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#### Problems to be solved

#### Classification

- assign samples to predefined classes
- [photo of an animal -> species]
- [text -> author]
- [scan-path -> novice/expert]

#### Regression

- calculate a value for each sample
- [images of the house -> price of the house]
- [eye image -> gaze coordinates]

#### Conversion

- convert object into another object
- [image -> text description of the image]
- [voice recording -> text of the speech]







#### Task and method

- Task: find a function Y = f(X) where
  - X sample (input)
  - Y result class, value (output) label
- Method (learning by example):
  - take some number of samples X with known output Y (examples, labeled samples)
  - build the function based on these examples (learning process)
  - use the function to predict the label for unknown samples





# Problem of "generality"

- It is relatively easy to create a function that correctly classifies all examples
- But is this function "general" enough?
  - is it able to correctly classify unknown samples?
- The answer is not trivial and that is why we have a lot of different classification methods
- "No free lunch" theorem





### Over-fitting

- If the function (model) is optimized for the given data (given examples) it may have poor generality
- This problem is called over-fitting
- Solution is to simplify the model, e.g. stop learning even when it is not perfect for examples





# The simplest algorithms

- K-Nearest Neighbors (kNN)
  - a new sample is classified as majority of its K nearest neighboring examples
- Linear Discriminant Analysis (LDA)
  - finds a linear equation separating positive and negative samples
- Naive Bayes
  - the class of a new sample is calculated based on examples using Bayes equation
- Decision Tree
  - the tree is built using examples by seaching for the most discriminative features
  - new samples are going through the tree reaching a leaf with the predicted class







### More sophisticated algorithms

- Random Forest
  - a set of randomly generated decision trees voting for the final results
- Support Vector Machines (SVM)
  - recalculates examples into another space where they are easier to separate lineary (kernel trick)
- Neural Networks
  - based on neurons organized into layers





### Hyperparameters

- Classification algorithms have parameters
  - (so called hyperparameters)
- kNN number of neighbors
- Random Forest number of trees
- SVM kernel function, parameters of the function, learning rate etc.
- Good choice of hyper parameters influences the quality of the model!
- Bad news: deep learning methods have A LOT hyper parameters





#### Scikit-learn

- Package implementing:
  - many popular classification algorithms
  - many classic methods for data handling
- General use:
  - load the dataset consisting of samples and their labels
  - create a model using one of the possible algorithms (classes)
  - train the model: model.fit(samples, labels)
  - use the model to predict classes:
    - predicted = model.predict(sample)





# Universal example







### Creating a model

```
def classification(model_name,samples,labels,rangex,rangey):
models = {
    "KNN": KNeighborsClassifier(),
    "LDA": LinearDiscriminantAnalysis(),
    "NB": GaussianNB(),
    "TREE":DecisionTreeClassifier(),
    "RF":RandomForestClassifier(n estimators=20),
    "SVM":SVC(gamma='scale'),
    "PERC":Perceptron(max iter=2000),
    "GB":GradientBoostingClassifier()
model = models.get(model_name)
```







# Using the model

```
samples = np.array(samples)
labels = np.array(labels)
model.fit(samples, labels)
# build the matrix of results using the model
result = np.zeros([rangex,rangey])
for x in range(rangex):
  for y in range(rangey):
      sample = np.array([x,y])
      result[x][y] = model.predict(sample.reshape(1, -1))
return result
```





# Classification of a single sample

- result = model.predict(samples)
  - samples must have the dimension:
    - [number of samples, number of attributes]
  - For one sample: [1,2]
- Code version 1:
  - sample = np.array([x,y]) # dimension [2,]
  - result[x][y] = model.predict(sample.reshape(1, -1))
- Code version 2:
  - sample = np.array([[x,y]]) # double brackets dimension [1,2]
  - result[x][y] = model.predict(sample)







