

Time Based Key-Value Store

Leetcode #981





Problem:

- Design a time-based key-value data structure that can store multiple values for the same key at different time stamps and retrieve the key's value at a certain timestamp.
 - SET: Stores the key `key` with the value `value` at the given time `timestamp`.
 - GET: Returns a value such that set was called previously, with `timestamp_prev ≤ timestamp`. If there are multiple such values, it returns the value associated with the largest `timestamp_prev`. If there are no values, it returns `""`.
- All the timestamps `timestamp` of set are strictly increasing
- A lot of calls made to set and get.



Examples:

Digit	1 → Sleeping
	3 → Stealing treats
	4 → Breakfast

Hannah	2 → Drinking
---------------	--------------



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`get(Digit, 3) → Stealing treats`

`get(Digit, 2) → Sleeping`

`get(Hannah, 0) → ""`

`get(Bobo, 3) → ""`

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- Key exists
- Timestamp ≤ exists

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- Key exists
- Timestamp \leq exists so choose max

Examples:

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- Key exists
- Timestamp <= doesn't exist

Examples:

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Hannah	2 → Drinking

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`get(Digit, 2) → Sleeping`

`get(Hannah, 0) → ""`

`get(Bobo, 3) → ""`

- Key doesn't exist



Needs:

- Quick insert for **key**
 - “Put Digit in as a key”
- Quick lookup on **key** (no sorting required)
 - “What timestamps does Digit have?”
- Quick insert for a new **timestamp for a key**
 - “Give Digit the timestamp 3 with a value ‘Sleeping’”
- Quick sorted lookup on **timestamps**
 - “Given these timestamps for Digit, what timestamp is less than or equal to 3?”



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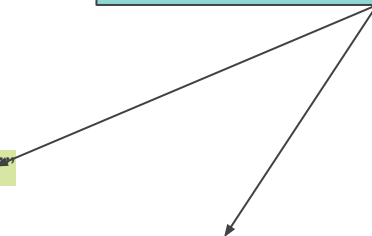
- HashMap has $O(1)$ average insert and lookup
 - $O(n)$ worst case with bad hash function



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- HashMap has $O(1)$ average insert
 - $O(n)$ worst case with bad hash function
- But data isn't sorted so won't be optimal for lookup

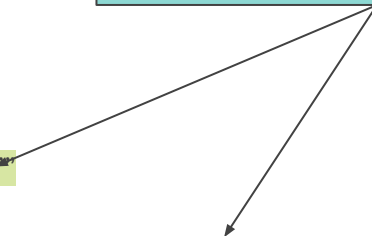




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- Instead, we can use an array to store values
 - $O(1)$ insert
- Perform binary search on array for $O(\log n)$ since we know it is sorted





Algorithm: Set

- If the key already exists, append the new timestamp and value to the current list associated with the key
- Otherwise, add the key and add a new list that contains the timestamp and value



Algorithm: Get

- If the key doesn't exist, return ""
- If the key exists but the smallest timestamp associated with it is larger than the timestamp we are looking for, return ""
- Run a binary search on the list associated with the key and find the largest timestamp that is \leq the timestamp. Return its value



