

## Causal Learning

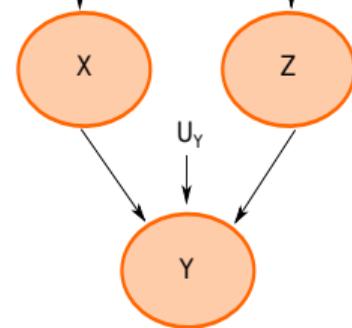
### Structural Causal Models (SCMs) – Example XOR

- $P(V) = P(X = x, Z = z, Y = y)$

#### Causal Network



$U_x$  **Structural Causal Model**  $U_z$



Source: YouTube – easy learning – Causality 3: Defining causality: Structural causal models (SCM), [Link](#)

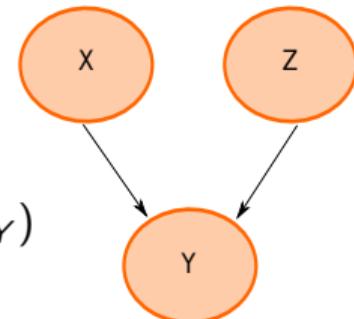
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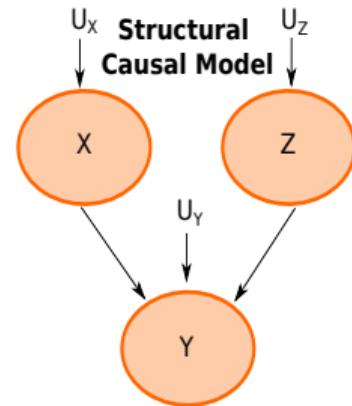
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Causal Network



Structural Causal Model



Source: YouTube – easy learning – Causality 3: Defining causality: Structural causal models (SCM), [Link](#)

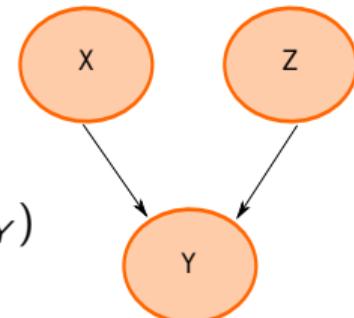
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## Causal Learning

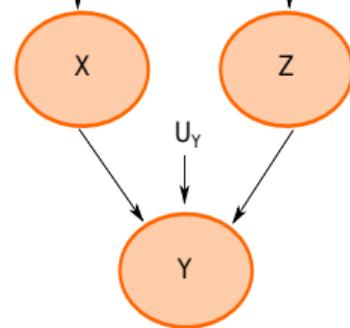
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- $Z = f_Z(Pa_Z, U_Z) = U_Z$
- $Y = f_Y(Pa_Y, U_Y)$ , with  $U_Y = 0 \rightarrow Y = (X, Z)$

#### Causal Network



$U_X$  **Structural Causal Model**  $U_Z$



Source: YouTube – easy learning – Causality 3: Defining causality: Structural causal models (SCM), [Link](#)

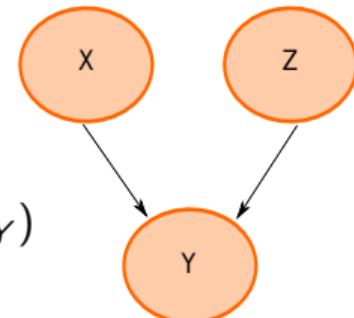
# Deep Learning Strategies – Part III

## Causal Learning

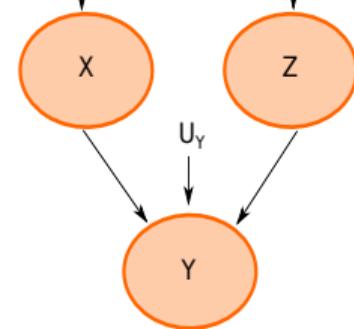
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- $Y = f_Y(Pa_Y, U_Y)$ , with  $U_Y = 0 \rightarrow Y = (X, Z)$
- $P(V) = P(x)P(z)P(y|x, z) = P(U_X = x)P(U_Z = z)1_y(x \oplus z)$   
with:  $1_y(b) = 1$ , if  $y = b$ , otherwise 0

#### Causal Network



$U_X$  **Structural Causal Model**  $U_Z$



Source: YouTube – easy learning – Causality 3: Defining causality: Structural causal models (SCM), [Link](#)

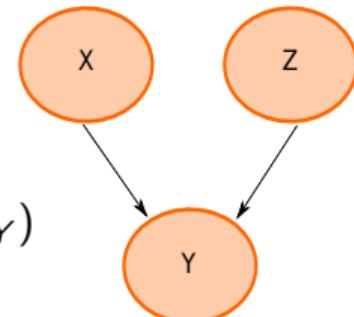
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## Causal Learning

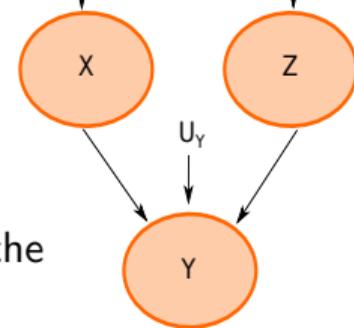
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- $X = f_X(Pa_X, U_X) = U_X$       x and z has only  $U_X$  and  $U_Z$  as parents
- $Z = f_Z(Pa_Z, U_Z) = U_Z$
- $Y = f_Y(Pa_Y, U_Y)$ , with  $U_Y = 0 \rightarrow Y = (X, Z)$
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with:  $1_y(b) = 1$ , if  $y = b$ , otherwise 0      xor operation here
- Note: From an SCM it is possible to compute the joint distribution of the given variables!