# Classification of all samples

- It is possible to classify all samples at once
- Create a list of points to classify:

```
samples = []
for x in range(rangex):
   for y in range(rangey):
      samples.append((x,y))
```

- A more pythonic way:
   samples = [(x,y) for x in range(rangex) for y in range(rangey)]
- Convert to numpy samples = np.array(samples)





# Classification of all samples at once

- Predictions for all pointsr = model.predict(samples)
- Create the array of results (shape: [rangex,rangey])
   result = np.zeros([rangex,rangey])
   for i in range(len(samples)):
   result[samples[i,0],samples[i,1]]=r[i]
- Is it possible to do it without the "for" loop?





### Example for the iris dataset

#### iris.ipynb

import pandas as pd from sklearn.neighbors import KNeighborsClassifier data = pd.read\_csv('iris.data')

model = KNeighborsClassifier()
samples = data.values[:,0:4] # first four columns
labels = data.values[:,4] # the fifth column
model.fit(samples, labels)
predicted = model.predict([(5.9, 3.0, 5.1, 1.8)])
print("predicted",predicted)

	sl	sw	рl	pw	iris
0	5.1	3.5	1.4	0.2	Iris-setosa
1	4.9	3.0	1.4	0.2	Iris-setosa
2	4.7	3.2	1.3	0.2	Iris-setosa
3	4.6	3.1	1.5	0.2	Iris-setosa
4	5.0	3.6	1.4	0.2	Iris-setosa



> predicted ['Iris-virginica']





### **Evaluating results**

- Hyperparameters may be tuned
  - it is important to be able to check if the model is general
- First rule: never check the model using the same data that you used for training (examples)
  - over-fitting!
- The dataset should always be divided into:
  - training set (used to build the model)
  - test set (to check how it works for unknown samples)





#### **Evaluation**

- Dividing into training set and test set may be not enough!
  - we optimize the model (by tuning hyper parameters) for the given test set
- The safest way:
  - training set (for learning)
  - validation set (for hyper parameters tuning)
  - test set (for final evaluation)
    - the "holdout" dataset





### Sklearn train\_test\_split

- (trainSamples, testSamples, trainLabels, testLabels) = sklearn.model\_selection.train\_test\_split(samples, labels)
   iris.ipynb / Train Test Split
- Two pairs:
  - trainSamples, trainLabels
  - testSamples, testLabels
- Default: 75% train, 25% test
- Parameters:
  - train\_size percent or number of samples
  - test\_size percent or number of samples





#### Stratification

- Problem: proportion of samples for classes may differ in training and test sets
- For instance: 50-50-50 in the original set
  - training: 40-30-25
  - test: 10-20-25
- Effect: class0 will be treated as more probable!
- Solution: stratified division (maintain distribution)
- Parameter: stratify=labels





### Check test samples

#### iris.ipynb / Check an error

Checking the test set

```
correct = 0;
predictedLabels = model.predict(testSamples)
for i in range(len(testSamples)):
  print(testLabels[i],"->",predictedLabels[i],end=' ')
  if(testLabels[i]==predictedLabels[i]):
    correct = correct + 1; print('OK')
  else:
    print('error!!!')
print("Correct: {} of {} accuracy = {:.2f}"
    .format(correct,len(testSamples),correct/len(testSamples)))
```





#### **Cross-validation**

- Dynamic division into training and test
  - the same examples are sometimes training and sometimes test samples
- 10-fold cross validation:
  - divide the whole dataset into 10 subsets
  - for each subset
    - train the model using the remaining 9 subsets
    - test the results using the chosen subset
  - average the results
- Folds are randomized but may be stratified
  - the same distribution of classes in each fold





### Sklearn cross\_validate

- iris.ipynb / Cross validation
  - sklearn.model\_selection.cross\_validate(model, samples, labels, cv=<number of folds>)
- Returns for each fold:
  - fit\_time
  - score\_time
  - test\_score
- Many parameters to check other metrics!





