

# **CS 663, Fall 2023**

## Assignment 3

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**Question 1:** Consider the two images in the homework folder ‘barbara256.png’ and ‘kodak24.png’. Add zero-mean Gaussian noise with standard deviation  $\sigma = 5$  to both of them. Implement a mean shift based filter and show the outputs of the mean shift filter on both images for the following parameter configurations: ( $\sigma_s = 2$ ,  $\sigma_r = 2$ ); ( $\sigma_s = 0.1$ ,  $\sigma_r = 0.1$ ); ( $\sigma_s = 3$ ,  $\sigma_r = 15$ ). Comment on your results in your report. Repeat when the image is corrupted with zero-mean Gaussian noise of  $\sigma = 10$  (with the same bilateral filter parameters). Comment on your results in your report. Include all image outputs as well as noisy images in the report.

**Solution:**

Figure 1 shows the original image as well as noisy image of Barbara with zero-mean Gaussian noise standard deviation  $\sigma = 5$ .

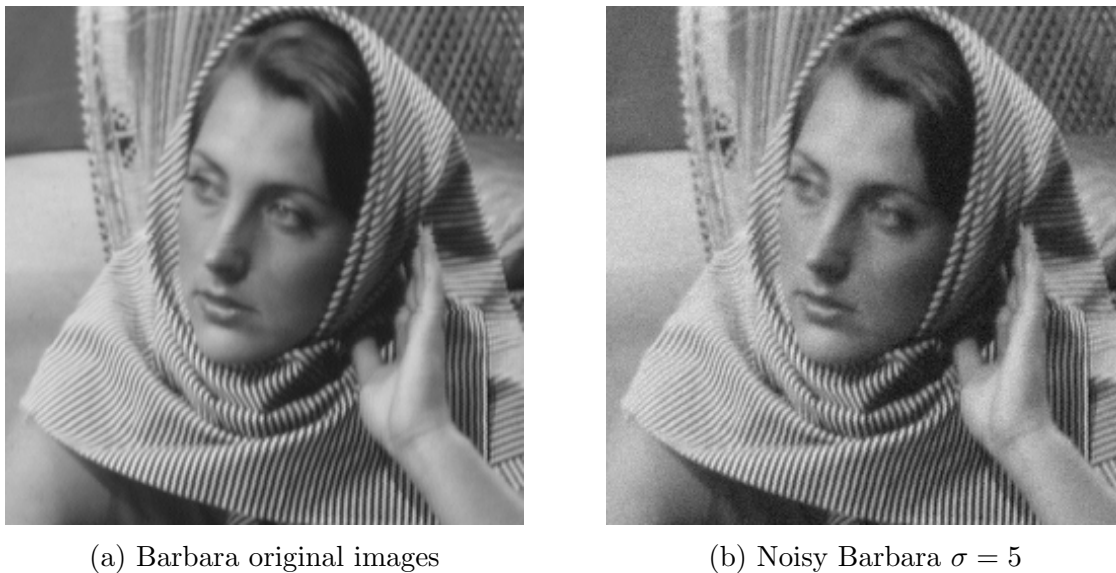


Figure 1: Barbara

Figure 2 shows the output of a mean shift based filter the parameter configurations: ( $\sigma_s = 2$ ,  $\sigma_r = 2$ ); ( $\sigma_s = 0.1$ ,  $\sigma_r = 0.1$ ); ( $\sigma_s = 3$ ,  $\sigma_r = 15$ ) with zero-mean Gaussian noise standard deviation  $\sigma = 5$ .

Figure 3 shows the original image as well as noisy image of Kodak with zero-mean Gaussian noise standard deviation  $\sigma = 5$ .

Figure 4 shows the output of a mean shift based filter the parameter configurations: ( $\sigma_s = 2$ ,  $\sigma_r = 2$ ); ( $\sigma_s = 0.1$ ,  $\sigma_r = 0.1$ ); ( $\sigma_s = 3$ ,  $\sigma_r = 15$ ) with zero-mean Gaussian noise standard deviation  $\sigma = 5$ .

Figure 5 shows the original image as well as noisy image of Barbara with zero-mean Gaussian noise standard deviation  $\sigma = 10$ .

Figure 6 shows the output of a mean shift based filter the parameter configurations: ( $\sigma_s = 2$ ,  $\sigma_r = 2$ ); ( $\sigma_s = 0.1$ ,  $\sigma_r = 0.1$ ); ( $\sigma_s = 3$ ,  $\sigma_r = 15$ ) with zero-mean Gaussian noise standard deviation  $\sigma = 10$ .

