## Programming Assignment: Neural Network Learning

**Deadline** The assignment was due on August 26, 11:59 PM PDT You can still pass this assignment before the course ends.

Instructions

My submission

**Discussions** 

← Assignment: Neural Network Learning



## ex4 Tutorial for forward propagation and cost

Tom Mosher Mentor Assignment: Neural Network Learning · 3 years ago · Edited

Note: this thread is closed to comments. If you have a question, please post it in the Week 5 Discussion Forum area.

This tutorial uses the vectorized method. If you're using a for-loop over the training examples, you're doing it the hard way, and you're on your own.

A note on Errata: The cost and gradient equations in the ex4.pdf file are correct. There may be some errata in the video lectures. Check the Course Wiki to be sure.

I'll use the less-than-helpful greek letters and math notation from the video lectures in this tutorial, though I'll start off with a glossary so we can agree on what they are. I will also suggest some common variable names, so students can more easily get help on the Forum.

It is left to the reader to convert these descriptions into program statements. You will need to determine the correct order and transpositions for each matrix multiplication, so that the result has the correct size.

#### **Glossary:**

Each of these variables will have a subscript, noting which NN layer it is associated with.

 $\Theta$ : A Theta matrix of weights to compute the inner values of the neural network. When we used a vector theta, it was noted with the lower-case theta character  $\theta$ .

a: The "activation" output from a neural layer. This is always generated using a sigmoid function g() on a z value. A typical variable name would be "a2".

 $\delta$  : lower-case delta is used for the "error" term in each layer. A typical variable name would be "d2".

 $\Delta$ : upper-case delta is used to hold the sum of the product of a  $\delta$  value with the previous layer's a value. In the vectorized solution, these sums are calculated automatically though the magic of matrix algebra. A typical variable name would be "Delta2".

 $\Theta$ \_gradient: This is the thing we're solving for, the partial derivative of theta. There is one of these variables associated with each  $\Delta$ . These values are returned by nnCostFunction(), so the variable names must be "Theta1\_grad" and "Theta2\_grad".

g() is the sigmoid function.

g'() is the sigmoid gradient function.

Tip: One handy method for excluding a column of bias units is to use the notation SomeMatrix(:,2:end). This selects all of the rows of a matrix, and omits the entire first column.

See the Appendix at the bottom of the tutorial for information on the sizes of the data objects.

A note regarding bias units, regularization, and back-propagation:

There are two methods for handing exclusion of the bias units in the Theta matrices in the back-propagation and gradient calculations. I've described only one of them here, it's the one that I understood the best. Both methods work, choose the one that makes sense to you and avoids dimension errors. It matters not a whit whether the bias unit is excluded before or after it is calculated - both methods give the same results, though the order of operations and transpositions required may be different. Those with contrary opinions are welcome to write their own tutorial.

#### **Forward Propagation:**

We'll start by outlining the forward propagation process. Though this was already accomplished once during Exercise 3, you'll need to duplicate some of that work because computing the gradients requires some of the intermediate results from forward propagation. Also, the y values in ex4 are a matrix, instead of a vector. This changes the method for computing the cost J.

1 - Expand the 'y' output values into a matrix of single values (see ex4.pdf Page 5). This is most easily done using an eye() matrix of size num\_labels, with vectorized indexing by 'y'. A useful variable name would be "y\_matrix", as this...

Note: For MATLAB users, this expression must be split into two lines, such as...

Q

#### coursera

- 1 eye\_matrix = eye(num\_labels)
- 2 y\_matrix = eye\_matrix(y,:)

#### 2 - Perform the forward propagation:

 $a_1$  equals the X input matrix with a column of 1's added (bias units) as the first column.

 $z_2$  equals the product of  $a_1$  and  $\Theta_1$ 

 $a_2$  is the result of passing  $z_2$  through g()

Then add a column of bias units to  $a_2$  (as the first column).

NOTE: Be sure you DON'T add the bias units as a new row of Theta.

