



# **Advanced Topics in Machine Learning**

**Winter Semester 2024/2025**

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Prof. Dr.-Ing. Christian Bergler | OTH Amberg-Weiden

### Topics of Today: Advanced Deep Learning Strategies – Part III

- Self-Supervised Learning
- Active Learning

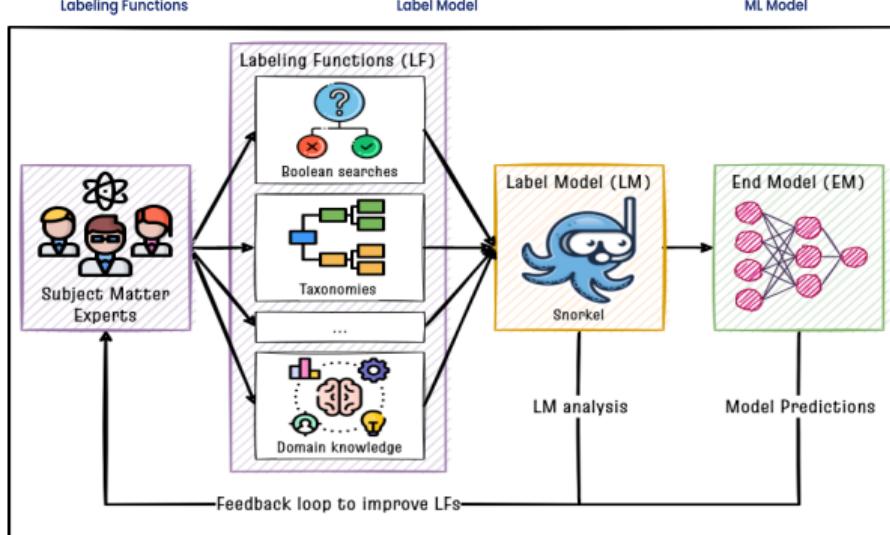
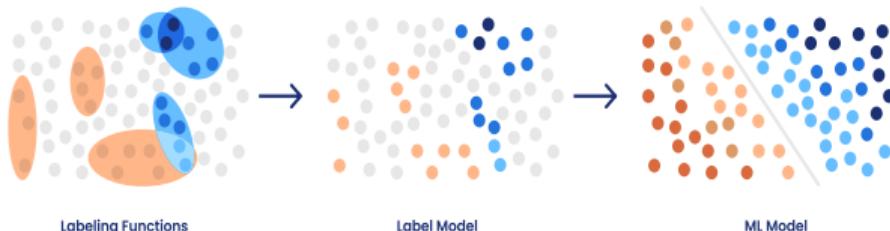
### Topics of Today: Advanced Deep Learning Strategies – Part III

- Weak Supervision
- N-Shot Learning
- Causal Learning

# Deep Learning Strategies – Part III

## Weak Supervision

- Goal: How to transfer an unsupervised to a (weakly) supervised task!



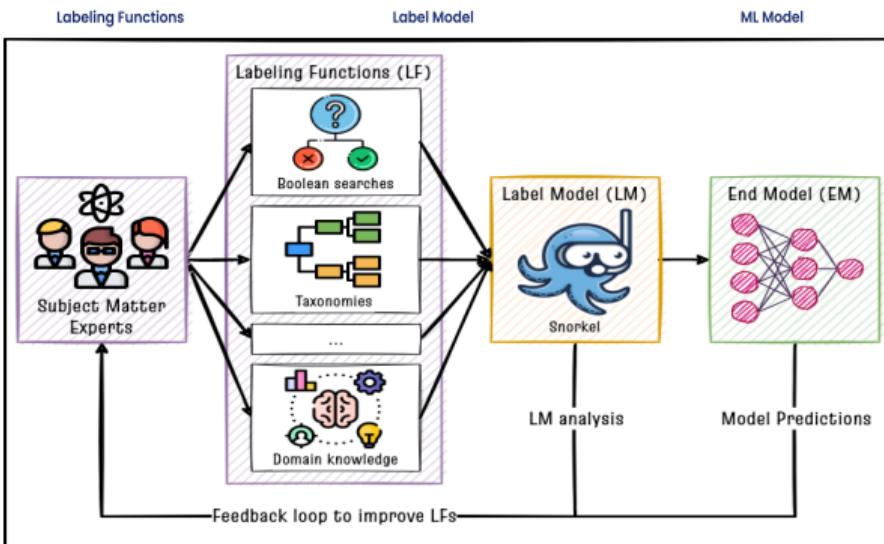
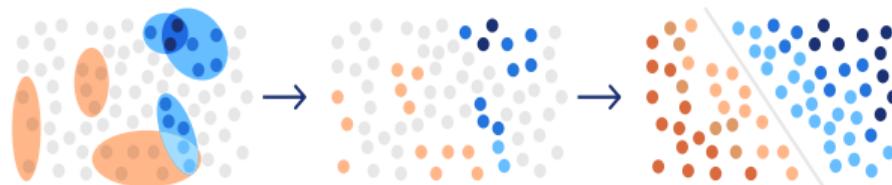
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# Deep Learning Strategies – Part III

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- **Goal:** How to transfer an unsupervised to a (weakly) supervised task!
- Interpret & categorize high-level, scalable, and potentially noisy signal sources by applying multiple sources of supervision



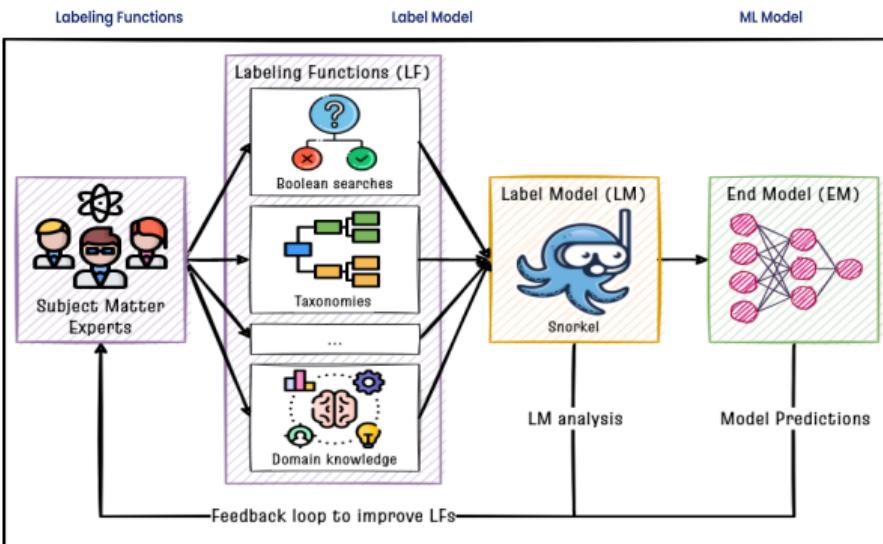
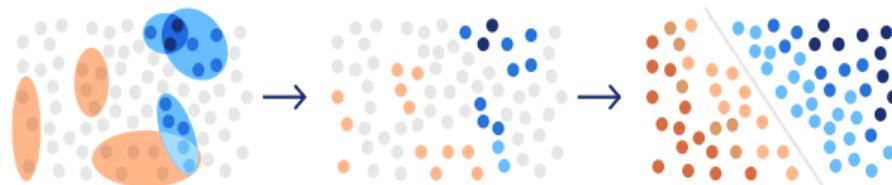
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- Create large training sets, based on unlabeled data, much more quickly than using a 1-by-1 manual supervision



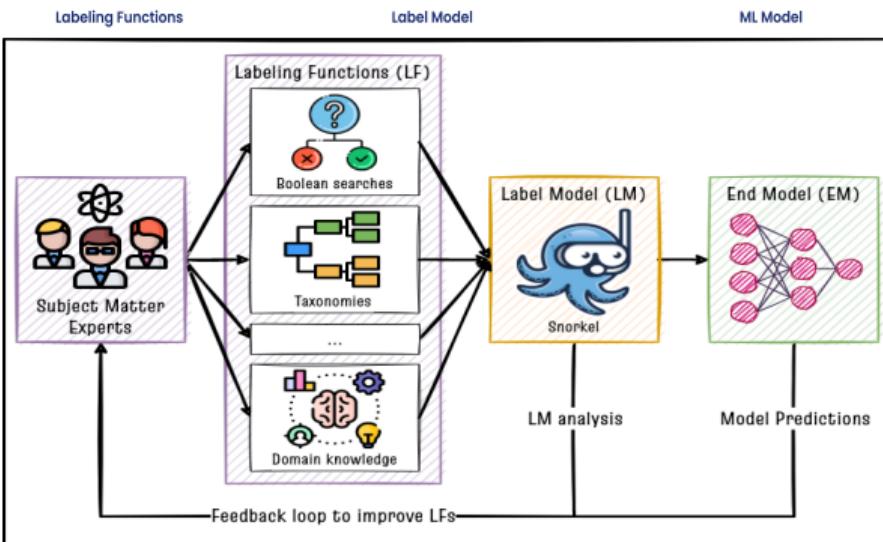
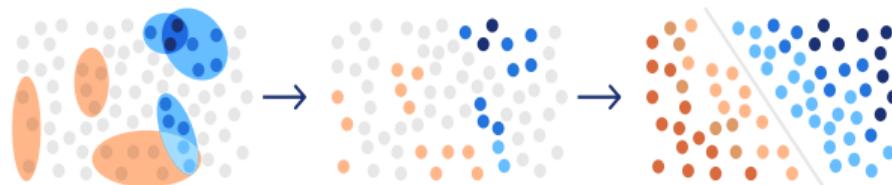
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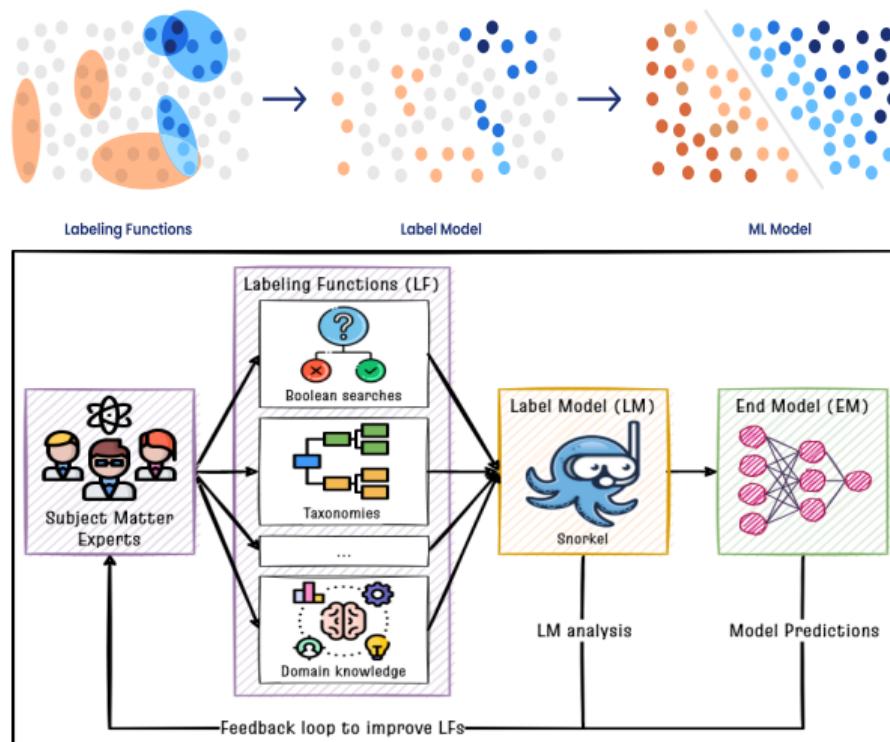
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- Weak supervision training on incomplete, partially (machine-)labeled data
- Lack of precision: completely labeled, but often not precisely enough to recognize subtle differences



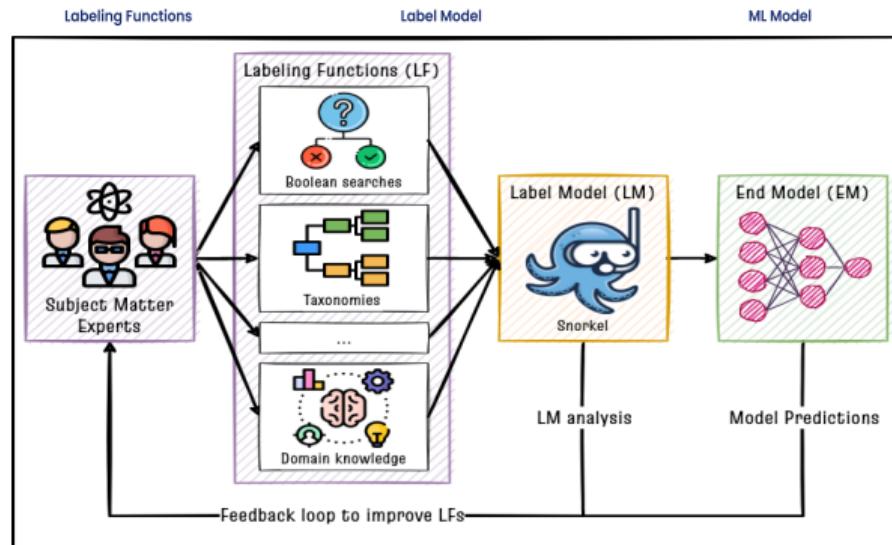
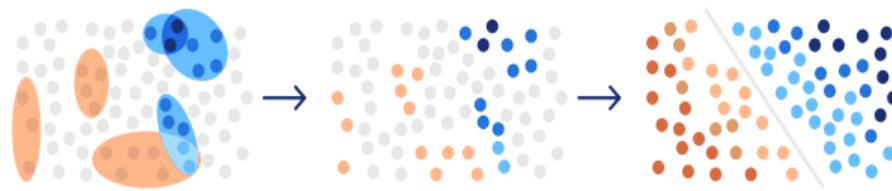
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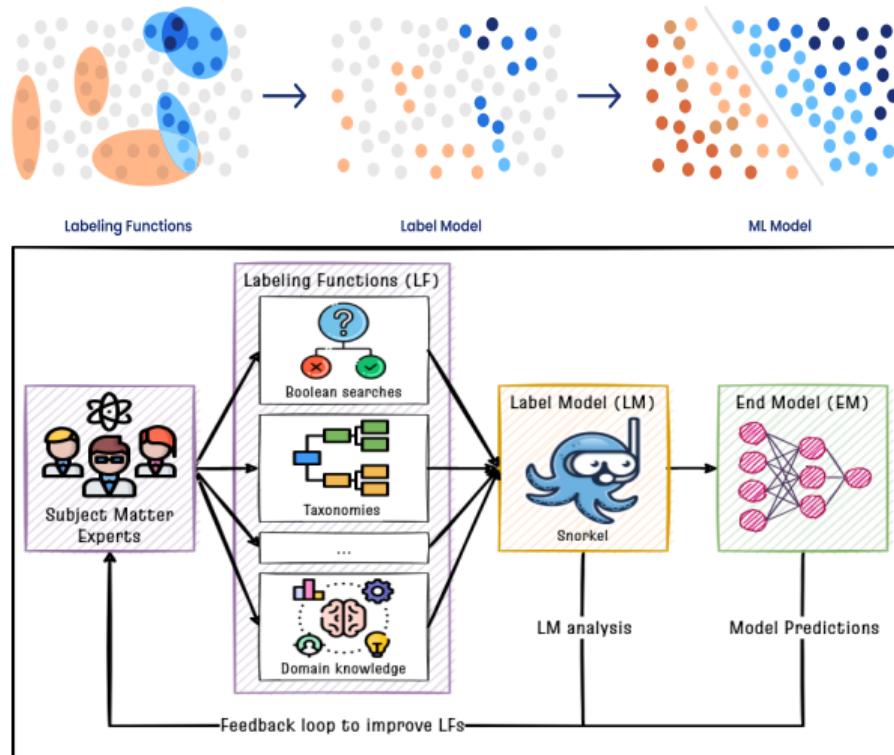


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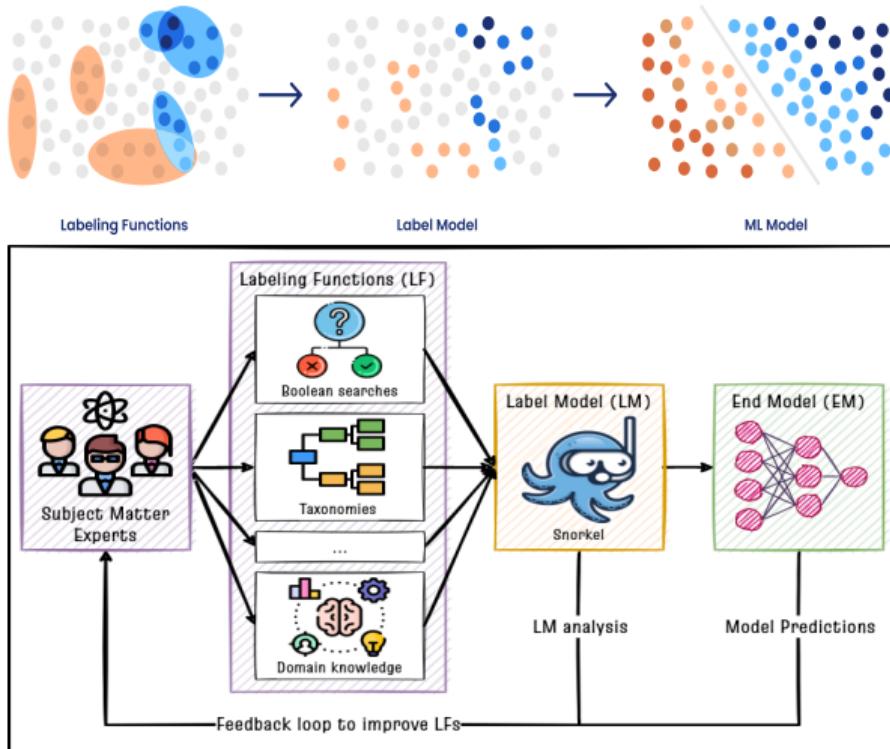
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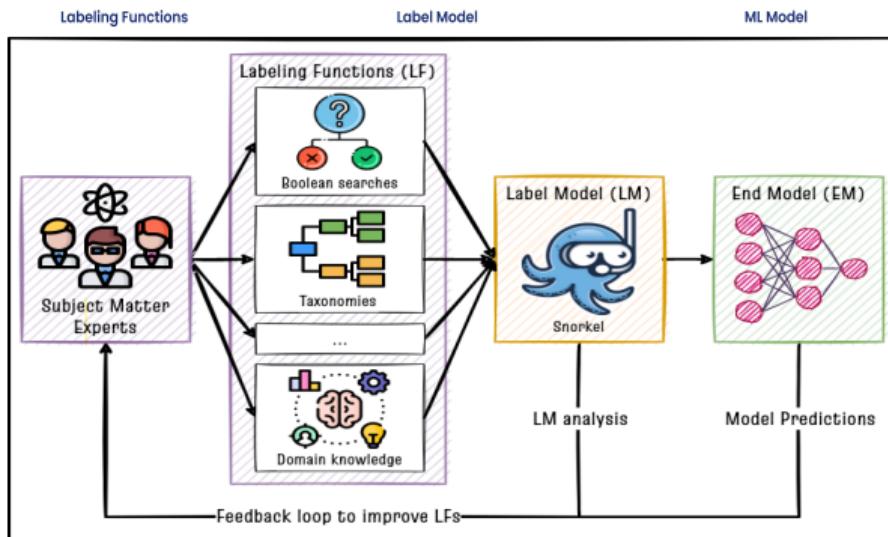
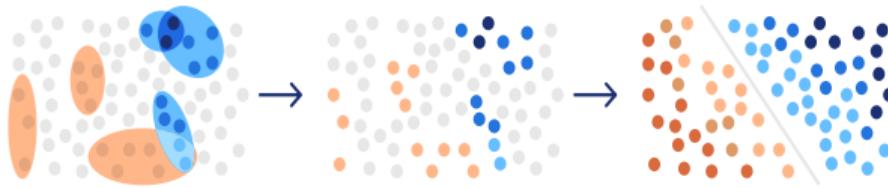


