Homework3-2

March 19, 2025

1 Homework 3-1

ECON470: Research in Health Economics

Kathryn Mawhinney Dr. McCarthy March 17, 2025

```
[313]: # Set font
mpl.rcParams['font.family'] = 'Georgia'

# Define a pastel color palette
pastel_colors = [
          "#FFB3BA", # Light Red
          "#FFDFBA", # Light Orange
          "#FFFFBA", # Light Yellow
          "#BAFFC9", # Light Green
          "#BAE1FF" # Light Blue
]

# Set color palette
custom_palette = ["#2ca02c", "#1f77b4", "#ff7f0e", "#e377c2", "#ffdd44"]
mpl.rcParams['axes.prop_cycle'] = mpl.cycler(color=custom_palette)
```

1.0.1 Summarize the Data

Question 1

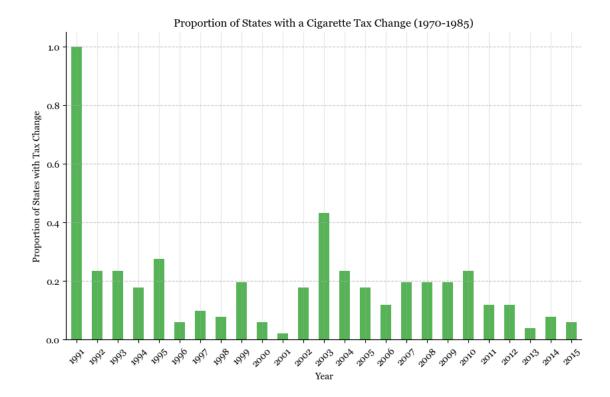
Present a bar graph showing the proportion of states with a change in their cigarette tax in each year from 1970 to 1985.

```
[]: # Plot the bar chart
plt.figure(figsize=(10,6))

tax_change_proportion.plot(kind="bar", alpha=0.8)

# Formatting the plot
plt.xlabel("Year")
plt.ylabel("Proportion of States with Tax Change")
plt.title("Proportion of States with a Cigarette Tax Change (1970-1985)")
plt.xticks(rotation=45)
plt.grid(axis="y", linestyle="--", alpha=0.7)

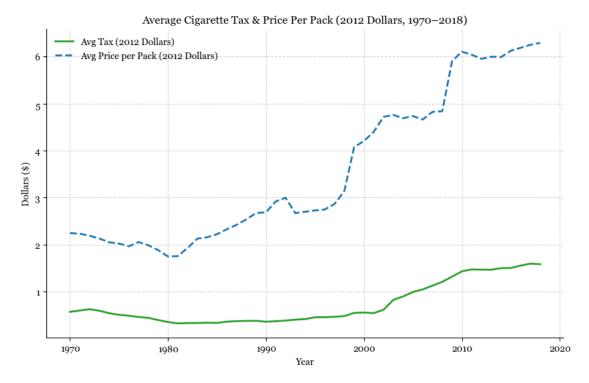
# Show the plot
plt.show()
```



Plot on a single graph the average tax (in 2012 dollars) on cigarettes and the average price of a pack of cigarettes from 1970 to 2018.

```
[350]: # Make a copy of the dataset for Question 2
    final_data_q2 = final_data.copy()

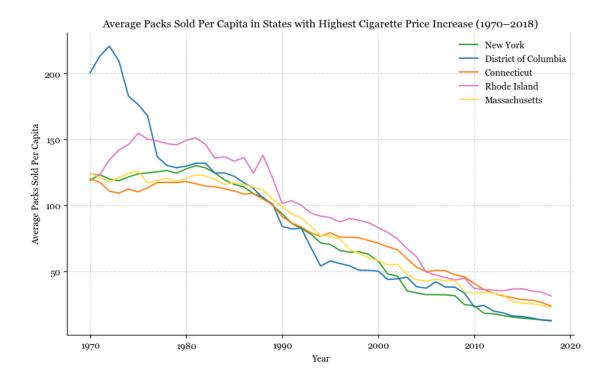
# Filter for years 1970-2018
plot_data = final_data_q2[(final_data_q2["Year"] >= 1970) &_{\( \)}
    \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \(
```