 $z_3$  equals the product of  $a_2$  and  $\Theta_2$ 

 $a_3$  is the result of passing  $z_3$  through g()

#### Cost Function, non-regularized:

3 - Compute the unregularized cost according to ex4.pdf (top of Page 5), using  $a_3$ , your y\_matrix, and m (the number of training examples). Note that the 'h' argument inside the log() function is exactly a3. Cost should be a scalar value. Since y\_matrix and a3 are both matrices, you need to compute the double-sum.

Remember to use element-wise multiplication with the log() function. For a discussion of why you can't (easily) use matrix multiplication here, see this thread:

https://www.coursera.org/learn/machinelearning/discussions/weeks/5/threads/ag\_zHUGDEeaXnBKVQldqyw

Also, we're using the natural log, not log10().

Now you can run ex4.m to check the unregularized cost is correct, then you can submit this portion to the grader.

#### **Cost Regularization:**

4 - Compute the regularized component of the cost according to ex4.pdf Page 6, using  $\Theta_1$  and  $\Theta_2$  (excluding the Theta columns for the bias units), along with  $\lambda$ , and m. The easiest method to do this is to compute the regularization terms separately, then add them to the unregularized cost from Step 3.

You can run ex4.m to check the regularized cost, then you can submit this portion to the grader.

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Appendix:
Here are the sizes for the Ex4 character recognition example, using the method described
in this tutorial.
NOTE: The submit grader (and the gradient checking process) uses a different test case; these sizes are NOT for the submit grader or for gradient checking.
a1: 5000x401
z2: 5000x25
a2: 5000x26
a3: 5000x10
d3: 5000x10
d2: 5000x25
Theta1, Delta1 and Theta1_grad: 25x401
Theta2, Delta2 and Theta2_grad: 10x26
=======
Here is a link to the test cases, so you can check your work:
https://www.coursera.org/learn/machine-learning/discussions/iyd75Nz_EeWBhgpcuSIffw
The test cases for ex4 include the values of the internal variables discussed in the tutorial.
=======
keywords: ex4 tutorial nncostfunction forward propagation

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Krishnang

Krishnang Dalal · 2 years ago

Hello Tom,

☆ 86 Upvotes

Reply

Can you please briefly explain what is double sum doing based on the cost function formula? Also where is the formula to calculate 'grad'?



# Tom Mosher Mentor · 2 years ago



The double-sum() is summing over the rows and columns of the cost values.

The grad formula is in the exercise PDF file.

↑ 16 Upvotes



victor yampolsky  $\cdot$  2 years ago  $\cdot$  Edited by moderator

I'm so frustrated...

I worked all night and morning on this and I still cant submit succesfully.

even when I regularize the cost function J in nnCostfunction the submit. only successful (partly) when I mark the regularization as comment this works:

1	{code removed}			

please HELP. this is really frustrating!!!

in general went through the tutorial, there is some issues with the matrices sizes in the appendix.

I really need help:

this is the full code:

why on earh this is wrong?

1 {code removed}

I anyone can help I'll be greatfull!!!



Paul T Mielke Mentor · 2 years ago

Hi, Victor.

I'm sorry that you are frustrated by this, but we are not allowed to post source code for solutions in this course. It probably will not be any consolation, but this assignment is by far the most challenging in the entire course. When you

say that your code is not generating the correct results, do you mean that you are using Tom's test that submit is failing. Q Also I'm not understanding your comment about setting lambda = 1 making everything work. I notice that you have the value of lamdba hard-wired to 1 and are ignoring the passed in argument in your code as posted. That's got to be a big clue as to what is wrong. ☆ 5 Upvotes Tom Mosher Mentor ⋅ 2 years ago Sorry, students are not allowed to post their code, per the course Honor Code. The matrix sizes in the appendix are correct. ⊕ 0 Upvotes Ayodeji Kuponiyi · 2 years ago · Edited by moderator Hi Tom, thanks a lot for you time and help. Up until this point everything worked well. I'm not sure what I am doing wrong with the FeedForward program, could you kindly help look through my pseudocode: I followed the following steps: {Mentor edit: detailed line-by-line code description removed} It runs without error but no marks. **Thanks**  ↑ 0 Upvotes ☐ Hide 2 Replies Tom Mosher Mentor · 2 years ago Your description is just as detailed as actually posting the code itself, which is not allowed under the course Honor Code. So I cannot comment on it. You may be able to debug your code by using the additional test cases, from

ΑK

the Resources menu.