#### Causal Network



$U_X$       **Structural Causal Model**       $U_Z$



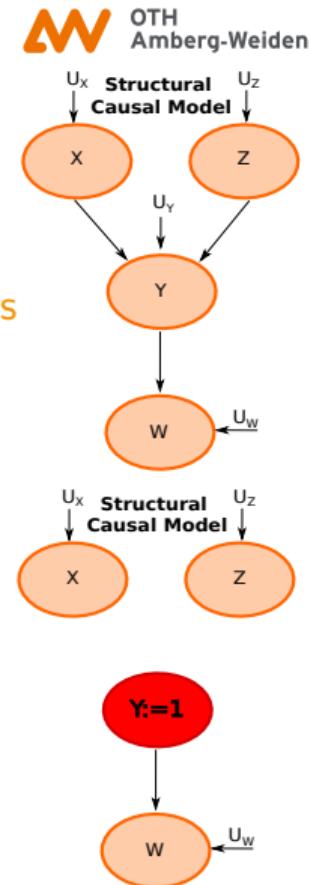
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# Deep Learning Strategies – Part III

## Causal Learning

### Structural Causal Models (SCMs) – Example XOR – Intervention

- Causal network turns into a Bayesian network if augmented with CPDs (prior probabilities, conditional probabilities) answering **probability queries**  $P(Y|Z = z)$  for all  $z \in Val(Z)$ ,  $Z, Y \subseteq V$



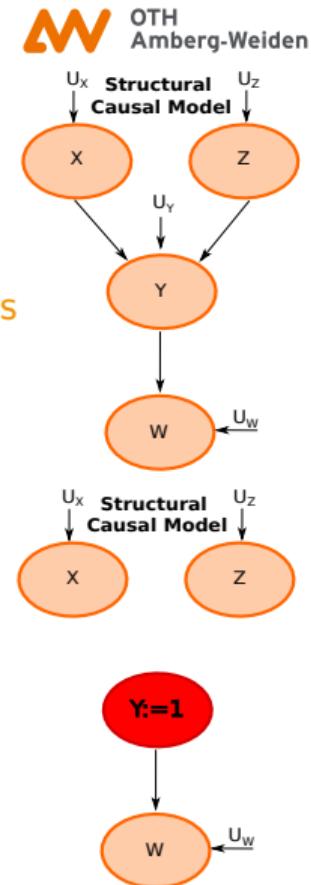
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# Deep Learning Strategies – Part III

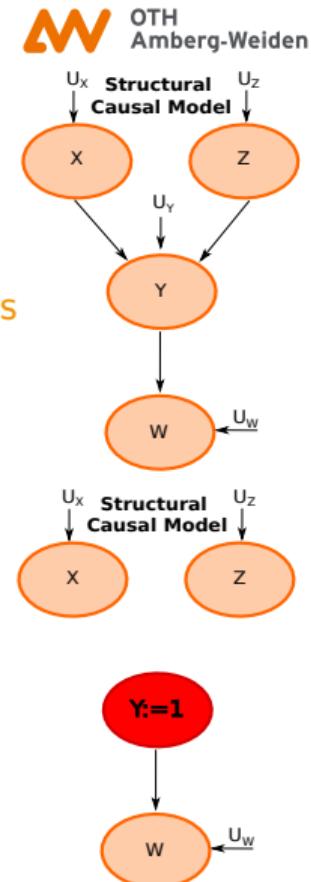
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- **Intervention in SCMs (do-operation):** setting  $Y := 1$

Before:  $X := U_X$ ,  $Z := U_Z$ ,  $Y := X \oplus Z + U_Y$ ,  $W := 2Y + U_W$

After:  $X := U_X$ ,  $Z := U_Z$ ,  $Y := 1$ ,  $W := 2Y + U_W \rightarrow U_W = W - 2$



Source: YouTube – easy learning – Causality 3: Defining causality: Structural causal models (SCM), [Link](#)

# Deep Learning Strategies – Part III

## Causal Learning

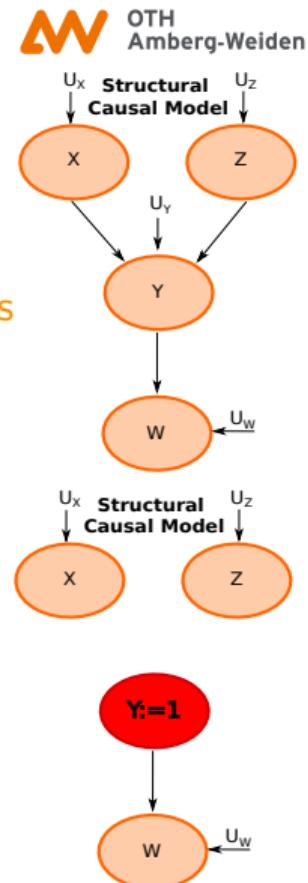
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- $Y$  does not depend on its endogenous/exogenous parents  $Pa_Y$  (all incoming links in the graph are removed!) → **Perfect intervention!**