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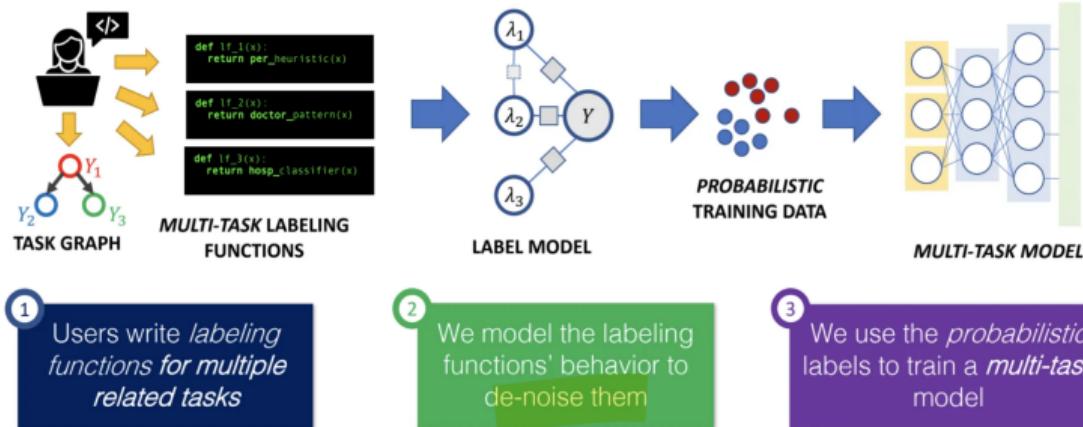
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- Idea: trade-off 100,000 pretty good vs. 100 perfect data labels



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prob of diversity of 100 perfect is less than prob diversity of 100000

# Labeling in Snorkel

## Snorkel Framework



- Labeling functions  $\lambda_N$  (simple functions/rules), providing multiple inconsistent or overlapping labels (commercialized version available here: [Snorkel](#))
- Combine noisy weak labels in a labeling model to generate a consensus more accurate final label
- Label model learns dependencies/reliabilities of the labeling functions, weighting each function according to its accuracy and overlap with others
- Probabilistic labels for each sample, allow to build a (weakly) supervised training set

Source: [Link to Image](#)

### Smart Labeling

- Labeling involves using automated or semi-automated techniques to label data intelligently (see pseudo-labeling, self-supervised approaches)

Source: Image from OTH-AW, Electrical Engineering, Media and Computer Science, Thomas Nierhoff – Vorlesung Advanced Topics in ML

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- Active Learning: label only the most uncertain or informative data points, making the labeling process more efficient

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## Weak Supervision

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### Application: Cut-In Prediction Autonomous Vehicle

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# Deep Learning Strategies – Part III

## Weak Supervision

every potential event has to be taken into account

here pattern recognition is important

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- Unlabeled data: process large amounts of unlabeled driving data with weakly supervised trained models that learn to identify “cut-in” scenarios indirectly

Source: Image from OTH-AW, Electrical Engineering, Mechanical Engineering, Source: Thomas Mischler, Advanced Topics in ML  
train model on weakly supervised data sets.  
from sensor data, heuristics etc and unlabeled

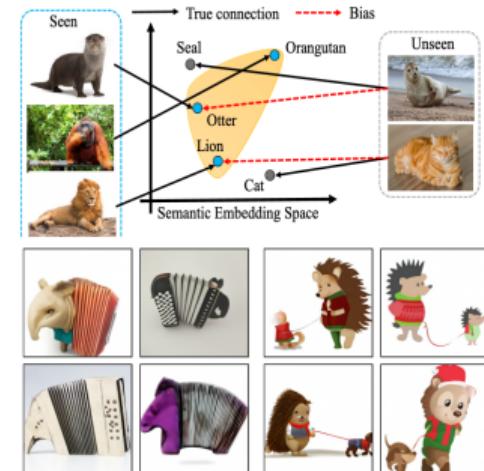
# Deep Learning Strategies – Part III

## N-Shot Learning

### N-Shot Learning – Zero-Shot, Single-Shot & Few-Shot Learning

**Idea:** Zero-shot, single/one-shot, and few-shot learning are learning paradigms where models identify/categorize or generate new categories with very few or even no labeled examples

- **Zero-Shot Learning:** identify new categories never seen in training by leveraging auxiliary semantic knowledge based on feature similarity via textual/visual embeddings!



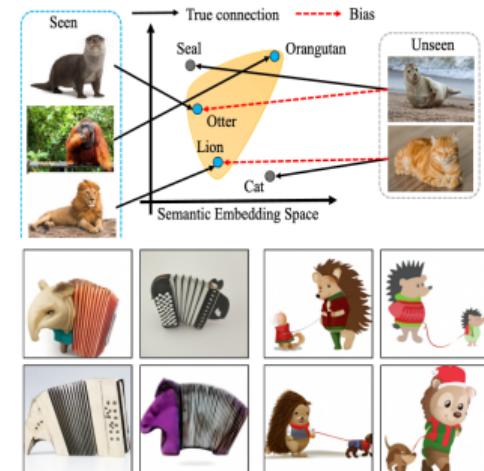
Source: <https://medium.com/@vireshj/zero-shot-learning-understanding-machines-that-learn-like-humans-e670f83186b8>  
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- Non-static set of classes, while unseen events will be stored in the high-dimensional feature space either near (related to “Knowns”) or far-apart (unrelated to “Knowns”)



(a) a tapir made of accordion. (b) an illustration of a baby a tapir with the texture of an hedgehog in a christmas sweater walking a dog

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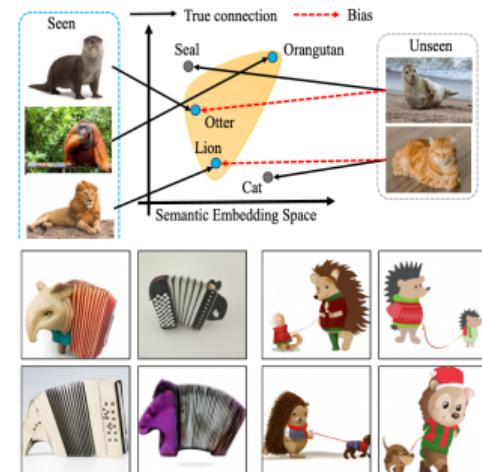
## N-Shot Learning

zero shot for first time seeing few shot is for few times seeing

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- Non-static set of classes, while unseen events will be stored in the high-dimensional feature space either near (related to “Knowns”) or far-apart (unrelated to “Knowns”)
- Class assignment for a first-time appearance of a new category requires pre-existing knowledge (embeddings, e.g. single-shot) describing the new class



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- These networks learn to measure similarity between data samples, enabling classification with just a single instance
- Class assignment is based on distance-related outcome (“close enough”) of an unseen sample w.r.t. the “single shot data point”



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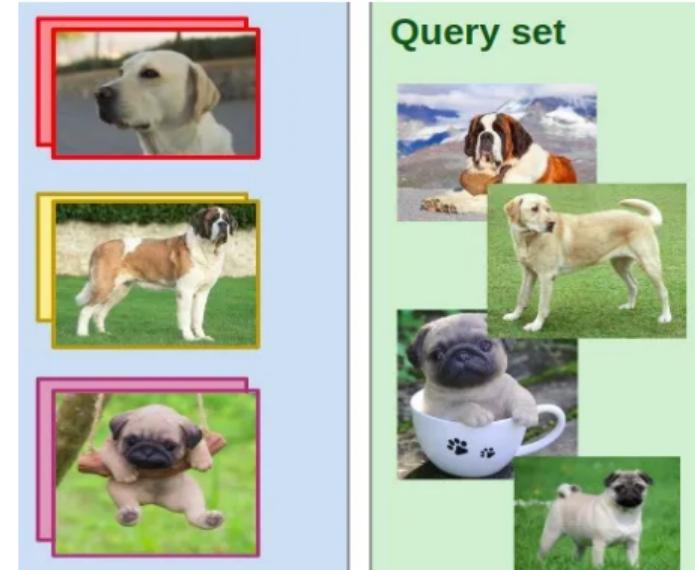


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causal learning home work

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- Classify  $Q$  query images among the  $K$  classes, with  $K \times N$  samples in the training set are the only representatives

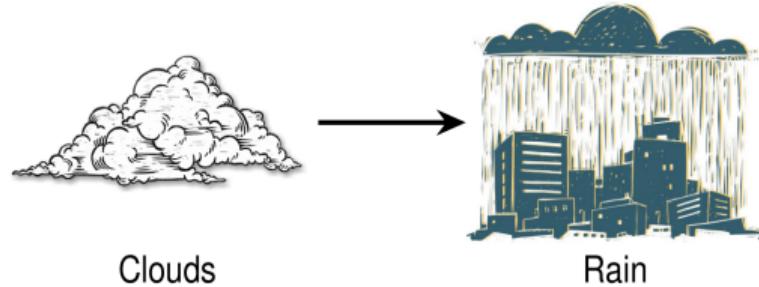


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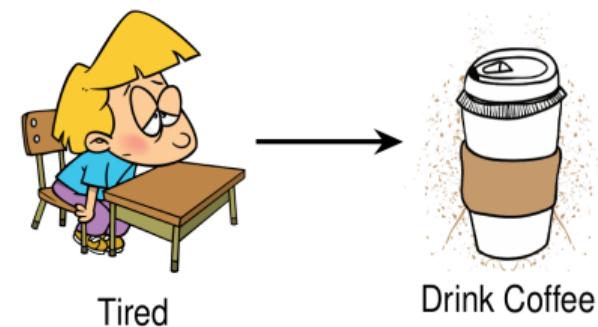
## Causal Learning

- Implies a direct cause-and-effect relationship (“explain the cause of an effect”) between two variables (change one variable will directly impact the other in a predictable way)



Clouds

Rain



Tired

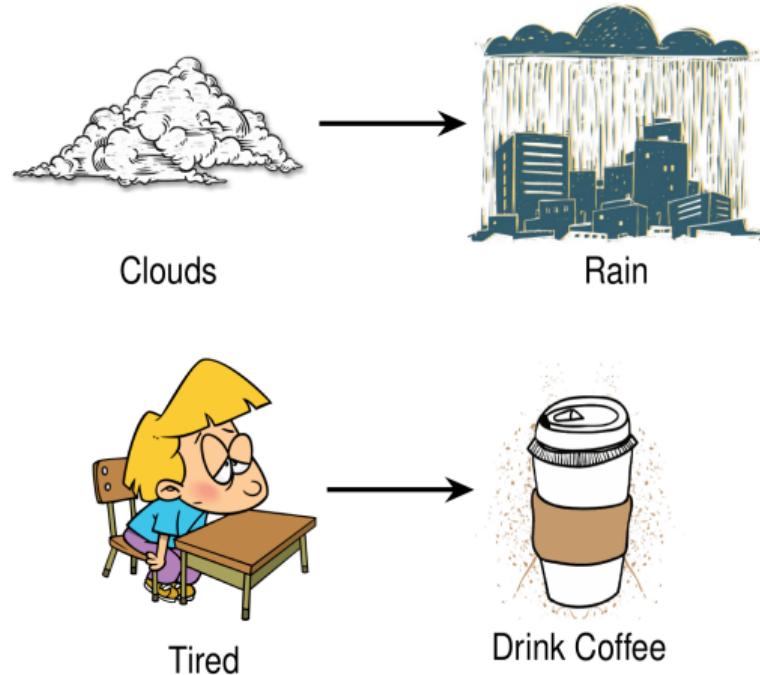
Drink Coffee

Source: FAU Erlangen-Nuremberg, Pattern Recognition Lab, K.Breininger, V. Christlein, Advanced Deep Learning – Interpretable/Causal Deep Learning

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- **Careful:** correlation describes a statistical association between two variables and indicates a simultaneous change (trend!) → However, not necessarily causing the other!

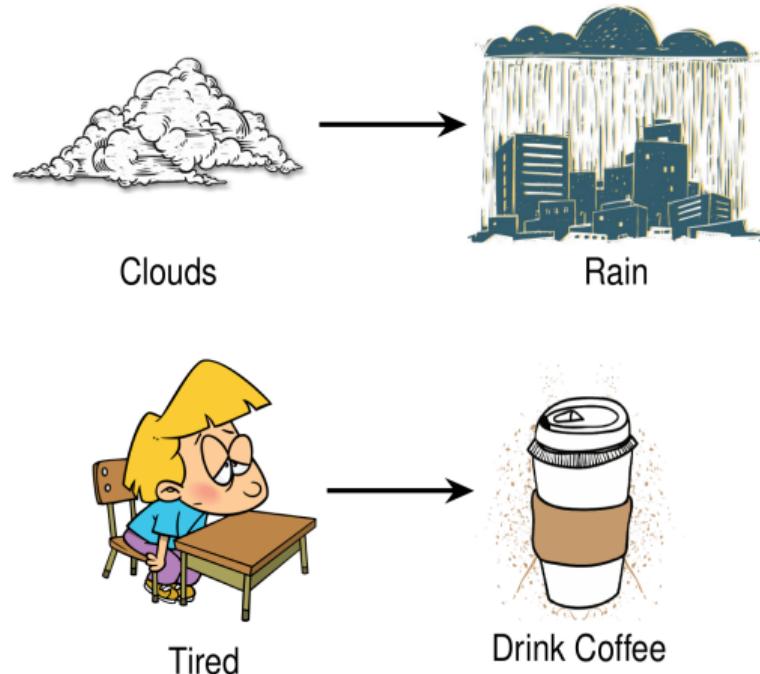


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- **Careful:** correlation describes a statistical association between two variables and indicates a simultaneous change (trend!) → However, not necessarily causing the other!
- Causal inference often uses statistical methods to identify relationships that are not simply correlations but have a directional influence



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## Causal Learning

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### Types of Causal Relationships

- **Direct Causal Relationships:** One variable directly affects another (e.g., smoking directly causes an increased risk of lung cancer)
- **Indirect Causal Relationships:** The effect of one variable on another is mediated through a third variable (e.g., education may lead to higher income, and higher income might then lead to better health outcomes)
- **Bidirectional Causality:** Some relationships may involve mutual causality, where two variables affect each other (e.g., diet and exercise can both affect each other over time)

Source: FAU Erlangen-Nuremberg, Pattern Recognition Lab, K.Breininger, V. Christlein, Advanced Deep Learning – Interpretable/Causal Deep Learning

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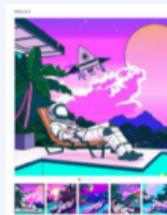
## Causal Learning

### Deep Learning

Representation Learning

Continuous Optimization

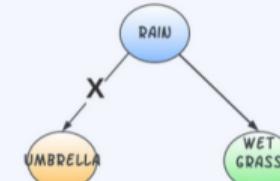
Handling Large Quantities of Data



### Causality

Model Cause and Effect

Answer Interventional Questions



Source: Image from Nan Rosemary Ke, Stefan Bauer, "Causality and Deep Learning: Synergies, Challenges and the Future", Slide 29

# Deep Learning Strategies – Part III

## Causal Learning

Correlation is NOT Causation!



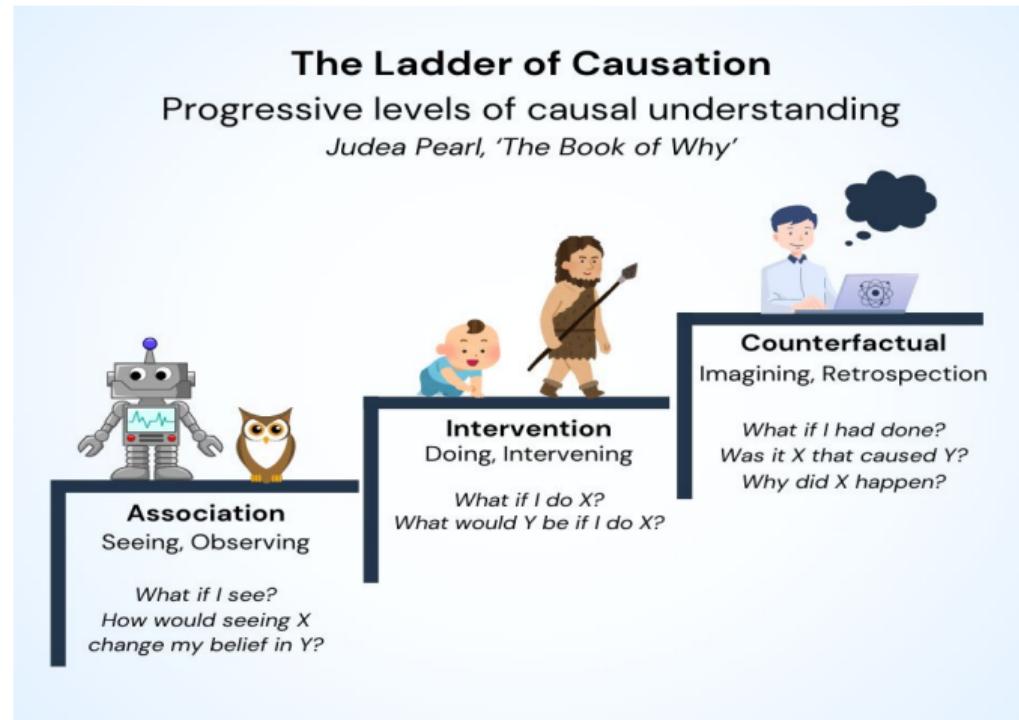
© marketoonist.com

Source: Image from <https://censemaking.com/2022/08/03/the-fear-and-folly-of-data/>

# Deep Learning Strategies – Part III

## Causal Learning

### Ladder of Causation



- Organizes causal reasons into three hierarchical levels: association, intervention, counterfactuals
- From simply observing data to fully understanding & reasoning about causal mechanisms

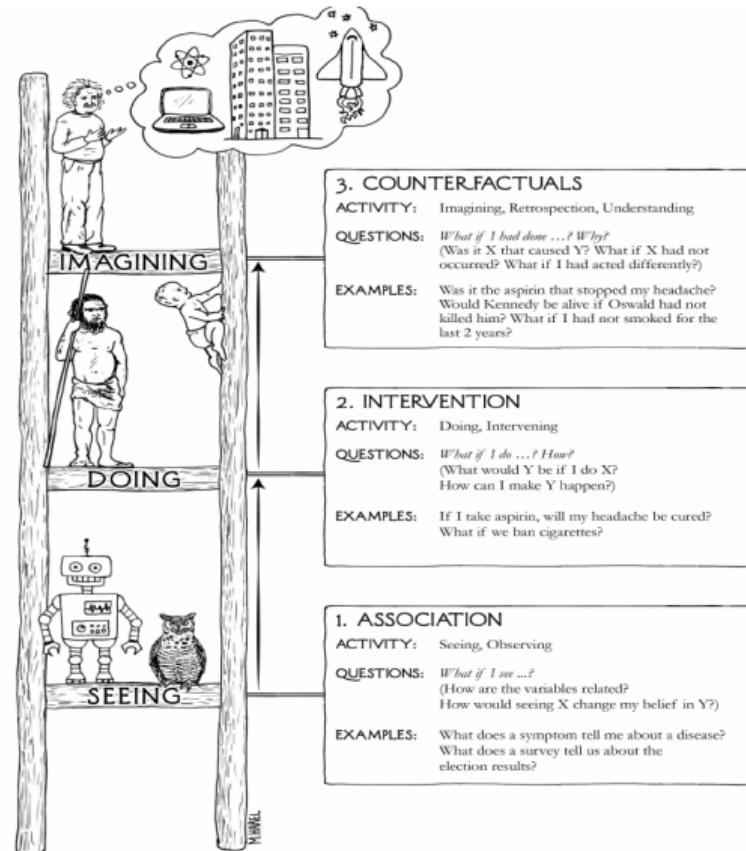
Source: Image from [https://www.linkedin.com/posts/causal-bv\\_ladderofcausation-causalai-decisionmaking-activity-7177992092458057729-hiP9](https://www.linkedin.com/posts/causal-bv_ladderofcausation-causalai-decisionmaking-activity-7177992092458057729-hiP9)

# Deep Learning Strategies – Part III

## Causal Learning

### Association

- Observing correlations/dependencies of variables:  
“What happens if we change this variable?”