AK Ayodeji Kuponiyi · 2 years ago

Apologies Tom and to the forum, it's my first time of posting and was trying to present my steps without being too vague. I promise that won't happen next time. I'd try the additional test cases.

**Thanks** 

û Upvotes

AS Andrey Shkabko · 2 years ago · Edited

About regularization term writtent in ex4.pdf p.6.

The sum for k should be from 1 to 401 and from 1 to 26 to get "correct" J = 0.383770 after biases (k=1) removal (and sum for k = 2 to 401 and k = 2 to 26).

If you do it according to the formula written in ex4.pdf p.6 than ....Theta1(:,2:400).^2)... and 0.381095 is a correct J

JF Justin Francis · 2 years ago

Sorry if this has been asked before already Tom, but exactly how is

y\_matrix = eye(num\_labels)(y,:)

Creating the indexed matrix of the values of y. I understand what it creates but how is it doing this?



Tom Mosher Mentor · 2 years ago · Edited

Reading left to right, it creates an eye matrix of num\_labels size. Then it uses 'y' as a vectorized index. For each value in y, it copies that row of the eye matrix into y\_matrix. That's what the (y,:) does - the colon means "use all columns".

Note that MATLAB doesn't support this syntax, so it must be split into two lines of code.

↑ 10 Upvotes



Paul T Mielke Mentor · 2 years ago · Edited

It's easier to understand if you split it into two lines:

So what that says is we index the rows of A using the vector y and then the ":" in the column position means "Use all corresponding columns of that row". So the first row of the output matrix will be determined by using y(1) to select one of the rows of A (which is eye(n)). And so on through the y vector. So each row of the output is the row of I(n) that corresponds to the value of y(i).

Justin Francis · 2 years ago

It finally clicks in my brain, my logic in explaining y\_matrix = A(y,:) follows:

For each value of y it creates a new matrix with the value of the y'th row in A

Seems so simple now but I could not wrap my mind around it earlier.

H Harpreet · 2 years ago

For calculating the delta\_2 correctly I have to do delta\_2 := delta\_2(:,2:end) in step 3 and skip this in step 4. If I dont do it my matrix multiplications and element multiplication with sigmoid doesnt work correctly. I do it after doing Theta2'\*delta\_3 and before element multiplication with sigmoid.

SB Suraj Bhandari · 2 years ago

Hi Tom,

In the videos, Andrew says that we don't calculate error term for input layer. So there isn't any  $\partial 1$  (smaller delta-1). So for a 3 layer network, we will have just  $\partial 3$  and  $\partial 2$ . But when we calculate  $\Delta$  (bigger delta) for the same 3 layer network, we don't have  $\Delta 3$  (bigger delta-3) and all we can have is  $\Delta 1$  and  $\Delta 2$ . If  $\Delta$  (bigger delta) is to accumulate the error, why do we have it for layer 1 and not for 3? Or am I missing something here? Please help.



Tom Mosher Mentor · 2 years ago

There are a lot of errors in the video lectures - especially for the NN exercise.

I'm not familar with this particular question. Maybe check the Course Wiki and see if there are some better notes on this lecture.

SB Suraj Bhandari · 2 years ago

Sure Tom. I'll go through the wiki.

↑ 0 Upvotes

JR Jeffrey Robinson · 2 years ago

The neural network in my brain couldn't manage the very first task of this assignment...until I read Tom's tutorial. Thanks, Tom. There was a huge difference in complexity between what I was trying to do and what the final solution ended up being -- such a simple and elegant line of code, whereas I was trying all sorts of for loops and other nonsense. Wow!



Tom Mosher Mentor · 2 years ago

Once you start thinking like a matrix, it all becomes clear.

MS MAHATHI SRINIVASAN · 2 years ago

hello,

i have followed the steps of calculating the non-regularized cost function using vector implementation. My a3 is of the correct dimension(5000 X 10) .i have performed element- wise multiplication of the two matrices(log of a3 and  $y_matrix$ (which is also5000 X 10)) but my answer comes out as

Cost at parameters (loaded from ex4weights): -66.727017

(this value should be about 0.287629).

i have used the correct formula. I am unable to figure out the error. How to rectify this and get the expected answer?