- Accuracy the number of correctly classified samples to all samples
  - a problem with unbalanced sets
  - if 90% of test samples is positive the blind classifier achieves
     90% accuracy
- Precision the cost of false positives
  - not belonging to class predicted as belonging
- Recall the cost of false negatives
  - belonging to class predicted as not belonging
- F1-Score combination of precision and recall
- Cohen's kappa compares prediction with random prediction







### Measures interpretation

- Example: We have built the model that diagnoses
   COVID-19 based on a genetic test
- For every eye movement sample the model returns:
  - H if a person is healthy
  - S when a person is sick
- We test the model using
  - 18 samples from sick people (S)
  - 82 samples from healthy people (H)
- We achieve 82% accuracy
  - is it bad or good?
  - it depends: we must examine a confusion matrix







#### **Confusion matrix**

Predicted as >> Real class	Н	S
Н	81	1
S	17	1

P	N
TP	FN
FP	TN

Accuracy 0.82

H:

precision: 0.83

recall: 0.99

F1-score: 0.90

S:

precision: 0.50

recall: 0.06

F1-score: 0.1







Predicted as >> Real class	Н	S
Н	80	2
S	15	3

P N
TP FN
FP TN

Accuracy 0.83

H:

precision: 0.84

recall: 0.98

F1-score: 0.90

S:

precision: 0.60

recall: 0.17

F1-score: 0.26







Predicted as >> Real class	Н	S
H	66	16
S	2	16

P	N
TP	FN
FP	TN

Accuracy 0.82

H:

precision: 0.97

recall: 0.80

F1-score: 0.88

S:

precision: 0.50

recall: 0.89

F1-score: 0.64







Predicted as >> Real class	Н	S
H	64	18
S	0	18

P	N
TP	FN
FP	TN

Accuracy 0.82

H:

precision: 1.00

recall: 0.78

F1-score: 0.88

S:

precision: 0.50

recall: 1.00

F1-score: 0.67







# Example for three classes

Confusion matr	rix			
[[24 3 9]				
[ 3 24 24]		11-1		
[ 2 15 49]]				1.44
class	precision	recall	f1-score	support
0	0.83	0.67	0.74	36
1	0.57	0.47	0.52	51
2	0.60	0.74	0.66	66
				SIF
micro avg	0.63	0.63	0.63	153
macro avg	0.67	0.63	0.64	153
weighted avg	0.64	0.63	0.63	153

Accuracy: 0.63







#### Scikit learn measures

- Useful functions from sklearn.metrics:
  - confusion\_matrix(labels, results)
  - classification\_report(labels, results)
  - accuracy\_score(labels, results)
  - precision\_score(labels, results)
  - recall\_score(labels, results)
  - cohen\_kappa\_score(labels, results)
  - **—** ...



#### Measures calculation

#### iris.ipynb / Measures calculation

from sklearn.metrics import classification\_report, confusion\_matrix, accuracy\_score,cohen\_kappa\_score

```
predictedLabels = model.predict(testSamples)
print(confusion_matrix(testLabels, predictedLabels))
print(classification_report(testLabels, predictedLabels))
accuracy = accuracy_score(testLabels, predictedLabels)
print("Accuracy: {:.2f}".format(accuracy))
c_kappa = cohen_kappa_score(testLabels, predictedLabels)
print("Cohen's Kappa: {:.2f}".format(c_kappa))
```







# Adding own scorers to cross validation

#### iris.ipynb / Adding own scorers to cross validation

from sklearn.metrics import make\_scorer, precision\_score, recall\_score

```
p_scorer = make_scorer(precision_score, average='micro')
r_scorer = make_scorer(recall_score, average='micro')
my_scorer = {'precision': p_scorer, 'recall': r_scorer}
```

```
sklearn.model_selection.cross_validate(model, samples, labels, cv=5, scoring=my_scorer)
```