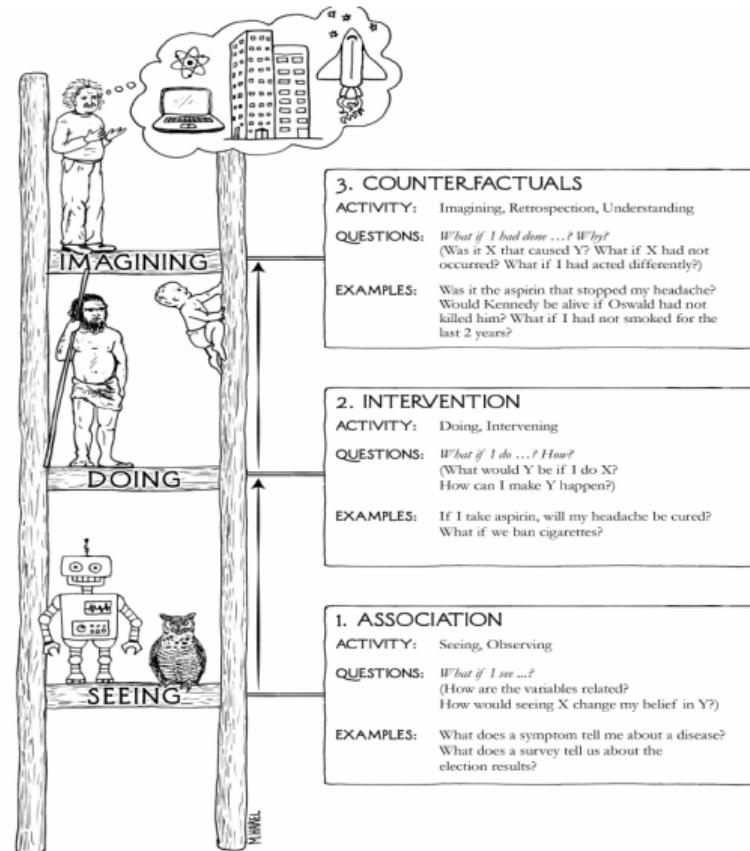
Source: FAU Erlangen-Nuremberg, Pattern Recognition Lab, K.Breininger, V. Christlein, Advanced Deep Learning – Interpretable/Causal Deep Learning

# Deep Learning Strategies – Part III

## Causal Learning

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- However, no explanation why one thing happens because of another (purely observational!)



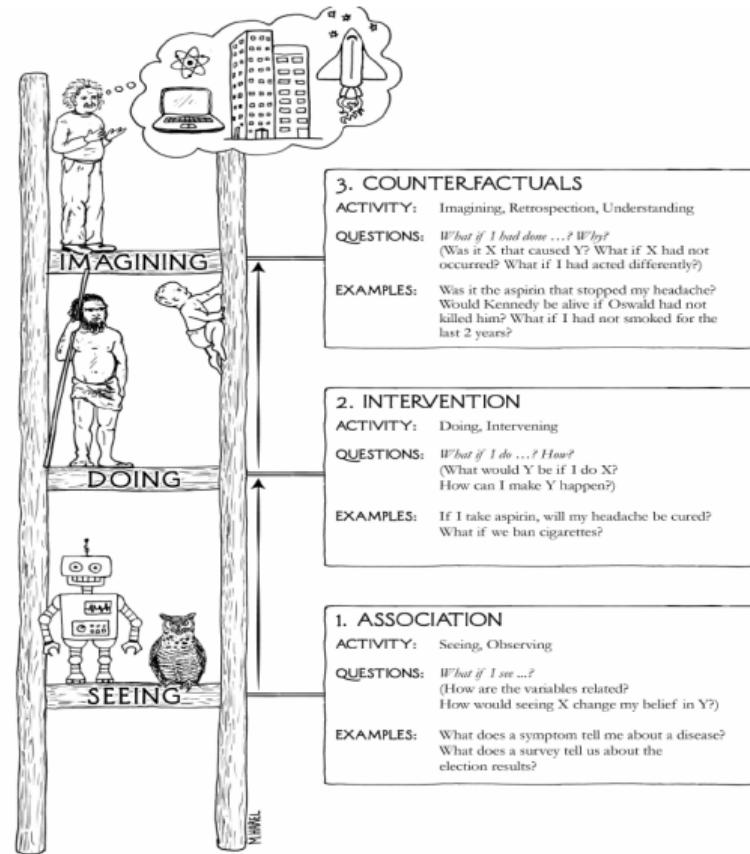
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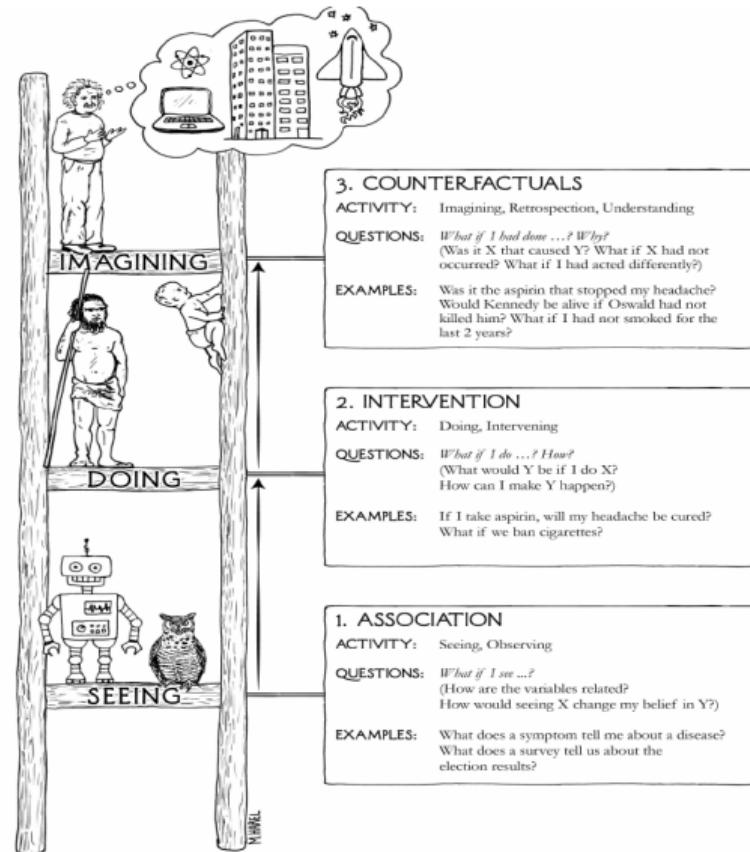
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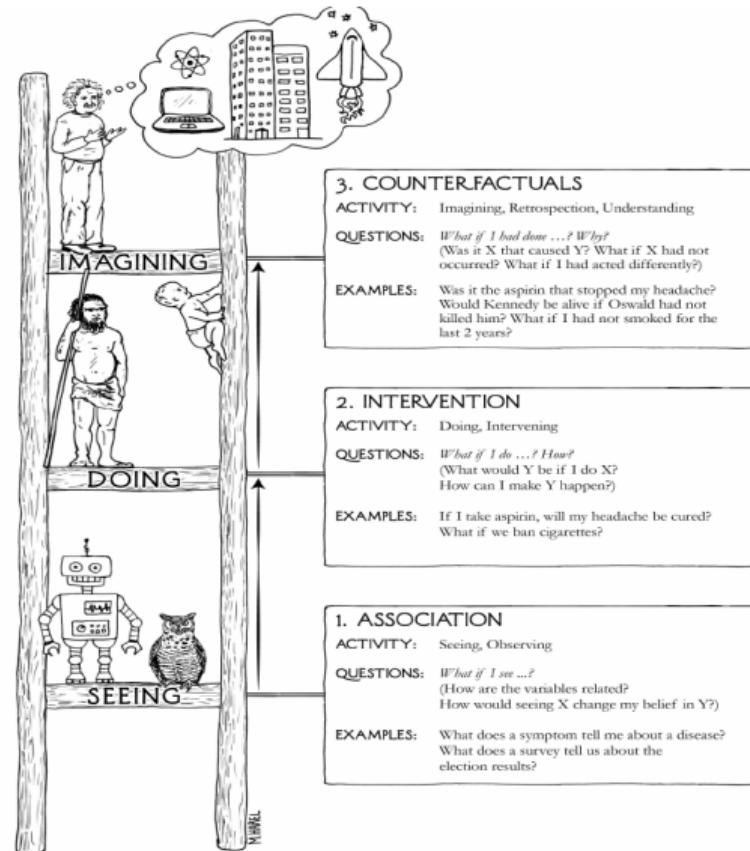
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- Association alone do not determine if a relationship is causal (correlation between ice cream sales and drowning incidents does not imply that buying ice cream causes drowning)



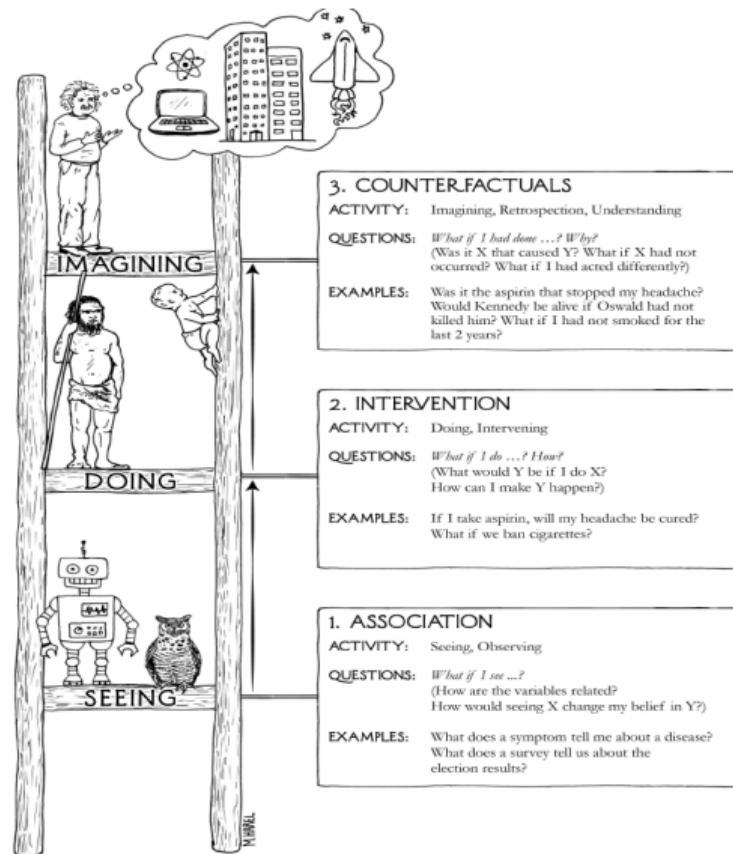
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# Deep Learning Strategies – Part III

## Causal Learning

### Intervention

- Moving beyond observation by introducing actions to change the system and observing the results: “What if I do this?”

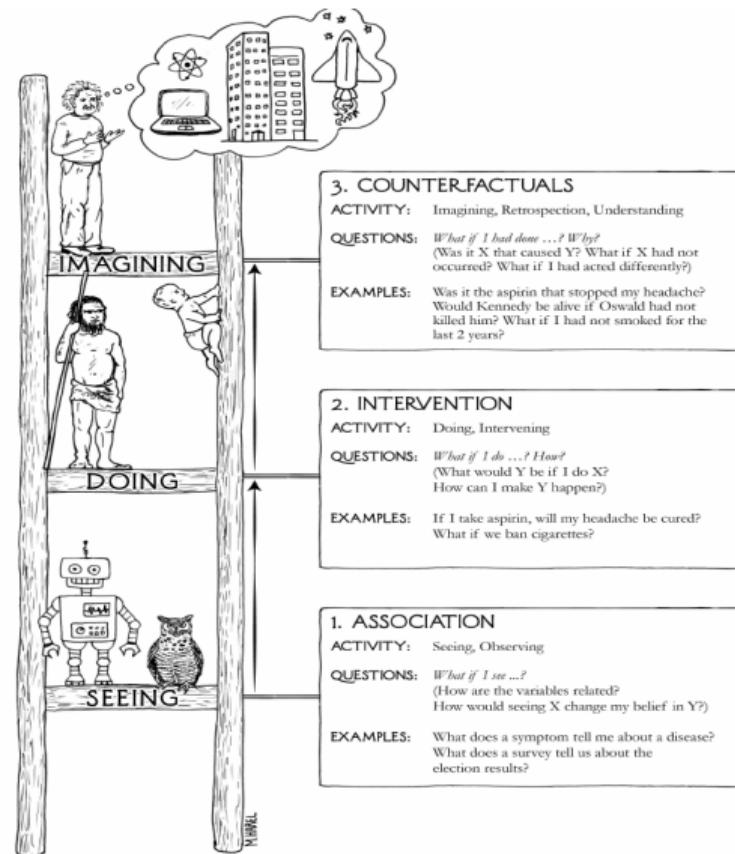


# Deep Learning Strategies – Part III

## Causal Learning

### Intervention

- Moving beyond observation by introducing actions to change the system and observing the results: “What if I do this?”
- Represent causal relationship by showing how changes in one variable affect another



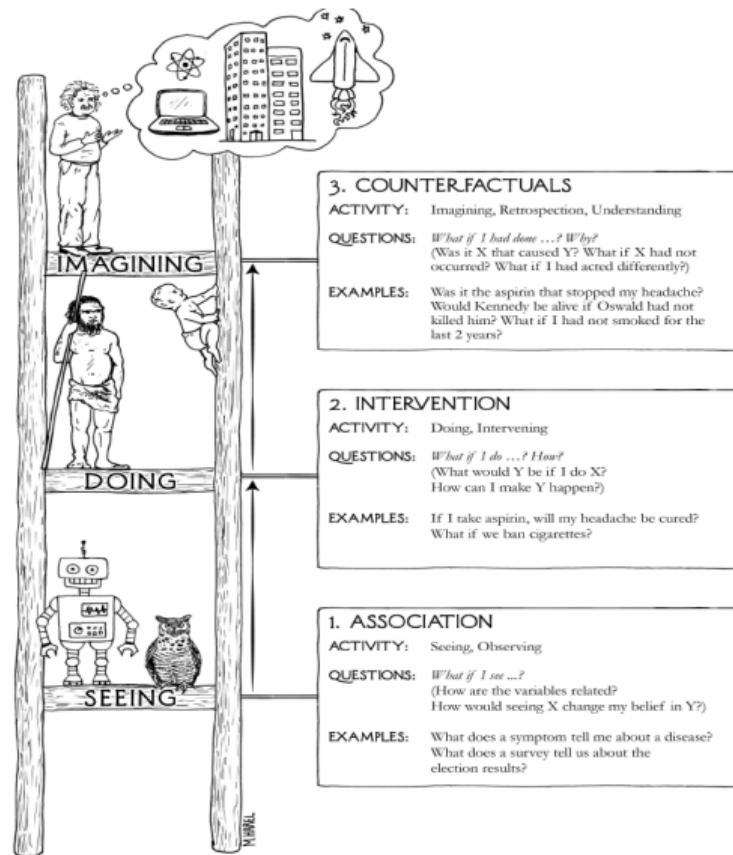
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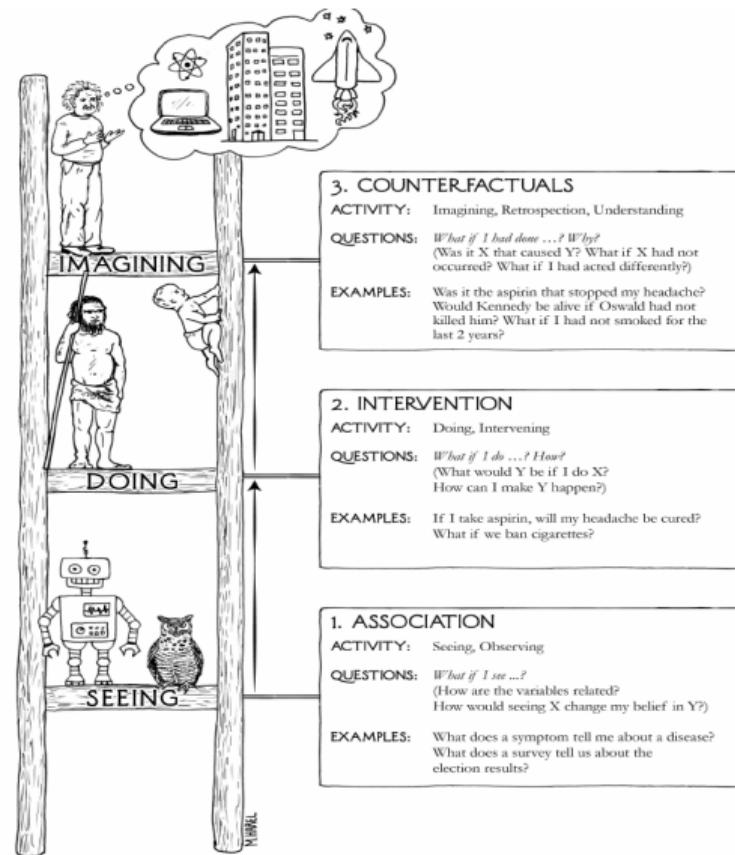
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- Methods: randomized controlled trials, where the experimenter manipulates the independent variable  $P(Y|do(X))$  (e.g. giving patients a treatment placebo) to observe the effect on a dependent variable (like recovery rates)

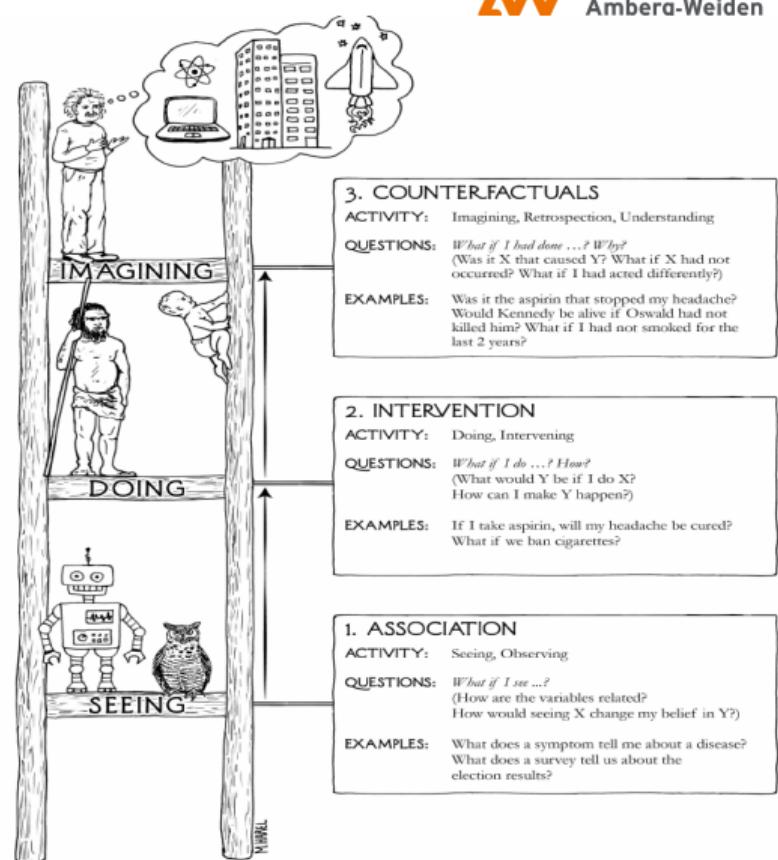


# Deep Learning Strategies – Part III

## Causal Learning

### Counterfactuals

- Asking about hypothetical alternatives to what actually happened, what would have happened “if”