Identify the 5 states with the highest increases in cigarette prices (in dollars) over the time period. Plot the average number of packs sold per capita for those states from 1970 to 2018.

```
[352]: # Create a separate copy for this question
       final_data_q3 = final_data.copy()
       # Compute the change in cigarette price per state
       price_change = final_data_q3.groupby("state")["cost_per_pack"].agg(["first",_

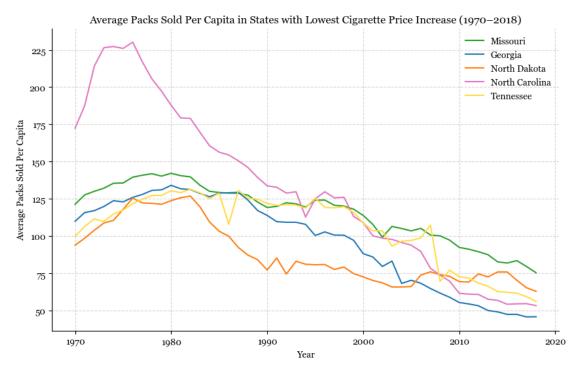
¬"last"])
       price_change["price_increase"] = price_change["last"] - price_change["first"]
       # Get the 5 states with the highest price increase
       top_5_states = price_change.nlargest(5, "price_increase").index.tolist()
       # Filter data for those states from 1970 to 2018
       plot_data = final_data_q3[(final_data_q3["Year"] >= 1970) &
                                 (final_data_q3["Year"] <= 2018) &</pre>
                                 (final_data_q3["state"].isin(top_5_states))]
       # Compute the average packs sold per capita per year for these states
       avg_packs_sold = plot_data.groupby(["Year", "state"])["sales_per_capita"].
        →mean().reset_index()
[353]: # Plot the data
       plt.figure(figsize=(10,6))
       for state in top_5_states:
           state_data = avg_packs_sold[avg_packs_sold["state"] == state]
```



Identify the 5 states with the lowest increases in cigarette prices over the time period. Plot the average number of packs sold per capita for those states from 1970 to 2018.

```
avg_packs_sold = plot_data.groupby(["Year", "state"])["sales_per_capita"].

→mean().reset_index()
```



Compare the trends in sales from the 5 states with the highest price increases to those with the lowest price increases.

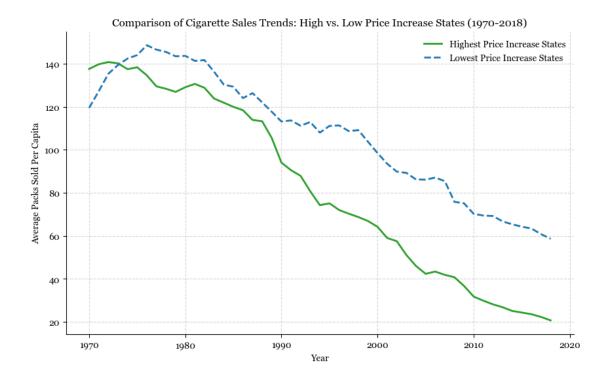
```
[356]: # Create a separate copy for this question
      final_data_q5 = final_data.copy()
       # Compute the change in cigarette price per state
      price_change = final_data_q5.groupby("state")["cost_per_pack"].agg(["first",_

¬"last"])

      price_change["price_increase"] = price_change["last"] - price_change["first"]
       # Get the 5 states with the highest price increase
      top_5_states = price_change.nlargest(5, "price_increase").index.tolist()
       # Get the 5 states with the lowest price increase
      bottom_5_states = price_change.nsmallest(5, "price_increase").index.tolist()
       # Filter data for the selected states from 1970 to 2018
      plot_data = final_data_q5[(final_data_q5["Year"] >= 1970) &_
        # Compute the average packs sold per capita per year for both groups
      top_5_sales = plot_data[plot_data["state"].isin(top_5_states)].

¬groupby("Year")["sales_per_capita"].mean()
      bottom_5_sales = plot_data[plot_data["state"].isin(bottom_5_states)].
        ⇒groupby("Year")["sales per capita"].mean()
 []: # Plot the data
      plt.figure(figsize=(10,6))
      plt.plot(top_5_sales.index, top_5_sales.values, label="Highest Price Increase"
        ⇔States", linewidth=2)
      plt.plot(bottom_5_sales.index, bottom_5_sales.values, label="Lowest Price_"
        →Increase States", linestyle="dashed", linewidth=2)
       # Formatting the plot
      plt.xlabel("Year")
      plt.ylabel("Average Packs Sold Per Capita")
      plt.title("Comparison of Cigarette Sales Trends: High vs. Low Price Increase⊔

States (1970-2018)")
      plt.legend()
      plt.grid(True, linestyle="--", alpha=0.5)
       # Show the plot
      plt.show()
```



