CATHONANIE NUMERYCENE

$$I = \int_{0}^{6} f(x)dx = \sum_{i=0}^{n} w_{i}f_{i} \qquad (1)$$

$$f_{i} = f(x_{i})$$

f' = f(xi)

Metody moste

1. Metoda traperous

Wzor (1) ma daé dottrache wesigeanie

de f(x)=1; f(x)= x crylin=1

 $X_0 = \alpha$, $X_n = 6$

I = JAdx = X, - Xo = Wo + W,

 $I = \int_{-\infty}^{\infty} x_n dx = \frac{x_n^2 - x_0}{2} = W_0 x_0 + W_1 x_n$

Stad ways Wo=W,= Xn-Xo=h Sfaldx= = (fo+fn)+O(h2)

CN-3

2. Metoda Simpsona (parabal)

Wzor (1) ma dae' doktodne rowigzamic

dla
$$f(x) = 1, x, x^2, tutay' n = 2$$
 $x_0 = a, x_1, x_2 = 6$
 x_2
 $\begin{cases} 1 dx = x_2 - x_0 = w_0 + w_1 + w_2 \end{cases}$
 $\begin{cases} x_2 \\ x_3 \end{cases}$
 $\begin{cases} x_2 \\ x_4 \end{cases} = \begin{cases} x_2 - x_0^2 \\ x_2 \end{cases} = w_0 \times 0 + w_1 \times 1 + w_2 \times 2 \end{cases}$
 $\begin{cases} x_2 \\ x_3 \end{cases} = \begin{cases} x_2^2 - x_0^2 \\ x_3 \end{cases} = w_0 \times 0 + w_1 \times 1 + w_2 \times 2 \end{cases}$
 $\begin{cases} x_2 \\ x_3 \end{cases} = \begin{cases} x_3^2 - x_0^3 \\ x_3 \end{cases} = w_0 \times 0 + w_1 \times 1 + w_2 \times 2 \end{cases}$
 $\begin{cases} x_2 \\ x_3 \end{cases} = \begin{cases} x_3^2 - x_0^3 \\ x_3 \end{cases} = w_0 \times 0 + w_1 \times 1 + w_2 \times 2 \end{cases}$
 $\begin{cases} x_2 \\ x_3 \end{cases} = \begin{cases} x_3 - x_0^3 \\ x_3 \end{cases} = w_0 \times 0 + w_1 \times 1 + w_2 \times 2 \end{cases}$
 $\begin{cases} x_3 \\ x_3 \end{cases} = w_0 \times 0 + w_1 \times 1 + w_2 \times 2 \end{cases}$
 $\begin{cases} x_3 \\ x_3 \end{cases} = w_0 \times 0 + w_1 \times 1 + w_2 \times 2 \end{cases}$
 $\begin{cases} x_3 \\ x_3 \end{cases} = w_0 \times 0 + w_1 \times 1 + w_2 \times 2 \end{cases}$

 $\int_{0}^{x_{2}} f(x)dx = \frac{h}{3} \left(f_{0} + 4f_{1} + f_{2} \right) + O(h^{5})$

CN-3

3. Metoda Simpsona 3/8
Wror (1) ma dai dollatachy rognila olla $f(X) = 1, X, X^2, X^3; n = 3$

Wymik: x^3 $\int f(x)dx = \frac{3h}{8} (f_0 + 3f_1 + 3f_2 + f_3) + C(h^5)$

u. Metoda Boole'a

f(x)=1, x, x², x³, x⁴, u=4

Wymik: $\int f(x)dx = \frac{2h}{45} \left(7f_0 + 32f_0 + 12f_2 + 32f_3 + 7f_4 \right) + O(h^{\frac{7}{4}})$

1. Metoda Enleva McClaimina (visiona metoda traperda) (Calol = h (20 + fat + t fat + fat) + h (fo-fu) + - hy (for fright) -Metody visione

2. Metoda Simpsona

(f(x) dx = 2 (fo+4 f) + 2 f2 + 4 f + ... + 2 fu-2 + 4 funt fy)

