

MutDafny: A Mutation-Based Approach to Assess Dafny Specifications

Isabel Amaral

INESC TEC, Faculdade de
Engenharia, Universidade do
Porto
Porto, Portugal

Alexandra Mendes

INESC TEC, Faculdade de
Engenharia, Universidade do
Porto
Porto, Portugal

José Campos

Faculdade de Engenharia,
Universidade do Porto & LASIGE
Porto, Portugal

Abstract

This paper explores the use of mutation testing to reveal weaknesses in formal specifications written in Dafny. In verification-aware programming languages, such as Dafny, despite their critical role, specifications are as prone to errors as implementations. Flaws in specs can result in formally verified programs that deviate from the intended behavior.

We present MutDafny, a tool that increases the reliability of Dafny specifications by automatically signaling potential weaknesses. Using a mutation testing approach, we introduce faults (*mutations*) into the code and rely on formal specifications for detecting them. If a program with a mutant verifies, this may indicate a weakness in the specification. We extensively analyze mutation operators from popular tools, identifying the ones applicable to Dafny. In addition, we synthesize new operators tailored for Dafny from bugfix commits in publicly available Dafny projects on GitHub. Drawing from both, we equipped our tool with a total of 32 mutation operators. We evaluate MutDafny's effectiveness and efficiency in a dataset of 794 real-world Dafny programs and we manually analyze a subset of the resulting undetected mutants, identifying five weak real-world specifications (on average, one at every 241 lines of code) that would benefit from strengthening.

1 Introduction

Proving that a software program is correct is necessary in critical systems, as failures in these can have drastic consequences. It is thus important to guarantee that such systems have no faults. Although traditional software testing [46] is used in many contexts for software validation, it only checks a system against specific inputs, not guaranteeing full correctness. In contrast, *formal software verification* [11, 30, 36] can mathematically prove complete correctness concerning a precise specification of the intended behavior.

Verification-aware languages, such as Dafny [35], are designed to support the development of formally verified software by embedding formal specifications directly into the code. It allows developers to specify program behavior through pre-conditions (*requires*), post-conditions (*ensures*), and invariants (*invariant*), which are automatically verified by Dafny, helping to guarantee that the implementation conforms to its intended behavior and ensuring code correctness beyond conventional testing. Dafny has seen adoption in industry, including at AWS¹ [15] and Consensys [14].

Since formal verification only guarantees that an implementation conforms to its specification, a flawed specification can lead to a verified program that does not exhibit the intended behavior. Although specifications are usually trusted to be correct, this should not be taken as a given.² A study conducted by Fonseca et al. [21] confirmed exactly that: it found 16 faults in three formally verified distributed systems (one written in Dafny). Some of these faults stemmed from incorrect and incomplete specifications, highlighting a critical limitation of verification when specifications themselves are flawed.

As a motivational example, consider Dafny's code in Listing 1 returning all elements belonging to both input arrays.

Listing 1: Example of a Dafny program with a weak specification.

```

1 predicate InArray(a: array<int>, x: int)
2   reads a
3 { exists i :: 0 <= i < a.Length && a[i] == x }
4
5 method SharedElements(a: array<int>, b: array<int>)
6   returns (result: seq<int>)
7 ensures forall x :: x in result ==> (InArray(a, x) && InArray(b, x))
8 ensures forall i, j :: 0 <= i < j < result ==> result[i] != result[j]
9 {
10  var res: seq<int> := [];
11  for i := 0 to a.Length
12    invariant 0 <= i <= a.Length
13    invariant forall x :: x in res ==> InArray(a, x) && InArray(b, x)
14    invariant forall i, j :: 0 <= i < j < res ==> res[i] != res[j]
15    {
16      if InArray(b, a[i]) && a[i] !in res {
17        res := res + [a[i]];
18      }
19    }
20  result := res;
21 }
```

Although this program verifies, removing the *if* block in Lines 16 to 18 (an error a human could do or a mutation a tool could insert) causes it to always return an empty list – an incorrect behavior that still satisfies the specification. Despite the inserted error, Dafny's ability to verify this program hints at a possible problem with the spec. This is indeed an example of a *weak specification*, i.e., one that does not sufficiently constrain the program's behavior. Its strengthening would require replacing the \Rightarrow in the first ensures (Line 7) with \Leftarrow and the addition of an invariant (between Lines 14 and 15) adding that, besides every element in *result* being in both arrays, every element that appears in both arrays must also be present in *result*, i.e.:

```
+ invariant forall j :: 0 <= j < i && InArray(b, a[j]) ==> a[j] in res
```

In this work, our main goal is to support Dafny developers in ensuring the strength of their specifications. To achieve this, we follow the *mutation testing* [23, 25, 49, 54]

²In this paper, we use *specification* or *spec* to refer to Dafny's formal contracts (e.g., requires, ensures, and invariants); we use *implementation* or *code* to refer to Dafny's code within method or function bodies.

¹<https://github.com/aws/aws-encryption-sdk-dafny>, accessed Nov. 2025.

concept, where the quality of a test suite is evaluated by introducing faults, called *mutants*, into a program, and evaluating whether these are detected by the test suite.

Mutants are automatically created by applying *mutation operators*, i.e., syntactic changes that mimic common programming errors, each differing from the original program by a small localized change. Mutants that cause tests to fail are considered *killed*, while those that go undetected are *alive*, indicating untested behavior. While the mutants run typically against a test suite, in our approach, they run against the formal specification. Surviving mutants may reveal weaknesses in the spec, indicating underspecified behavior, which may help developers identify and strengthen those specs. Nevertheless, an alive mutant may not always indicate the presence of a weak specification, i.e., the mutant might just be equivalent to the original program [13, 43, 55], meaning that, despite the change, its behavior is the same as that of the original program.

This raises the questions: **(RQ1)** *Which small syntactic changes could mimic programming errors in Dafny?* and **(RQ2)** *Are mutation operators for Dafny programs helpful in the identification of specification weaknesses?* To answer these, we first assembled a compilation of 147 mutation operators previously proposed for other six programming languages and studied their application in Dafny. Secondly, we complemented this set with new operators tailored for the language derived from analyzing 1,475 bugfix commits from Dafny programs available in 112 public GitHub repositories. Thirdly, given there is not, to the best of our knowledge, a tool that mutates Dafny implementations, we developed one, **MutDafny**, supporting these mutation operators. Finally, we conducted an empirical study on 112,810 pairs of original-mutant Dafny programs to assess the effectiveness of our approach and, additionally, to answer the questions: **(RQ3)** *How effective are the different mutation operators?* and **(RQ4)** *How efficient is MutDafny at generating mutants?*

Contributions. The main contributions of this paper are:

- ★ An extensive analysis of which mutation operators supported by the most popular mutation tools can be applied to Dafny programs, and why. (Section 3)
- ★ The proposal of a set of novel mutation operators tailored for Dafny programs. (Section 4)
- ★ MutDafny: a novel mutation testing tool for signaling possible specification weaknesses in Dafny programs. The tool is publicly available at <https://github.com/MutDafny/mutdafny>. (Section 5)
- ★ Evidence of MutDafny's usefulness in assisting Dafny developers increase the reliability of their specs, gathered through an empirical study on 794 Dafny programs and a manual evaluation of 284 alive mutants. All the scripts, data, and instructions required to reproduce the study are publicly available at <https://github.com/MutDafny/mutdafny-study-data>. (Section 6)

Even though this paper explores mutation testing in the context of Dafny, an added benefit is that this approach is applicable to any verification-aware language.

2 Related Work

Mutations in verification-aware languages. To our knowledge, IronSpec³ [22] is the only previous work dealing with mutations in Dafny, being the work more closely related to ours. It aims to increase the reliability of formal specifications, operating on three different dimensions, one including mutation testing, which, unlike our approach, mutates specifications. Their approach considers mutants that are stronger than the original specification. If the method still verifies with the mutation, it means that the original specification is weaker than the implementation and can potentially be strengthened. In 14 Dafny methods, IronSpec detected two specification faults through this approach.