### Summary

- Accuracy is often not enough
  - especially for unbalanced datasets
- Cohen's kappa is the reliable way to evaluate results
  - but has some drawbacks as well!
- The evaluation depends on the target we want to achieve
  - False Acceptance Rate (FAR=0)
    - no incorrectly classified healthy people
  - False Rejection Rate (FRR=0)
    - no incorrectly classified sick people







### Regression

- The model does not search for one of N classes but for a value
  - E.g. price of the house
- Examples:
  - Linear Regression
  - Support Vector Regression
  - Decision Tree Regression
  - Neural Network Regression





# Evaluation of regression

- Mean Absolute Error
- Mean Squared Error
  - penalizes predictions differing greatly (outliers)
- Root Mean Squared Error
  - comparable to real values
- Coefficient of Determination (R<sup>2</sup>)
  - value 0-1
  - negative value if worse than random







## Example: wine quality dataset

- Every wine has 11 numerical features
  - 1 fixed acidity
  - 2 volatile acidity
  - 3 citric acid
  - 4 residual sugar
  - 5 chlorides
  - 6 free sulfur dioxide
  - 7 total sulfur dioxide
  - 8 density
  - 9-pH
  - 10 sulphates
  - 11 alcohol
- The result: wine quality in 0-10 scale
- Dataset: 4898 wines







## Wine dataset analysis

## wine.ipynb

- Simple classification
- Train-test split
- Measures calculation confusion matrix
- Problem:
  - quality is an ordinal value not just a class
  - results should be calculated as a distance from the correct one
    - it is not bad when wine with quality 3 is classified as 4
    - it is a big problem when it is classified as 9







## Regression measures

#### • Errors:

from sklearn.metrics import mean\_squared\_error, r2\_score print('MSE=',mean\_squared\_error(testLabels, predictedLabels)) print('R2=',r2\_score(testLabels, predictedLabels))

#### Results:

- MSE = 0.99
- -R2 = -0.27



## Linear Regression

- Using Linear Regression:

   from sklearn import linear\_model
   model = linear\_model.LinearRegression()
   model.fit(trainSamples, trainLabels)
   predictedLabels = model.predict(testSamples)
- The result for each sample is a float!
- Errors:
  - MSE = 0.53
  - -R2 = 0.31





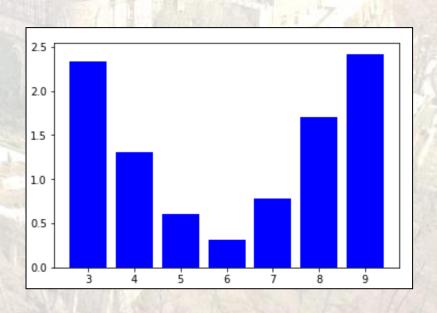
## Errors per class estimation

#### Mean errors per class

```
errors = np.abs(modelResults-testLabels)
for i in range(3,10):
    print('class',i,' avg error=',errors[np.where(testLabels==i)].mean())
```

#### Results

- class 3 avg error= 2.33
- class 4 avg error= 1.31
- class 5 avg error= 0.61
- class 6 avg error= 0.31
- class 7 avg error= 0.78
- class 8 avg error= 1.71
- class 9 avg error= 2.42







#### Problem: inbalanced classes

- Some qualities are rare, some are common
- Solution: Calculate weight for each class:

Using weights:

model.fit(trainSamples, trainLabels, <a href="mailto:sample\_weight=weights">sample\_weight=weights</a>)







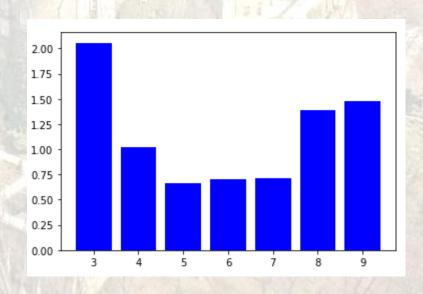
## Regression with weights

#### Mean errors per class

```
errors = np.abs(modelResults-testLabels)
for i in range(3,10):
    print('class',i,' avg error=',errors[np.where(testLabels==i)].mean())
```