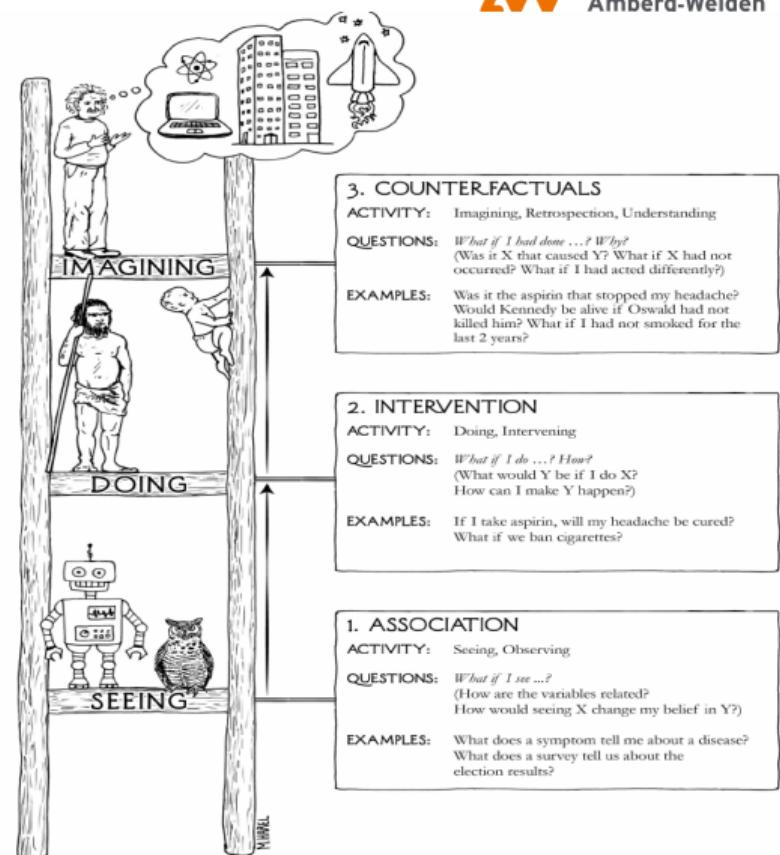
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# Deep Learning Strategies – Part III

## Causal Learning

### Counterfactuals

- Asking about hypothetical alternatives to what actually happened, what would have happened “if”
- Alternative realities by imagining what the outcome would have been if a different action or condition had been in place



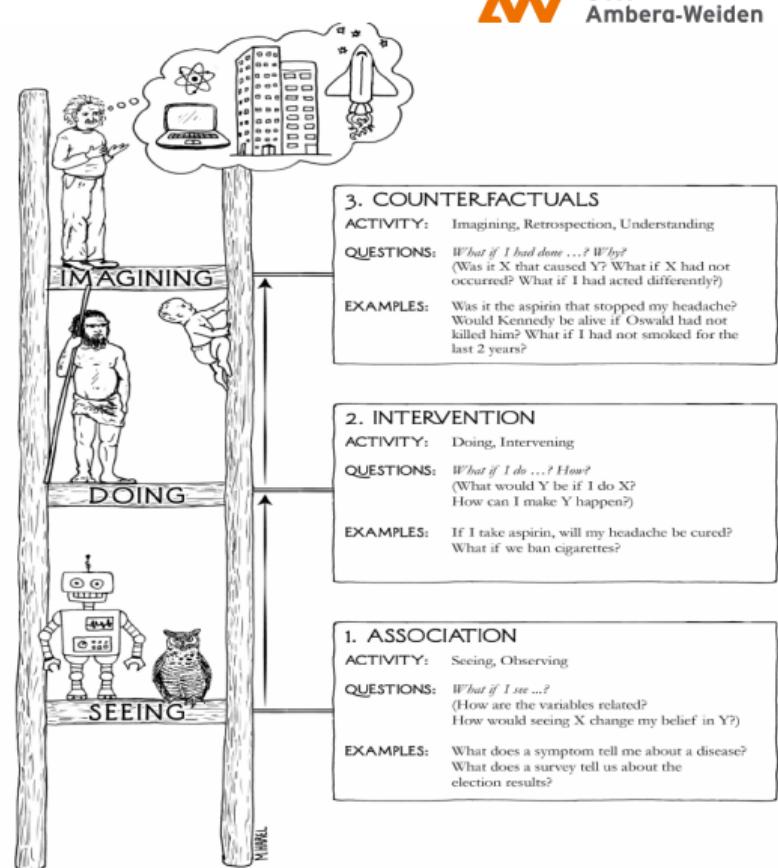
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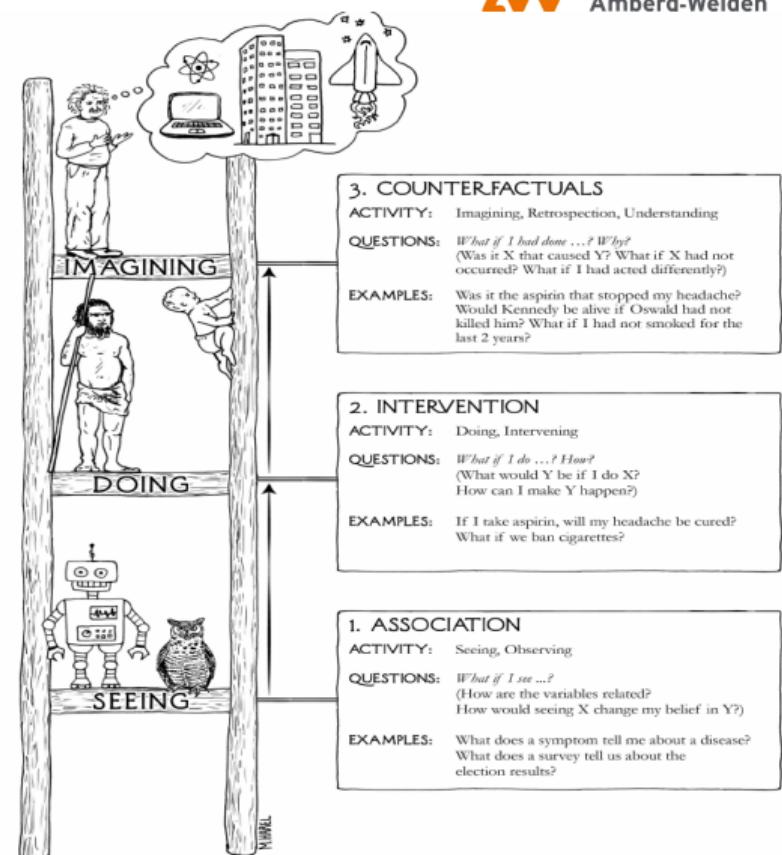
# Deep Learning Strategies – Part III

## Causal Learning

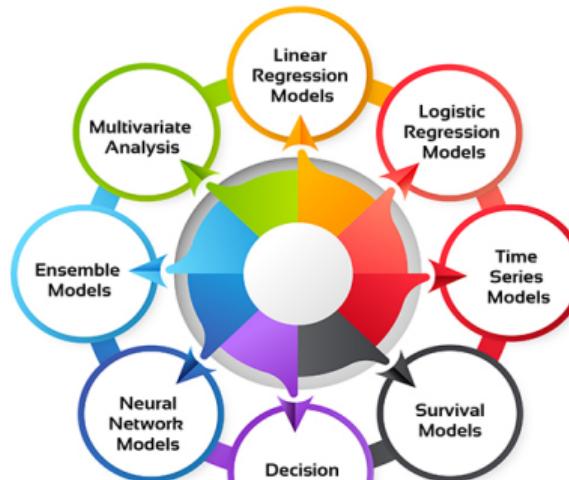
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- Alternative realities by imagining what the outcome would have been if a different action or condition had been in place
- Question: “What would have happened to  $Y$  if  $X$  had been different?”
- Methods: structural causal models (SCMs), provide a framework for understanding causal relationships at a deeper level by specifying equations reflecting mechanisms of causation

Source: FAU Erlangen-Nuremberg, Pattern Recognition Lab, K.Breininger, V. Christlein, Advanced Deep Learning – Interpretable/Causal Deep Learning



# Types of Statistical Models

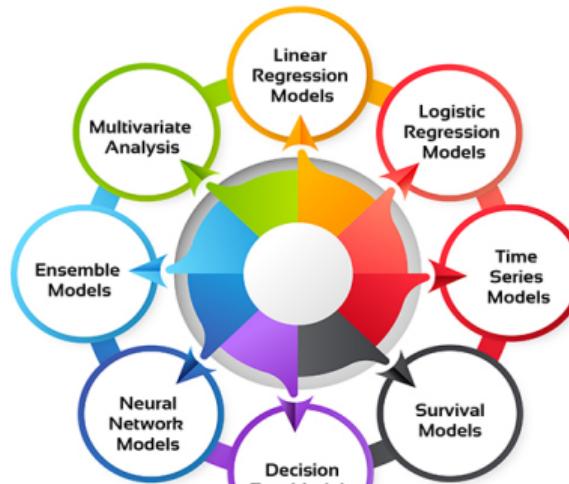


- Current ML-Models or statistical models can only do “Association”

Source: <https://www.dasca.org/world-of-data-science/article/what-is-statistical-modeling-in-data-science>

Source: FAU Erlangen-Nuremberg, Pattern Recognition Lab, K.Breininger, V. Christlein, Advanced Deep Learning – Interpretable/Causal Deep Learning

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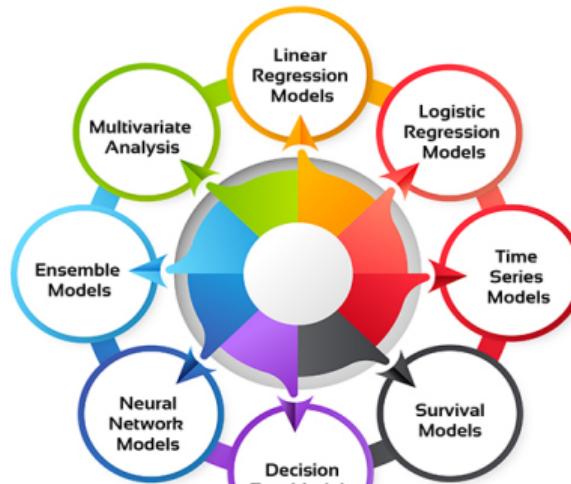


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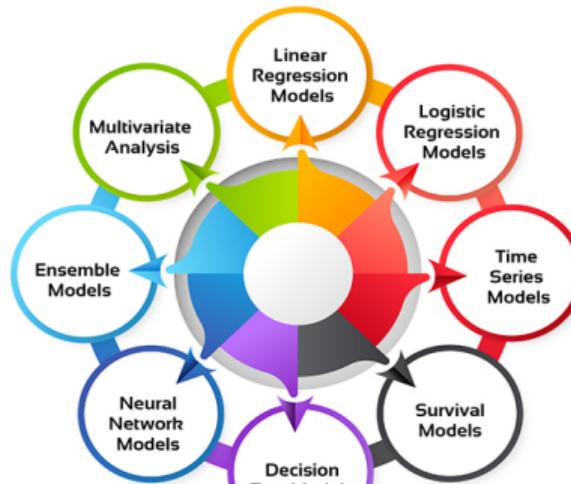


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- Successful because: massive amount of data, high number of parameters, strong computational power, independent and identically distributed (i.i.d.) assumption

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# Deep Learning Strategies – Part III

## Causal Learning

- **Independent:** each data sample is collected independently of others, one sample does not influence/depend on another



$$\begin{array}{ccc} \text{x} & + .007 \times & \text{sign}(\nabla_{\text{x}} J(\theta, \text{x}, y)) \\ \text{"panda"} & & \text{"nematode"} \\ 57.7\% \text{ confidence} & & 8.2\% \text{ confidence} \\ & = & \\ & & \text{x} + \text{esign}(\nabla_{\text{x}} J(\theta, \text{x}, y)) \\ & & \text{"gibbon"} \\ & & 99.3 \% \text{ confidence} \end{array}$$

Source: Szegedy et al., Intriguing properties of neural networks, Figure 5  
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# Deep Learning Strategies – Part III

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- **Introducing an unexpected distribution change?**

Source: FAU Erlangen-Nuremberg, Pattern Recognition Lab, K.Breininger, V. Christlein, Advanced Deep Learning – Interpretable/Causal Deep Learning



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$x$   
sign( $\nabla_x J(\theta, x, y)$ )

## Causal Learning

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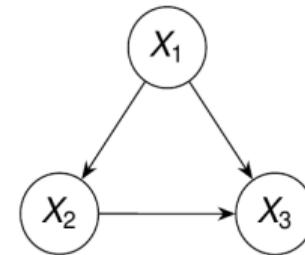
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- Example: exercise frequency ( $Z$ ), body weight ( $X$ ), cholesterol levels ( $Y$ )  $\rightarrow$  without considering  $Z$ , it might appear that body weight directly affects cholesterol, however, exercise impacts both independently

Source: FAU Erlangen-Nuremberg, Pattern Recognition Lab, K.Breininger, V. Christlein, Advanced Deep Learning – Interpretable/Causal Deep Learning

## Causal Learning

### Causal Graphical Models (CGMs)

- Directed Acyclic Graphs (DAGs) or Bayesian Networks  
("acyclic" part → no loops, flow in one direction without cycling back)



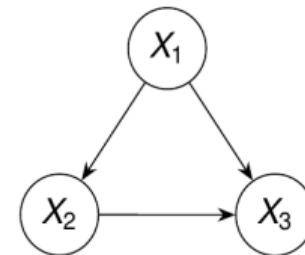
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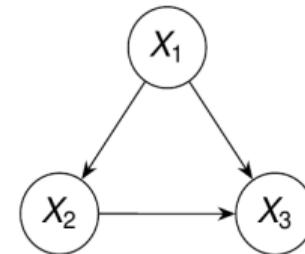
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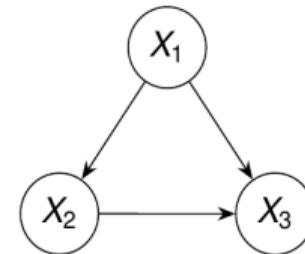
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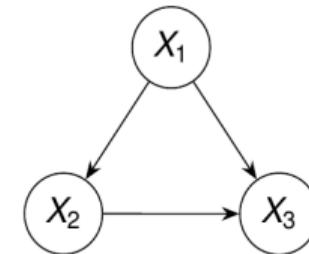
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- Variables  $X$  (observations) as nodes and causal relationships between them as directed edges
- Causal Markov condition (Causal Independence!):  
 $P(X_1, \dots, X_n) = \prod_{i=1}^n P(X_i | PA_i)$ , with  $PA_i$  as the parents of  $X_i$ , having a direct causal link (e.g.  $X_1 \rightarrow X_2$ )



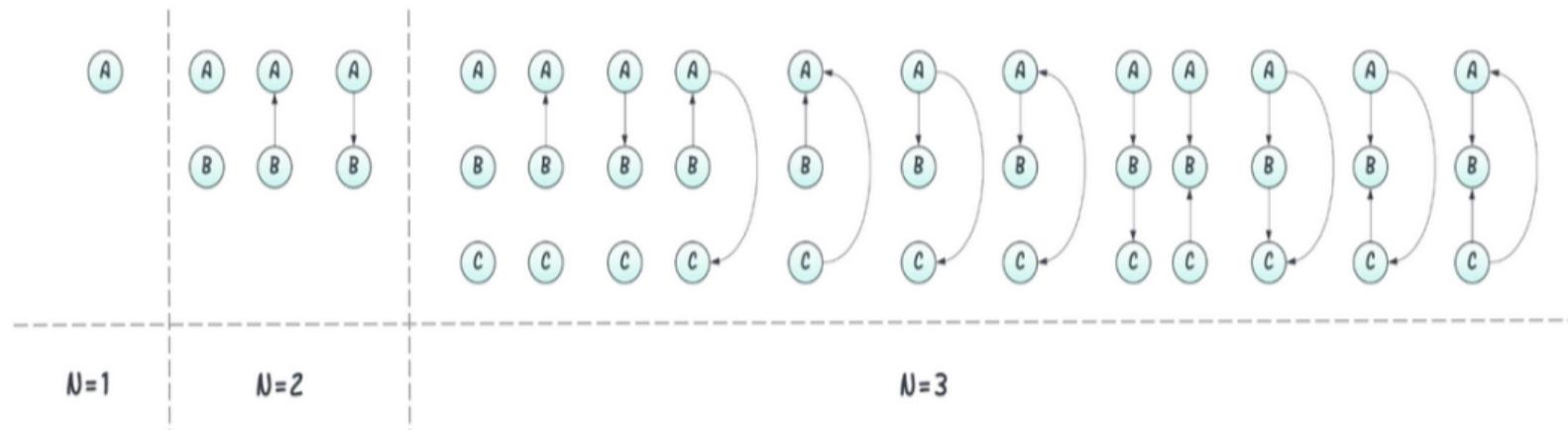
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Source: FAU Erlangen-Nuremberg, Pattern Recognition Lab, K.Breininger, V. Christlein, Advanced Deep Learning – Interpretable/Causal Deep Learning

# Deep Learning Strategies – Part III

## Causal Learning

Space of causal graphs (i.e. DAGs) grows **super-exponentially**.



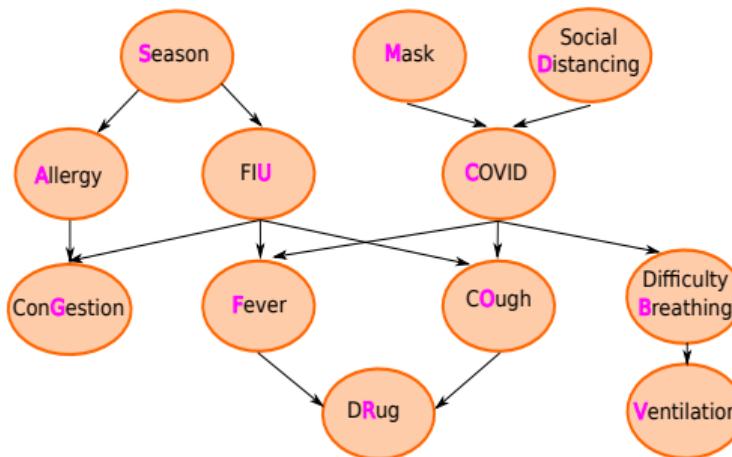
Source: Image from Nan Rosemary Ke, Stefan Bauer, "Causality and Deep Learning: Synergies, Challenges and the Future", Slide 26

# Deep Learning Strategies – Part III

## Causal Learning

### Bayesian Network

#	COVID	Mask	Soc. Distance	FIU	Cough	Fever	Ventilate	Season	ConGestion	Difficulty Breath	Drug	Allergy
1	1	0	1	0	1	0	1	Spring	0	0	1	0
2	0	1	0	1	0	1	0	Summer	1	1	0	0
3	1	1	1	0	0	0	1	Fall	1	0	1	1
4	0	0	1	1	1	0	0	Winter	0	1	0	0
...	...	...	...	...	...	...	...	...	...	...	...	...
500	0	1	1	1	0	0	0	Summer	0	0	1	1

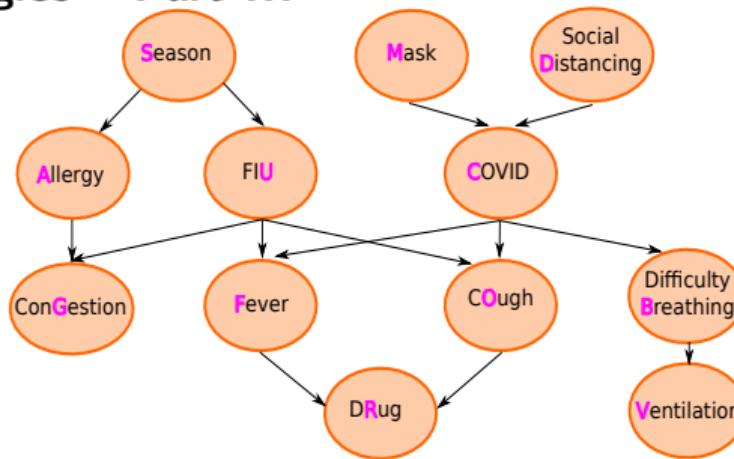


Source: YouTube – easy learning – Causality 1: Bayesian networks are not causal, [Link](#)

# Deep Learning Strategies – Part III

## Causal Learning

### Bayesian Network



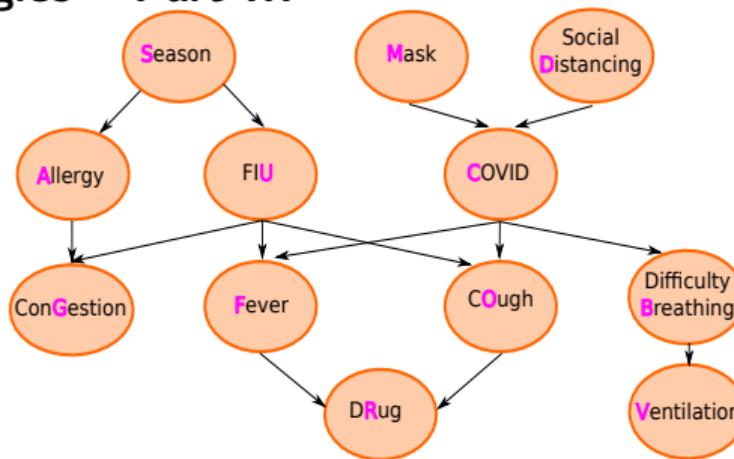
- Random (dependent/independent) variables, e.g. Fever/COVID and Allergy/Cough