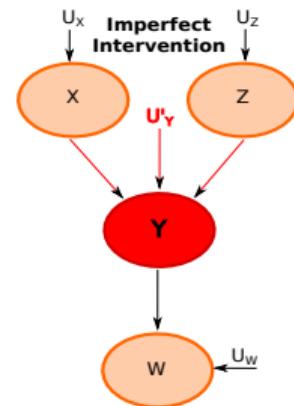
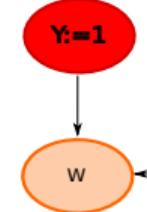
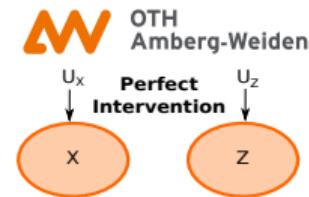
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# Deep Learning Strategies – Part III

## Causal Learning

### Structural Causal Models (SCMs) – Example XOR – Intervention

- In a **perfect intervention** the variable  $Y$  has a fixed/static value, based on its intervened value



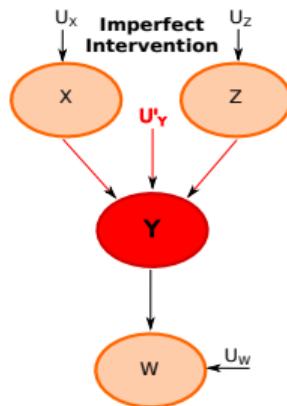
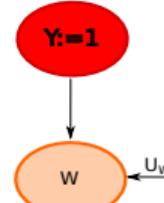
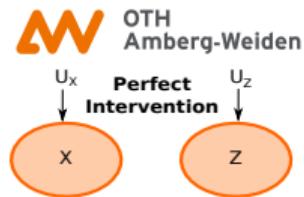
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# Deep Learning Strategies – Part III

## Causal Learning

### Structural Causal Models (SCMs) – Example XOR – Intervention

- In a **perfect intervention** the variable  $Y$  has a fixed/static value, based on its intervened value
- However: there exist also an **imperfect/parametric intervention**, known as **mechanism change ( $f'$  assignment)** (still some remaining parents)  $\rightarrow Y := f(P_{aY}, U_Y) \rightarrow Y := f'(P_{aY}, U'_Y)$  (e.g.  $Y := X - Z + U'_Y$ )



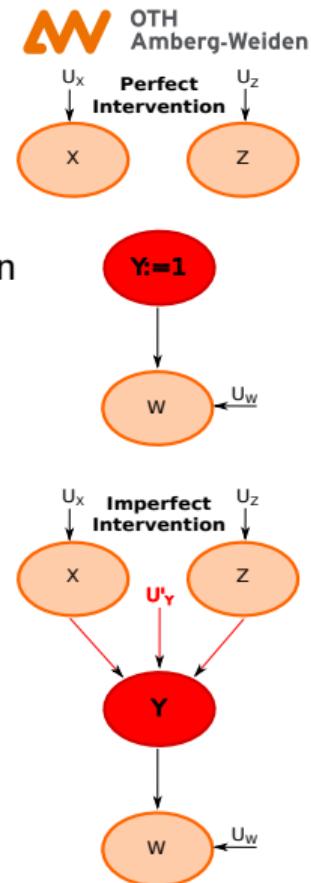
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# Deep Learning Strategies – Part III

## Causal Learning

### Structural Causal Models (SCMs) – Example XOR – Intervention

- In a **perfect intervention** the variable  $Y$  has a fixed/static value, based on its intervened value
- However: there exist also an **imperfect/parametric intervention**, known as **mechanism change ( $f'$  assignment)** (still some remaining parents)  $\rightarrow Y := f(P_{aY}, U_Y) \rightarrow Y := f'(P_{aY}, U'_Y)$  (e.g.  $Y := X - Z + U'_Y$ )
- Every intervention leads to a CPD change w.r.t.  $Y$  from:  
$$Y : P(Y|Pa_Y) \text{ to } P^*(Y|Pa_Y)$$



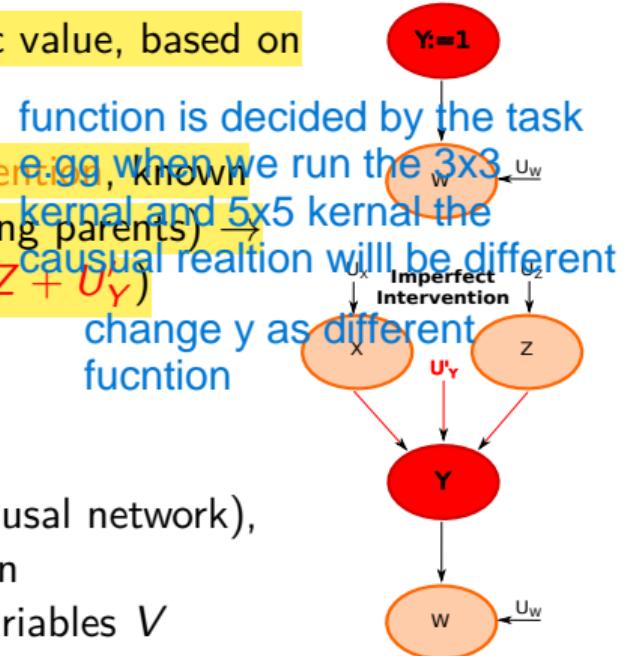
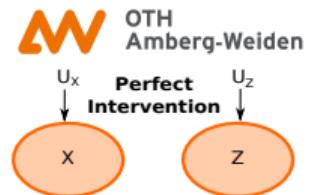
Source: YouTube – easy learning – Causality 3: Defining causality: Structural causal models (SCM), [Link](#)