#### Results

- class 3 avg error= 2.06
- class 4 avg error= 1.02
- class 5 avg error= 0.66
- class 6 avg error= 0.70
- class 7 avg error= 0.72
- class 8 avg error= 1.39
- class 9 avg error= 1.48







#### Results

- Distribution is more equal for the weighted model
- But the error is higher (both MSE and R2)
- Question:
  - what do we really need?
  - what is our objective?
- Possibilities:
  - minimize absolute error
  - minimize MSE/RMSE
  - minimize error for high quality wines
  - **—** ...







#### Feature selection

- Not every feature is valuable
  - adds some knowlegde about a class
  - e.g. bottle's color is *probably* not significant for wine quality
- Not important features may spoil classification!
- There are plethora of algoritms that aim at selecting only the relevant features from the dataset
  - topic for a new lecture (or even a new subject)
- Sklearn has a very convenient class to solve the problem





## SelectKBest

#### Code:

```
from sklearn.feature_selection.univariate_selection import SelectKBest
```

```
newSamples = SelectKBest(<algorithm>, k=<number>)
   .fit_transform(samples, labels)
```

#### Available algorithms:

(see: https://scikit-learn.org/stable/modules/generated/sklearn.feature\_selection.SelectKBest.html

```
f_classif, mutual_info_classif, chi2, f_regression,
    mutual_info_regression, SelectPercentile, SelectFpr,
    SelectFdr, SelectFwe, GenericUnivariateSelect
```







## Example

Select 5 best features using f\_regression algorithm:
 from sklearn.feature\_selection.univariate\_selection import SelectKBest
 print("Samples before",samples.shape)
 newSamples = SelectKBest(sklearn.feature\_selection.f\_regression,k=5)

.fit\_transform(samples, labels)
print("Samples after", newSamples.shape)
samples = newSamples

- Output:
  - Samples before (4898, 10)
  - Samples after (4898, 5)
- Task for you: check if it works better!

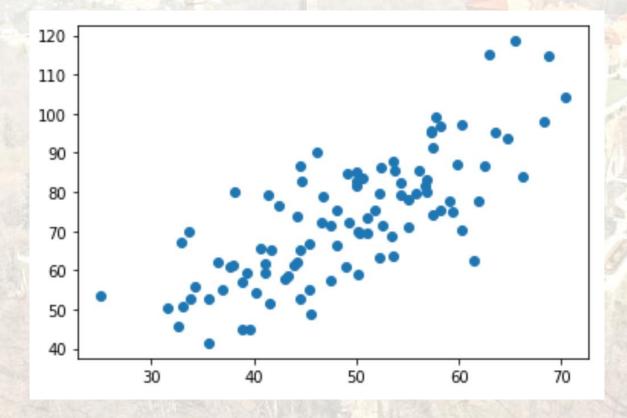






# Simple linear regression

Find the best linear approximation of points







## **Example: Linear Regression**

 Given a training set of pairs (X,Y) find coefficients of a linear function

$$y = a * x + b$$

Error (loss) function Mean Squared Error

$$E = \frac{1}{n} \sum_{i=1}^{n} (y_i - \hat{y}_i)^2 = \frac{1}{n} \sum_{i=1}^{n} (y_i - (ax_i + b))^2$$

Goal: minimize this function





# Linear Regression using Gradient Descent

Gradient Descent algorithm:

initialize randomly a and b repeat:

calculate error (loss)

change a and b in such way that error is smaller until error is small enough or it is not decreasing

Question: how to find the direction of change for a and b?