Source: YouTube – easy learning – Causality 1: Bayesian networks are not causal, [Link](#)

# Deep Learning Strategies – Part III

## Causal Learning

### Bayesian Network



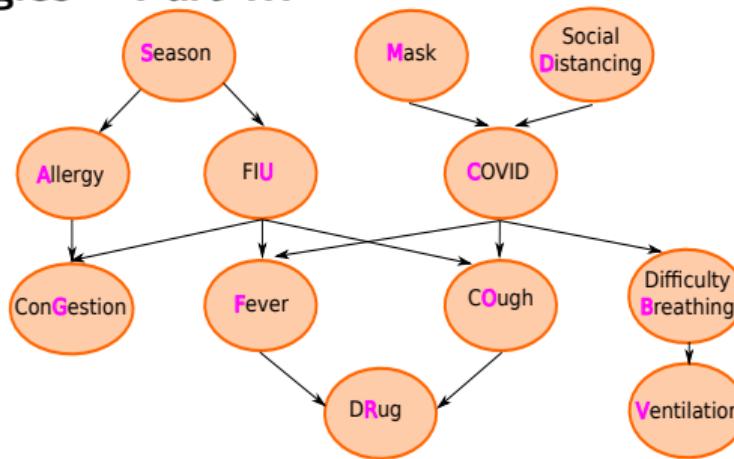
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# Deep Learning Strategies – Part III

## Causal Learning

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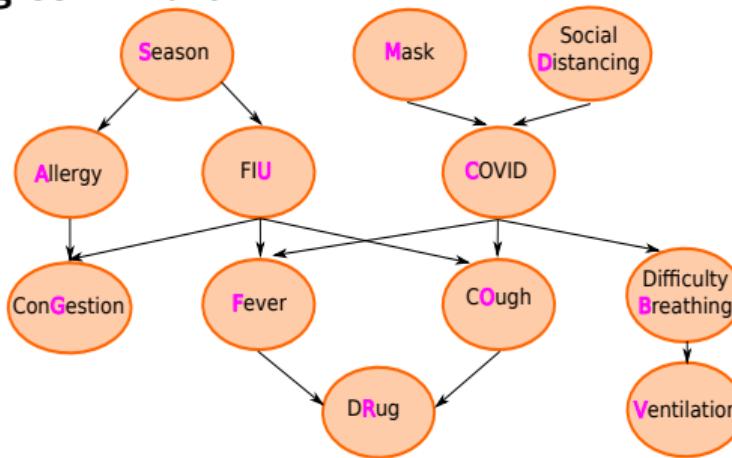
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# Deep Learning Strategies – Part III

## Causal Learning

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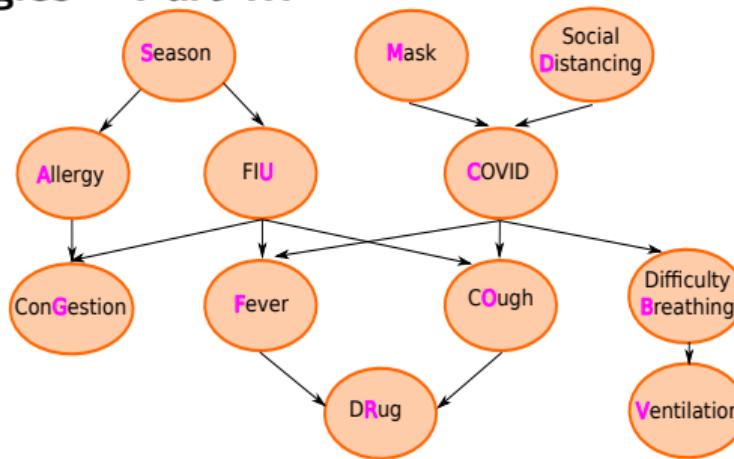
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# Deep Learning Strategies – Part III

## Causal Learning

### Bayesian Network



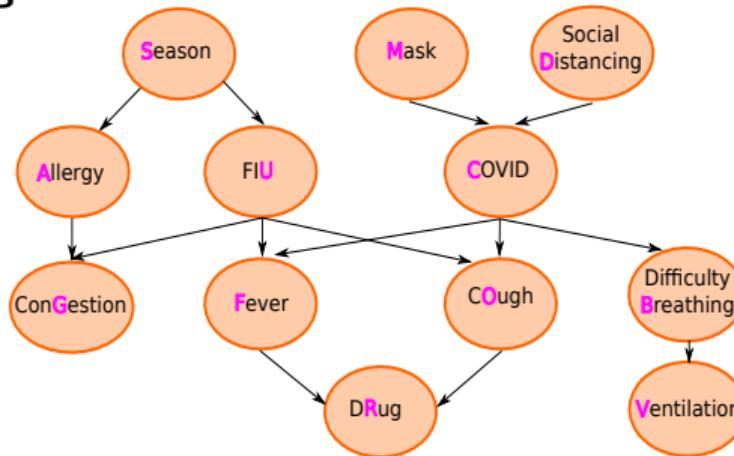
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- How to read statistical dependence as causal dependence?

Source: YouTube – easy learning – Causality 1: Bayesian networks are not causal, [Link](#)

# Deep Learning Strategies – Part III

## Causal Learning

### Bayesian Network



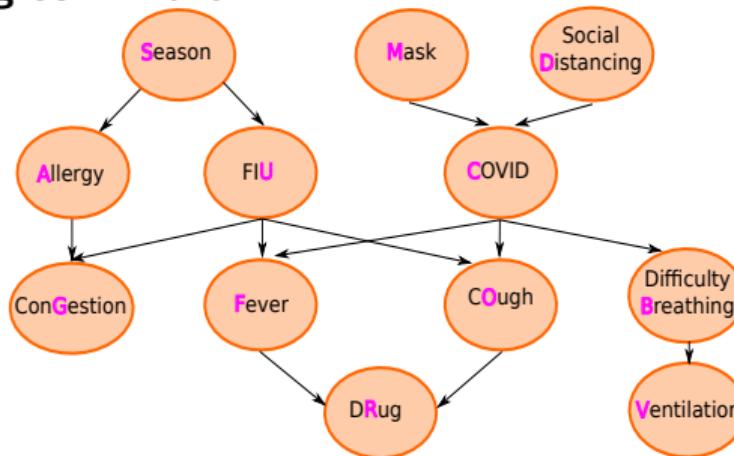
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# Deep Learning Strategies – Part III

## Causal Learning

### Bayesian Network



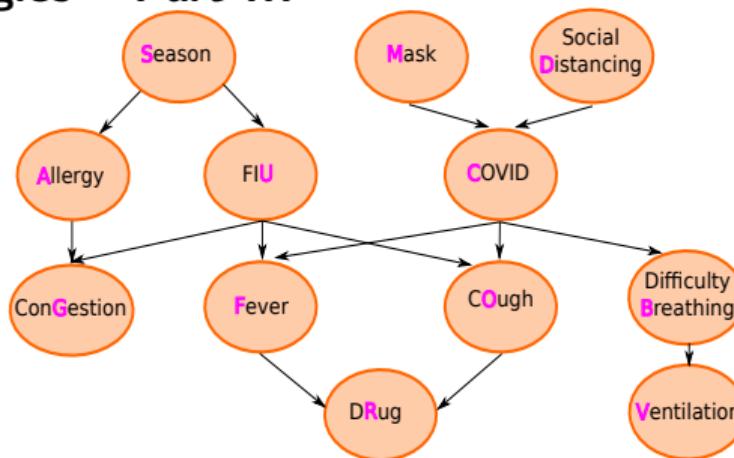
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# Deep Learning Strategies – Part III

## Causal Learning

### Bayesian Network



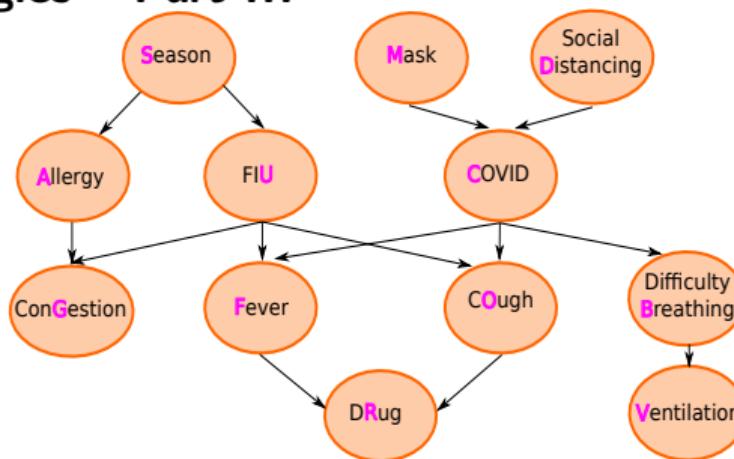
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# Deep Learning Strategies – Part III

## Causal Learning

### Bayesian Network



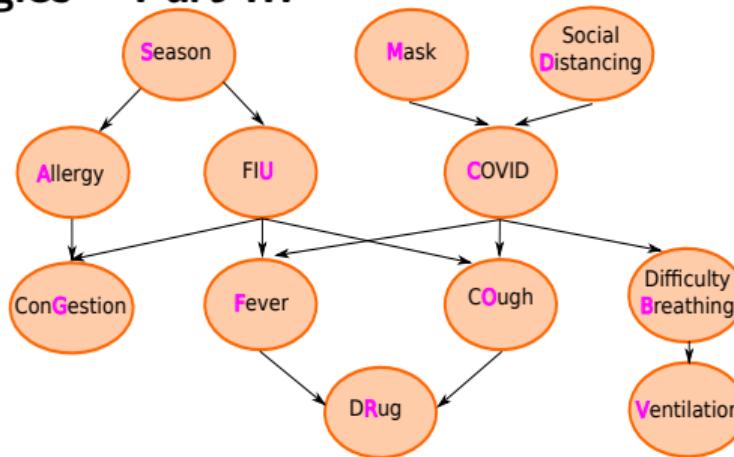
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- Still: No Causality!
- Goal: Given data  $D$ , what is causing what (the other)?

Source: YouTube – easy learning – Causality 1: Bayesian networks are not causal, [Link](#)

# Deep Learning Strategies – Part III

## Causal Learning

### Bayesian Network



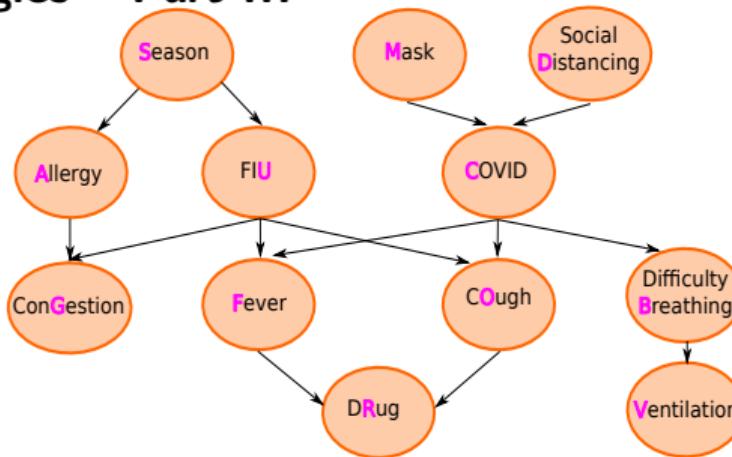
- Consider binary variables  $\text{COVID} \in \{\text{COVID}, \neg\text{COVID}\}$  and  $\text{Fever} \in \{\text{Fever}, \neg\text{Fever}\}$

Source: YouTube – easy learning – Causality 2: Intervention, [Link](#)

# Deep Learning Strategies – Part III

## Causal Learning

### Bayesian Network



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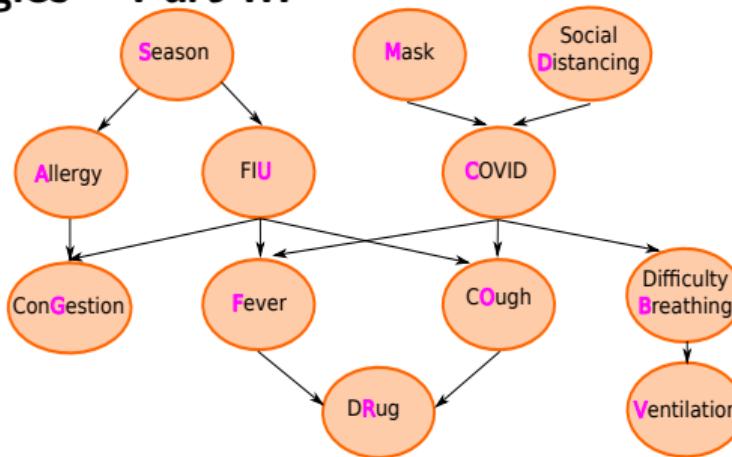
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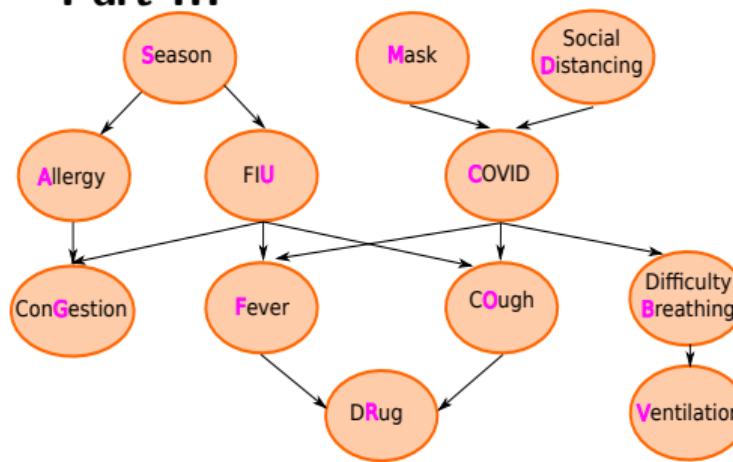
- Observing one of them, increases probability of the other! → Statistical dependence (correlation!) – Which one causes the other, how to figure it out – more data?

Source: YouTube – easy learning – Causality 2: Intervention, [Link](#)

# Deep Learning Strategies – Part III

## Causal Learning

### Observation vs. Intervention



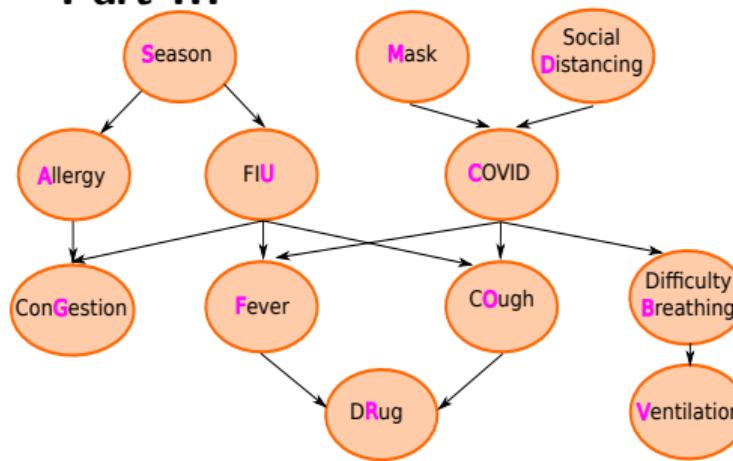
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# Deep Learning Strategies – Part III

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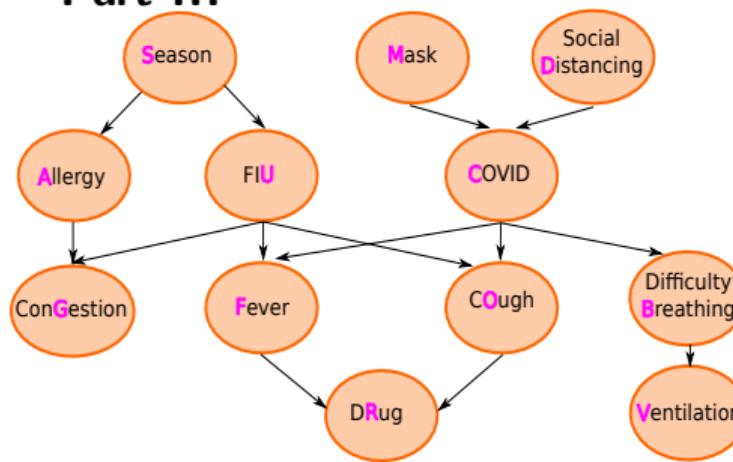
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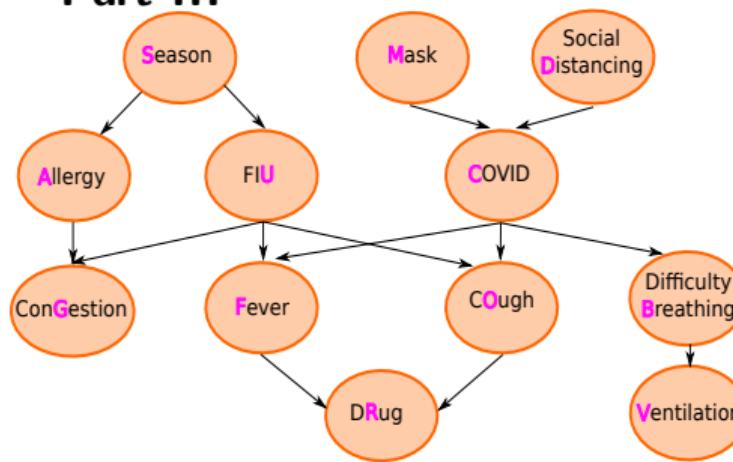
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# Deep Learning Strategies – Part III

## Causal Learning

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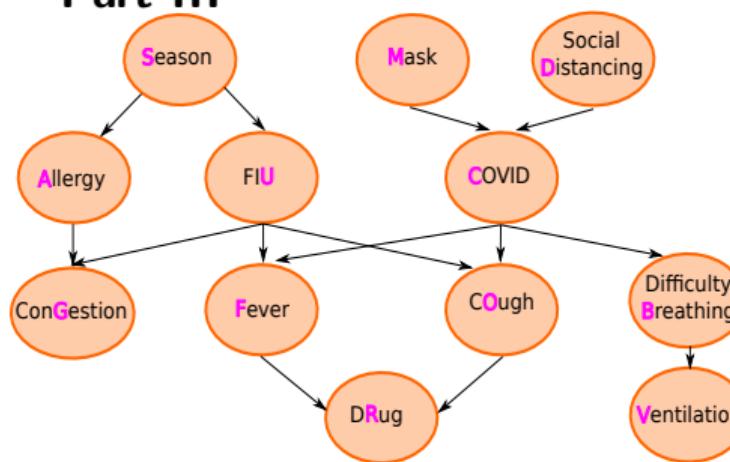
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# Deep Learning Strategies – Part III

## Causal Learning

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- Force variables to certain values and check changes in the other variable
- Intervention  $\rightarrow$  Causality!!! (...Find causal relationships)

Source: YouTube – easy learning – Causality 2: Intervention, [Link](#)

## Causal Learning

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### Intervention – Do-Operator

- Definition “Intervention”: an ideal intervention on a given random variable  $Z$  is described by forcing its value to  $z$ , denoted  $\text{do}(Z := z)$  or  $\text{do}(z)$

Source: YouTube – easy learning – Causality 2: Intervention, [Link](#)

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Source: YouTube – easy learning – Causality 2: Intervention, [Link](#)

## Causal Learning

- Intervene on Fever (induce/remove fever) and observe COVID (person has/has not COVID), should not result in any probability difference of seeing/causing COVID:

$$P(\text{COVID}|\text{do}(\text{Fever})) = P(\text{COVID}|\text{do}(-\text{Fever}))$$

indicating that Fever does not cause COVID!

$$P(\text{COVID}|\text{see}(\text{Fever})) > P(\text{COVID}|\text{see}(-\text{Fever}))$$

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- However: intervene on COVID and observe Fever, lead to:

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COVID causes Fever!

