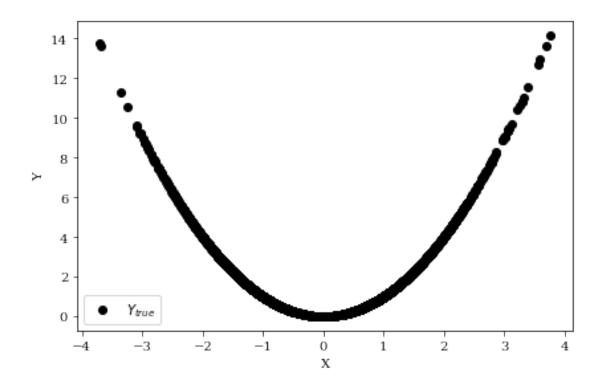
DLM_basic

January 29, 2019

```
In [1]: # IMPORT PACKAGES
        from keras.layers import Input, Dense, Dropout
        from keras.models import Model
        from keras.callbacks import EarlyStopping, ReduceLROnPlateau, CSVLogger
        from sklearn.metrics import mean_squared_error
        import numpy as np
        from matplotlib import rcParams # next 3 lines set font family for plotting
        rcParams['font.family'] = 'serif'
        rcParams['font.sans-serif'] = ['TImes New Roman']
        import matplotlib.pyplot as plt
        import os
        import time
In [2]: # SETTINGS FOR REPRODUCIBLE RESULTS DURING DEVELOPMENT
        #import numpy as np
        import tensorflow as tf
        import random as rn
        # The below is necessary in Python 3.2.3 onwards to
        # have reproducible behavior for certain hash-based operations.
        # See these references for further details:
        # https://docs.python.org/3.4/using/cmdline.html#envvar-PYTHONHASHSEED
        # https://github.com/keras-team/keras/issues/2280#issuecomment-306959926
        #import os
        os.environ['PYTHONHASHSEED'] = '0'
        # The below is necessary for starting Numpy generated random numbers
        # in a well-defined initial state.
        np.random.seed(42)
        # The below is necessary for starting core Python generated random numbers
        # in a well-defined state.
        rn.seed(12345)
```

```
# Force TensorFlow to use single thread.
        # Multiple threads are a potential source of
        # non-reproducible results.
        # For further details, see: https://stackoverflow.com/questions/42022950/which-seeds-hau
        session_conf = tf.ConfigProto(intra_op_parallelism_threads=1, inter_op_parallelism_thread
        from keras import backend as K
        # The below tf.set_random_seed() will make random number generation
        # in the TensorFlow backend have a well-defined initial state.
        # For further details, see: https://www.tensorflow.org/api_docs/python/tf/set_random_see
        tf.set_random_seed(1234)
        sess = tf.Session(graph=tf.get_default_graph(), config=session_conf)
        K.set_session(sess)
In [3]: # Create some simple data for a known function (y = x^2)
        # generate 100,000 samples (x dimension) with 1 features each (y dimension)
        X = np.random.randn(100000,1)
        Y = np.square(X)
        X_Nfeatures = X.shape[1]
        Y_Nfeatures = Y.shape[1]
        # partition X and Y into training (90%) and test (10%) sets
        X_train = X[:90000,:]
        X_{\text{test}} = X[90000:,:]
        Y_train = Y[:90000,:]
        Y_{test} = Y[90000:,:]
        print('X dimensions:',X.shape)
        print('Y dimensions:',Y.shape)
        fig = plt.figure(num=1)
        ax = fig.add_subplot(111)
        y_true = ax.plot(X_test,Y_test,'ko',label=r'$Y_{true}$')
        ax.set_xlabel('X')
        ax.set_ylabel('Y')
        curves = y_true
        labels = [c.get_label() for c in curves]
        ax.legend(curves, labels, loc=0)
        plt.tight_layout()
        plt.savefig('ytrue.pdf')
        plt.show()
```