## **Gradient Descent**

Gradient dE/da – a function describing how E changes when a changes

$$\frac{\delta E}{\delta a} = \frac{-2}{n} \sum_{i=1}^{n} (\hat{y}_i - y_i) x_i$$

 Gradient dE/db - function describing how E changes when b changes

$$\frac{\delta E}{\delta b} = \frac{-2}{n} \sum_{i=1}^{n} (\hat{y}_i - y_i)$$





## **Gradient Descent algorithm**

- for each step (iteration)
  - calculate error E
  - calculate gradients dE/da and dE/db
  - a = a learning rate \* dE/da
  - b = b learning rate \* dE/db
- Every iteration gives better values of a and b
  - error (loss) is smaller
- Learning rate controls how fast the parameters are updated
  - too fast we may pass the minimum
  - too slow we may wait forever







## Analytical solution

 For linear regression the best parameters may be calculated using equations:

$$a = \frac{\sum_{i}^{N} (x_{i} - \bar{x})(y_{i} - \bar{y})}{\sum_{i}^{N} (x_{i} - \bar{x})^{2}}$$

$$b = \bar{y} - a\bar{x}$$

 but the presented example shows how Gradient Descent algorithm works (and we will use this algorithm later!)

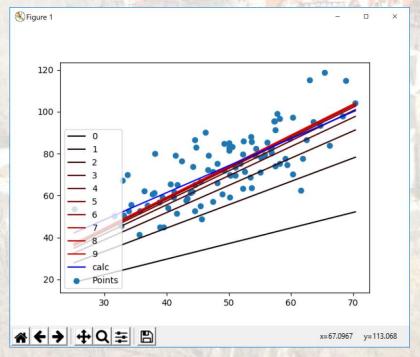




# Example

## linear\_descent.ipynb

 Simple code calculating linear regression using gradient descent for a set of points





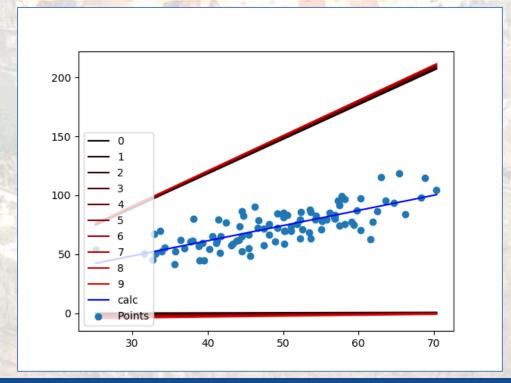
## Observations

- If we change initial values of a and b we have different results
  - b is reluctant to change
  - kind of "vanishing gradient" problem
- (1) Change the learning rate for b:
  - nb = b L\*100 \* D\_b # Update b
- (2) Change the number of iterations
  - epochs = 100 (1000?)
- · The results are better!



## Learning rate

- Change to:
  - -L = 0.0004 # The learning rate
- Results jump over the solution
  - too big step!