Much like in MutDafny, mutations to the implementation of Eiffel programs have been used to evaluate their specs [34]. However, no developer-oriented tool based on the mutation of implementations exists for providing specification quality feedback, nor has any in-depth study on suitable mutation operators been conducted.

Other related work in using mutation testing to assess specification quality includes Lahiri [33] and Endres et al. [20]. Lahiri [33] uses the mutation of test cases to validate specifications without the need for an implementation. Endres et al. [20] capture a specification's ability to reject LLM-generated implementation mutants. The results of both align closely with the human assessment of specification quality.

Mutation in other specification-related contexts. MuAlloy [52] is a mutation testing and mutation-based test generation tool for Alloy. Although both Alloy and Dafny support formal methods, Alloy is a specification modeling language with a distinct purpose from verification-aware languages. Ma'ayan et al. [42] used mutations consisting of the deletion of specification guarantees (weakening) to validate a coverage-based scenario generation algorithm for systems generated by reactive synthesis. Finally, in a mutation-based study on the effectiveness of the JML-JUnit [16] tool for automatic unit test generation from Java specifications, Tan and Edwards [50] concluded that mutation testing can also be helpful in unveiling specification bugs, not just implementation errors.

Synthesis of mutation operators. Unlike our manual approach, Tufano et al. [51] used a deep learning approach trained on 787,178 bug-fixing commits from GitHub to automatically generate mutants that closely resemble real faults. However, replicating their approach is difficult due to the need for large-scale bug-fix data, and we found only 1,475 (*likely*) bug-fixing commits (0.19% of their dataset).

3 Mutation tools and operators proposed for traditional programming languages

Aiming to answer RQ1, in this section, we compile the mutation operators proposed for other, more traditional, programming languages and investigate their applicability to Dafny programs. We consider a mutation operator applicable to a Dafny program if the language supports the operation performed by the operator and it has the potential of leading to a valid program.

³<https://github.com/GLaDOS-Michigan/IronSpec>, accessed Nov. 2025.

3.1 Mutation tools proposed for other programming languages but Dafny

Sánchez et al. [48] conducted a study of the use of mutation testing in practice and identified 127 mutation testing tools. The most popular tools for the programming languages for which Dafny compiles to (i.e., C#, C++, Java, JavaScript, Go, and Python), are: Stryker.NET [9] for C#; Mull [5, 18] for C++; Major [3, 27, 28], MuJava [4, 38–41], and PIT [7, 17] for Java; StrykerJS [8] for JavaScript; Go-Mutesting [1, 2] for Go; Mutmut [6] and MutPy [19] for Python. These were selected based on the overall top 10 most popular tools and on the most popular for each language.

3.2 Mutation operators proposed for other programming languages but Dafny

Given the tools listed in Section 3.1, we identified the set of mutation operators supported by each. This involved reading the papers (when available), documentation, and, specifically for Mutmut [6], studying its source code due to a lack of documentation.

We found many similar operators among the different tools and languages, but most use different names for these common operators. We attempted to group operators according to our perceived similarity between them. *Operator replacement*, which apply to binary operators: Arithmetic (e.g., +, *), Relational (e.g., ==, <=), Conditional (e.g., &&, ||), Logical (e.g., &, |), Shift (e.g., <<, >>), Assignment (e.g., +=, >>=); *Operator insertion/deletion*, which apply to the unary operators: Arithmetic (e.g., -, ++), Conditional (e.g., !), Logical (e.g., ~); *Literal value replacement*; *Expression replacement*; *Statement, variable, constant or operator deletion* – where the latter differs from unary operator deletion in that it applies to all types of operators, both unary and binary, and because it involves the deletion of all occurrences of a specific operator; *Object-Oriented (OO) specific*: Inheritance, Polymorphism, and Overloading. The operators listed for the arithmetic, relational, conditional, logical, shift, and assignment are the ones that exist specifically in Java.

3.3 Mutation operators proposed for other languages that are applicable in Dafny

Following the process detailed in Section 3.2, we compiled a total of 147 mutation operators.⁴ Of these, we identified 97 that can be applied to Dafny programs and 50 that cannot due to the syntax structure of Dafny 4.10.0.⁵ From the 97 operators that can be applied to Dafny, we concluded that seven always generate equivalent mutants when applied to Dafny. Finally, these 90 operators were later narrowed down to 30 unique ones due to many reflecting the same behavior. Next, we partially answer RQ1 by listing and describing the applicability of these operators as well as any restrictions on their use.

⁴The list of mutation operators, including their description, which tools implement them, and whether they can be applied to Dafny, can be found in Chapter 1 of the supplementary material at <https://doi.org/10.6084/m9.figshare.30640202.v1>.

⁵At the time of writing, the latest version of Dafny available was 4.10.0.

3.3.1 Arithmetic operators. Dafny provides five arithmetic binary (+, -, *, /, %) and a single unary operator (-). Shortcut arithmetic operators (++, --), although common in other programming languages, are not available in Dafny.

Arithmetic Operator Replacement (AOR) [1, 6, 8, 9, 17–19, 27, 28, 39] replaces an arithmetic binary operator by another. However, in Dafny one cannot replace an arithmetic operator with / or % out-of-the-box, as the verifier requires a pre-condition stating that the divisor is not zero, to ensure a division by zero error does not occur. One approach adopted by some tools consists of restricting which operators can be replaced by which. In Dafny, this could reflect in allowing free replacement between the +, -, and * group of operators, and only allowing / to be replaced with % and vice-versa. Replacement of unary arithmetic operators cannot be applied in Dafny as it only supports one unary operator (-).

Arithmetic Operator Insertion (AOI) [17, 39] and *Arithmetic Operator Deletion (AOD)* [17, 19, 39], both self-explanatory, can only apply to unary operators. These can be applied to Dafny’s single unary operator (-) without any restriction.

3.3.2 Relational Operator Replacement (ROR) [1, 2, 6, 8, 9, 17–19, 27, 28, 39]. Dafny supports the six relational operators that are common to most languages (==, !=, <, <=, >, >=) and their replacement can be applied without any restriction. Additionally, the replacement of expressions using relational operators with just true or false is also implemented and possible in Dafny. Henceforth, we denote this as *Boolean-Binary Expression Replacement (BBR)* [39].

3.3.3 Conditional operators. Dafny supports three conditional operators: two binary (&&, ||) and one unary (!).

Conditional Operator Replacement (COR) [1, 2, 6, 8, 9, 18, 19, 27, 39] replaces a binary operator by its alternative. As in ROR, many tools replace conditionals with true or false, another use of BBR [1, 2, 6, 8, 9, 17, 27]

Conditional Operator Insertion (COI) [6, 8, 9, 19, 39] and *Conditional Operator Deletion (COD)* [6, 19, 39] can be both applied to Dafny’s single unary conditional operator (!).

3.3.4 Logical operators. Dafny’s binary logical bitwise operators are: &, |, and ^. Additionally, there is one unary operator, !, which returns the logical complement of a bit-vector type. While the ! operator is considered both conditional and logical, it is used in different contexts, one for boolean expressions and the other for bit-vectors, returning different types accordingly.

Logical Operator Replacement (LOR) [1, 6, 9, 17, 19, 27, 28, 39] can be applied to Dafny’s binary logical operators without restrictions, replacing them interchangeably. It cannot be applied to the unary operator as there is only one.

Logical Operator Insertion (LOI) [39] and *Logical Operator Deletion (LOD)* [6, 19, 39] can be applied to Dafny without restrictions, e.g., any bit-vector expression in Dafny can be modified by inserting or removing the ! operator.

3.3.5 Shift Operator Replacement (SOR) [1, 6, 9, 27, 28, 39]. Like *logical operators*, SOR operates over bit-vector types. Dafny supports the binary shift operators << and >>. Since

there are no unary shift operators, insertion or deletion cannot be applied.

