U1P1_Version2 due 10/2/20

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Goals of computations:

- 1) Read in data
- 2) Manipulate data so that table is readable (with confidence intervals)
- 3) Create confidence intervals and add them to table
- 4) Perform log_lik test on three groupings of 9 weeks each of data from table

Making sure Rmd can knit

```
#1 # Reading in the data
```

```
mydata = read.csv("http://dept.stat.lsa.umich.edu/~bbh/s485/data/UMCovid_SPSU+4_2020.csv")
mydata
```

```
week_of tests positivity
## 1
      3/8/20
                36
                         0.194
                         0.125
## 2 3/15/20
               273
## 3 3/22/20
               179
                         0.223
## 4 3/29/20
               120
                         0.167
      4/5/20
                106
                         0.085
## 5
## 6 4/12/20
                86
                         0.047
## 7 4/19/20
                124
                         0.040
## 8 4/26/20
                131
                         0.008
      5/3/20
                         0.025
                163
## 10 5/10/20
                162
                         0.006
## 11 5/17/20
                159
                         0.019
## 12 5/24/20
                156
                         0.006
## 13 5/31/20
                204
                         0.005
## 14 6/7/20
                339
                         0.015
## 15 6/14/20
                431
                         0.049
```

```
## 16 6/21/20
                 348
                          0.029
## 17 6/28/20
                 398
                          0.025
      7/5/20
                 572
                          0.023
## 19 7/12/20
                 525
                          0.029
## 20 7/19/20
                 454
                          0.046
## 21 7/26/20
                 664
                          0.035
## 22 8/2/20
                          0.018
                 871
## 23
       8/9/20
                 865
                          0.010
## 24 8/16/20
                 853
                          0.012
## 25 8/23/20
                1497
                          0.025
## 26 8/30/20
               1717
                          0.011
## 27
      9/6/20
               2240
                          0.019
## 28 9/13/20
                3687
                          0.013
## 29 9/20/20
               3387
                          0.017
## 30 9/27/20
                          0.143
```

#2 Manipulating data

Next I must create a third numerical variable in mydata for the number of Covid-19 tests that came out positive. This value will be p_hat multiplied by n, or V2 multiplied by X

```
mydata$X_positive <- mydata$tests*mydata$positivity
mydata</pre>
```

```
##
      week_of tests positivity X_positive
## 1
       3/8/20
                  36
                           0.194
                                      6.984
## 2
      3/15/20
                 273
                           0.125
                                      34.125
## 3
      3/22/20
                 179
                           0.223
                                     39.917
## 4
      3/29/20
                 120
                           0.167
                                     20.040
       4/5/20
## 5
                 106
                           0.085
                                      9.010
## 6
      4/12/20
                  86
                           0.047
                                      4.042
## 7
                                      4.960
      4/19/20
                 124
                           0.040
## 8
      4/26/20
                           0.008
                                      1.048
                 131
## 9
       5/3/20
                 163
                           0.025
                                      4.075
## 10 5/10/20
                 162
                           0.006
                                      0.972
## 11 5/17/20
                 159
                           0.019
                                      3.021
## 12 5/24/20
                 156
                           0.006
                                      0.936
## 13 5/31/20
                 204
                           0.005
                                      1.020
## 14 6/7/20
                 339
                           0.015
                                      5.085
## 15 6/14/20
                 431
                           0.049
                                      21.119
## 16 6/21/20
                 348
                           0.029
                                     10.092
## 17 6/28/20
                 398
                           0.025
                                      9.950
## 18
      7/5/20
                 572
                           0.023
                                     13.156
## 19 7/12/20
                 525
                           0.029
                                     15.225
## 20 7/19/20
                                     20.884
                 454
                           0.046
## 21 7/26/20
                 664
                           0.035
                                     23.240
## 22 8/2/20
                 871
                           0.018
                                     15.678
## 23 8/9/20
                 865
                           0.010
                                      8.650
## 24 8/16/20
                           0.012
                                     10.236
                 853
```

```
## 25 8/23/20 1497
                      0.025
                                37.425
## 26 8/30/20 1717
                      0.011
                               18.887
## 27 9/6/20 2240
                      0.019
                               42.560
## 28 9/13/20 3687
                      0.013
                               47.931
## 29 9/20/20 3387
                      0.017
                               57.579
## 30 9/27/20 7
                      0.143
                               1.001
```