# Deep Learning Strategies – Part III

## Causal Learning

### Structural Causal Models (SCMs) – Example XOR – Intervention

- In a **perfect intervention** the variable  $Y$  has a fixed/static value, based on its intervened value
- However: there exist also an **imperfect/parametric intervention** as **mechanism change ( $f'$  assignment)** (still some remaining parents)  $\rightarrow Y := f(P_{aY}, U_Y) \rightarrow Y := f'(P_{aY}, U'_Y)$  (e.g.  $Y := X - Z + U_Y$ )
- Every intervention leads to a CPD change w.r.t.  $Y$  from:  
$$Y : P(Y|P_{aY}) \text{ to } P^*(Y|P_{aY})$$
- After every intervention there exist still a (new) SCM (causal network), with different dependencies and a intervention distribution  
 $P(V \setminus Z, \text{do}(Z))$  a intervention distribution over all the variables  $V$

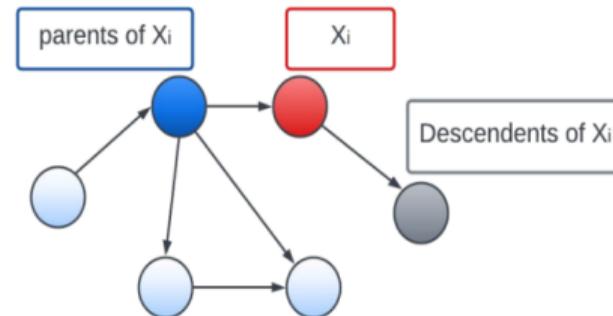


Source: YouTube – easy learning – Causality 3: Defining causality: Structural causal models (SCM), [Link](#)

### summary slide

Describing the causal mechanisms of a system.

- **Variables:**  $\mathbf{X} = \{X_1, \dots, X_N\}$
- **Noise:**  $U = \{U_1, \dots, U_N\}$
- **Causal parents of  $X_i$ :**  $X_{pa(i,G)}$
- **Structural Equations:**  $X_i = f_i(X_{pa(i,G)}, U_i) \quad \forall i \in \{1, \dots, N\}$   
(Causal Mechanisms)

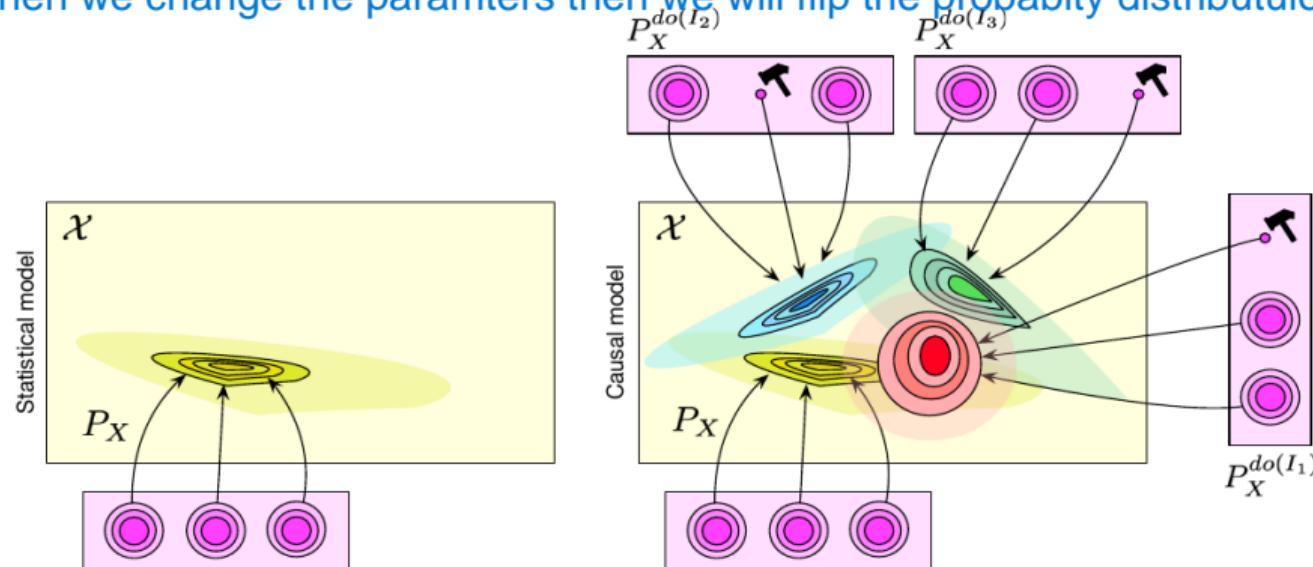


Source: Image from Nan Rosemary Ke, Stefan Bauer, "Causality and Deep Learning: Synergies, Challenges and the Future", Slide 22

# Deep Learning Strategies – Part III

## Causal Learning

when we change the parameters then we will flip the probability distribution



- Statistical (Bayesian) Model: can only capture one probability distribution
- Causal Model: every intervention defines new joint distribution intervention

Source: FAU Erlangen-Nuremberg, Pattern Recognition Lab, K.Breininger, V. Christlein, Advanced Deep Learning – Interpretable/Causal Deep Learning

Source: Image from Nan Rosemary Ke, Stefan Bauer, "Causality and Deep Learning: Synergies, Challenges and the Future", Slide 22