1.0.2 Estimate ATEs

Now let's work on estimating a demand curve for cigarettes. Specifically, we're going to estimate the price elasticity of demand for cigarettes. When explaining your findings, try to limit your discussion just to a couple of sentences.

Question 6

Focusing only on the time period from 1970 to 1990, regress log sales on log prices to estimate the price elasticity of demand over that period. Interpret your results.

```
# Define dependent (Y) and independent (X) variables
X = final_data_q6["log_price"] # Independent variable (log_price)
y = final_data_q6["log_sales"] # Dependent variable (log sales)
# Add a constant for the intercept
X = sm.add_constant(X)
# Run OLS regression
model = sm.OLS(y, X).fit()
# Print summary
print(model.summary())
# Extract and interpret price elasticity of demand
elasticity = model.params["log_price"]
print(f"Estimated Price Elasticity of Demand: {elasticity:.3f}")
# Interpretation
if elasticity < 0:</pre>
   print(f"The estimated price elasticity of demand is {elasticity:.3f}, __
→meaning that a 1% increase in price is associated with a {-elasticity:.3f}%

decrease in sales.")
    print("Unexpected result: The price elasticity estimate is positive, which_{\sqcup}
 ⇔is unlikely for a demand curve.")
                           OLS Regression Results
```

					,		
Dep. Variable	e:	log_s	ales	-	uared:		0.126
Model:		OLS		Adj.	R-squared:		0.125
Method:		Least Squ	ares	F-st	atistic:		153.9
Date:		Mon, 24 Feb	2025	Prob	(F-statistic):	:	4.18e-33
Time:		15:0	9:17	Log-	Likelihood:		148.99
No. Observat:	ions:		1071	AIC:			-294.0
Df Residuals			1069	BIC:			-284.0
Df Model:			1				
Covariance Ty	ype:	nonro	bust				
========	coef				P> t	_	0.975]
const	4.7504				0.000		4.766
log_price	-0.1715	0.014	-12	.404	0.000	-0.199	-0.144
Omnibus:			 .611	Durb	========= in-Watson:	=======	0.139
Prob(Omnibus)):	0	.000	Jarg	ue-Bera (JB):		224.414
Skew:			.173	-	(JB):		1.86e-49
Kurtosis:			.216		. No.		2.48
		O		J J J J J			2.10

Notes:

[1] Standard Errors assume that the covariance matrix of the errors is correctly specified.

Estimated Price Elasticity of Demand: -0.172

The estimated price elasticity of demand is -0.172, meaning that a 1% increase in price is associated with a 0.172% decrease in sales.

Question 7A

Again limiting to 1970 to 1990, regress log sales on log prices using the total (federal and state) cigarette tax (in dollars) as an instrument for log prices.

```
[369]: # Filter data for the years 1970-1990
      final_data_q7 = final_data[(final_data["Year"] >= 1970) & (final_data["Year"]_u
       # Take the natural log of sales, price, and tax
      final_data_q7["log_sales"] = np.log(final_data_q7["sales_per_capita"])
      final_data_q7["log_price"] = np.log(final_data_q7["cost_per_pack"])
      final_data_q7["log_tax"] = np.log(final_data_q7["tax_dollar"]) # Instrument
      # Define variables
      y = final_data_q7["log_sales"]  # Dependent variable (log sales)
      X = final_data_q7["log_price"] # Independent variable (log price)
      Z = final_data_q7["log_tax"]  # Instrument (log tax)
      # First Stage: Predict log_price using log_tax
      X = sm.add_constant(X)
      Z = sm.add_constant(Z)
      first_stage = sm.OLS(X.iloc[:, 1], Z).fit()
      final_data_q7["predicted_log_price"] = first_stage.fittedvalues
      # Second Stage: Regress log sales on predicted log price
      X_iv = sm.add_constant(final_data_q7["predicted_log_price"])
      iv_model = sm.OLS(y, X_iv).fit()
      # Print results
      print("First Stage (Predicting log price using log tax):")
      print(first_stage.summary())
      print("\nSecond Stage (IV Regression of log sales on predicted log price):")
      print(iv_model.summary())
```