Binary Search

FIND: 4

1	5	6	8	10	11	15	81
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LOW



MID

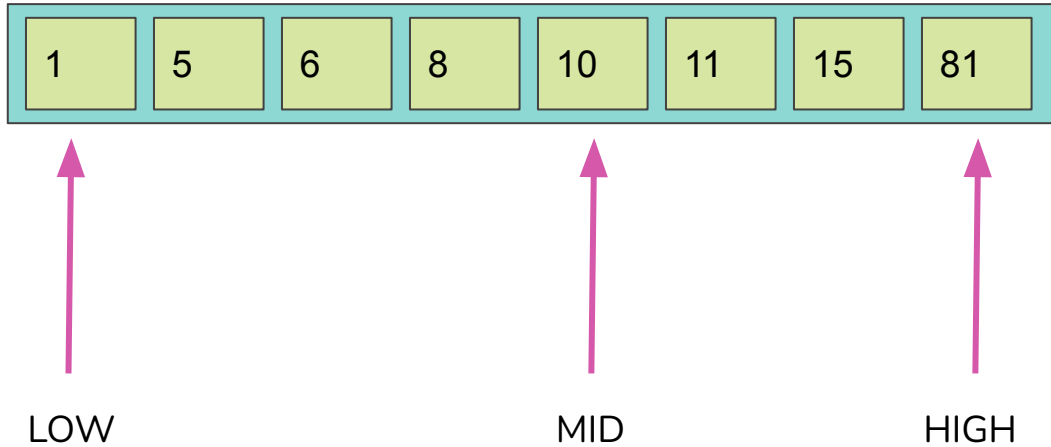


HIGH



Binary Search

FIND: 4

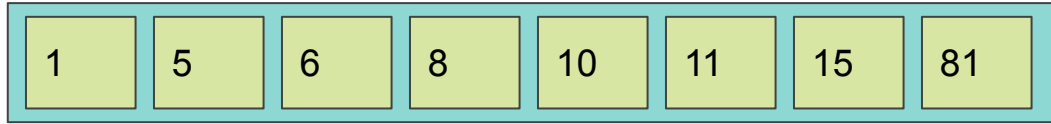


Our special case: is $4 \geq \text{lowest number}$? $4 \geq 1$? Yes -> continue



Binary Search

FIND: 4



LOW



MID



HIGH

$4 < 10$



Set HIGH=MID-1



Binary Search

FIND: 4

1	5	6	8	10	11	15	81
---	---	---	---	----	----	----	----



LOW

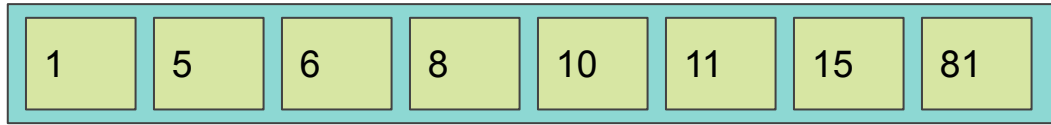


HIGH



Binary Search

FIND: 4



LOW



MID



HIGH

$4 < 6$

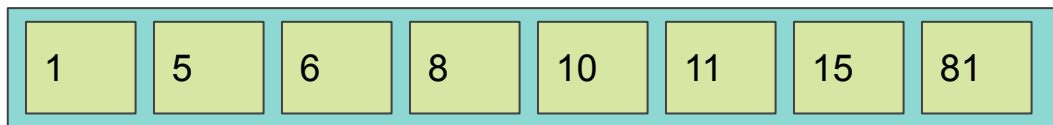


Set HIGH=MID-1



Binary Search

FIND: 4



LOW

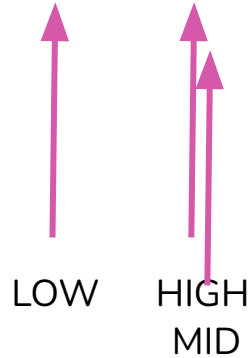
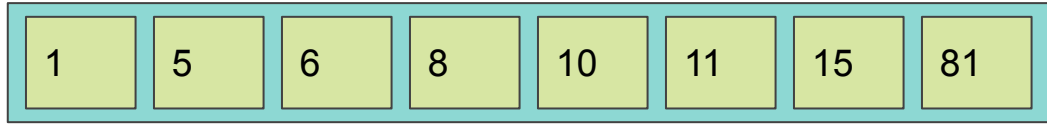


HIGH



Binary Search

FIND: 4





Binary Search

FIND: 4

1	5	6	8	10	11	15	81
---	---	---	---	----	----	----	----

LOW
HIGH



Binary Search

FIND: 4

1	5	6	8	10	11	15	81
---	---	---	---	----	----	----	----

↑
↑
LOW
HIGH

LOW=HIGH so do this must be the max number less than 4