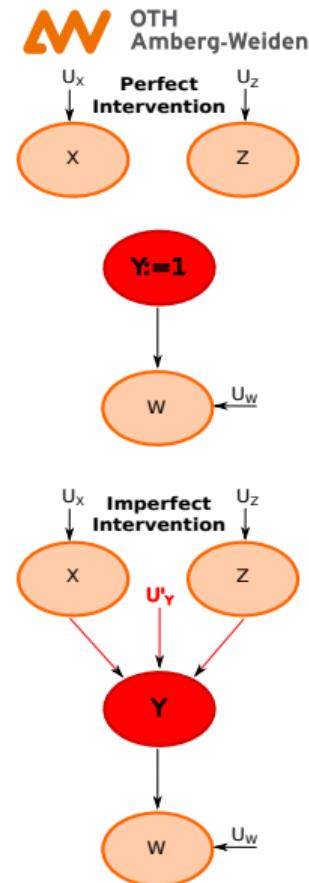
Source: Schölkopf et al., "Toward Causal Representation Learning"

# Deep Learning Strategies – Part III

## Causal Learning

### Structural Causal Models (SCMs) – Example XOR – Mutilated Network

- Converting an **intervention** to an **observation** query (remove all do's)



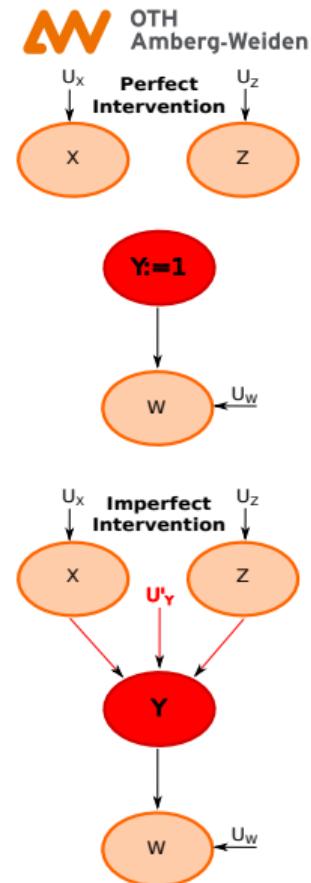
Source: YouTube – easy learning – Causality 3: Defining causality: Structural causal models (SCM), [Link](#)

# Deep Learning Strategies – Part III

## Causal Learning

### Structural Causal Models (SCMs) – Example XOR – Mutilated Network

- Converting an **intervention** to an **observation query** (remove all do's)
- In case of the previous Bayesian Network, and for a **perfect intervention query**,  $P(Y|do(z), x)$  is transformed to  $P(Y|z, x)$ , by removing all incoming edges to the intervened nodes  $Z$ , and set a fixed intervention value  $Z = z$



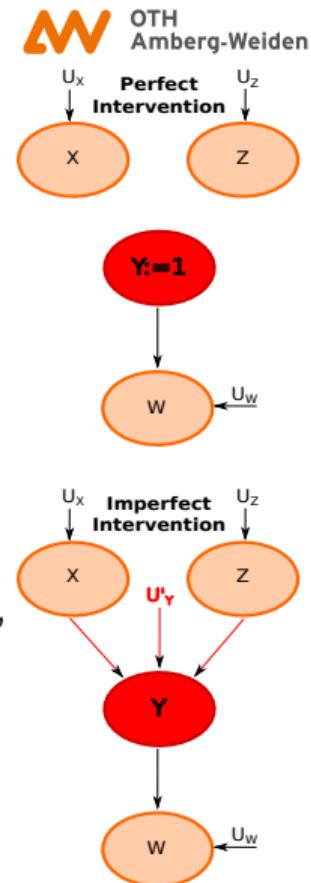
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# Deep Learning Strategies – Part III

## Causal Learning

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- **Mutilated Network:**  $\mathcal{B}_{Z:=z}$ , given a Bayesian Network  $\mathcal{B}$ , while removing all incoming links to the set of nodes  $Z$  and setting  $Z = z$  (static value),  $P(Z = z') = 1$  if  $z' = z$ , otherwise 0



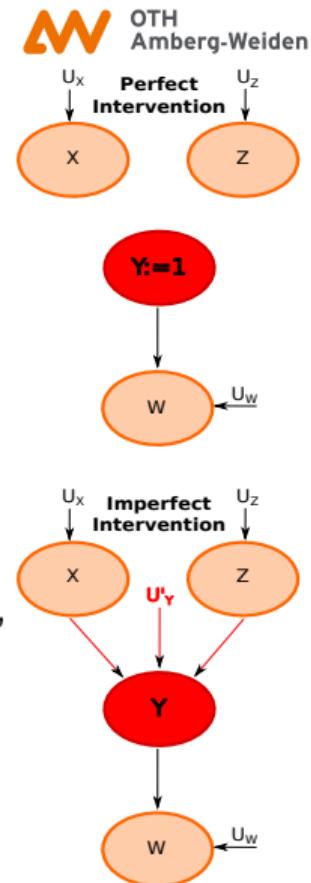
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# Deep Learning Strategies – Part III

## Causal Learning

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- Answering intervention queries:  $P(Y|\text{do}(z), x) = P_{\mathcal{B}_{Z:=z}}(Y|z, x)$



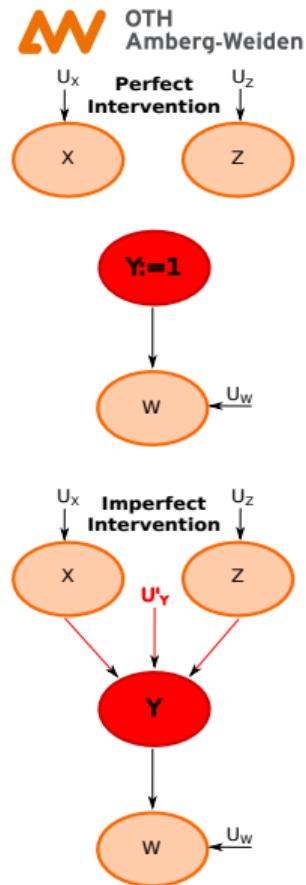
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# Deep Learning Strategies – Part III