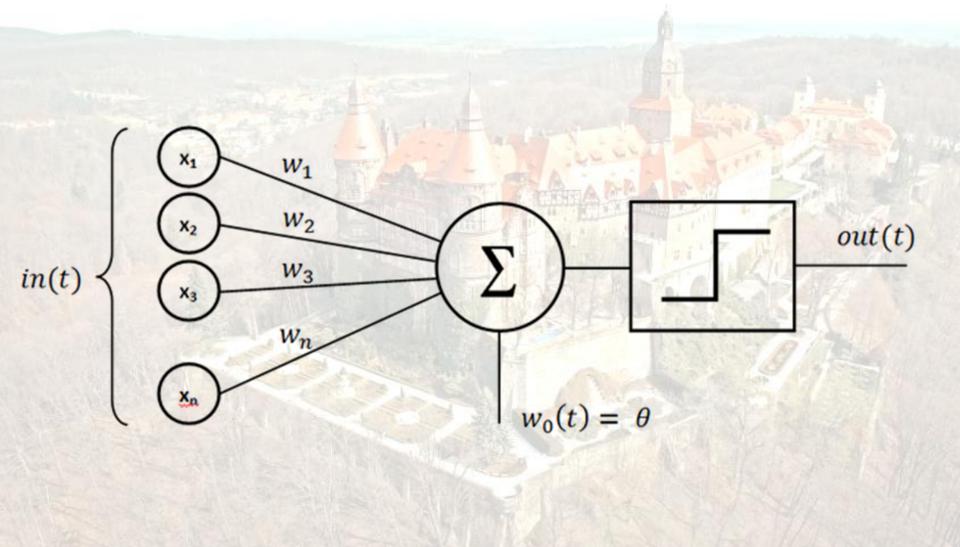
## Summary

- There are many different classification algorithms
- There are many ways to tune these algorithms
- There are many measures to estimate the quality of classification/regression
- So what is so special about the deep learning methods?
  - Wait for the following sections!



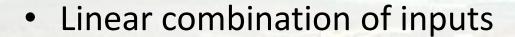


# Perceptron (Rosenblatt 1957)

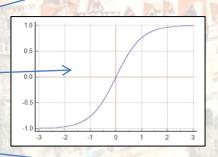




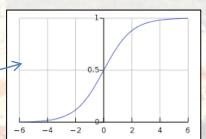
## **Activation function**

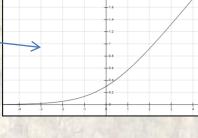


- Activation functions may be different
  - threshold function
  - sigmoid function
  - tanh function
  - softplus
  - RELU







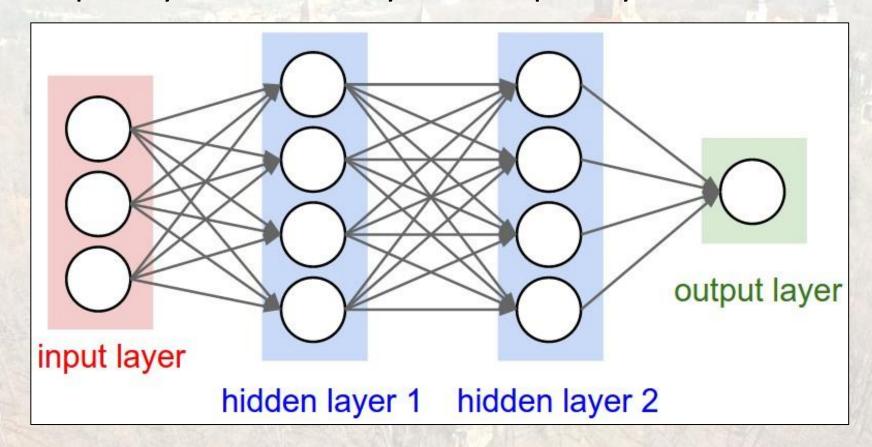




R(z) = max(0, z)

## Artifical Neural Network (ANN)

input layer > hidden layers > output layer







## Training the network

- Back propagation
  - the state-of-the art method to train the network
  - utilizes the already mentioned Gradient Descent algorithm
- The algorithm:

initialize weights

repeat many times:

use network to calculate output (Y<sub>pred</sub>) for some examples (X)

calculate error (loss function) using Y<sub>pred</sub> and Y (real)

update weights to minimize loss (using gradient for direction)







# Tuning - hyperparameters

- Network structure
  - Number of layers
  - Number of neurons for layer
  - Connections
  - Activation functions for layers
- Loss function
- Optimization algorithm
  - how to change the weights
  - learning rate (how big changes of weights)





## **Implementations**

- Many classification libraries like scikit-learn or WEKA implement the neural networks
  - but only the simplest models
- For Deep Learning there are many libraries developed by leading companies:
  - Tensorflow, Google
  - PyTorch, Facebook
  - CNTK, Microsoft
  - \_ ...
- We will use the most popular: Keras/Tensorflow





