

Computer Algorithm

Binary Search Algorithm:

Algorithm: Recursive binary search

Algorithm BinSrch (a,i,l,x)

//Given an array a[i:l] of elements in non-decreasing order, $1 \leq i \leq l$, determine

//whether x is present and if so, return j such that $x=a[j]$; else return 0;

```
{
    if (l == i) then // If small (P)
    {
        if (x = a[i]) then return i;
    else return 0;
    }
    else
    { // Reduce p into a smaller subproblem.
        mid:= [(i + l) / 2];
        if (x = a[mid]) then return mid;
        else if (x < a[mid]) then
            return BinSrch(a, i, mid - 1, x);
        else return BinSrch(a, mid + 1, l, x);
    }
}
```

Algorithm: Iterative binary search

Algorithm BinSrch (a, n, x)

//Given an array a[1 : n] of elements in non-decreasing order, $n \geq 0$, determine //whether x is present and if so, return j such that $x=a[j]$; else return 0;

```
{
    low := 1; high := n;
    while (low<=high) do
    {
        mid := [(low+high)/2];
        if (x < a[mid]) then high := mid - 1;
        else if (x > a[mid]) then low := mid + 1;
        else return mid;
    }
    return 0;
}
```

MinMax Algorithm:

Algorithm: Recursively finding the maximum and minimum

Algorithm Minmax (i, j, max, min)

// $a[1 : n]$ is a global array. Parameters i and j are integers, $1 \leq i \leq j \leq n$.

// The effect is to set max and min to the largest and smallest values in $a[i : j]$, respectively.

```
{
    if ( $i = j$ ) then  $max := min := a[i]$ ; // Small(P)
    else if ( $i = j - 1$ ) then // Another case of Small(P)
        {
            if ( $a[i] < a[j]$ ) then
            {
                 $max := a[j]$ ;  $min := a[i]$ ;
            }
            else
            {
                 $max := a[i]$ ;  $min := a[j]$ ;
            }
        }

    else
    { // If  $P$  is not small, divide  $P$  into subproblem.
      // Find where to split the set.
         $mid := [(i + j) / 2]$ ;
      //Solve the subproblem
        MaxMin( $i, mid, max, min$ ) ;
        MaxMin( $mid+1, j, max1, min1$ ) ;
      // Combine the solution
        if ( $max < max1$ ) then  $max := max1$ ;
        if ( $min < min1$ ) then  $min := min1$ ;

    }
}
```

Merge Sort:

Algorithm: Merge Sort

Algorithm MergeSort(*low* , *high*)

//*a[low : high]* is a global array to be sorted.

// Small(*P*) is true if there is only one element to sort. In this case the list is

// already sorted.

```
{
    if (low < high) then // If there are more than one element
    {
        // Divide P into subproblems.
        // Find where to split the set.
        mid := [(low + high)/2];
        // Solve the subproblems.
        MergeSort(low, mid);
        MergeSort(mid+ 1, high);
        // Combine the solutions.
        Merge(low, mid, high);
    }
}
```

Algorithm: Merging two sorted subarrays using auxiliary storage.

Algorithm Merge(*low, mid, high*)

// *a[low : high]* is a global array containing two sorted subsets in
// *a[low : mid]* and in *a[mid + 1 : high]*. The goal is to merge these two sets
// into a single set residing in *a[low : high]*. *b[]* is an auxiliary global array.
{

h := low; i := low; j := mid + 1;

while ((*h <= mid*) **and** (*j <= high*)) **do**

 {

if (*a[h] <= a[j]*) **then**

 {

b[i] := a[h]; h := h + 1;

 }

else

 {

b[i] := a[j]; j := j + 1;

 }

i := i + 1;

 }

if (*h > mid*) **then**

for *k := j to high* **do**

 {

b[i] := a[k]; i := i + 1;

 }

else

for *k := h to mid* **do**

 {

b[i] := a[k]; i := i + 1;

 }

for *k := low to high* **do** *a[k] := b[k];*

}

Quick Sort:

Algorithm: Sorting by partitioning

Algorithm QuickSort(p, q)

// Sorts the elements $a[p], \dots, a[q]$ which reside in the global array $a[1 : n]$
// into ascending order; $a[n + 1]$ is considered to be defined and
// must be \geq all the elements in $a[1 : n]$.

```
{
    if ( $p < q$ ) then // If there are more than one element
    {
        // divide  $P$  into two subproblems
         $j := \text{Partiton}(a, p, q+1)$ ;
        // j is the position of the partitioning element.
        // Solve the subproblems.
        QuickSort( $p, j - 1$ );
        QuickSort( $j + 1, q$ );
        // There is no need for combining solutions.
    }
}
```

Prim's Algorithm:

Prim's minimum cost spanning tree algorithm.

Algorithm Prim($E, cost, n, t$)

// E is the set of edges in G . $cost[1:n, 1:n]$ is the cost adjacency matrix of an
// n vertex graph such that $cost[i, j]$ is either a positive real number or
// infinity if no edge (i, j) exists. A minimum spanning tree is computed and
// sorted as a set of edges in the array $t[1:n-1, 1:2]$. ($t[i, 1], t[i, 2]$) is an edge
// in the minimum cost spanning tree. The final cost is returned.

```
{
    Let  $(k, l)$  be an edge of minimum cost in  $E$ ;
     $mincost := cost[k, l]$ ;
     $t[1, 1] := k; t[1, 2] := l$ ;
    for  $i := 1$  to  $n$  do // Initialize near.
        if  $(cost[i, l] < cost[i, k])$  then  $near[i] := l$ ;
        else  $near[i] := k$ ;
     $near[k] := near[l] := 0$ ;
    for  $i := 2$  to  $n-1$  do
    { // Find  $n - 2$  additional edges for  $t$ .
        Let  $j$  be an index such that  $near[j] \neq 0$  and
         $cost[j, near[j]]$  is minimum;
         $t[i, 1] := j; t[i, 2] := near[j]$ ;
         $mincost := mincost + cost[j, near[j]]$ ;
         $near[j] := 0$ ;
        for  $k := 1$  to  $n$  do // Update near[ ].
            if  $((near[k] \neq 0) \text{ and } (cost[k, near[k]] > cost[k, j]))$ 
                then  $near[k] := j$ ;
    }
    return  $mincost$ ;
}
```

Kruskal's Algorithm:

Kruskal's minimum cost spanning tree algorithm.

Algorithm Kruskal($E, cost, n, t$)

// E is the set of edges in G . G has n vertices. $cost[u, v]$ is the cost of

// edge (u, v) . t is the set of edges in the minimum-cost spanning tree.

// The final cost is returned.

```
{
    Construct a heap out of the edge costs using Heapify;
    for i := 1 to n do parent[i] := -1;
    // Each vertex is in a different set.
    i := 0; mincost := 0.0;
    while ((i < n-1) and (heap not empty)) do
    {
        Delete a minimum cost edge (u, v) from the heap
        and reheapify using Adjust;
        j := Find(u); k := Find(v);
        if (j != k) then
        {
            i := i+ 1;
            t[i,1] := u; t[i,2] := v;
            mincost := mincost + cost[u, v];
            Union(j, k);
        }
    }
    if (i != n -1) then write ("No spanning tree);
    else return mincost;
}
```