X dimensions: (100000, 1)
Y dimensions: (100000, 1)



```
In [4]: # Build the DLM
       tic = time.time()
                          # start a timer
        # HYPERPARAMETERS
       epochs = 5000
       batch_size = 5000
       do = 0.2
       N_nodes = 64
        # create input layer.....
       main_input = Input(shape=(X_Nfeatures),
                          dtype='float',
                          batch_shape=(batch_size,X_Nfeatures),
                          name='main_input'
                          )
        #create hidden layer.....
       hidden_layer1 = Dense(N_nodes, activation='relu', name='hidden_layer1')(main_input)
        # add dropout to hidden layer
       Dropout(do)(hidden_layer1)
```

```
hidden_layer2 = Dense(N_nodes, activation='relu', name='hidden_layer2')(hidden_layer1)
# add dropout to hidden layer
Dropout(do)(hidden_layer2)
# create output layer
main_output = Dense(Y_Nfeatures, name='main_output')(hidden_layer2) # default
activation is linear
# feed datasets into model for training
model = Model(inputs=[main_input],
              outputs=[main_output]
# compile the model with desired configuration
model.compile(loss='mean_squared_error',
              optimizer='adagrad',
              metrics=['mae'])
# one of several callbacks available in Keras, csv_logger saves metrics for every epoch
csv_logger = CSVLogger('training_' + str(epochs) + '.log')
early_stop = EarlyStopping(monitor='val_loss', # quantity to monitor
                           min_delta=0.0001, # min change to qualify as an improvement
                           patience=10, # stop after #epochs with no improvement
                           verbose=1) # print messages
reduce_lr = ReduceLROnPlateau(monitor='val_loss',
                              factor=0.2, # reduction factor (new_lr = lr * factor)
                              patience=5,
                              verbose=1)
# train the model, and store training information in the history object
history = model.fit([X_train],[Y_train],
                    epochs=epochs,
                    batch_size = batch_size,
                    validation_data=(X_test, Y_test),
                    callbacks=[reduce_lr,early_stop,csv_logger]
model.summary() # print out a summary of layers/parameters
config = model.get_config() # detailed information about the configuration
of each layer
# evaluate the trained model on the test data set
test = model.evaluate([X_test],[Y_test],batch_size=batch_size)
names = model.metrics_names
X_pred = np.random.randn(100000,1)
```

```
Y_mse = mean_squared_error(predict,Y_pred)
    print('Y_mse:',Y_mse)
Train on 90000 samples, validate on 10000 samples
Epoch 1/5000
Epoch 2/5000
Epoch 3/5000
Epoch 4/5000
90000/90000 [=============] - Os 1us/step - loss: 0.1642 - mean_absolute_error:
Epoch 5/5000
Epoch 6/5000
90000/90000 [=============] - Os 1us/step - loss: 0.0866 - mean_absolute_error:
Epoch 7/5000
90000/90000 [=============] - Os 1us/step - loss: 0.0676 - mean_absolute_error:
Epoch 8/5000
90000/90000 [============== ] - Os 1us/step - loss: 0.0547 - mean_absolute_error:
Epoch 9/5000
90000/90000 [=============] - Os 1us/step - loss: 0.0453 - mean_absolute_error:
Epoch 10/5000
90000/90000 [=============] - Os 1us/step - loss: 0.0384 - mean_absolute_error:
Epoch 11/5000
Epoch 12/5000
90000/90000 [=============] - Os 1us/step - loss: 0.0287 - mean_absolute_error:
Epoch 13/5000
90000/90000 [=============] - Os 1us/step - loss: 0.0252 - mean_absolute_error:
Epoch 14/5000
Epoch 15/5000
90000/90000 [=============] - Os 1us/step - loss: 0.0201 - mean_absolute_error:
Epoch 16/5000
Epoch 17/5000
Epoch 18/5000
90000/90000 [============== ] - Os 1us/step - loss: 0.0151 - mean_absolute_error:
Epoch 19/5000
Epoch 20/5000
90000/90000 [=============] - Os 1us/step - loss: 0.0129 - mean_absolute_error:
Epoch 21/5000
```