## Causal Learning

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- Answering intervention queries:  $P(Y|\text{do}(z), x) = P_{\mathcal{B}_{Z:=z}}(Y|z, x)$
- **Modularity:** conditional probability of a node is only affected if intervention is on its parents  $P(Y|P_{\text{ay}}, \text{do}(z)) = P(Y|P_{\text{ay}})$ ,  $\forall Y \notin Z$



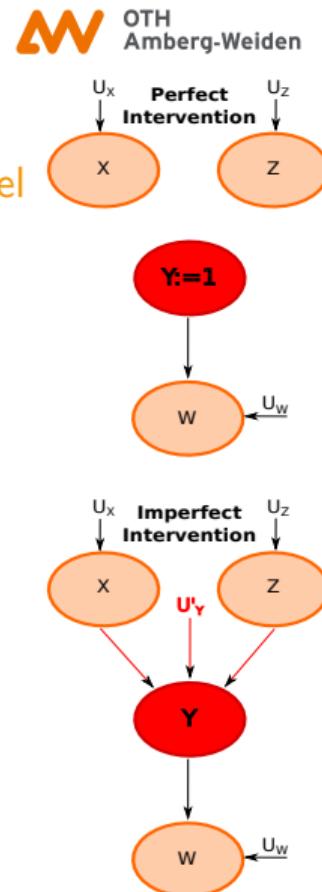
Source: YouTube – easy learning – Causality 3: Defining causality: Structural causal models (SCM), [Link](#)

# Deep Learning Strategies – Part III

## Causal Learning

### Structural Causal Models (SCMs) – Example XOR – Causal (Bayesian) Model

- **Causal (Bayesian) Network  $\mathcal{C}$  (CBN):** over a set of random variables  $V$  (joint distribution  $P$ ),  $\mathcal{C}$  is a Bayesian network  $\mathcal{B}(\mathcal{G}, P_{\mathcal{C}})$ , with  $\mathcal{G}$  is an I-Map for  $P$ , over  $V$ , answering both probability queries:
  1.  $P(Y|x) = P_{\mathcal{C}}(Y|x)$  and intervention queries:
  2.  $P(Y|Pa_Y, \text{do}(z)) = P_{\mathcal{C}_{Z:=z}}(Y|Pa_Y), \forall Y \notin Z, z \in \text{Val}(Z)$



Source: YouTube – easy learning – Causality 4: Causal Bayesian Networks, [Link](#)

# Deep Learning Strategies – Part III

## Causal Learning

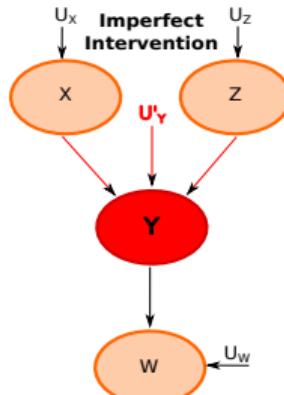
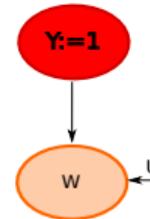
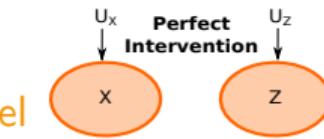
### Structural Causal Models (SCMs) – Example XOR – Causal (Bayesian) Model

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2.  $P(Y|Pa_Y, do(z)) = P_{\mathcal{C}_{Z:=z}}(Y|Pa_Y), \forall Y \notin Z, z \in Val(Z)$

- Recap: Causal Hierarchy

1. **Association (Seeing!)** – Probabilistic query  $P(Y|X)$  (e.g. probability of developing cancer given that the individual smokes?) – BN, CBN, SCM
2. **Intervention (Doing!)** – Intervention query  $P(Y|do(X))$  (e.g. What is the prob. of developing cancer if individuals stop smoking?) – CBN, SCM
3. **Counterfactual (Imagining!)** – Counterfactual query  $P(Y_{X=1}|X=0)$  (e.g. What would have happened if individuals had quitted smoking?) – SCM



Source: YouTube – easy learning – Causality 4: Causal Bayesian Networks, [Link](#)

## Causal Learning

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### Structural Causal Models (SCMs) – Counterfactual Queries

- Bayesian Network (BN) is able to answer probabilistic queries (associations), while Causal Bayesian Networks (CBN) & SCM can also handle intervention queries

Source: YouTube – easy learning – Causality 6: Counterfactual Queries, [Link](#)

## Causal Learning

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### Structural Causal Models (SCMs) – Counterfactual Queries

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- What about the last topic, addressing **counterfactual queries?**

Source: YouTube – easy learning – Causality 6: Counterfactual Queries, [Link](#)

## Causal Learning

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### Structural Causal Models (SCMs) – Counterfactual Queries

- Bayesian Network (BN) is able to answer probabilistic queries (associations), while Causal Bayesian Networks (CBN) & SCM can also handle intervention queries
- What about the last topic, addressing **counterfactual queries**?
- **Example:** There was a fork in the road, where a decision must be made – take the freeway ( $X = 1$ ) or go on a surface street ( $X = 0$ ). The person took the surface street with a lot of traffic and arrived one hour later ( $Y = 1$ ). He asked himself – If he had taken the freeway, he would have gotten home earlier!!!

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- Such an **unrealized situation from the past**, wrapped in an “if-statement” is known as **counterfactual** → How to model a counterfactual query/situation?