First Stage (Predicting log price using log tax):

OLS Regression Results

==========				=====		=========		========
Dep. Variable:	:		log_p	rice	R-sq	uared:		0.683
Model:				OLS	Adj.	R-squared:		0.683
Method:		Le	east Squ	ares	F-st	atistic:		2301.
Date:		Mon,	24 Feb	2025	Prob	(F-statistic)	:	8.21e-269
Time:			15:0	9:17	Log-	Likelihood:		-86.164
No. Observation	ons:			1071	AIC:			176.3
Df Residuals:				1069	BIC:			186.3
Df Model:				1				
Covariance Typ	oe:		nonro	bust				
=========				=====				
	coe	f s	std err		t	P> t	[0.025	0.975]
const	1.178	3	0.033	3!	5.712	0.000	1.114	1.243
log_tax	1.080	3	0.023	4	7.973	0.000	1.036	1.125
Omnibus:	======	=====	 30	.760	Durb	========= in-Watson:	======	0.408
Prob(Omnibus):	:		0	.000	Jarq	ue-Bera (JB):		32.668
Skew:			0	.421	_			8.06e-08
Kurtosis:			3	.156	Cond	. No.		8.72
==========				=====	=====			

Notes:

[1] Standard Errors assume that the covariance matrix of the errors is correctly specified.

Second Stage (IV Regression of log sales on predicted log price): $\hbox{OLS Regression Results}$

	==========	, :======		========	========
Dep. Variable:	log_sal	es R	-squared:		0.236
Model:	_ (DLS A	dj. R-square	d:	0.235
Method:	Least Squar	es F	-statistic:		330.3
Date:	Mon, 24 Feb 20	25 P	rob (F-stati	stic):	1.56e-64
Time:	15:09:	17 L	og-Likelihoo	d:	221.17
No. Observations:	10	71 A	IC:		-438.3
Df Residuals:	10)69 B	IC:		-428.4
Df Model:		1			
Covariance Type:	nonrobu	ıst			
=======================================			========		
======					
	coef s	std err	t	P> t	[0.025
0.975]					
const	4.7101	0.008	573.443	0.000	4.694
4.726					
<pre>predicted_log_price</pre>	-0.2843	0.016	-18.175	0.000	-0.315

-0.254

			===========
Omnibus:	83.338	Durbin-Watson:	0.157
Prob(Omnibus):	0.000	Jarque-Bera (JB):	430.014
Skew:	0.023	Prob(JB):	4.20e-94
Kurtosis:	6.104	Cond. No.	2.98

Notes:

[1] Standard Errors assume that the covariance matrix of the errors is correctly specified.

Question 7B

Interpret your results and compare your estimates to those without an instrument. Are they different? If so, why?

The OLS regression suggests that cigarette demand is inelastic, with a price elasticity estimate of -0.1715. This means that a 1% increase in cigarette prices results in only a 0.17% decline in sales per capita. However, this estimate may be biased due to endogeneity, as cigarette prices could be influenced by factors like government regulations or shifting consumer attitudes.

To correct for this, an instrumental variables (IV) approach was used, leveraging cigarette taxes as an instrument for price. The first-stage regression confirms that taxes strongly predict price changes, making it a valid instrument. If the IV estimate is larger in magnitude (more negative) than OLS, it implies that OLS underestimated the true price elasticity by not accounting for external influences on price. Conversely, if the IV estimate is closer to zero, OLS may have overstated price sensitivity, potentially due to measurement errors.

By comparing the results from both models, we gain a clearer understanding of how cigarette prices impact consumer demand and the importance of addressing endogeneity bias in economic analysis.