Figure 3 shows the original image as well as noisy image of Kodak with zero-mean Gaussian noise standard deviation  $\sigma = 10$ .

Figure 4 shows the output of a mean shift based filter the parameter configurations: ( $\sigma_s = 2$ ,  $\sigma_r = 2$ ); ( $\sigma_s = 0.1$ ,  $\sigma_r = 0.1$ ); ( $\sigma_s = 3$ ,  $\sigma_r = 15$ ) with zero-mean Gaussian noise standard deviation  $\sigma = 10$ .

### **Conclusion:**

We have seen that for  $\sigma_s = 0.1$ ,  $\sigma_r = 0.1$  filtered image has no changes it is quite same as original image but for ( $\sigma_s = 2$ ,  $\sigma_r = 2$ ) there are very few regions which are smoothened and in case of ( $\sigma_s = 3$ ,  $\sigma_r = 15$ ) there is more smootheness than other two cases.

For higher values of  $\sigma_s$  and  $\sigma_r$ , the number of local maximas of the kernel density estimate decrease which makes more pixels to converge to the same point. For  $\sigma_s = 0.1$ ,  $\sigma_r = 0.1$  every feature vector is a local maxima and hence every pixel is a cluster point of itself. We have also observed that the convergence takes more time for higher  $\sigma_s$ , or values because with fewer local maximas, a pixel is at more distant to reach through gradient ascent. The same can be observed for the kodak images.

As we increase the value of  $\sigma$ , here we have increased as by 5, the error in intensity increases. Also the convergence time also reduce.



(a) Barbara (  $\sigma_s = 2$  ,  $\sigma_r = 2$  )



(b) Barbara (  $\sigma_s = 0.1$ ,  $\sigma_r = 0.1$  )



(c) Barbara (  $\sigma_s = 3$ ,  $\sigma_r = 15$  )

Figure 2: Mean shift based filtering on Barbara with  $\sigma = 5$



(a) Kodak original images



(b) Noisy Kodak  $\sigma = 5$

Figure 3: Kodak



(a) Kodak ( $\sigma_s = 2$ ,  $\sigma_r = 2$ )



(b) Kodak ( $\sigma_s = 0.1$ ,  $\sigma_r = 0.1$ )



(c) Kodak ( $\sigma_s = 3$ ,  $\sigma_r = 15$ )

Figure 4: **Mean shift based filtering on Kodak with  $\sigma = 5$**



(a) Barbara original images



(b) Noisy Barbara  $\sigma = 10$

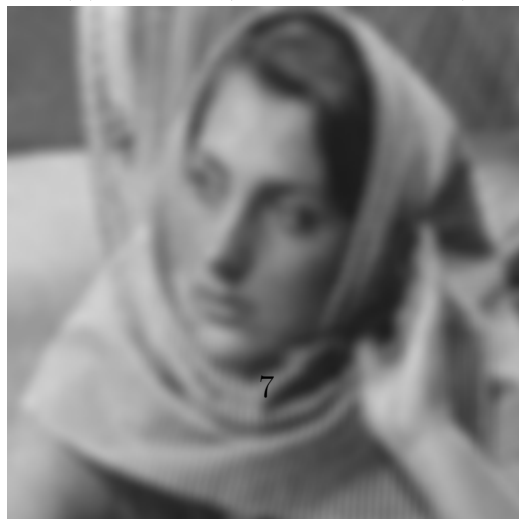
Figure 5: Barbara



(a) Barbara (  $\sigma_s = 2$  ,  $\sigma_r = 2$  )



(b) Barbara (  $\sigma_s = 0.1$ ,  $\sigma_r = 0.1$  )



(c) Barbara (  $\sigma_s = 3$ ,  $\sigma_r = 15$  )

Figure 6: Mean shift based filtering on Barbara with  $\sigma = 10$





(a) Kodak original images



(b) Noisy Kodak  $\sigma = 10$

Figure 7: Kodak



(a) Kodak ( $\sigma_s = 2$ ,  $\sigma_r = 2$ )



(b) Kodak ( $\sigma_s = 0.1$ ,  $\sigma_r = 0.1$ )



(c) Kodak ( $\sigma_s = 3$ ,  $\sigma_r = 15$ )

Figure 8: **Mean shift based filtering on Kodak with  $\sigma = 10$**