3.3.6 Literal Value Replacement (LVR) [1, 6, 8, 9, 17–19, 27, 28]. This operator is traditionally applied to booleans, string literals, and numericals, with modifications that vary significantly between tools. The simplest case is the boolean: the only possible replacement is the logical complement, i.e., true with false and vice-versa. For string literals, common transformations include replacing non-empty with empty ones, replacing with default values, or inserting random characters in any position. Numerical literals are often incremented, decremented, negated, or replaced by pre-defined constants, e.g., 0, 1, and -1. *LVR* can be applied in Dafny without restriction, provided the original type is maintained.

3.3.7 Expression Value Replacement (EVR) [3, 6, 17]. Corresponds to the replacement of primitive-typed expressions (e.g., numerical or boolean) with literal values. Given the broad definition of what constitutes an expression in a program, mutation tools implement a wide range of expression value replacement operators. Some target any primitive-typed expression throughout the code, while others target specific contexts (e.g., return values) and perform more specific replacements (e.g., true, false, and null returns).

Method call replacement. Some tools replace method calls with a default value matching their return type. As these target return values, this operator only applies to non-void methods. In Dafny, methods may return multiple values, making the operation more complex. Due to this difference from the *EVR* operator, this will be treated as a distinct operator, *Method Return Value Replacement (MRR)* [17, 18].

A more specific method call replacement operator is the *Method Argument Propagation (MAP)* [7], which replaces a method call with one of its arguments. This must match the method's return type to preserve program validity.

Object initialization replacement. An example of this is the *Collection Initialization Replacement (CIR)* [8, 9] operator, which handles collection initialization with collection-specific construction syntax. Stryker.NET implements this to C# arrays, lists, collections, and dictionaries. Although lists and dictionaries are not available in Dafny or have different designations, this concept extends to its collection types (e.g., arrays, (multi)sets, sequences, and maps). On the other hand, in class instances, initialization through a constructor call can be replaced with null [17].

3.3.8 Loop constructs replacement. This operator targets loop-specific constructs, replacing break with continue and vice-versa. Additionally, replacing these types of statements with a return is also valid when the enclosing method is void. We refer to this as the *Loop Statement Replacement (LSR)* [1, 6, 19]. A related operator, *Loop Break Insertion (LBI)* [1], inserts a break at the start of the loop.

It is possible to apply these operators to Dafny programs, but their validity often depends on how the loop is structured. For instance, as in Dafny all loops must be proved to terminate, certain mutations (e.g., inserting a continue before a counter update) may prevent Dafny from verifying termination. As a result, these mutations can easily cause verification to fail simply due to the application context.

3.3.9 Case Block Replacement (CBR) [7]. This operator replaces bodies of case blocks in switch statements: the default case is replaced with the first non-default label body, and the remaining cases are replaced with the default body. Dafny's analogous construct is the match statement, where the default case is denoted by an underscore (_).

3.3.10 Statement Deletion (SDL) [1, 2, 9, 27, 39]. Like *EVR*, statement deletion operators can be categorized by context. The most general form deletes any statement type (return, break, assignments, calls, etc) without targeting a specific category. While applicable to Dafny, such deletions may lead to invalid programs (e.g., as with other languages, if a variable's initialization is removed but later used).

Block deletion. An extreme form of statement deletion is removing entire code blocks. In Dafny, this includes deleting method bodies [8, 9], entire if, else if, and else branches, or case blocks in match statements [1, 2]. Method bodies can only be deleted for void methods, and if branches only when no alternatives (i.e., no else) are present.

Method call deletion [7, 18]. Calls to void methods can be deleted without making the program invalid. Deleting non-void calls is not supported (in existing work or in MutDafny), as their return values are typically used elsewhere in the program (e.g., in assignments or expressions), and removing them would result in a syntactically incorrect program. Such cases are better handled by the *MRR* operator.

The *Method Naked Receiver (MNR)* [7] operator is a specific type of deletion operator for methods that are a member of a class. It deletes the method call while preserving the receiver object. To avoid type errors, the receiver must have the same type as the method's return value. This operator can be applied to non-void methods in Dafny.

Field initialization. Finally, there are two operators that initialize class fields with arbitrary values.

The first targets fields initialized at declaration [7]. Dafny does not provide specific default values for each type but ensures that variables of certain types, called *auto-initializable*, always hold legal values. While it ensures these values are legal, it does not define fixed defaults for each type, assigning arbitrary values. This feature does not work for user-defined classes, as they are not auto-initializable. Also, Dafny allows only constants to be initialized at declaration.

The second, implemented by MuJava [38, 40], deletes a class's constructor. Java automatically generates a default constructor that initializes fields with default values. Dafny also supports automatic constructor creation, but these are invoked without parentheses, e.g., new Car instead of new Car(). Applying this operator to a Dafny program would invalidate it, as constructor calls with parentheses would not be valid. An alternative is to delete the constructor body, allowing fields to remain initialized with arbitrary values.

3.3.11 Variable Deletion (VDL) [39]. This operator deletes all uses of a variable. If the variable is used in a binary expression, the corresponding operator must also be deleted.

Also, Python supports slicing as s[start:end:step], and MutPy [19] includes an operator that deletes one of the slice elements. Dafny has similar slicing for sequences, supporting start and end but not step. Since this operator

removes only part of a slice, unlike *VDL*, we refer to it as *Subsequence Limit Deletion (SLD)*.

3.3.12 Operator Deletion (ODL). Similar to the *VDL* operator, *ODL* deletes all occurrences of a specific operator (e.g., arithmetic, relational). For binary operators, program validity entails deleting one of the operands as well.

3.3.13 Object-Oriented operators. MuJava [38, 40] was the first tool to propose a comprehensive set of mutation operators targeting OO features like inheritance, polymorphism, and encapsulation. Some of these can be adapted to Dafny, which also supports OO features.

Polymorphic Reference Replacement (PRV) replaces an assignment to a parent class object with an instance of a different child class. It applies when the parent has multiple children and at least two variables of different child types are in scope. This may cause side effects if subclasses implement common methods differently or initialize fields differently. In the example below, each subclass sets a different value for `numSides`, so the mutation leads the program to output an incorrect value.

```
var shape: Shape;
var rectangle := new Rectangle(10.0, 20.0);
var triangle := new Triangle();
- shape := rectangle; // numSides = 4
+ shape := triangle; // numSides = 3
print shape.numSides, "\n";
```

This Keyword Insertion (THI) and *This Keyword Deletion (THD)*. These two operators manipulate the `this` keyword, one by inserting, the other by deleting it. These apply only when a class method has a parameter named like a class field. Neither can be used on the Left-Hand Side (LHS) of an assignment because Dafny does not allow assignments to parameters: inserting `this` there would require the LHS to be a parameter, which is no possible, and deleting it would leave a parameter on the LHS, invalidating the program.

Accessor Method Replacement (AMR) and *Modifier Method Replacement (MMR)* replace one method with another with the same signature. The first targets accessor methods, typically starting with `get`, which access class fields. The second targets modifier methods, usually starting with `set`, which update an object's state.

3.4 Mutation operators proposed for other languages excluded for Dafny

Most operators from other languages that cannot be applied to Dafny target syntax constructs that do not exist in the language, such as shortcut operators, compound assignments (e.g., `+=`), switch statements, exception-catching blocks, and method overloading. Others rely on language-specific elements like Python's `None`, Java's `BigInteger`, or libraries like C#'s Language Integrated Query (LINQ).

Some constructs exist in Dafny, but the mutations are invalid or generate equivalent mutants due to language constraints. Below, we highlight operators excluded for more complex reasons.

3.4.1 Operator replacement operators. Major's *Operator Replacement Unary (ORU)* [27, 28] cannot be applied to Dafny, as it replaces unary operators that do not necessarily belong

to the same group (e.g., Java's `-` and `~`). The unary operators supported in Dafny are `-`, for numeric types, and `!`, for booleans or bit-vectors, and cannot replace each other.

3.4.2 Expression replacement operators. Stryker.NET's *Initialization* [9] operator replaces a parameterized constructor with an empty one. This is not applicable in Dafny, which allows only one constructor per class.

StrykerJS's *Method Expression* [8] replaces JavaScript methods specific to strings, arrays, and math. Stryker.NET's *String Methods* [9], is similar, but for .NET string-related methods (e.g., `toUpperCase()` is replaced with `toLowerCase()`). These are not applicable in Dafny, since (i) Dafny provides limited built-in support for its types, and (ii) its strings are not objects and have no class methods.