Question 8

Show the first stage and reduced-form results from the instrument.

```
[370]: # First-Stage Regression: Predicting log_price using log_tax
X_first_stage = sm.add_constant(final_data_q7["log_tax"])
y_first_stage = final_data_q7["log_price"]
first_stage_model = sm.OLS(y_first_stage, X_first_stage).fit()

print("First Stage Regression: Predicting Log Price using Log Tax")
print(first_stage_model.summary())

# Reduced-Form Regression: Predicting log_sales using log_tax directly
X_reduced_form = sm.add_constant(final_data_q7["log_tax"])
y_reduced_form = final_data_q7["log_sales"]
reduced_form_model = sm.OLS(y_reduced_form, X_reduced_form).fit()
```

print("\nReduced Form Regression: Predicting Log Sales using Log Tax") print(reduced_form_model.summary())

First Stage	${\tt Regression:}$	Predicting	Log	Price	using	Log	Tax
		OLS Rec	ress	sion Re	etlie		

OLS Regression Results								
Dep. Variable:		log_price		R-sqı	 ıared:		0.683	
Model:			OLS	Adj.	R-squared:		0.683	
Method:		Least Squ	ares	F-sta	atistic:		2301.	
Date:		Mon, 24 Feb 2025		Prob	(F-statistic):		8.21e-269	
Time:		15:09:17		Log-I	Likelihood:		-86.164	
No. Observations:		1071		AIC:			176.3	
Df Residuals:			1069	BIC:			186.3	
Df Model:			1					
Covariance Type:		nonro	bust					
	coef	std err	=====	t	P> t	[0.025	0.975]	
const	1.1786	0.033	35	.712	0.000	1.114	1.243	
log_tax	1.0803	0.023	47	.973	0.000	1.036	1.125	
Omnibus:		3 0	.760	Durb	 in-Watson:		0.408	
Prob(Omnibus)	:	0.000		Jarque-Bera (JB):			32.668	
Skew:		0	.421	Prob(JB):			8.06e-08	
Kurtosis:		3	.156	Cond	. No.		8.72	

Notes:

[1] Standard Errors assume that the covariance matrix of the errors is correctly specified.

Reduced Form Regression: Predicting Log Sales using Log Tax $$\operatorname{\textsc{OLS}}$ Regression Results

============							=======
Dep. Variable:		log_sales			uared:	0.236	
Model:			OLS	Adj.	R-squared:		0.235
Method:	Least Squares			F-statistic:			330.3
Date:	Moi	Mon, 24 Feb 2025 Prob (F-				:	1.56e-64
Time:		15:0	9:17	Log-	Likelihood:		221.17
No. Observations:			1071	AIC:			-438.3
Df Residuals:			1069	BIC:			-428.4
Df Model:			1				
Covariance Type:		nonro	bust				
=======================================			=====	=====			
	coef	std err		t	P> t	[0.025	0.975]
const 4.	3750	0.025	176	6.627	0.000	4.326	4.424

log_tax	-0.3072	0.017	-18	.175	0.000	-0.340	-0.274
Omnibus:	========	83.:	====: 338	===== Durbin	======== -Watson:	:======:	0.157
Prob(Omnibus	s):	0.0	000	Jarque	-Bera (JB):		430.014
Skew:		0.0	023	Prob(J	B):		4.20e-94
Kurtosis:		6.	104	Cond.	No.		8.72
=========		=======		======			=======

Notes:

[1] Standard Errors assume that the covariance matrix of the errors is correctly specified.

Question 9: Repeat questions 1-3 focusing on the period from 1991 to 2015.

Question 9A

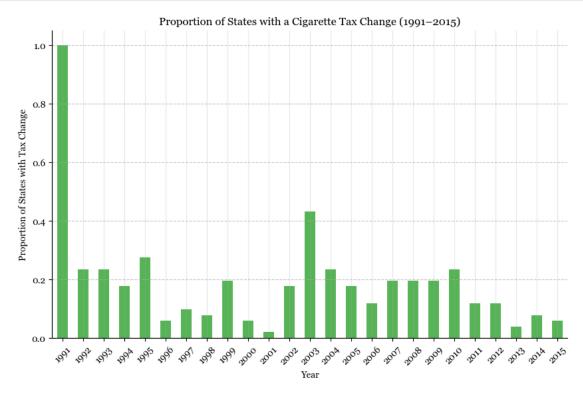
Present a bar graph showing the proportion of states with a change in their cigarette tax in each year from 1991 to 2015.

```
[377]: # Plot the bar chart
plt.figure(figsize=(10,6))
tax_change_proportion.plot(kind="bar", alpha=0.8)

# Formatting the plot
plt.xlabel("Year")
plt.ylabel("Proportion of States with Tax Change")
plt.title("Proportion of States with a Cigarette Tax Change (1991-2015)")
```