Source: YouTube – easy learning – Causality 6: Counterfactual Queries, [Link](#)

## Causal Learning

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### Structural Causal Models (SCMs) – Counterfactual Queries

- Let  $Y$  be the arriving time ( $Y = 1$  for being late,  $Y = 0$  for being in time)

Source: YouTube – easy learning – Causality 6: Counterfactual Queries, [Link](#)

## Causal Learning

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### Structural Causal Models (SCMs) – Counterfactual Queries

- Let  $Y$  be the arriving time ( $Y = 1$  for being late,  $Y = 0$  for being in time)
- Causal inference: prediction of  $Y$  from the past, by intervening on the road (change from surface road  $X = 0$  to freeway  $X = 1$ ):  $P(Y|\text{do}(X = 1))$

Source: YouTube – easy learning – Causality 6: Counterfactual Queries, [Link](#)

## Causal Learning

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- **Counterfactual problem:** asking about  $Y$ , if we had forced  $X := 1$  in the past observed event with  $X = 0, Y = 1 \rightarrow$  Clash regarding  $Y$ :  $P(Y|\text{do}(X = 1), Y = 1, X = 0)$

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## Causal Learning

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- **Counterfactual inference:** reformulate as:  $P(Y_{X=1}|X = 0, Y = 1)$

Source: YouTube – easy learning – Causality 6: Counterfactual Queries, [Link](#)

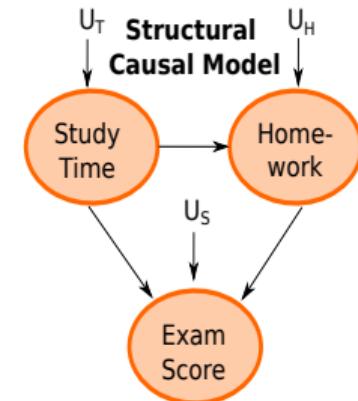
## Causal Learning

### Structural Causal Models (SCMs) – Counterfactual Queries

- Example Counterfactual Event:

►  $T := U_T, \quad H := 0.5T + U_H, \quad S := 0.7T + 0.4H + U_S$

with:  $T$  as the students studying time,  $H$  as the number of completed homeworks,  $S$  student's exam score,  $U_T$  student's free time at home,  $U_H$  student's intelligence,  $U_S$  student's anxiety



Source: YouTube – easy learning – Causality 6: Counterfactual Queries, [Link](#)

## Causal Learning

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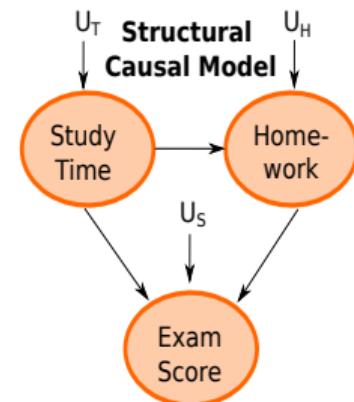
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- Let  $T = 0.5$ ,  $H = 1$ , and  $S = 1.5$  for a particular student, resulting in:

$$U_T := T = 0.5, \quad U_H = H - 0.5T = 1 - 0.5 \cdot 0.5 = 0.75,$$

$$U_S = S - 0.7T - 0.4H = 1.5 - 0.7 \cdot 0.5 - 0.4 \cdot 1 = 0.75$$



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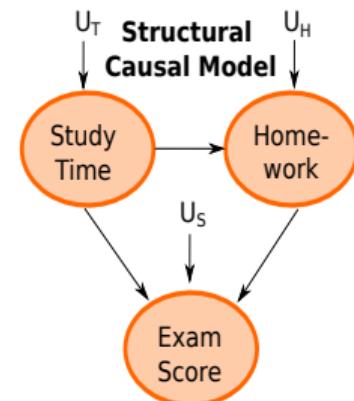
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- Counterfactual problem: what would the student's score have been if he had doubled his done homework?



Source: YouTube – easy learning – Causality 6: Counterfactual Queries, [Link](#)

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### Structural Causal Models (SCMs) – Counterfactual Queries

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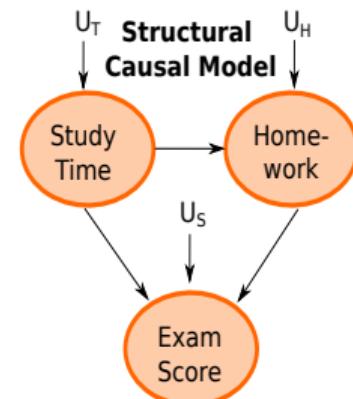
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- Intervention: do-operator to  $P(S|Pa_S, U_S) = P(S|T, \text{do}(H := 2), U_S)$



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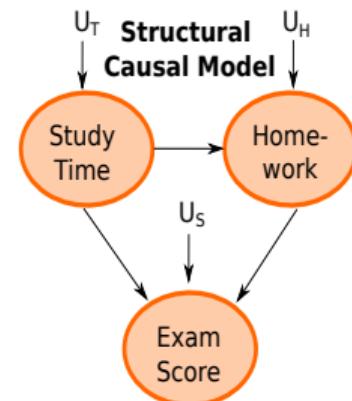
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- Intervention: do-operator to  $P(S|Pa_S, U_S) = P(S|T, \text{do}(H := 2), U_S)$