Also, are all the entries of matrices Theta1 and Theta2 from ex4weights.mat zero?

thanks,

↑ 2 Upvotes



Tom Mosher Mentor ⋅ 2 years ago

No, they are not all zero.

Tom Mosher Mentor · 2 years ago

Good news.

M manish · 2 years ago · Edited

Hi,

I'm following correct steps, dimensions of matrix are also correct(printing at each step for debug) but still I'm getting cost as -25.484421 instead of 0.287629. Plz help.

In last step I'm doing matrix multiplication for a3 and y.(transpose of y). which gives 10x10 matrix. Then double sum over the result dividing by input size. I'm not clear where I'm going wrong. Signs are used as per PDF.

TIA.

T	0 Upvotes	



Tom Mosher Mentor ⋅ 2 years ago

The tutorial says to use element-wise multiplication.

↑ 1 Upvote

M manish · 2 years ago

element wise multiplication gives me same answer. :(

↑ 0 Upvotes

M manish ⋅ 2 years ago

Hi Tom,

I figured out that I was passing a3 again through sigmoid function. But when I removed that part of code I'm getting NaN instead of cost. Any clue where I'm going wrong?

TIA.

↑ 0 Upvotes



Tom Mosher Mentor · 2 years ago · Edited

Im your post, you said "In the last step...". Can you be specific which "last step" you're referring to?

When you element-wise multiply using the log() of a3 and y\_matrix, the results should be size (m x k); that is,  $5000 \times 10$ , not  $10 \times 10$ . So I don't really understand what you're doing well enough to offer any advice.

⊕ 0 Upvotes

Reply

RLi · 2 years ago

⊕ 0 Upvotes

Tks Tom



Michael Hesse · 2 years ago

#### coursera



Thanks Tom. Was really scratching my head about an efficient way to compute y\_matrix from y. :-)

↑ 1 Upvote

Reply



Julie Lorin · 2 years ago

Hi,

I have another question about the computation of the cost function. I'd just like to check if I am doing it the correct way of if there is a better way. (It is annoying not to be able to just copy paste my code in this situation :D )

I took the cost "formula" from the previous exercice, but as I am doing it with matrix instead of vector, my result is a 10\*10 matrix, instead of a scalar. In this 10\*10 matrix, I only keep the diagonal (using a .\* eye(10)) and I sum and sum again this result, which gives me a correct cost (well after my division by m and the regularization if I need it). I am kind of sceptic with this method, because I compute thing that I don't use after (everything that is not on the diagonal), so I am thinking that maybe there is a better way.

I had to put all my matrices on paper to find this logic, and it works both for the cost and the regularization, but is this the better way?

#### Thanks!

↑ 1 Upvote

Hide 4 Replies



Tom Mosher Mentor · 2 years ago

I presume you've read the tutorial at the top of this thread.

A modification to your method would be using the trace() function, instead of using element-wise multiplication by an eye matrix.

Which method is better depends on how you define "better".

û ∪ Upvotes



Julie Lorin · 2 years ago

Thanks for the answer! I didn't know the trace function but it seems way easier than my multiplication by the eye matrix and then my double sum. It does exactly what I wanted (sum the diagonal elements). At least it conforts me that I was not totally wrong with my method and that I have to calculate useless numbers (the ones that are not in the diagonal). I just wanted to know if there was a "cleaner" method where we doesn't need to compute those numbers not on the diagonal.

(I am only a beginner in this, I am trying to do it the best way each time but matrix calculations are classical me and I am not too good with the computation cost of my method! So maybe it is the best way:))

Q

û Upvotes



Tom Mosher Mentor · 2 years ago

The knock against trace() is that it is reputed to run rather slowly.

You can instrument your code by framing it with the "tic" and "toc" statements. When "tic" is executed, a timer is started. When "toc" is executed, the timer is stopped and the runtime is displayed. It's one of several ways of measuring relative code performance.