3.4.3 Statement deletion operators. Mutmut's *Argument List Mutation* [6] deletes an element from a method's argument list. This is valid in Python due to optional arguments with default values. Dafny, however, requires a fixed number of arguments, making this operator inapplicable.

3.4.4 Object-Oriented operators. It is important to note that Dafny's classes are only allowed to extend traits, which can be viewed as abstract superclasses and cannot declare constructors or be instantiated. Methods and fields can both either be declared in the trait and used in its subclasses and methods, or at the subclass level.

Inheritance. MuJava's inheritance-related operators [38, 40] test three different aspects of this feature in Java: overriding methods, hiding variables, and the use of the `super` keyword, none of which are supported in Dafny.

Polymorphism. MuJava's polymorphism operators [38, 40] replace child types with parent types (and vice-versa) in various contexts, such as variable and parameter declarations and type casting. While some are possible in Dafny, resulting mutants are always equivalent to the original.

Since superclasses cannot be instantiated, object creation always uses subclass constructors. Thus, even when declared with a type of a superclass, Dafny knows the type of the object, using the correct values for its fields and the correct child-specific implementation for methods that are declared but not implemented in the parent.

In mutations that replace child with parent types, if child-specific methods or fields are used then it leads to invalid programs in Dafny. Otherwise, the mutant is equivalent.

The inverse, parent-to-child replacements via type casting, requires prior type checking — for instance, inside of an `if var is Type` block in which `Type` is the type `var` will be cast into. These type checking statements are unlikely to be present in most programs that do not already perform downcasting, thus these operators will almost always produce invalid programs.

In summary, child-parent type replacements in Dafny yield either invalid or equivalent mutants and, hence, are not useful. However, we can note that child-to-child replacement (Section 3.3.13) is a valid polymorphic mutation.

Static keyword. MuJava defines operators that insert or delete the `static` keyword from class fields [38, 40]. In Java, this operator is useful because the behavior of a class will differ depending on whether the updated fields are static. If

a field is made static by mistake, its update in one object will cause all of the other objects of the same class to wrongfully have the same field updated to the same value. The inverse can also generate unwanted side effects.

In Dafny, only constant fields can be static. While static fields are stored in memory shared among all class instances, their value remains unchanged. Thus, these operators always generate equivalent mutants in Dafny.

4 Novel mutation operators for Dafny

Mutation operators typically try to mimic errors commonly made by developers when writing a program and it has been shown that tailored mutants are well-coupled to real faults [10]. These may differ based on the features of each programming language. Although most of the mutation operators presented in Section 3 can be applied to Dafny programs, mimicking human errors in Dafny may require operators tailored for Dafny’s specificities. In this section, we analyze bugfixes in real Dafny programs and synthesize them into a novel set of mutation operators for Dafny, with the goal of complementing the answer to RQ1.

4.1 Methodology

To the best of our knowledge, no prior study has identified which errors commonly occur in Dafny programs. To study this, and inspired by Brown et al. [12]’s approach, we analyzed evidence of bugfixes in publicly available Dafny projects on GitHub. This analysis allowed us to extract new mutation operators tailored to Dafny, some of which are applicable to other languages. These operators aim to simulate realistic developer errors and strengthen the relevance of our mutation testing tool, MutDafny (described in Section 5).

4.1.1 Dafny programs’ repositories. DafnyBench⁶ [37] is currently the largest dataset of Dafny programs with 785 programs from 120 software repositories. Out of these, we noted that (a) there is no url, in DafnyBench’s paper, for four repositories⁷, (b) two were unavailable⁸, (c) three were repeated⁹, and (d) one was a subset of another¹⁰, resulting in the exclusion of 10 repositories. Additionally, we included the repositories for the AWS encryption SDK¹¹ and Dafny-EVM¹², which are recognized as key examples of Dafny programs in industry, leaving us with 112 repositories.¹³

⁶<https://github.com/sun-wendy/DafnyBench/tree/0cd28fe>, accessed Nov. 2025.

⁷BinarySearchTree, CO3408-Advanced-Software-Modelling-Assignment-2022-23-Part-2-A-Specification-Spectacular, Programmverifikation-und-synthese, and Prog-Fun-Solutions.

⁸<https://github.com/AoxueDing/Dafny-Projects> and <https://github.com/Aaryan-Patel-2001/703FinalProject>, accessed Nov. 2025.

⁹<https://github.com/Eggy115/Dafny>, <https://github.com/vladstejeroiu/Dafny-programs>, and <https://github.com/isobelm/formal-verification>, accessed Nov. 2025.

¹⁰<https://github.com/secure-foundations/iron-sync> ⊂ <https://github.com/secure-foundations/ironsync-osdi2023>, accessed Nov. 2025.

¹¹<https://github.com/aws/aws-encryption-sdk/tree/1be4d62>, accessed Nov. 2025.

¹²<https://github.com/Consensys/evm-dafny/tree/e2e52e8>, accessed Nov. 2025.

¹³The list of 112 repositories can be found at <https://github.com/MutDafny/mutdafny-study-data/blob/main/subjects/data/generated/repositories.csv>.

4.1.2 Bugfix commits. Evidence of programming errors in software repositories may manifest in bug reports (i.e., issues labeled *bug* on GitHub) or commit messages referring to fixes or corrections. Given 108 of the 112 repositories had no bug reports, our analysis focused on commit messages, covering a total of 12,308 commits. To identify potential bugfixes without complete manual inspection, and aiming to achieve replicability in identifying which commit messages hint at bugfixes, we selected commit messages using the `git log` command together with `grep`, and a set of keyword patterns: “fix”; “correct”, including other variations such as “correction”, “corrected”; “updat”, and variations like “update”, “updating”; and “chang”, including words like “change” and “changing”. This resulted in a total of 1,475 commits with messages hinting at possible bugfixes – some containing more than one of the listed patterns.

4.1.3 Procedure. Since our goal is to mutate implementations, changes involving specifications were disregarded. Each author of this study individually analyzed one-third (≈ 491) of the 1,475 commits¹⁴ and registered any changes that had the potential to be synthesized as mutation operators – e.g., modifications to expressions, altered conditions, added or removed lines of code – that could reflect common coding mistakes. We identified 270 (18.3%) commits as potential candidates. The authors then met to review each registered potential operator and discuss each collectively until a consensus was reached. Out of the 270, 148 were accepted and 123 were not (Section 4.3 describes some reasons why they were not accepted). The list of 1,475 commits and the outcome for each one can be found in `bugfixes.csv` of the *supplementary material*¹⁵. The list of operators synthesized from bugfixes together with the source commits is available in Chapter 2 of the *supplementary material*¹⁵.

4.2 Synthesized operators

Our bugfix analysis led to (i) the synthesis of 10 new mutation operators (nine that although were found in bugfixes of Dafny programs, could be applied to programs written in other programming languages; and one tailored for Dafny programs), and (ii) the extension of the previously proposed mutation operator *COR* to support Dafny specificities. We briefly describe the 11 mutation operators in the following subsections. For each operator, we provide the url to one example from the analyzed commits. For some operators, we provide a code example of the original and mutated version in diff format to complement their description.¹⁶ Next, we complete our answer to RQ1 by listing and describing these new mutation operators.

4.2.1 Conditional Operator Replacement (COR). Dafny supports the standard conditional operators (Section 3.3.3) && and ||, common to most traditional programming languages, as well as additional ones: ==> (implication), <==

¹⁴Given we aim to synthesize modifications, as mutation operators, that introduce mistakes to the code and not that fix the code, we analyzed the inverse of bugfix commits, i.e., bugfixes as bug-introducing.

¹⁵<https://doi.org/10.6084/m9.figshare.30640202.v1>

¹⁶Each diff applies the corresponding mutation operator to an existing code, i.e., introduces a *mistake*.

(reverse implication), and \Leftrightarrow (equivalence). We found evidence¹⁷ of replacements occurring between these operators in Dafny code. We have thus extended the previously defined conditional replacement operator to include them.