- Counterfaction:  $P(S_{H=2}|T = 0.5, H = 1, S = 1.5)$

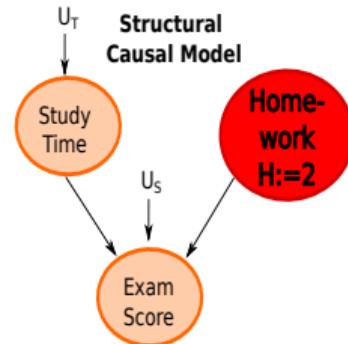


Source: YouTube – easy learning – Causality 6: Counterfactual Queries, [Link](#)

## Causal Learning

### Structural Causal Models (SCMs) – Counterfactual Queries

- Example Counterfactual Event
  - ▶ Create mutilated graph, by removing all incoming links to the intervened node  $Z = H$ , with  $P(H = 2) = 1$



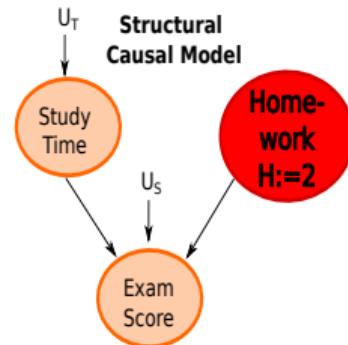
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Source: YouTube – easy learning – Causality 6: Counterfactual Queries, [Link](#)

## Causal Learning

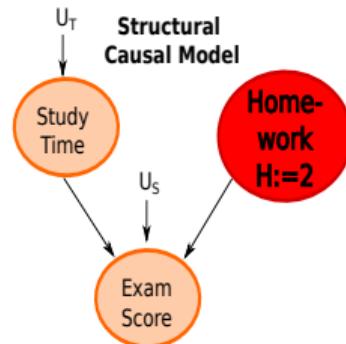
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- Abduction-Action-Prediction

1. Abduction – use evidence  $E = e$  in order to determine all the values of  $U$



Source: YouTube – easy learning – Causality 6: Counterfactual Queries, [Link](#)

## Causal Learning

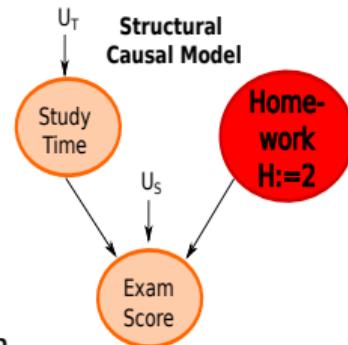
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- Abduction-Action-Prediction

1. Abduction – use evidence  $E = e$  in order to determine all the values of  $U$
2. Action – Removing structural equations for variables  $X$  and replace it with the appropriate functions  $X = x$  (Mutilated Graph!)



Source: YouTube – easy learning – Causality 6: Counterfactual Queries, [Link](#)

## Causal Learning

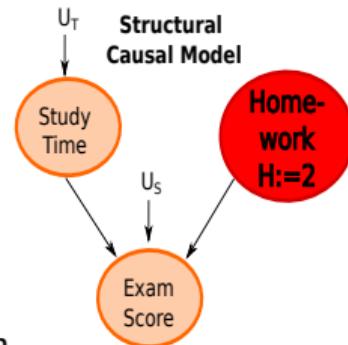
### Structural Causal Models (SCMs) – Counterfactual Queries

- Example Counterfactual Event

- ▶ Create mutilated graph, by removing all incoming links to the intervened node  $Z = H$ , with  $P(H = 2) = 1$
- ▶ Compute  $S$  in the mutilated graph, by  $S := 0.7T + 0.4H + U_S$  with:  
 $S_{H=2}(T = 0.5, U_S = 0.75) = 0.7 \cdot 0.5 + 0.4 \cdot 2 + 0.75 = 1.9$

- Abduction-Action-Prediction

1. Abduction – use evidence  $E = e$  in order to determine all the values of  $U$
2. Action – Removing structural equations for variables  $X$  and replace it with the appropriate functions  $X = x$  (Mutilated Graph!)
3. Prediction – Use the mutilated model and the value of  $U$  to compute the value of  $Y$ , the consequence of the counterfactual



Source: YouTube – easy learning – Causality 6: Counterfactual Queries, [Link](#)

## Causal Learning

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### Summary – Difference BN, CBN and SCM

- Bayesian Network (BN)
- 1. BN is a directed acyclic graph (DAG) that represents probabilistic relationships among variables, while each random variable (node) connection represents a conditional dependence → No causation, only correlations, and conditional independencies

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  2. Example: Bayesian Network, with nodes: Flu → Fever, Flu → Cough, while the model/graph shows the association between Flu and Fever, as well as Flu and Cough, however, no information that Flu causes both

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  5. Example: same graph w.r.t. causation, show that Flu causes Fever and Cough, while intervening Flu causes an impact with respect to Fever and Cough

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- Structural Causal Model (SCM)
1. SCM is a causal model providing a more formal framework than a CBN, using a set of structural equations that specify how each variable is generated as a function of its causal parents and some random “noise” term, along with a causal DAG structure

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  2. SCMs allow for both causal inference and formal intervention analysis, while being used for counterfactual reasoning, interventions, and predicting causal effects
  3. SCM would not only represent Flu causing Fever & Cough, but also provide equations –  $\text{Fever}=f(\text{Flu}, U_F)$ ,  $\text{Cough}=g(\text{Flu}, U_C)$  – specifying how Flu influences Fever & Cough under different conditions

# Further Questions?



<https://www.oth-aw.de/hochschule/ueber-uns/personen/bergler-christian/>

Source: <https://emekaboris.medium.com/the-intuition-behind-100-days-of-data-science-code-c98402cdc92c>