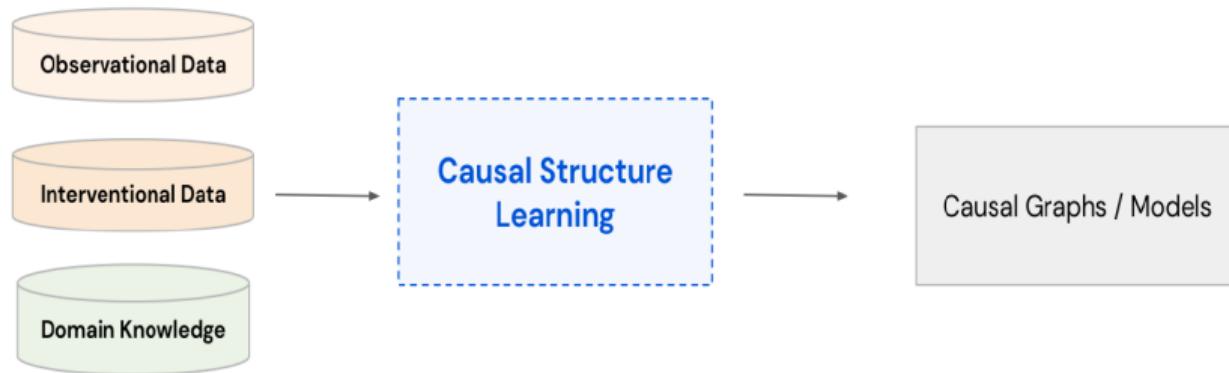
$$P(\text{Fever}|\text{COVID}) > P(\text{Fever}|-\text{COVID})$$

Interventional and observational relation is in line!

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# Deep Learning Strategies – Part III

## Causal Learning

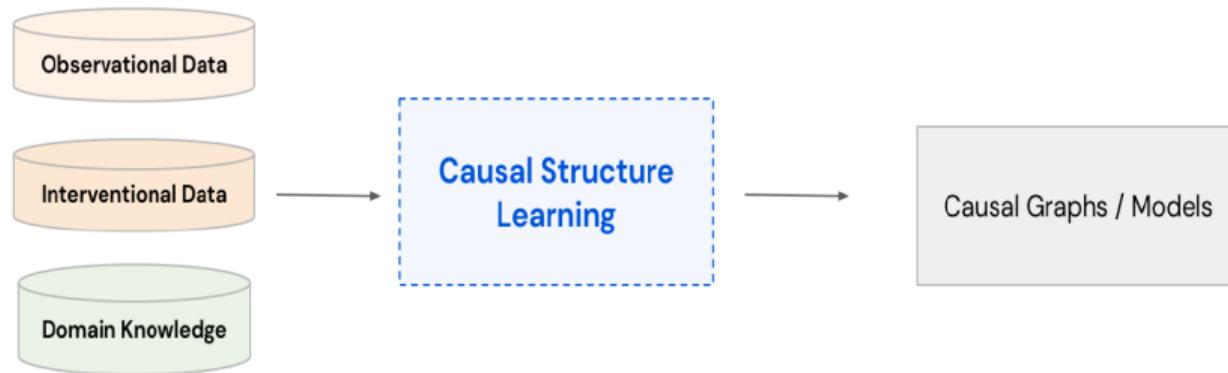


- **Observational Data:** collected without actively manipulating variables, just observing the natural state of the system (correlations/associations)

Source: FAU Erlangen-Nuremberg, Pattern Recognition Lab, K.Breininger, V. Christlein, Advanced Deep Learning – Interpretable/Causal Deep Learning

# Deep Learning Strategies – Part III

## Causal Learning

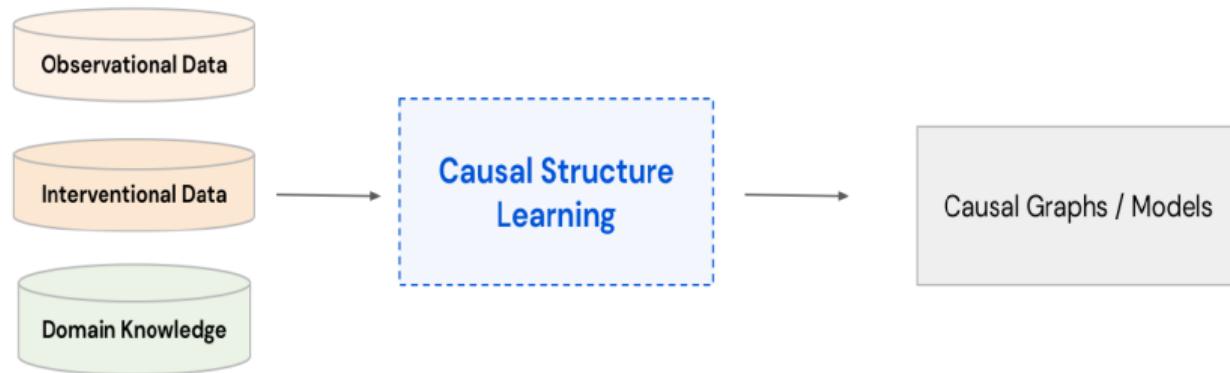


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# Deep Learning Strategies – Part III

## Causal Learning



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- **Domain Knowledge:** includes expert understanding, assumptions, or prior information about the system being studied, to help guiding the interpretation of observational data and the design of meaningful interventions

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## Causality

- **Average Causal Effect (ACE):** Binary variable  $Z \in \{0, 1\}$ , causes variable  $Y$ , if the average causal effect (ACE) of  $Z$  on  $Y = y$  is defined as:

$$ACE(Z \rightarrow Y_y) = P(Y = y | do(Z := 1)) - P(Y = y | do(Z := 0))$$

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- However: Let  $Y = X \oplus Z$  be the XOR-Function of  $X$  and  $Z$ , then:

$$P(Y | do(X = 0)) = P(Y | do(X = 1)) = P(Y)$$

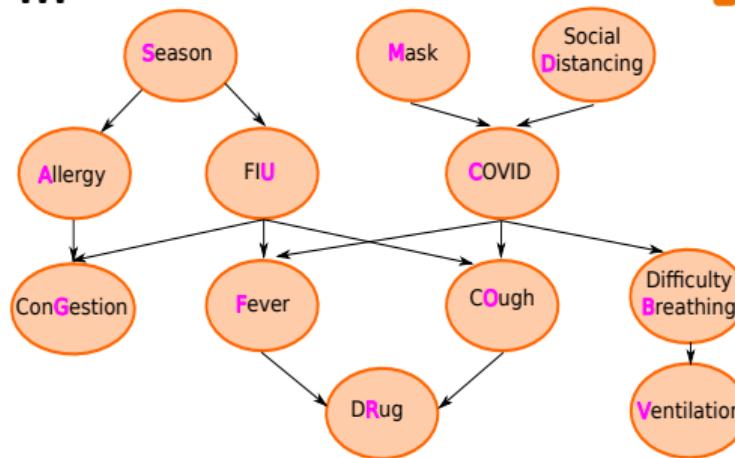
→ Better Definition as Deterministic Function!

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# Deep Learning Strategies – Part III

## Causal Learning

Causality as Deterministic Function!



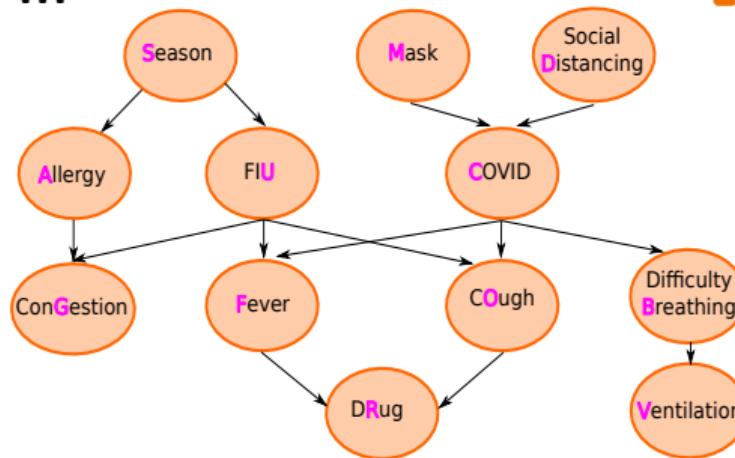
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# Deep Learning Strategies – Part III

## Causal Learning

Causality as Deterministic Function!



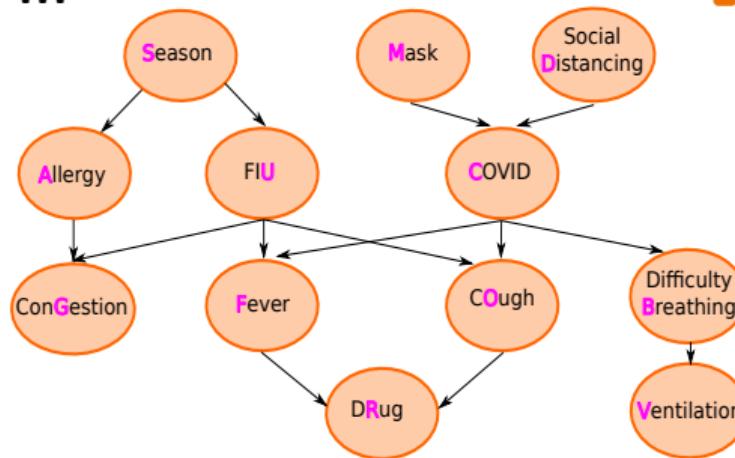
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# Deep Learning Strategies – Part III

## Causal Learning

Causality as Deterministic Function!



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- $C := f_C(U_C) = U_C, O := f_O(C, U_O), R := f_R(O, U_R)$   
→ **Structural Causal Model (SCM)**

Source: YouTube – easy learning – Causality 3: Defining causality: Structural causal models (SCM), [Link](#)

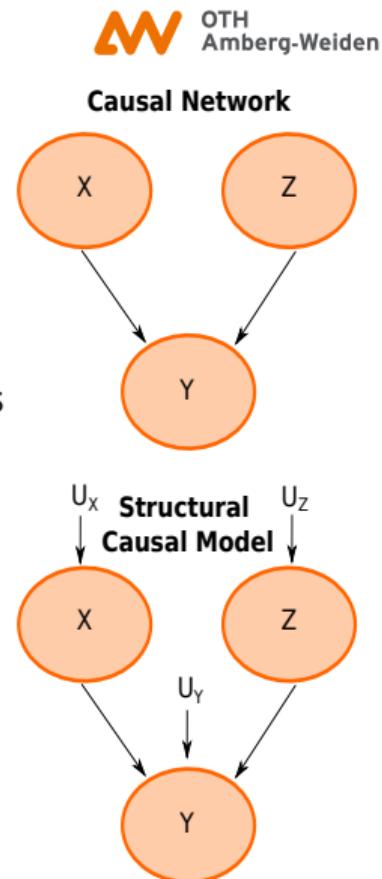
# Deep Learning Strategies – Part III

## Causal Learning

### Structural Causal Models (SCMs)

- SCM defined as a tuple  $\langle V, U, P_U, F \rangle$  with:
  1.  $V$  as the set of **endogenous** random variables
  2.  $U = \{U_X | X \in V\}$  as set of **exogenous/latent/noise** random variables
  3.  $P_U$  is the joint distribution over  $U$  satisfying  $P_U(U) = \prod_X P_U(U_X)$
  4.  $F$  set of functions  $f_X$ , how values are assigned to each variable  $X \in V$ , based on a subset of endogenous variables  $P_{AX} \subset V \setminus \{X\}$  (**parents**), with a parent exogenous variable  $U_X \subset U$ , leading to:

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# Deep Learning Strategies – Part III

## Causal Learning

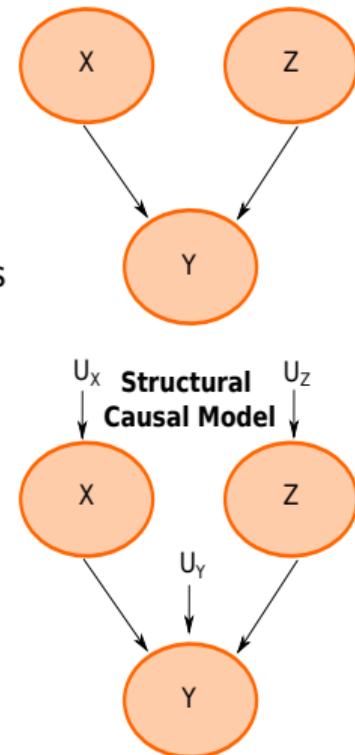
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$$X := f_X(P_{AX}, U_X)$$

- **Causal graph (network)** over nodes  $V$ , where the parents of each node are linked to it (assume the graph as DAG)

Causal Network



Source: YouTube – easy learning – Causality 3: Defining causality: Structural causal models (SCM), [Link](#)

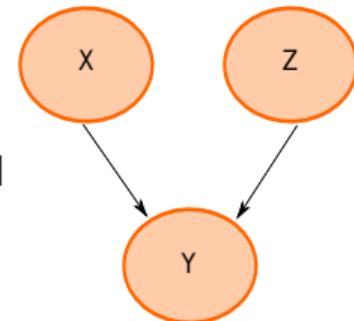
# Deep Learning Strategies – Part III

## Causal Learning

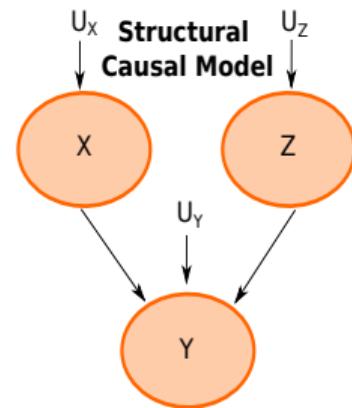
### Structural Causal Models (SCMs)

- Parents of a variable  $V$  are also called **direct causes** (one hierarchy level above), while the ancestors are known as **indirect causes** (multiple previous hierarchy levels)

#### Causal Network



#### Structural Causal Model



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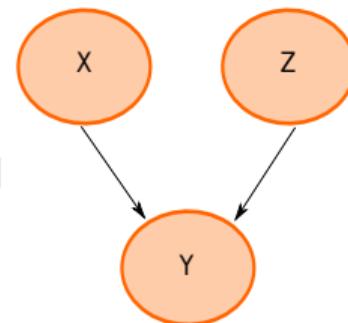
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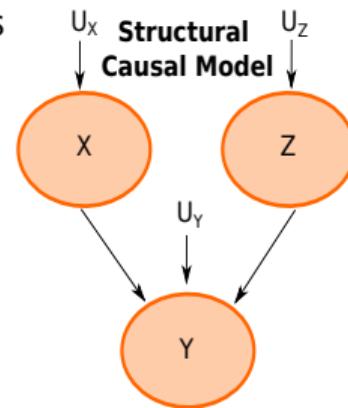
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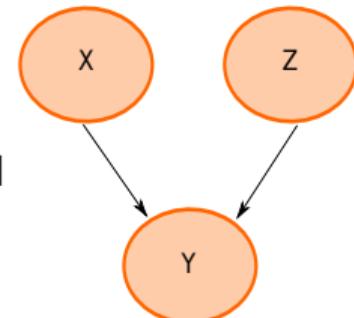
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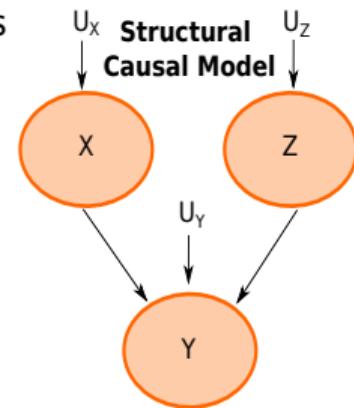
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- The variable  $X = f_X(Pax, U_X)$  (e.g.  $Y$ ) depends only on endogenous parents (e.g  $X, Z$ ), together with the exogenous variable (e.g  $U_Y$ )

Causal Network



Structural Causal Model



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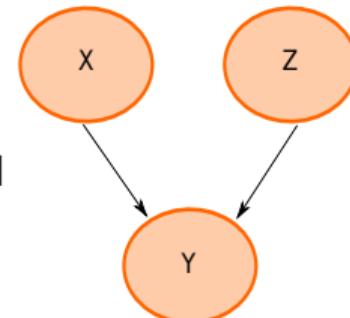
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## Causal Learning

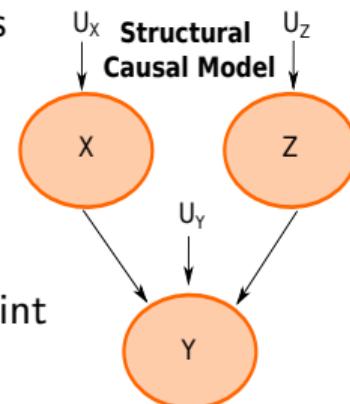
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- The variable  $X = f_X(P_{ax}, U_X)$  (e.g.  $Y$ ) depends only on endogenous parents (e.g  $X, Z$ ), together with the exogenous variable (e.g  $U_Y$ )
- Observational distribution of all endogenous variables  $V$  refers to the joint probability distribution  $P(V) = \prod_X P(X|P_{ax})$

Causal Network



Structural Causal Model



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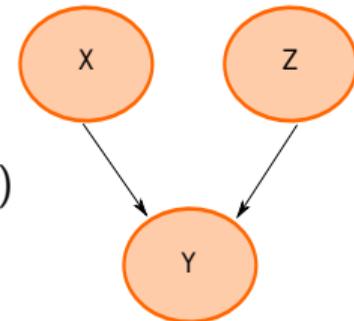
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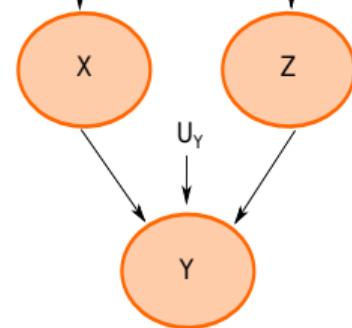
### Structural Causal Models (SCMs)

- The causal network  $\mathcal{G}$  is an I-Map for  $P(V) = \prod_X P(X|Pax)$  (**Bayesian Network Factorization**) with  $P(X|Pax)$  obtained from  $X = f_X(Pax, U_X)$

Causal Network



Structural Causal Model



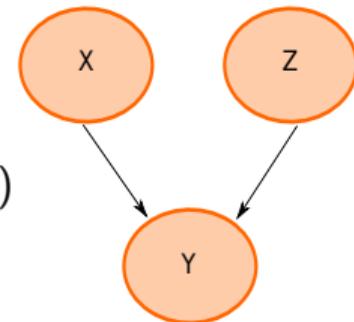
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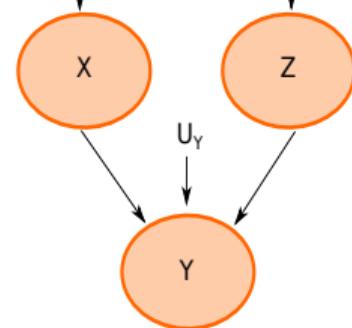
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#### Causal Network



#### Structural Causal Model



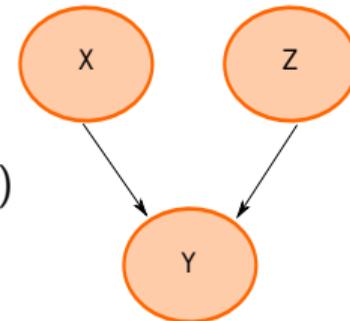
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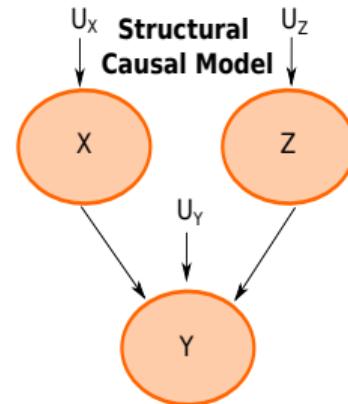
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Causal Network



Structural Causal Model



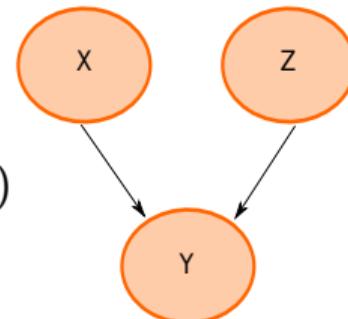
# Deep Learning Strategies – Part III

## Causal Learning

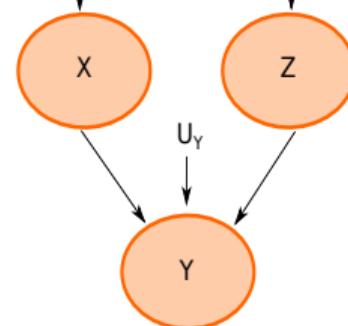
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- **Example I-MAP Graph:**  $X \rightarrow Y \rightarrow Z$  – with  $X$  = Having Disease,  $Y$  = Taking Medication,  $Z$  = Observing Side Effects

Causal Network



Structural Causal Model



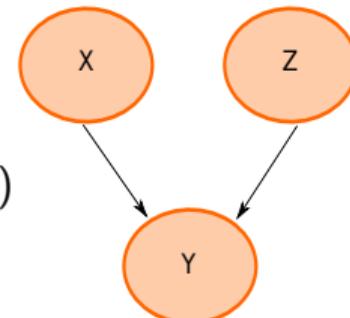
# Deep Learning Strategies – Part III

## Causal Learning

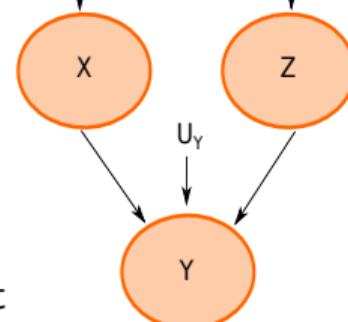
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- Example I-MAP Graph:**  $X \rightarrow Y \rightarrow Z$  – with  $X$  = Having Disease,  $Y$  = Taking Medication,  $Z$  = Observing Side Effects
- Captures **direct dependencies** ( $X \rightarrow Y$ ,  $Y \rightarrow Z$ ) and **conditional independencies** ( $X$  and  $Z$  are independent given  $Y$ , disease  $X$  alone not directly lead to side effects  $Z$ , only through the medication  $Y$  – parents!!!)