4.2.2 Expression replacement.

Evidence shows expressions, in particular identifiers, to be commonly swapped.

*Variable Expression Replacement (VER)*¹⁸ targets references to variables' names. The original variable's type should be considered when choosing a replacement, limiting it to variables of the same type in scope.

*Field Access Replacement (FAR)*¹⁹ replaces a class member access's field with another of the same class, preserving the object reference and typing, as in the following example:

```
class Item {
    var item: string
    var price: int
    var stock: int
}

method GetProfit(item: Item) returns (profit: int)
{
-   profit := item.price * item.stock;
+   profit := item.price * item.price;
}
```

*Method Call Replacement (MCR)*²⁰ and *Datatype Constructor Replacement (DCR)*²¹ work similarly to VER and FAR. MCR replaces one method (or function) call with another:

```
-   var n := Sum(10, 20); // return type int
+   var n := Multiply(10, 20); // return type int
```

The DCR operator replaces one datatype constructor call with another available from the same datatype:

```
datatype MyQuantifier = None | Some(x: set<int>) | All(y: set<int>)
method Main()
{
-   var selection := Some({1, 2, 3, 4});
+   var selection := All({1, 2, 3, 4});
```

Both operators retain the original arguments. To preserve program validity, replacements are limited to callable elements with matching signatures, i.e., same return types (for MCR) and the same number, types, and order of arguments.

*Method-Variable Replacement (MVR)*²² besides replacing variables with variables and methods with other methods, we also found evidence of method-to-variable replacements. In such cases, the replacement variable must match the return type of the target method to satisfy type constraints.

¹⁷<https://github.com/ConsenSys/evm-dafny/commit/4946bec#diff-5f537a3009d26ba61bcb2a3b39a3c4d0dbc32ff56fd177427b7e5a245dd6a3fl61-R61>, accessed Nov. 2025.

¹⁸<https://github.com/dafny-lang/Dafny-VMC/commit/27a6601#diff-9ead0207f306a1ba28e42076fd59fe8bb6802fa2faa5288b6e43bc42d95f3b9cL28-R28>, accessed Nov. 2025.

¹⁹<https://github.com/secure-foundations/ironsync-osdi2023/commit/9420f92#diff-8bf6e65b7c3a6ba702032935fb409c82b5a20dac0efcd4517966f82c1b980ee2L196-R196>, accessed Nov. 2025.

²⁰<https://github.com/aws/aws-encryption-sdk/commit/36d1fad#diff-d6402a5709ccca6c7b42036edacf38b136517d3b5d6206557decd0f8123522adL258-R258>, accessed Nov. 2025.

²¹<https://github.com/secure-foundations/ironsync-osdi2023/commit/1d7eabc#diff-dd4cf8cbf6aa5b5b44a285c7bec0890c1092315f2b6a3548b0bfa4ad4f28c2a0L666-R666>, accessed Nov. 2025.

²²<https://github.com/dafny-lang/Dafny-VMC/commit/ef3152c#diff-66dcba1192e097932aec9462cd8e65134fc25c93afca612894b2c94e64af5bL99-R99>, accessed Nov. 2025.

4.2.3 Argument Swapping (SAR). A common change involves swapping the arguments of a callable element²³, e.g., a method, a function, or a constructor. The corresponding mutation operator replicates this by swapping two arguments in the same call. The mutated program is only valid if the swapped arguments are of the same type.

4.2.4 Tuple Access Replacement (TAR). In Dafny, tuple elements can be accessed by their positional index (as in `tuple.0`)²⁴. This operator replaces a tuple index with another that refers to an element of the same type.

4.2.5 Conditional Block Extraction (CBE). In addition to deleting a branch of an `if` statement (see Section 3.3.10), our study found a common modification²⁵ where one branch's contents are extracted outside the `if`, and the remaining branches are deleted. Unlike the first operator, which preserves the `if` statement, this one replaces the `if` entirely with one branch's code block, as in the following:

```
-   if a <= 0 then
-     []
-   else
+   var b, c := a + a, a * a;
+   [a, b, c]
```

4.2.6 Statement Swapping (SWS). A common program fix involves swapping two or more lines of code²⁶, affecting logical flow and program behavior. While the concept is too broad to be fully translated into a mutation operator, due to the exponential mutant possibilities that would result from swapping every line and group of lines in a program, simpler operations can approximate it. We propose swapping a statement with the one directly above or below it.

4.2.7 Variable Declaration Swapping (SWV). Lastly, the SWV operator reflects another case related to the swapping of program constructs, but this time, applied to the declaration of variables in the same scope.²⁷

```
-   var perimeter := 2.0 * radius * 3.14;
-   var area := radius * radius * 3.14;
+   var perimeter := radius * radius * 3.14;
+   var area := 2.0 * radius * 3.14;
```

This operator is similar to VER, however, it affects the entire scope of the variable, unlike VER, which affects the single place where the variable is replaced.

4.3 Excluded modifications

Many commits contained modifications that, at first glance, seemed promising, especially to those unfamiliar with Dafny's syntax, but that were not included as mutation

²³<https://github.com/aws/aws-encryption-sdk/commit/b409ea5#diff-f945451ea4d5cc43ed01a97ffb7bfabf7fc17727818427f892b90a7ce2c04e7L55>

²⁴<https://github.com/aws/aws-encryption-sdk/commit/4c9d5d6#diff-00af0f655962fd28a7232ec2053eadda1257bb4587d838f9957a75c069e80437L64-R64>, accessed Nov. 2025.

²⁵<https://github.com/benreynwar/SiLemma/commit/4da22d6#diff-0eff5d0d272121340e6e9d6bad0e03612a3057426e284b56cd185a1524d7937aL572-R577>, accessed Nov. 2025.

²⁶<https://github.com/dafny-lang/libraries/commit/5ecd461#diff-3a16ac84e5bda345c586253ae5dbaa34730085d17a587393650195f5248eea80L46-R48>, accessed Nov. 2025.

²⁷<https://github.com/ConsenSys/evm-dafny/commit/58abe25#diff-eec5c501c95e783482e4062ad3c9c30e947c394e0388bc197ad2306a5840ea5L315-R316>, accessed Nov. 2025.

operators. We can highlight three groups of common modifications: (a) changes that alone do not alter program behavior, (b) changes inherent to migrations from Dafny 3 to Dafny 4, and (c) code improvements.

The first group includes, e.g., replacing types that have subset relationships (like `nat` with `int`) and type parameter property changes.^{28,29} The second relates to syntax changes introduced by Dafny 4 in how functions and callables are declared.³⁰ For example, functions were *ghost* by default (i.e., not compiled, only available for verification purposes), but now all functions compile unless declared as *ghost*. Finally, the last group includes common code improvement changes, e.g., the replacement of the declaration of a callable element as a method, function, predicate, or lemma, and the insertion or deletion of *ghost* keywords^{31,32}, which optimizes compilation by eliminating the need to compile certain elements, without affecting program behavior.

5 MutDafny

MutDafny is a tool integrated into the Dafny verification framework, implemented as a Dafny plugin. Dafny’s plugin architecture provides an extensible interface for Abstract Syntax Tree (AST) analysis and manipulation, allowing MutDafny to integrate directly with Dafny’s execution flow without modifying its source code. MutDafny works at the level between the parser and verifier and consists of a two-phase pipeline: *mutant generation* and *mutation analysis*. Figure 1 illustrates the overall pipeline.

Mutation operators. MutDafny supports 32 mutation operators³³. We identify three groupings of operators described in Section 3 that behave similarly:

Binary Operator Replacement (BOR) \leftarrow *AOR, ROR, COR, LOR, and SOR*. *Unary Operator Insertion (UOI)* \leftarrow *AOI, COI, and LOI*. *Unary Operator Deletion (UOD)* \leftarrow *AOD, COD, and LOD*. Furthermore, MutDafny includes the 10 new ones described in Section 4, and the remaining 19 described in Section 3.