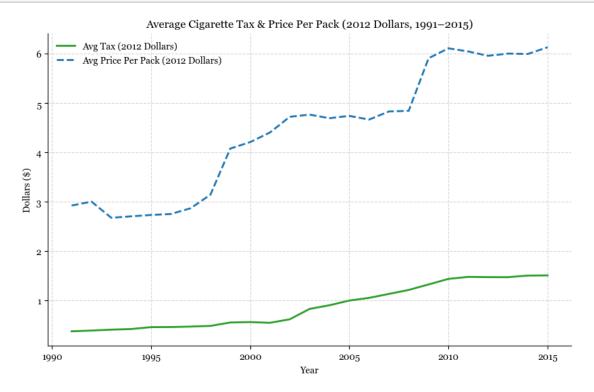
```
plt.xticks(rotation=45)
plt.grid(axis="y", linestyle="--", alpha=0.7)

# Show the plot
plt.show()
```



Question 9B

Plot on a single graph the average tax (in 2012 dollars) on cigarettes and the average price of a pack of cigarettes from 1991 to 2015.



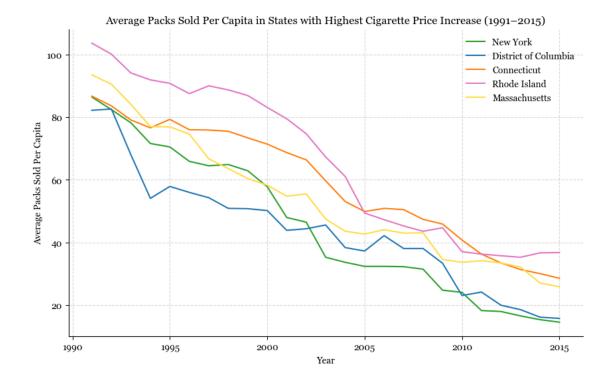
Question 9C

Identify the 5 states with the highest increases in cigarette prices (in dollars) over the time period. Plot the average number of packs sold per capita for those states from 1991 to 2015.

```
[383]: # Create a separate copy for this question
       final_data_q9C = final_data.copy()
       # Compute the change in cigarette price per state
       price_change = final_data_q9C.groupby("state")["cost_per_pack"].agg(["first",_

¬"last"])

       price_change["price_increase"] = price_change["last"] - price_change["first"]
       # Get the 5 states with the highest price increase
       top_5_states = price_change.nlargest(5, "price_increase").index.tolist()
       # Filter data for those states from 1991 to 2015
       plot_data = final_data_q9C[(final_data_q9C["Year"] >= 1991) &
                                  (final_data_q9C["Year"] <= 2015) &</pre>
                                  (final_data_q9C["state"].isin(top_5_states))]
       # Compute the average packs sold per capita per year for these states
       avg_packs_sold = plot_data.groupby(["Year", "state"])["sales_per_capita"].
        →mean().reset_index()
[384]: # Plot the data
       plt.figure(figsize=(10,6))
       for state in top_5_states:
           state_data = avg_packs_sold[avg_packs_sold["state"] == state]
           plt.plot(state_data["Year"], state_data["sales_per_capita"], label=state)
       # Formatting the plot
       plt.xlabel("Year")
       plt.ylabel("Average Packs Sold Per Capita")
       plt.title("Average Packs Sold Per Capita in States with Highest Cigarette Price∪
        →Increase (1991-2015)")
       plt.legend()
       plt.grid(True, linestyle="--", alpha=0.5)
       # Show the plot
       plt.show()
```



Compare your elasticity estimates from 1970-1990 versus those from 1991-2015. Are they different? If so, why?

The decrease in price elasticity over time suggests that non-price factors (e.g., regulations, health awareness, smoking bans) played a growing role in reducing cigarette consumption, making smokers less sensitive to price changes.