Causal Network



Structural Causal Model



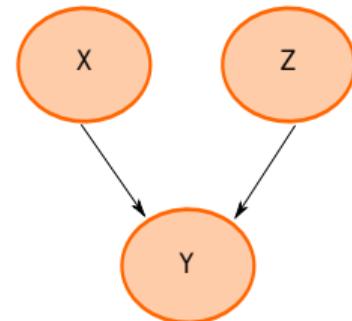
# Deep Learning Strategies – Part III

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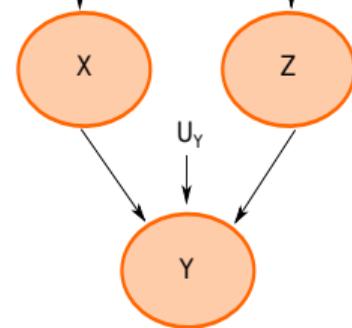
### Structural Causal Models (SCMs) – Example XOR

- $P(V) = P(X = x, Z = z, Y = y)$

#### Causal Network



$U_x$  **Structural Causal Model**  $U_z$



Source: YouTube – easy learning – Causality 3: Defining causality: Structural causal models (SCM), [Link](#)

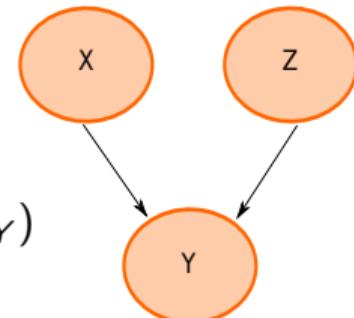
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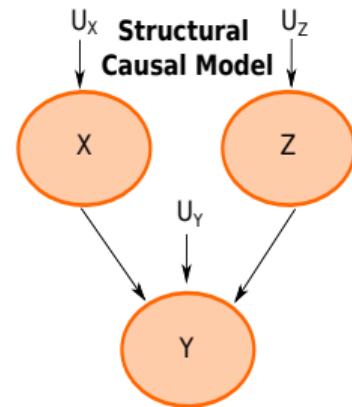
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Causal Network



Structural Causal Model



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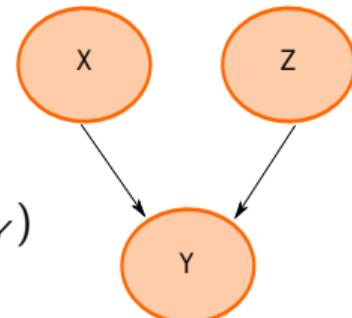
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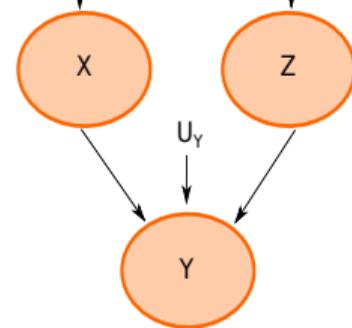
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- $Z = f_Z(Pa_Z, U_Z) = U_Z$
- $Y = f_Y(Pa_Y, U_Y)$ , with  $U_Y = 0 \rightarrow Y = (X, Z)$

#### Causal Network



$U_X$  **Structural Causal Model**  $U_Z$



Source: YouTube – easy learning – Causality 3: Defining causality: Structural causal models (SCM), [Link](#)

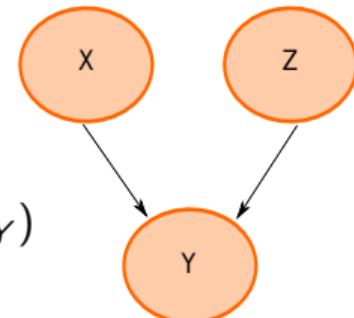
# Deep Learning Strategies – Part III

## Causal Learning

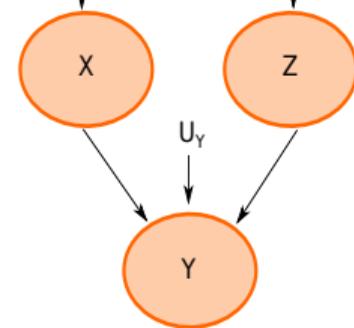
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- $Y = f_Y(Pa_Y, U_Y)$ , with  $U_Y = 0 \rightarrow Y = (X, Z)$
- $P(V) = P(x)P(z)P(y|x, z) = P(U_X = x)P(U_Z = z)1_y(x \oplus z)$   
with:  $1_y(b) = 1$ , if  $y = b$ , otherwise 0

#### Causal Network



$U_X$  **Structural Causal Model**  $U_Z$



Source: YouTube – easy learning – Causality 3: Defining causality: Structural causal models (SCM), [Link](#)

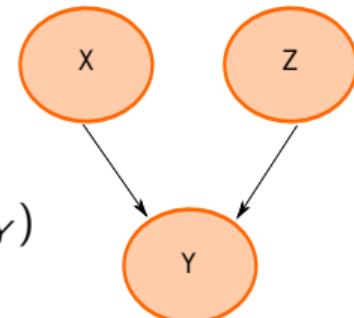
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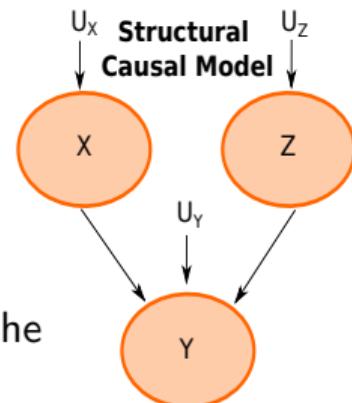
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with:  $1_y(b) = 1$ , if  $y = b$ , otherwise 0
- **Note:** From an SCM it is possible to compute the joint distribution of the given variables!

Causal Network



Structural Causal Model



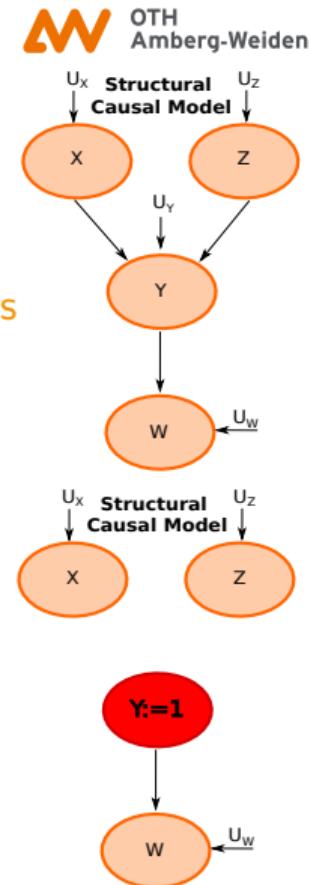
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# Deep Learning Strategies – Part III

## Causal Learning

### Structural Causal Models (SCMs) – Example XOR – Intervention

- Causal network turns into a Bayesian network if augmented with CPDs (prior probabilities, conditional probabilities) answering **probability queries**  $P(Y|Z = z)$  for all  $z \in Val(Z)$ ,  $Z, Y \subseteq V$



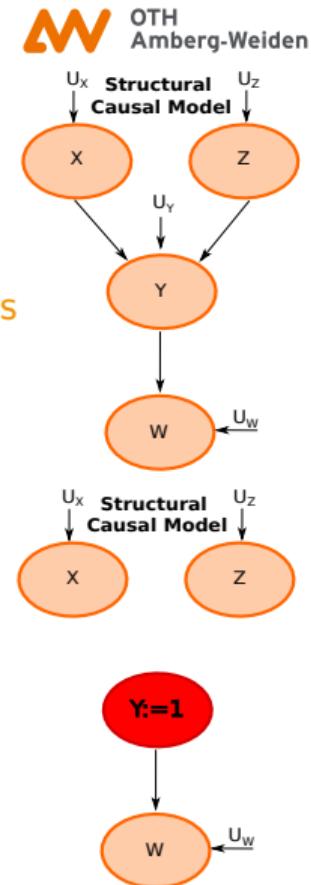
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# Deep Learning Strategies – Part III

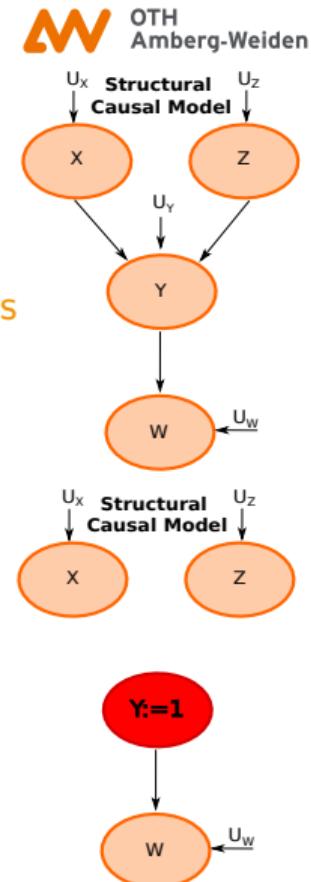
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- **Intervention in SCMs (do-operation):** setting  $Y := 1$

Before:  $X := U_X$ ,  $Z := U_Z$ ,  $Y := X \oplus Z + U_Y$ ,  $W := 2Y + U_W$

After:  $X := U_X$ ,  $Z := U_Z$ ,  $Y := 1$ ,  $W := 2Y + U_W \rightarrow U_W = W - 2$



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# Deep Learning Strategies – Part III

## Causal Learning

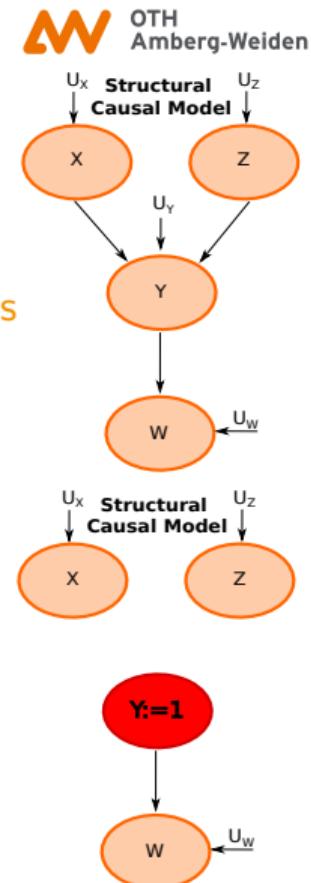
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- $Y$  does not depend on its endogenous/exogenous parents  $Pa_Y$  (all incoming links in the graph are removed!) → **Perfect intervention!**



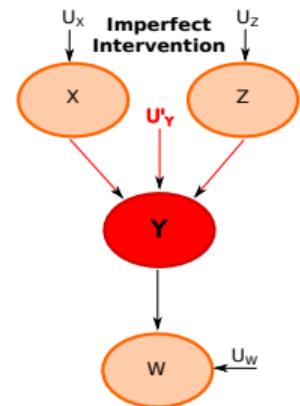
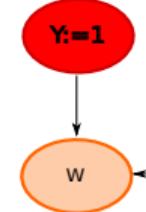
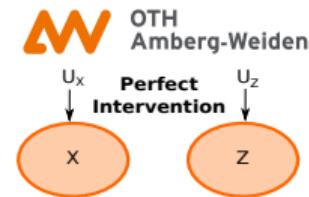
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# Deep Learning Strategies – Part III

## Causal Learning

### Structural Causal Models (SCMs) – Example XOR – Intervention

- In a **perfect intervention** the variable  $Y$  has a fixed/static value, based on its intervened value



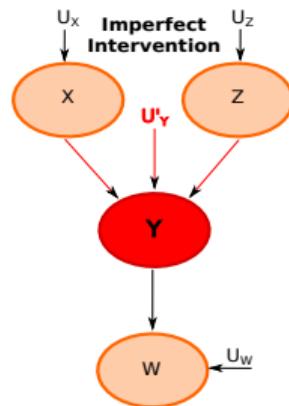
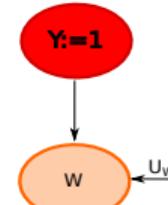
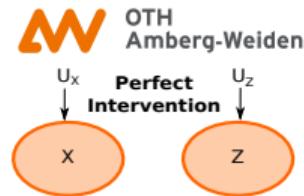
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# Deep Learning Strategies – Part III

## Causal Learning

### Structural Causal Models (SCMs) – Example XOR – Intervention

- In a **perfect intervention** the variable  $Y$  has a fixed/static value, based on its intervened value
- However: there exist also an **imperfect/parametric intervention**, known as **mechanism change ( $f'$  assignment)** (still some remaining parents)  $\rightarrow Y := f(P_{aY}, U_Y) \rightarrow Y := f'(P_{aY}, U'_Y)$  (e.g.  $Y := X - Z + U'_Y$ )



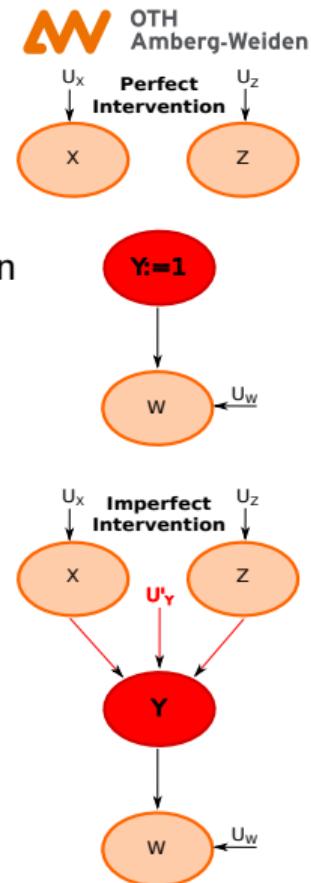
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- Every intervention leads to a CPD change w.r.t.  $Y$  from:  
$$Y : P(Y|Pa_Y) \text{ to } P^*(Y|Pa_Y)$$



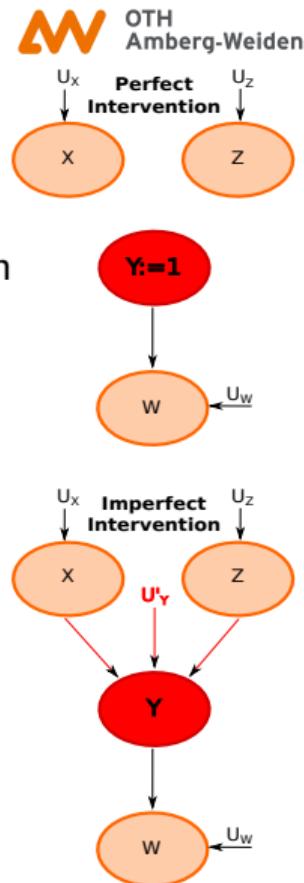
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- Every intervention leads to a CPD change w.r.t.  $Y$  from:  
$$Y : P(Y|Pa_Y) \text{ to } P^*(Y|Pa_Y)$$
- After every intervention there exist still a (new) SCM (causal network), with different dependencies and a intervention distribution  
 $P(V \setminus Z, do(Z))$  a intervention distribution over all the variables  $V$



Source: YouTube – easy learning – Causality 3: Defining causality: Structural causal models (SCM), [Link](#)

Describing the causal mechanisms of a system.

- **Variables:**

$$\mathbf{X} = \{X_1, \dots, X_N\}$$

- **Noise:**

$$U = \{U_1, \dots, U_N\}$$

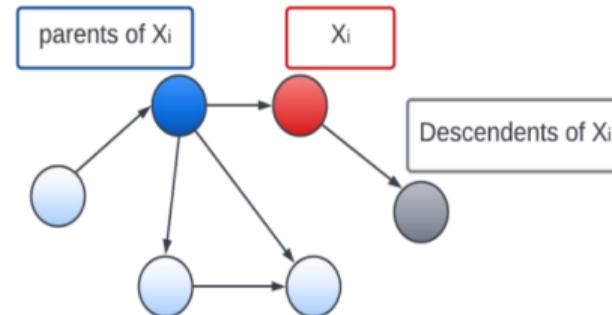
- **Causal parents of  $X_i$ :**

$$X_{pa(i,G)}$$

- **Structural Equations:**

$$X_i = f_i(X_{pa(i,G)}, U_i) \quad \forall i \in \{1, \dots, N\}$$

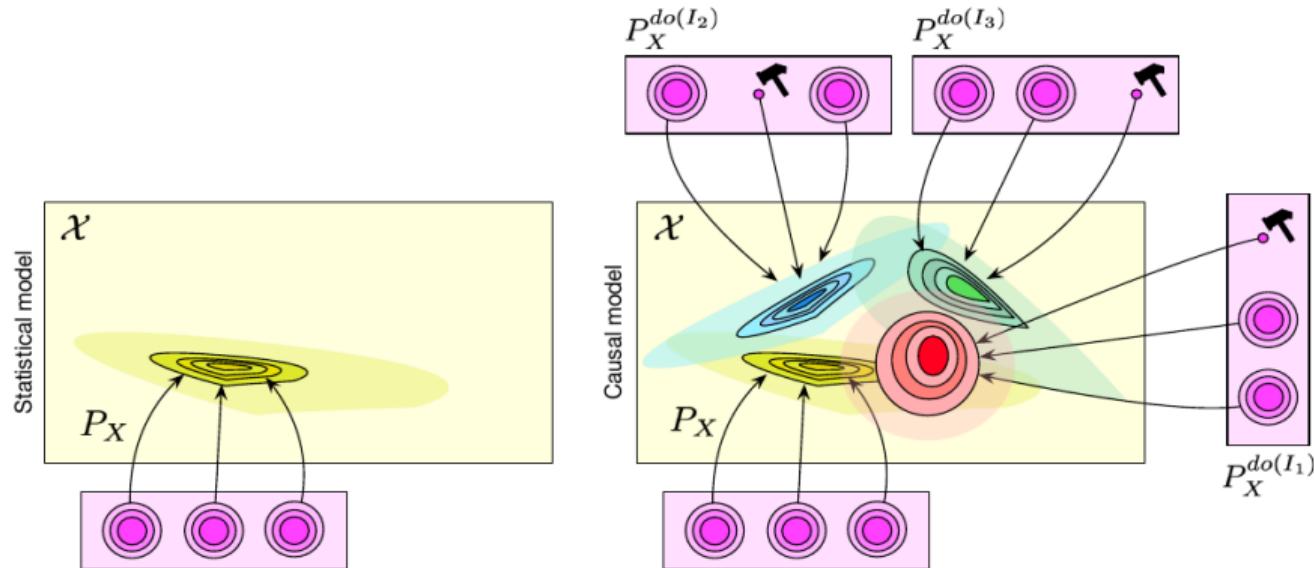
(Causal Mechanisms)