Mutant generation. Operates by directly manipulating Dafny’s internal representation. A *scanner* component traverses the AST to identify *mutation targets* – i.e., specific locations in the program where specific types of mutations can be applied – and collects the necessary context for performing those mutations. For instance, for each target, MutDafny records the node’s position, the type of mutation operator to be used, and any additional arguments required to apply the mutation. The *mutator* component takes each of the identified mutation targets and changes the program’s

²⁸<https://github.com/secure-foundations/ironsync-osdi2023/commit/e27b26c#diff-7091ca089a282c06587ac4406db89d238ea977e5e47b93c290d769c1221f2be3L14-R14>, accessed Nov. 2025.

²⁹<https://dafny.org/dafny/DafnyRef/DafnyRef.html#sec-type-characteristics>, accessed Nov. 2025.

³⁰<https://github.com/namin/dafny-sandbox/commit/21e148e#diff-4698b1118ee26951776954c2d28642a7dc6ad3abb38743d0034655ffd302364L112-R112>, accessed Nov. 2025.

³¹<https://github.com/secure-foundations/ironsync-osdi2023/commit/0da7158>, accessed Nov. 2025.

³²<https://github.com/secure-foundations/ironsync-osdi2023/commit/de87232#diff-10aacdf18deb66491a2e4bb876eaeff2e7979b41d427563229817337b5302753L412-R420>, accessed Nov. 2025.

³³The full list of operators implemented in MutDafny can be consulted in Chapter 3 of the supplementary material at <https://doi.org/10.6084/m9.figshare.30640202.v1>.

AST to create individual mutants, which are inserted prior to Dafny’s resolution phase. This is done by traversing the AST until the target’s location, i.e., the node to mutate, is reached, and then performing the necessary operations on it. The changes can involve altering a node’s data, replacing an expression or statement with a different one by creating a new node (e.g., the replacement of a relational or conditional binary expression with `true` or `false` (*BBR*) involves the replacement of a binary expression with a literal), or deleting nodes by removing their reference from the parent.

For certain mutation operators, identifying mutation targets involves analyzing the target node’s type information, which is only available post-resolution. This is the case, for example, of the *UOI* operator, which consists of inserting a minus (`-`) in numerical expressions, or negation (`!`) in boolean expressions. Here, to know whether a tree node constitutes a valid mutation target, we must first know its type. As a result, and as depicted in Figure 1, a portion of the targets are identified during a pre-resolve tree visit, and the remaining are identified during a final post-resolve one.

Mutation analysis. The generated mutants are evaluated using Dafny’s verification capabilities and the specification under test. Mutants are classified according to the verification outcome: *Alive (survived)*: the mutant verifies successfully against the original spec, hinting at a potential specification weakness; *Killed*: the mutant fails verification, meaning that the spec successfully detected the inserted fault; *Invalid*: the mutant fails during Dafny’s resolution process (before verification), indicating a semantically incorrect program; *Timed Out*: the verifier could not determine an outcome within a set time limit.³⁴

6 Empirical Evaluation

In this section, we describe and discuss the results of our empirical evaluation, which aims to answer the following research questions:

RQ2: Are mutation operators for Dafny programs helpful in the identification of specification weaknesses?

RQ3: How effective are the different mutation operators?

RQ4: How efficient is MutDafny at generating mutants?

6.1 Experimental procedure

The empirical evaluation of MutDafny was conducted on a dataset with 43,178 lines of code consisting of 743 Dafny files³⁵ from DafnyBench [37], 17 from AWS encryption SDK and 34 from Dafny-EVM. DafnyBench includes 785 files, but 42 of these were unverifiable with our environment. We excluded any files that (a) had validity errors with our Dafny/Z3 version, (b) timed out, (c) had verification errors, and (d) verified nothing at all (e.g., Dafny program verifier finished with 0 verified, 0 errors).³⁶

³⁴By default, Dafny’s verifier runs for 20 seconds.

³⁵In this paper, we consider a Dafny *file*, .dny, as a Dafny *program* (as defined in DafnyBench [37]), and we may use the terms *file* or *program* interchangeably, in which case we imply the former.

³⁶Examples of excluded files: (a) *groupTheory_tmp_tmppmmxvu8h_assignment1*; (b) *Wrappedether*; (c) *Clover_insert*; and (d) *DafnyExercises_tmp_tmppd6qyevja_QuickExercises_testing2*. The full list of files and

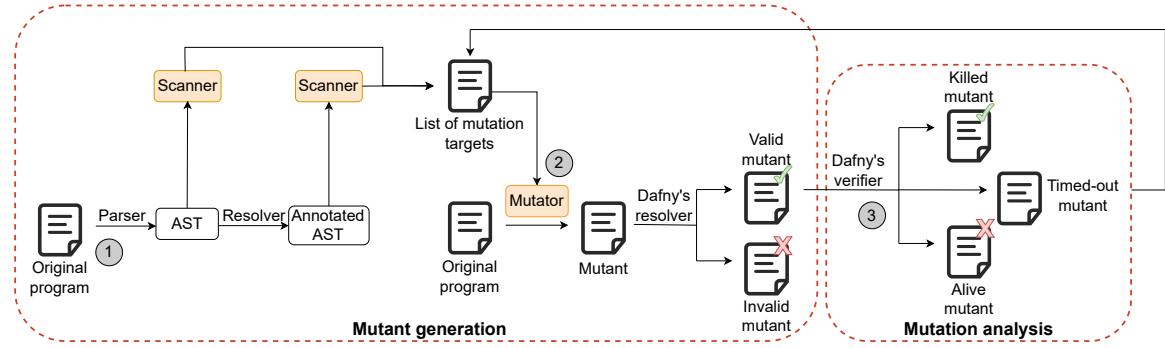


Figure 1: Mutation testing pipeline with MutDafny. MutDafny’s components are depicted by the filled boxes, the rest corresponding to Dafny.

The 794 program files that constitute our experimental subjects gather a total of 2,747 methods, functions, and similar constructs: 1,668 of these have no pre-conditions, 1,403 no post-conditions, and 1,044 have neither. This does not necessarily imply that the spec is *weak*. In fact, it is common for functions and predicates to omit such contracts. However, when these are invoked within methods that *do* have specs, mutations affecting them can still contribute to measuring the quality of the overall program’s specification.

Our experimental procedure consists of running MutDafny against the 794 files. To measure the performance of each mutation operator individually, we perform mutation testing by applying each of our operators individually in successive iterations. This requires, for each program, 32 runs of the scanner (one for each operator) and 32 rounds of invoking the mutator on the identified mutation targets. This phased approach has no impact on the generated mutants, but 32 partial scans differ from a single full one as each scan traverses the AST. To achieve faithful results for runtime with all operators enabled, we also perform a default scan that collects all targets in one execution. Moreover, to accelerate the experiment runtime, we parallelized some workflow components. For the scanner, each job involves scanning a single program for mutation targets using a single mutation operator, while for the mutator, each job entails generating mutants for a single program.

We executed each experiment (i.e., a mutation operator on a file) 10 times. We then removed 20% of the repetitions with the highest and the lowest runtimes.

The experimental procedure was run on a cluster running Ubuntu 20.04 operating system, Linux kernel version 5.15, with 1GB of RAM, and an Intel(R) E5-2450 CPU at 2.1GHz. We use the version of Dafny 4.10.0 corresponding to commit hash 7159879³⁷ and Z3 v4.12.6.

6.2 Experimental metrics

The dataset resulting from running this experiment includes all generated mutants, runtime measurements and mutation target data for all file scans, and runtime measurements for generated mutants, alongside data identifying the applied mutation and its analysis status. For each execution,

³⁷the reason why each one did not verify can be found in Chapter 4 of the supplementary material at <https://doi.org/10.6084/m9.figshare.3064020.v1>.