↑ 0 Upvotes



Julie Lorin · 2 years ago

Thanks for the info, I'll try that!

û Upvotes



Darwin R.C. · 2 years ago

Good day, all

I know I'm missing something here, I followed the tutorial but I'm getting the following results with the test case without regularization:

```
J = -19.281
2
   grad =
3
4
   -0.56599
5
   -0.56063
6 -0.55609
7
   -0.55228
8 -0.77765
9
10
11
12
```

I also don't understand what is meant by "NOTE: Be sure you DON'T add the bias units as a new row of Theta."

Maybe my issue lies there.

Can anyone give me a hint about it?



Tom Mosher Mentor · 2 years ago

The note is a reminder that bias units are columns, not rows. It is frightfully easy to make some datings in the cost function and still end up with a NNQ that almost works.

The cost J should always be a positive value. Be sure you haven't made any sign errors. The first thing to check is that you're using the equations from the ex4.pdf file, and not the ones you may have seen in the videos.

↑ 0 Upvotes



Darwin R.C. · 2 years ago

Thanks for your quick answer Tom, I will take a look at my equation, surely the problem is there then.

↑ 0 Upvotes



Darwin R.C. · 2 years ago

Just found my mistake... I was using y instead of y\_matrix in the formula. I can't believe I spent 3 hours struggling with this :( Thanks for the insight Tom!

↑ 2 Upvotes



Tom Mosher Mentor · 2 years ago

Good catch. As I said, "frightfully easy...".

↑ 0 Upvotes



Julie Lorin · 2 years ago · Edited

Hi,

I hope the question hasn't been already asked, but I didn't find it. For the first step, to have the y matrix, I don't understand why it works.

I tested the code in command line, but I don't understand. Working with matrix, and selecting them is not the most natural thing for me yet.

First, I don't understand why we need the "eye" matrix, and not one full of zeros (but I may understand this part if I understood the next, I guess)

I don't understand why selecting eye\_matrix(y,:) gives the good result. y is a vector of values between 1 and 10, and for me, the y here must be used to select the rows, and then saying all columns. And the result is supposed to have 5000 rows, but we only select from a 10 rows matrix. I guess I totally misunderstood what this does, but I can't figure out myself. So what happens here?

When I first did it without the tutorial, I had to use a for loop as I was unable to do it in a vectorized way like this!



Tom Mosher Mentor · 2 years ago · Edited

Good questions.

The 'y' vector we're provided in this exercise is valued from 1 to 10, just as it was in ex3. But to train a logistic classifier, we need the output values to be 0's and 1's only.

Q

In ex3, we accomplished this by using the code "y == c" inside the for loop from c=1:num\_labels. That gives us 0's and 1's like this (try the commands in your console):

```
1  y = [1 3 4 2]
2  c = 2
3  y == c
```

On each iteration of the loop, the statement "y == c" returns a different vector, which is passed to our cost function as the 'y' values it expects. Each pass through the for-loop give us back a theta vector, which is trained to recognize one class only.

In ex4, we also need to train on 0's and 1's. But since we're training all 10 classifiers at once (the NN has 10 outputs), we can't use 'y' as a vector. 'y' must be a matrix, and since this is a classifier, the values must be limited to only 0's and 1's.

That's where the eye matrix trick comes in.

The statement "eye(num\_labels)" returns an identity matrix. For each row, there is a '1' in a single column. That's perfect for training all of our classifiers at once. There is one column for each label.

The syntax "y\_matrix = eye(num\_labels)(y,:)" is a vector addressing trick. For each row of 'y', the statement is executed once. The 'y' value is an index into the identity matrix. Essentially, 'y,:' causes the appropriate row of the identity matrix to be copied entirely and placed in y\_matrix.



Tom Mosher Mentor · 2 years ago

Example for eye\_matrix:

```
1  y = [1 3 4 2]
2  eye_matrix(4)
3  y_matrix = eye_matrix(y,:)
4  |
```



Tom Mosher Mentor · 2 years ago



Also note, I've edited my previous posts, so please refresh your browser to get the latest version.