#### Keras

- General interface to use deep networks
- Works with Tensorflow, Theano, CNTK...
- User-friendly, modular, and extensible
- Created in Google
- Works in Python
- Tensorflow library includes Keras by default
  - that is why we installed Tensorflow and we use Keras
- Tensorflow 2 is integrated with Keras





#### FRAMEWORKS USAGE

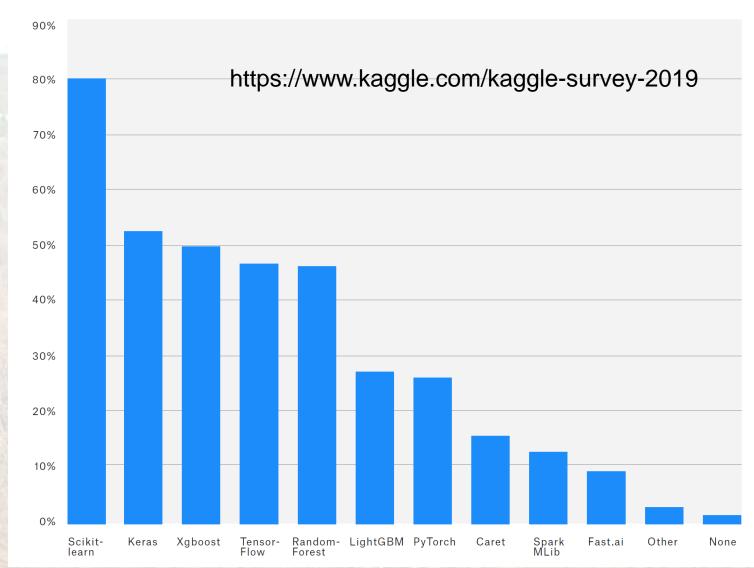








Table 3: Major Deep Learning Platforms

Platform	2019 % share	2018 % share	% change
Tensorflow	31.7%	29.9%	5.8%
Keras	26.6%	22.2%	19.7%
PyTorch	11.3%	6.4%	75.5%
Other Deep Learning Tools	5.6%	4.9%	15.2%
DeepLearning4J	2.5%	3.4%	-25.6%
Apache MXnet	1.7%	1.5%	13.1%
Microsoft Cognitive Toolkit	1.6%	3.0%	-45.5%
Theano	1.6%	4.9%	-67.4%
Torch	0.9%	1.0%	-6.1%
TFLearn	0.7%	1.1%	-34.7%
Caffe	0.6%	1.5%	-58.3%

https://www.kdnuggets.com/2019/05/poll-top-data-science-machine-learning-platforms.html







## Keras basics

- Build the model (network)
  - contains layers with neurons and connections
- Compile the model (model.compile)
  - define loss function and optimizer
- Train the model (model.fit)
  - provide samples with known labels
- Use the model for predictions (model.predict)
  - predict labels of unknown samples





# The simplest example

```
# import keras
from tensorflow.keras.models import Sequential
from tensorflow.keras.layers import Dense
# build model
model = Sequential()
model.add(Dense(50, activation='sigmoid'))
model.add(Dense(1, activation='sigmoid'))
# compile model
model.compile(loss='binary crossentropy',
   optimizer="adam", metrics=['accuracy'])
# train model
model.fit(samples, labels, epochs=100, batch size=10)
# use model
predicted = model.predict(sample)
```





## Decoder

#### decoder1.ipynb

- Decodes a binary list:
  - -[1,0,0,1,0,0,0,1]
- to the number:
  - -145
- Input: 8 values (0 or 1)
- Output: one value (the number)





photo: Ksiaż Castle, Poland

Deep Learning with Python

**Next lecture:** 

Neural Networks in Keras/Tensorflow

Introduction to Data Mining

Paweł Kasprowski, PhD, DSc.