Creating Confidence Intervals -> Agresti - Coull

```
#lower bound
lower <- function(X, n){</pre>
    k <- qnorm(0.975)
    X_{tilda} \leftarrow X + k^2/2
    n_{tilda} < n + k^2
    p_tilda <- X_tilda/n_tilda</pre>
    q_tilda <- 1 - p_tilda
 p_tilda - k*sqrt(p_tilda * q_tilda)*n_tilda^(-1/2)
#Finding lower bound and adding to table
mydata$lower.bound <- round(lower(mydata$X_positive, mydata$tests), digits = 3)</pre>
#upper bound
upper <- function(X, n){</pre>
    k < -qnorm(0.975)
    X_{tilda} \leftarrow X + k^2/2
    n_{tilda} \leftarrow n + k^2
    p_tilda <- X_tilda/n_tilda</pre>
    q_tilda <- 1 - p_tilda
 p_tilda + k*sqrt(p_tilda * q_tilda)*n_tilda^(-1/2)
#Finding upper bound and adding to table
mydata$upper.bound <- round(upper(mydata$X_positive, mydata$tests), digits = 3)</pre>
```

Log-Likelihood Computations:

```
#First I must divide up the data into three periods, so I will have 3 periods each of length 9
#I must then take the mean of each period's test-positivity

#########
#Period 1
########
p_First_9 <- mean(mydata$positivity[1:9])
#For the number of tests taken in period 1
sum(mydata$tests[1:9])</pre>
```

```
## [1] 1218
First_9_weeks <- (mean(mydata$positivity[1:9]) * sum(mydata$tests[1:9]))</pre>
First_9_weeks <- round(First_9_weeks)</pre>
########
#Period 2
########
p_Middle_9 <- mean(mydata$positivity[10:18])</pre>
sum(mydata$tests[10:18])
## [1] 2769
Middle_9_weeks<- (mean(mydata$positivity[10:18]) * sum(mydata$tests[10:18]))
Middle_9_weeks <- round(Middle_9_weeks)</pre>
#########
#Period 3
#######
p_Last_9<- mean(mydata$positivity[19:27])</pre>
sum(mydata$tests[19:27])
## [1] 9686
Last_9_weeks <- (mean(mydata$positivity[19:27]) * sum(mydata$tests[19:27]))
Last_9_weeks <- round(Last_9_weeks)</pre>
#Now, I can consider taking the likelihood estimates of the underlying probabilities of each period
\# I must also then compare H_0 and H_a
H_0: p_First_9 = p_Middle_9 = p_Last_9
H_A: p_First_9 > p_Middle_9 > p_Last_9
p_First_9
## [1] 0.1015556
p Middle 9
## [1] 0.01966667
p_Last_9
## [1] 0.02277778
# Log-likelihood function
###############################
n_1 = c(sum(mydata$tests[1:9]),sum(mydata$tests[10:18]), sum(mydata$tests[19:27]))
```

p_u = c(p_First_9, p_Middle_9, p_Last_9)

```
log_lik = function(p) {
   sum(dbinom(round(n_1*p_u), size=n_1, prob=p, log=T))
}
var = 2*(log_lik(p_u) - log_lik(sum(round(n_1*p_u))/sum(n_1)))
pchisq(var, 2, lower=F)
```

Likelhood Ratio Test and the overall positivity rate

[1] 1.443793e-36

```
overall_test_positivity <- c(p_First_9, p_Middle_9, p_Last_9)
mean_overall_test_positivity <- mean(overall_test_positivity)

log_lik(mean_overall_test_positivity)

## [1] -153.5796

var_2 = 2*(log_lik(mean_overall_test_positivity) - log_lik(sum(round(n_1*p_u))/sum(n_1)))
pchisq(var_2, 2, lower=F)

## [1] 1</pre>
```