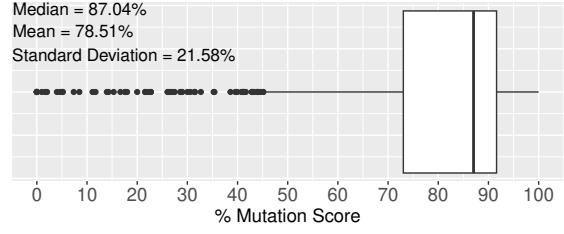


Figure 2: Mutation score distribution.

we record the total runtime of each scan/mutation process and the time spent in each of Dafny’s workflow stages and executing the plugin. This data allows us to compute the mutant generation, mutation analysis, and total runtime.

Additionally, we compute the *mutation score* [26], i.e., the ratio of killed mutants to the total number of mutants, excluding invalid mutants, e.g., that introduce non-compiling changes, and time-out ones, which reflect an inconclusive result. This metric reflects the fault detection capability, typically of the test suite, and, in the context of this work, of the specifications. A higher mutation score increases confidence in the test suite/specification.

6.3 Experimental results

Overall, **MutDafny generated a total of 112,810 mutants** across our dataset of 794 programs, an average of 2.6 mutants per line of code.

6.3.1 Answer to RQ2. We compute the mutation score of each program in the dataset, illustrated in Figure 2. On average, the dataset’s **specifications are able to kill 79% of the mutants**. The middle 50% scores range from 73% to 92% with a standard deviation of 22%, indicating a concentration of high mutation scores. These results show that Dafny specifications present high mutant detection capability, but even a single alive mutant may be enough to reveal a weakness.

From the 31,515 surviving mutants, 13,156 affect methods with post-conditions. The remaining 18,359 can be weak due to the lack of a specification in the mutated component, a hint at a weakness in a component calling the mutated one, or be equivalent to the original program. Being unfeasible to manually analyze 13,156 mutants to assess if they survived due to a weak specification or equivalence to the original program, we focused on 24 randomly selected files, manually

analyzing all their 284 surviving mutants in methods with post-conditions. This took eight hours of one person’s effort (≈ 1.7 minutes per mutant), with the files averaging 50.2 lines-of-code (1,205 total) and 3.3 functions (79 total).

In these 24 files, we found five specification weaknesses^{38,39,40,41,42} in five programs from two different projects, one⁴¹ corresponding to the motivational example presented in Section 1. The repository of one of the weak specs³⁸ became unavailable, so we could not contact its developers. The remaining programs were generated by LLMs for a study [45], and a manual inspection led Misu et al. [45] to report one of the weaknesses³⁹ (providing us confirmation). We contacted them for reporting the remaining three that went unnoticed and, while Misu et al. acknowledged our discoveries, it was also pointed out that two of the weaknesses^{40,41} had previously been detected by Endres et al. [20], the third one⁴² being a new discovery.

In the case of bst4copy³⁸, the `insert` method ensures that the output tree is a valid binary search tree, but there is no condition asserting that the insertion of the input value indeed occurred. Similarly, the `insertRecursion` method checks the relation between the tree’s lowest and highest value and the value to be inserted, but does not check if the latter is present in the output tree. If no modification is made to the input tree, neither method’s specification would be able to detect the incorrect behavior. In `task_id_126`³⁹, the postcondition states that every divisor common to two input numbers is lower than their sum. However, if an incorrect implementation caused only some of the common divisors to be added to the sum, this single postcondition would not be able to detect it. The purpose of `task_id_161`⁴⁰ is to return every unique element present in the first input array but not in the second. While the specification states that every element in the result is in the first array but not in the second, it does not enforce that every element in the first array that is not present in the second must be a part of the result, making empty lists a valid output. `task_id_2`⁴¹ and `task_id_249`⁴² are very similar to `task_id_161`, the goal being to compute the unique elements common to two input arrays, and the weakness being the same. All of these weaknesses miss a crucial guarantee.

From the 284 analyzed mutants, 77 hinted at these weaknesses and were successfully killed upon strengthening the specifications; 157 turned out to be equivalent to the original program, and we could not draw meaningful conclusions from the remaining 50. The number of equivalent mutants, alongside the time to perform manual verification of the surviving mutants, is an evident challenge. In practice, we

³⁸https://github.com/sun-wendy/DafnyBench/blob/main/DafnyBench/dataset/ground_truth/BinarySearchTree_tmp_tmp_bn2twp5_bst4copy.dfy#L58, accessed Nov. 2025.

³⁹https://github.com/sun-wendy/DafnyBench/blob/main/DafnyBench/dataset/ground_truth/dafny-synthesis_task_id_126.dfy#L1, accessed Nov. 2025.

⁴⁰https://github.com/sun-wendy/DafnyBench/blob/main/DafnyBench/dataset/ground_truth/dafny-synthesis_task_id_161.dfy#L7, accessed Nov. 2025.

⁴¹https://github.com/sun-wendy/DafnyBench/blob/main/DafnyBench/dataset/ground_truth/dafny-synthesis_task_id_2.dfy#L7, accessed Nov. 2025.

⁴²https://github.com/sun-wendy/DafnyBench/blob/main/DafnyBench/dataset/ground_truth/dafny-synthesis_task_id_249.dfy#L7, accessed Nov. 2025.

Table 1: Number of generated, killed, survived, invalid, and timeout mutants.

Op.	# Mut	# Killed	# Survived	# Invalid	# Timeout
AMR	0	0 (0.00%)	0 (0.00%)	0 (0.00%)	0 (0.00%)
BBR	5,762	3,729 (64.72%)	1,866 (32.38%)	153 (2.66%)	14 (0.24%)
BOR	20,381	13,465 (66.07%)	5,222 (25.62%)	1,592 (7.81%)	102 (0.50%)
CBE	1,817	1,177 (64.78%)	619 (34.07%)	15 (0.83%)	6 (0.33%)
CBR	369	3 (0.81%)	364 (98.64%)	2 (0.54%)	0 (0.00%)
CIR	936	654 (69.87%)	242 (25.85%)	40 (4.27%)	0 (0.00%)
DCR	415	243 (58.55%)	112 (26.99%)	58 (13.98%)	2 (0.48%)
EVR	13,992	10,081 (72.05%)	3,289 (23.51%)	560 (4.00%)	62 (0.44%)
FAR	93	60 (64.52%)	26 (27.96%)	7 (7.53%)	0 (0.00%)
LBI	738	621 (84.15%)	115 (15.58%)	1 (0.14%)	1 (0.14%)
LSR	54	30 (55.56%)	24 (44.44%)	0 (0.00%)	0 (0.00%)
LVR	13,409	9,217 (68.74%)	4,093 (30.52%)	66 (0.49%)	33 (0.25%)
MAP	649	222 (34.21%)	158 (24.35%)	266 (40.99%)	3 (0.46%)
MCR	504	111 (22.02%)	357 (70.83%)	35 (6.94%)	1 (0.20%)
MMR	20	10 (50.00%)	10 (50.00%)	0 (0.00%)	0 (0.00%)
MNR	253	1 (0.40%)	114 (45.06%)	136 (53.75%)	2 (0.79%)
MRR	854	385 (45.08%)	380 (44.50%)	88 (10.30%)	1 (0.12%)
MVR	2,060	439 (21.31%)	1,595 (77.43%)	13 (0.63%)	13 (0.63%)
ODL	4,666	1,345 (28.83%)	1,712 (36.69%)	1,601 (34.31%)	8 (0.17%)
PRV	0	0 (0.00%)	0 (0.00%)	0 (0.00%)	0 (0.00%)
SAR	923	458 (49.62%)	400 (43.34%)	60 (6.50%)	5 (0.54%)
SDL	6,052	3,328 (54.99%)	1,304 (21.55%)	1,408 (23.27%)	12 (0.20%)
SLD	130	88 (67.69%)	41 (31.54%)	0 (0.00%)	1 (0.77%)
SWS	3,782	1,266 (33.47%)	2,259 (59.73%)	242 (6.40%)	15 (0.40%)
SWV	400	188 (47.00%)	153 (38.25%)	59 (14.75%)	0 (0.00%)
TAR	16	8 (50.00%)	3 (18.75%)	5 (31.25%)	0 (0.00%)
THD	0	0 (0.00%)	0 (0.00%)	0 (0.00%)	0 (0.00%)
THI	8	5 (62.50%)	1 (12.50%)	2 (25.00%)	0 (0.00%)
UOD	331	264 (79.76%)	67 (20.24%)	0 (0.00%)	0 (0.00%)
UII	17,303	14,390 (83.16%)	2,589 (14.96%)	240 (1.39%)	84 (0.49%)
VDL	1,242	364 (29.31%)	609 (49.03%)	269 (21.66%)	0 (0.00%)
VER	15,651	9,649 (61.65%)	3,791 (24.22%)	2,101 (13.42%)	110 (0.70%)
Total	112,810	71,801 (63.65%)	31,515 (27.94%)	9,019 (7.99%)	475 (0.42%)

expect MutDafny to be used as a validation tool alongside development to incrementally validate new components, not entire projects at once. This will result in fewer mutants per iteration and shorten analysis time, making it feasible.