û Upvotes



Julie Lorin · 2 years ago

Hi! Thanks for the answer! I think that I understand this way better! As y is full of numbers between 1 and 10, the (y,:) selects the row with the same index as the number in y (as the first parameter is the row selection). (That's what I understood, I may not be explaining it very well, but I was trying to tell it in my own words so that if I totally misunderstood, someone can tell me:D)

Anyway, I think that I got it, it makes sense! Thanks!

↑ 0 Upvotes



June Yu · 2 years ago

This makes alot more sense to me now as well! Thanks, Tom!

û 0 Upvotes

JR Jonathan Roman · 2 years ago

Super dumb questions: What does "train a logistic classifier" mean?

Is num\_labels the number of classifiers?

(I successfully submitted this assignment-just asking a dumb question)

⊕ 0 Upvotes



Tom Mosher Mentor · 2 years ago · Edited

Is num\_labels the number of classifiers?

Yes. It can be called the number of labels, the number of classes, or the number of NN outputs.

↑ 0 Upvotes

LL lennie leong · 2 years ago

HI Tom and mentors,

### coursera

I am curenttly getting " J = NaN 1.6054 0.5897 3.0771 2.0912" & I am not able to get the correct scores. Is there any areas where i could look at to solve the problem?

Q

(On a side note: i had used the test cases. My results for J were: J = NaN 5.7023 6.2358 6.7824 7.3402, and my "grad" were all zeros.)

please help mentors. Thank you very much in advanced!

Û	0 Upvotes	
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Tom Mosher Mentor · 2 years ago · Edited

The cost "J" should be a scalar. Yours appears to be a vector. Fix that first.

Follow the tutorial. Use the test cases. Really, everything we know about this exercise is right there.

There's not much more help we can offer than that.

↑ 0 Upvotes

LL lennie leong · 2 years ago

Thanks Tom,

I had relooked at my codes. I think I am getting close. Currently, my

J = 2.4593 0.5791 1.2843 3.6999 1.4549

It is still a vector though. I would like to check, scalar is just one number. How do I turn my J into scalar?

I was searching "scalar" in the search bar but it isn't returning much discussions around "scalar". Is there any link / test cases you can direct me for this insight please?

Thank you very much in advanced!

⊕ 0 Upvotes



Tom Mosher Mentor · 2 years ago

Please re-read the last two lines of my previous post.

 $\,\,\,\,\,\,\,$  0 Upvotes

I had re-read it. Using the test cases, it seems that my z3 (i.e product a2 and theta2) is having error: "Error using \* Inner matrix dimensions must agree", "Error in nnCostFunction"

Q

I had printed both a2 and Theta 2. a2 is showing 16x4 matrix. while Theta2 is showing 4x5 matrix. And i took product of the 2 which prints out 16x5. But when i did a test case, it is showing this error. (No transposition were used)

this seems odd given i am very sure i didn't make a error. more specifically, i understand that if Matrix  $A = h \times r$ , and Matrix  $B = r \times t$ . Multiplying A\*B gives us a  $h \times t$  matrix.

Can mentors kindly help please?

↑ 0 Upvotes

LL lennie leong · 2 years ago · Edited

I was also re-reading the tutorials. Tom mentioned about:

"Then add a column of bias units to a2 (as the first column).

NOTE: Be sure you DON'T add the bias units as a new row of Theta"

What does it mean to say dont add ... as a new row of Theta? I had added a column of 1's in a2. ie. Initially a2 = 16x4. Now, a2 = 16x4 (but with 1's on first column). I used someMatrix(:,1) = 1. Not sure this might be the hiccup - as i don't quite understand this part after re-reading it again. Just wanted to be sure i am working them on the right track.

Using the test-case, it has showed:

a2 = [1.0000 0.5415; 1.0000 0.3571; 1.0000 0.7088]

I = 0

Grad = column\_of\_zeros

û Upvotes



Tom Mosher Mentor · 2 years ago · Edited

Don't do what it says to not do, and you'll be fine.

↑ 0 Upvotes

LL lennie leong · 2 years ago · Edited

My a2 is a matric of 16x4 now. Should it remain 16x4 after adding 1's?

I'm just curious why is Theta in the picture when we are working on a2.