3. Rosta analogicai e

CN-5

$$I_{a}(h) = \int_{a}^{b} g(x) dx, \quad 2 |ho| kiem h$$

$$I_{1}(h) = \int_{0}^{\infty} \int_{$$

$$I_{2}(h) = \frac{2^{2}I_{1}(\frac{h}{2}) - I_{1}(h)}{2^{2} - 1} + O(h^{2})$$

$$I_3(h) = \frac{2^{2\cdot 2}I_2(\frac{1}{2})-I_2(\frac{1}{2}h)}{2^{2\cdot 2}-1} + O(h^6)$$

$$T_{i+1}(h) = \frac{2^{2i}T_{i}(\frac{h}{2}) - I_{i}(\frac{h}{2})}{2^{2i}-1}$$

WYMORZYSTANIE METODY

CATROWANIA ROMBERGA

RZAD MEDU Nh Nh nh nh

I, (h)

 $I_1(2h)$ $I_2(h)$

 $I_{1}(4h)$ $I_{2}(2h)$ $I_{3}(h)$

I, (8h) I2 (4h) I3 (2h)

I, (164) I2 (84) I3 (84)

In (324) In (164) In (84)

OSZACOWANIE BEEDU W MET. TRANEZŚW

no pundet a

 $f(x)dx = \int \int \int (a) + (x-a) \int (a) + \frac{(x-a)^{2}}{2!} \int (a) + \frac{(x-a)^{2}}{3!} \int (a)^{2}$ (a) + ... /

 $(X-\alpha)^{n+2}$ $= h f(a) + \frac{h^2}{2!} f(a) + \frac{h^3}{3!} f''(a) + \frac{h^4}{4!} f'''(a) + \dots + \frac{h^4}{4!} f'''(a) + \dots$

 $(x-a)^n dx = ((x-a)^n d(x-a) =$ 24 7 1

 $\begin{cases} \frac{1}{3} \frac{$ (** **) = hf(6) - h2 f(6) + h3 f(6) - h4 m(6) + ... $(x-6)^{u+1}$ 1 (6) + (1) (1) - $\int_{-\infty}^{\infty} (x-6)^{n} dx = \int_{0}^{\infty} (x-6)^{n} d(x-6) = -$ (-h) + + in purther 6

N+7

 $\begin{cases} \int (x) dx = \frac{h^2}{2} \int \int (a) + \frac{h^2}{2^2} \int \int (a) - \int (b) dx + \frac{h^3}{2^2} \int \int (a) + \int (b) dx \\ \end{cases}$ $+\frac{h^{3}}{2.4i}\left[3(a)-f''(b)\right]+\frac{h^{5}}{2.5i}\left[3(a)+f''(b)\right]+...$ ho would f(x) woke't a $(x-a)^2 f''(a) + (x-a)^3 f''(a$ 161 = 8(a) + h 2 (a) + h 2 (a) + h 2 (a) + ... 3° doday showarm (x) to (x x), eles showy poetred price 2 costaw x=6

$$f'(x) = f'(b) + (x-b)f''(b) + \frac{(x-b)^2}{2!}f''(b) + \frac{(x-b)^3}{2!}f''(b) + \frac{(x-b)^3}{2!}f''(b) + \frac{(x-b)^3}{2!}f''(b) + \frac{(x-b)^3}{2!}f''(b) + \frac{(x-b)^3}{2!}f''(b) + \frac{h^2}{2!}f''(b) + \frac{h^2}{2!}f''($$

1"(a) + 3"(b) = 2 [8 (6)-8(a)] - 4 [8 (a)-9(b)] - ha [f' (a) + f' (b)] + ... 60 2 superian ua d'(6) i f'(a) serre

x [f (a) - f (b)] +... x (for ful) +. (8) (x) dx = h (30 + for + for + for + for) + hr (for - for) - Ly x 5 (K) dK = \frac{h}{\pi} \frac{f(a) + f(b)]}{\pi \pi} + \frac{h^2}{\pi \pi} \frac{h^2}{\pi \pi} \frac{h^2}{\pi \pi} \tag{60] - \frac{h^2}{\pi \pi} \tag{80} 30 2 p. 80 work ni metode Eulers-Mclauming 8° World dua ostature wyning do (+xx) 70 anabogiume voici' f''(X) wokest a; 6