6.3.2 Answer to RQ3. Table 1 reports, for every mutation operator, how many of the mutants generated with it were killed, survived, invalid, or whose verification timed out. *BOR*, *UII*, *EVR*, *LVR*, and *VER* are responsible for the generation of the higher number of mutants, which is expected since they target common syntactic constructs: respectively, binary operators, expressions, and variables. On the other hand, *AMR*, *PRV*, and *THD* do not generate any mutants, and *THI*, *TAR*, *MMR*, *LSR*, and *FAR* generate a low number (less than 100 each). This happens because each of these operators can only be applied in very specific scenarios. For example, *THD* entails a program location where a class field is accessed using the `this` keyword inside a method whose argument has the same name as that field. *THI* entails the opposite.

As summarized in Table 2, the five specification weaknesses unveiled during our manual analysis resulted from mutants generated by nine of the existing and five of the newly proposed operators. *EVR*, *VER* (new), and *BOR* were the ones that generated the largest number of weakness-revealing mutants. These do not correspond to the operators that, out of the 32, generate the highest percentages of survivors; only around 25%. Instead, they generate more mutants overall, which suggests a correlation between a high mutant count and a greater likelihood of discovering weaknesses.

Table 2: The number of mutants generated by each mutation operator that led to the identification of weak specifications.

Op.	bst4copy ³⁸	task_id_126 ³⁹	task_id_161 ⁴⁰	task_id_2 ⁴¹	task_id_249 ⁴²	Total
EVR	1	5	4	1	4	15
VER	2	11	1	0	0	14
BOR	5	6	1	0	1	13
BBR	2	3	1	0	1	7
MAP	6	0	0	0	0	6
MVR	4	0	0	0	0	4
SDL	0	0	2	0	2	4
DCR	3	0	0	0	0	3
LBI	0	0	1	1	1	3
CBE	1	1	0	0	0	2
CIR	0	0	1	0	1	2
SWS	0	0	1	0	1	2
LVR	0	1	0	0	0	1
UOI	1	0	0	0	0	1
<i>Total</i>	25	27	12	2	11	77

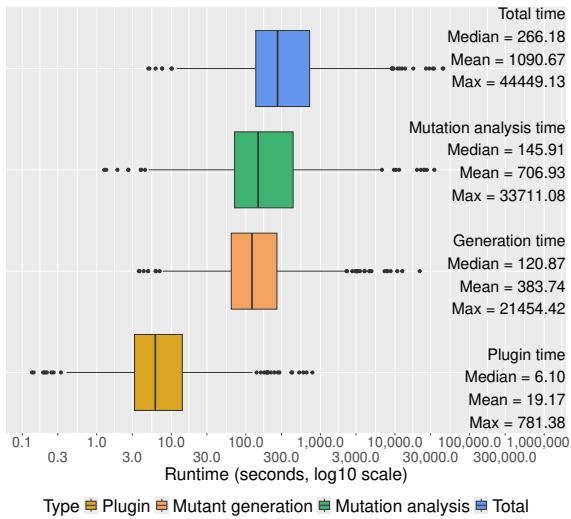


Figure 3: Plugin, mutant generation, mutation analysis, and total runtime to perform mutation testing of a Dafny file.

Regarding the relative effectiveness between the previously proposed and the novel mutation operators, the Wilcoxon test reports that programs’ specifications are statistically significantly ($p\text{-value} < 2.2 \times 10^{-16}$) more effective at killing mutants generated by the former than by the latter. These results further motivate one of our contributions, highlighting the need for mutation operators tailored for Dafny to more effectively evaluate Dafny specifications.

6.3.3 Answer to RQ4. Figure 3 shows the distribution of the runtime of the mutation testing process of each program. **The average total runtime is 18 minutes, with half of the experiments falling between two and 13 minutes.** These runtimes may be acceptable for the analysis of individual files, but can raise scalability concerns for multi-file projects. However, these issues can be mitigated through parallelization, as done in our experimental procedure.

The two phases of the mutation testing pipeline – generation and analysis – present similar average runtimes. Therefore, we conclude that the total runtime is approximately divided between mutant generation and verification.

While MutDafny usually takes one to five minutes to generate all the mutants for one file, this does not accurately reflect our implementation’s runtime. In half the files, the plugin scans and mutates the program in three to 15 seconds,

accounting for about 5% of the mutant generation runtime. The remaining time consists of mutant resolution, a regular part of Dafny’s execution but crucial for identifying invalid mutants. MutDafny’s efficiency is, thus, mainly affected by the resolution and verification of the mutated file.

6.4 Threats to validity

In this subsection, we discuss the threats to validity based on the guidelines defined by Wohlin et al. [53] and Yin [56].

Threats to construct validity. We identify two main constructs in our study: MutDafny’s integration with Dafny and specification effectiveness. Regarding the former, we define how the tool integrates into Dafny’s workflow, identifying the mutation and verification points. For the latter, we adopt the standard mutation score to evaluate specification effectiveness, clearly defining mutant statuses and detection criteria to align with established mutation measurements.

Threats to internal validity. The main threats we identify are CPU warm-up distortion and software bugs in MutDafny. The first was mitigated by running the experiment 10 times and removing outliers. Regarding software bugs, we employed testing and manually validated a subset of results. Our source code and experimental results are publicly available to support independent verification and reproducibility.

Threats to external validity. To support external validity, we rely on the representativeness of DafnyBench, which includes synthesized and real-world program files, the latter constituting 75% of the dataset and collected from GitHub with minimal filtering. Programs vary in complexity, some comprising introductory examples written by new learners of the language, thus with less relevance for rigorous assessment. Yet, all include specifications, allowing to evaluate their response to the tool. On the other hand, the files from AWS and Dafny-EVM are recognized as key industry examples. Nevertheless, the limited availability of high-quality open source Dafny repositories is still a notable challenge.

7 Future Work

It is crucial to ease the manual examination of the surviving mutants by minimizing the number of weakness hints that are either equivalent or false positives. As future work, we aim to investigate the application of code coverage of Dafny specifications to minimize the number of generated mutants [28], i.e., if a particular code portion is not covered by any existing specification in the program, then no mutant in it can ever be killed. In addition, we aim to explore automatic techniques to find and discard equivalent [24, 29, 31, 32, 47] or ineffective [44] mutants in the context of Dafny.

8 Conclusion

We presented a methodology for verification-aware languages and its implementation in a novel tool for detecting specification weaknesses through mutation of Dafny programs, benefiting from direct integration with the language’s workflow. Another key contribution of this paper is the systematic study of mutation operators suitable for Dafny, resulting in the synthesis of 22 operators based on a compilation of 30 unique ones previously proposed for other

programming languages, as well as 10 newly synthesized from collected evidence of real-world Dafny bugfixes.

Our empirical evaluation across 794 Dafny programs and 112,810 mutants demonstrated the value of MutDafny in detecting weaknesses. The results show that Dafny specifications have a high mutant detection capability. However, the analysis of a sample of alive mutants revealed five weaknesses in the benchmark programs. Despite the runtimes being highly conditioned by Dafny’s verification pipeline and the lengthy manual inspection of alive mutants, the tool can be feasibly applied in real-world settings. Ultimately, MutDafny has the potential to advance formal verification by aiding Dafny developers in improving system confidence.

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