Source: Image from Nan Rosemary Ke, Stefan Bauer, "Causality and Deep Learning: Synergies, Challenges and the Future", Slide 22

# Deep Learning Strategies – Part III

## Causal Learning



- Statistical (Bayesian) Model: can only capture one probability distribution
- Causal Model: every intervention defines new joint distribution intervention

Source: FAU Erlangen-Nuremberg, Pattern Recognition Lab, K.Breininger, V. Christlein, Advanced Deep Learning – Interpretable/Causal Deep Learning

Source: Image from Nan Rosemary Ke, Stefan Bauer, "Causality and Deep Learning: Synergies, Challenges and the Future", Slide 22

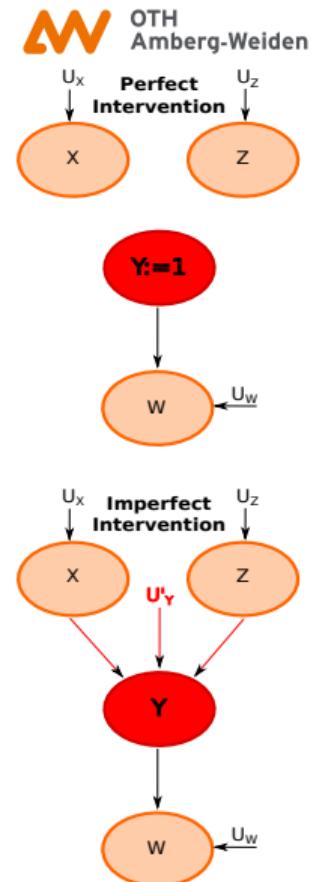
Source: Schölkopf et al., "Toward Causal Representation Learning"

# Deep Learning Strategies – Part III

## Causal Learning

### Structural Causal Models (SCMs) – Example XOR – Mutilated Network

- Converting an **intervention** to an **observation** query (remove all do's)



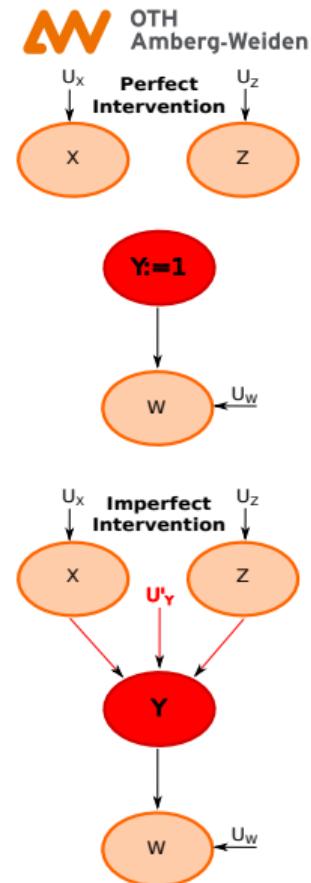
Source: YouTube – easy learning – Causality 3: Defining causality: Structural causal models (SCM), [Link](#)

# Deep Learning Strategies – Part III

## Causal Learning

### Structural Causal Models (SCMs) – Example XOR – Mutilated Network

- Converting an **intervention** to an **observation query** (remove all do's)
- In case of the previous Bayesian Network, and for a **perfect intervention query**,  $P(Y|do(z), x)$  is transformed to  $P(Y|z, x)$ , by removing all incoming edges to the intervened nodes  $Z$ , and set a fixed intervention value  $Z = z$



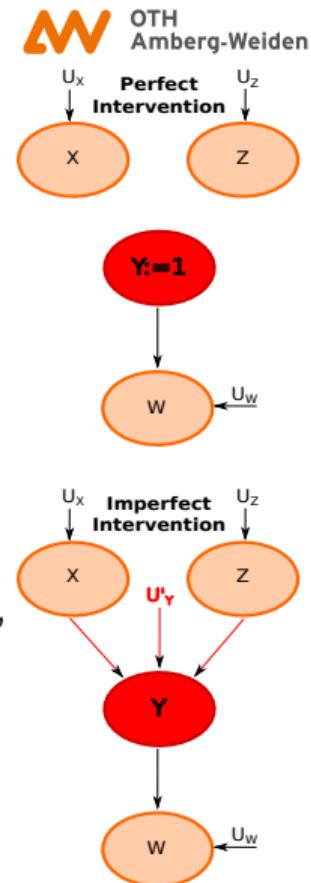
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# Deep Learning Strategies – Part III

## Causal Learning

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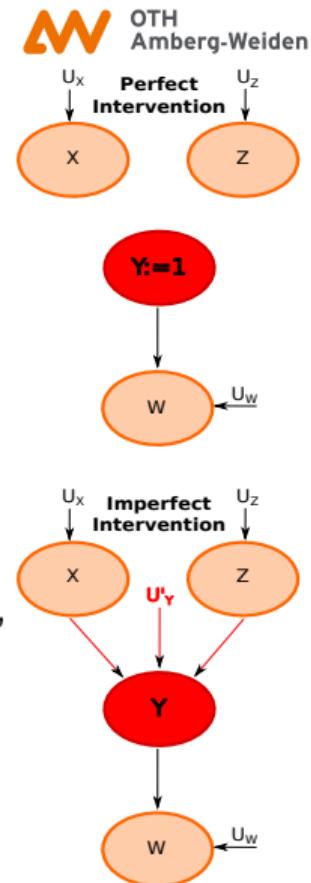
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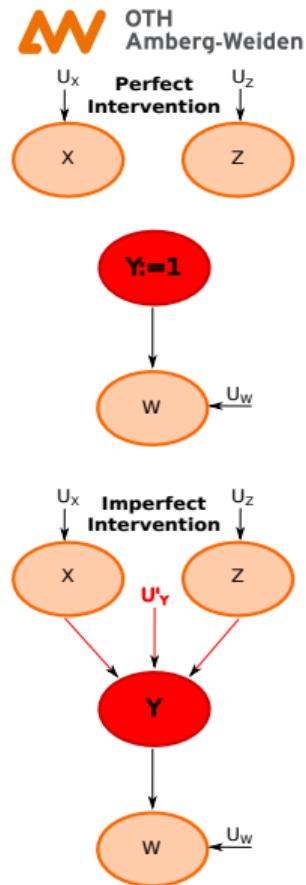
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# Deep Learning Strategies – Part III

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- Answering intervention queries:  $P(Y|do(z), x) = P_{\mathcal{B}_{Z:=z}}(Y|z, x)$
- **Modularity:** conditional probability of a node is only affected if intervention is on its parents  $P(Y|Pa_Y, do(z)) = P(Y|Pa_Y)$ ,  $\forall Y \notin Z$



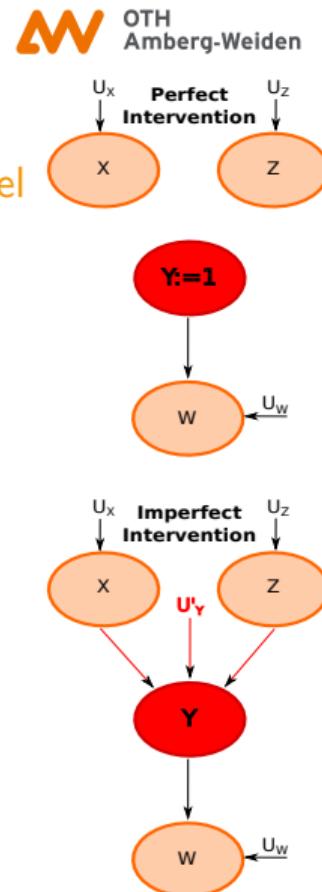
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# Deep Learning Strategies – Part III

## Causal Learning

### Structural Causal Models (SCMs) – Example XOR – Causal (Bayesian) Model

- **Causal (Bayesian) Network  $\mathcal{C}$  (CBN):** over a set of random variables  $V$  (joint distribution  $P$ ),  $\mathcal{C}$  is a Bayesian network  $\mathcal{B}(\mathcal{G}, P_{\mathcal{C}})$ , with  $\mathcal{G}$  is an I-Map for  $P$ , over  $V$ , answering both probability queries:
  1.  $P(Y|x) = P_{\mathcal{C}}(Y|x)$  and intervention queries:
  2.  $P(Y|Pa_Y, \text{do}(z)) = P_{\mathcal{C}_{Z:=z}}(Y|Pa_Y), \forall Y \notin Z, z \in \text{Val}(Z)$



Source: YouTube – easy learning – Causality 4: Causal Bayesian Networks, [Link](#)

# Deep Learning Strategies – Part III

## Causal Learning

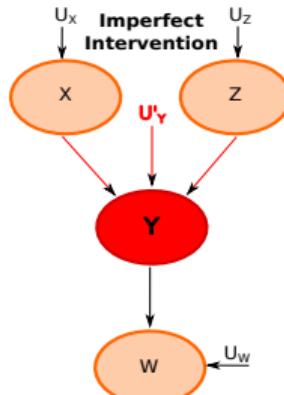
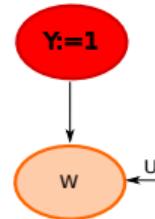
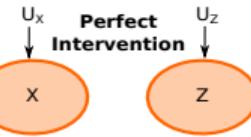
### Structural Causal Models (SCMs) – Example XOR – Causal (Bayesian) Model

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- Recap: Causal Hierarchy

1. **Association (Seeing!)** – Probabilistic query  $P(Y|X)$  (e.g. probability of developing cancer given that the individual smokes?) – BN, CBN, SCM
2. **Intervention (Doing!)** – Intervention query  $P(Y|do(X))$  (e.g. What is the prob. of developing cancer if individuals stop smoking?) – CBN, SCM
3. **Counterfactual (Imagining!)** – Counterfactual query  $P(Y_{X=1}|X=0)$  (e.g. What would have happened if individuals had quitted smoking?) – SCM



Source: YouTube – easy learning – Causality 4: Causal Bayesian Networks, [Link](#)

## Causal Learning

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### Structural Causal Models (SCMs) – Counterfactual Queries

- Bayesian Network (BN) is able to answer probabilistic queries (associations), while Causal Bayesian Networks (CBN) & SCM can also handle intervention queries

Source: YouTube – easy learning – Causality 6: Counterfactual Queries, [Link](#)

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Source: YouTube – easy learning – Causality 6: Counterfactual Queries, [Link](#)

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- **Example:** There was a fork in the road, where a decision must be made – take the freeway ( $X = 1$ ) or go on a surface street ( $X = 0$ ). The person took the surface street with a lot of traffic and arrived one hour later ( $Y = 1$ ). He asked himself – If he had taken the freeway, he would have gotten home earlier!!!

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- Such an **unrealized situation from the past**, wrapped in an “if-statement” is known as **counterfactual** → How to model a counterfactual query/situation?

Source: YouTube – easy learning – Causality 6: Counterfactual Queries, [Link](#)

## Causal Learning

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### Structural Causal Models (SCMs) – Counterfactual Queries

- Let  $Y$  be the arriving time ( $Y = 1$  for being late,  $Y = 0$  for being in time)

Source: YouTube – easy learning – Causality 6: Counterfactual Queries, [Link](#)

## Causal Learning

### Structural Causal Models (SCMs) – Counterfactual Queries

- Let  $Y$  be the arriving time ( $Y = 1$  for being late,  $Y = 0$  for being in time)
- Causal inference: prediction of  $Y$  from the past, by intervening on the road (change from surface road  $X = 0$  to freeway  $X = 1$ ):  $P(Y|\text{do}(X = 1))$

Source: YouTube – easy learning – Causality 6: Counterfactual Queries, [Link](#)

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- **Counterfactual inference:** reformulate as:  $P(Y_{X=1}|X = 0, Y = 1)$

Source: YouTube – easy learning – Causality 6: Counterfactual Queries, [Link](#)

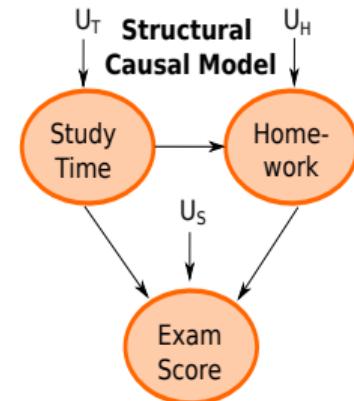
## Causal Learning

### Structural Causal Models (SCMs) – Counterfactual Queries

- Example Counterfactual Event:

►  $T := U_T, \quad H := 0.5T + U_H, \quad S := 0.7T + 0.4H + U_S$

with:  $T$  as the students studying time,  $H$  as the number of completed homeworks,  $S$  student's exam score,  $U_T$  student's free time at home,  $U_H$  student's intelligence,  $U_S$  student's anxiety



Source: YouTube – easy learning – Causality 6: Counterfactual Queries, [Link](#)

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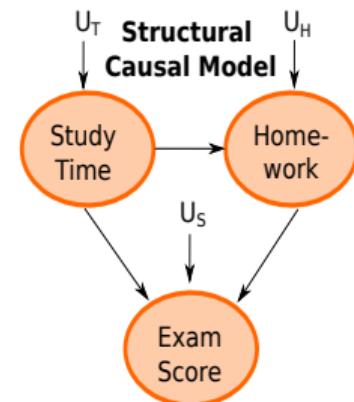
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- Let  $T = 0.5$ ,  $H = 1$ , and  $S = 1.5$  for a particular student, resulting in:

$$U_T := T = 0.5, \quad U_H = H - 0.5T = 1 - 0.5 \cdot 0.5 = 0.75,$$

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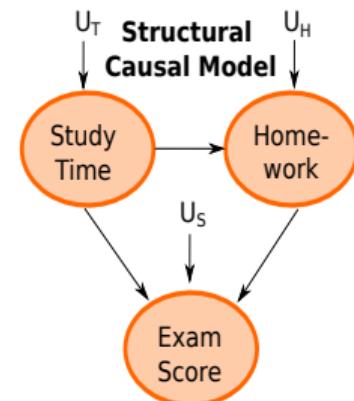
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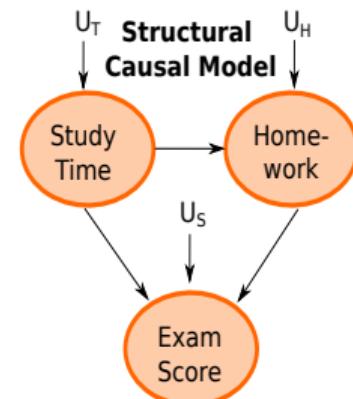
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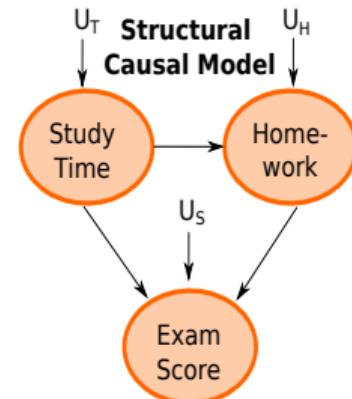
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- Counterfaction:  $P(S_{H=2}|T = 0.5, H = 1, S = 1.5)$

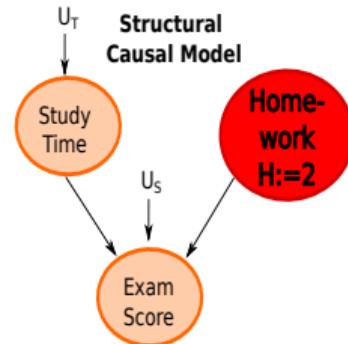


Source: YouTube – easy learning – Causality 6: Counterfactual Queries, [Link](#)

## Causal Learning

### Structural Causal Models (SCMs) – Counterfactual Queries

- Example Counterfactual Event
  - ▶ Create mutilated graph, by removing all incoming links to the intervened node  $Z = H$ , with  $P(H = 2) = 1$



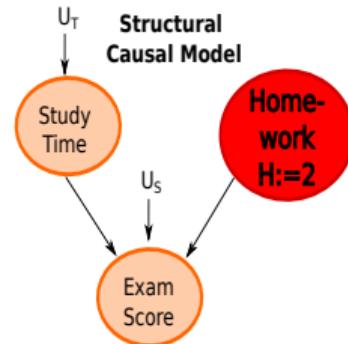
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## Causal Learning

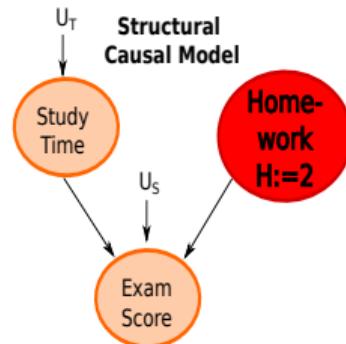
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- Abduction-Action-Prediction

1. Abduction – use evidence  $E = e$  in order to determine all the values of  $U$



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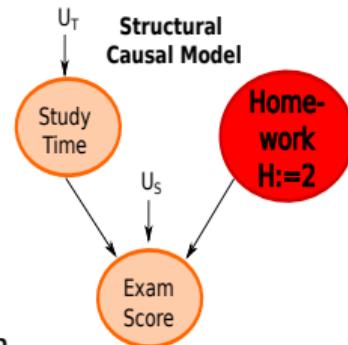
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Source: YouTube – easy learning – Causality 6: Counterfactual Queries, [Link](#)

## Causal Learning

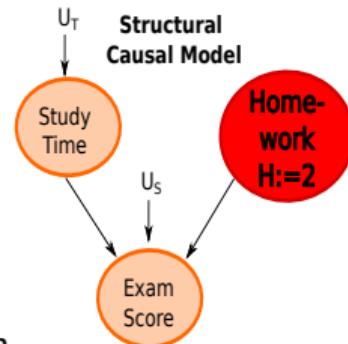
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2. Action – Removing structural equations for variables  $X$  and replace it with the appropriate functions  $X = x$  (Mutilated Graph!)
3. Prediction – Use the mutilated model and the value of  $U$  to compute the value of  $Y$ , the consequence of the counterfactual



Source: YouTube – easy learning – Causality 6: Counterfactual Queries, [Link](#)

## Causal Learning

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### Summary – Difference BN, CBN and SCM

- Bayesian Network (BN)
- 1. BN is a directed acyclic graph (DAG) that represents probabilistic relationships among variables, while each random variable (node) connection represents a conditional dependence → No causation, only correlations, and conditional independencies

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- Bayesian Network (BN)
  1. BN is a directed acyclic graph (DAG) that represents probabilistic relationships among variables, while each random variable (node) connection represents a conditional dependence → No causation, only correlations, and conditional independencies
  2. Example: Bayesian Network, with nodes: Flu → Fever, Flu → Cough, while the model/graph shows the association between Flu and Fever, as well as Flu and Cough, however, no information that Flu causes both

## Causal Learning

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### Summary – Difference BN, CBN and SCM

- Causal Bayesian Network (CBN)
- 1. CBN is a BN with an additional assumption – the edges represent causal relationships – explicitly encoding causation, not just correlation or conditional independence

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  4. CBNs are used for causal inference, with predictions not just about associations, but also the effects of interventions
  5. Example: same graph w.r.t. causation, show that Flu causes Fever and Cough, while intervening Flu causes an impact with respect to Fever and Cough

## Causal Learning

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### Summary – Difference BN, CBN and SCM

- Structural Causal Model (SCM)
1. SCM is a causal model providing a more formal framework than a CBN, using a set of structural equations that specify how each variable is generated as a function of its causal parents and some random “noise” term, along with a causal DAG structure

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  1. SCM is a causal model providing a more formal framework than a CBN, using a set of structural equations that specify how each variable is generated as a function of its causal parents and some random “noise” term, along with a causal DAG structure
  2. SCMs allow for both causal inference and formal intervention analysis, while being used for counterfactual reasoning, interventions, and predicting causal effects
  3. SCM would not only represent Flu causing Fever & Cough, but also provide equations –  $\text{Fever}=f(\text{Flu}, U_F)$ ,  $\text{Cough}=g(\text{Flu}, U_C)$  – specifying how Flu influences Fever & Cough under different conditions

# Further Questions?



<https://www.oth-aw.de/hochschule/ueber-uns/personen/bergler-christian/>

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