Y_pred = np.square(X_pred)

predict = model.predict([X_pred],batch_size=batch_size)

```
Epoch 22/5000
90000/90000 [=============] - Os 1us/step - loss: 0.0111 - mean_absolute_error:
Epoch 23/5000
90000/90000 [==============] - Os 1us/step - loss: 0.0105 - mean_absolute_error:
Epoch 24/5000
Epoch 25/5000
Epoch 26/5000
90000/90000 [============== ] - Os 1us/step - loss: 0.0087 - mean_absolute_error:
Epoch 27/5000
Epoch 28/5000
Epoch 29/5000
Epoch 30/5000
90000/90000 [=============] - Os 1us/step - loss: 0.0070 - mean_absolute_error:
Epoch 31/5000
Epoch 32/5000
90000/90000 [=============] - Os 1us/step - loss: 0.0064 - mean_absolute_error:
Epoch 33/5000
90000/90000 [=============] - Os 1us/step - loss: 0.0061 - mean_absolute_error:
Epoch 34/5000
90000/90000 [=============] - Os 1us/step - loss: 0.0058 - mean_absolute_error:
Epoch 35/5000
90000/90000 [=============] - Os 1us/step - loss: 0.0056 - mean_absolute_error:
Epoch 36/5000
90000/90000 [=============] - Os 1us/step - loss: 0.0054 - mean_absolute_error:
Epoch 37/5000
90000/90000 [=============] - Os 1us/step - loss: 0.0052 - mean_absolute_error:
Epoch 38/5000
90000/90000 [============== ] - Os 1us/step - loss: 0.0050 - mean_absolute_error:
Epoch 39/5000
90000/90000 [=============] - Os 1us/step - loss: 0.0048 - mean_absolute_error:
Epoch 40/5000
Epoch 41/5000
90000/90000 [============== ] - Os 1us/step - loss: 0.0045 - mean_absolute_error:
Epoch 42/5000
90000/90000 [=============] - Os 1us/step - loss: 0.0043 - mean_absolute_error:
Epoch 43/5000
Epoch 44/5000
Epoch 45/5000
90000/90000 [=============] - Os 1us/step - loss: 0.0040 - mean_absolute_error:
```

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Epoch 46/5000
90000/90000 [=============] - Os 1us/step - loss: 0.0038 - mean_absolute_error:
Epoch 47/5000
90000/90000 [=============] - Os 1us/step - loss: 0.0037 - mean_absolute_error:
Epoch 48/5000
Epoch 49/5000
Epoch 50/5000
90000/90000 [=============] - Os 1us/step - loss: 0.0034 - mean_absolute_error:
Epoch 51/5000
Epoch 52/5000
Epoch 53/5000
Epoch 54/5000
90000/90000 [=============] - Os 1us/step - loss: 0.0031 - mean_absolute_error:
Epoch 55/5000
Epoch 56/5000
90000/90000 [============== ] - Os 1us/step - loss: 0.0029 - mean_absolute_error:
Epoch 57/5000
90000/90000 [============== ] - Os 1us/step - loss: 0.0029 - mean_absolute_error:
Epoch 58/5000
90000/90000 [============== ] - Os 1us/step - loss: 0.0028 - mean_absolute_error:
Epoch 59/5000
90000/90000 [=============] - Os 1us/step - loss: 0.0028 - mean_absolute_error:
Epoch 60/5000
90000/90000 [=============] - Os 1us/step - loss: 0.0027 - mean_absolute_error:
Epoch 61/5000
90000/90000 [=============] - Os 1us/step - loss: 0.0026 - mean_absolute_error:
Epoch 62/5000
90000/90000 [============= ] - Os 1us/step - loss: 0.0026 - mean_absolute_error:
Epoch 63/5000
90000/90000 [============== ] - Os 1us/step - loss: 0.0025 - mean_absolute_error:
Epoch 64/5000
Epoch 65/5000
90000/90000 [=============] - Os 1us/step - loss: 0.0024 - mean_absolute_error:
Epoch 66/5000
90000/90000 [=============] - Os 1us/step - loss: 0.0024 - mean_absolute_error:
Epoch 67/5000
Epoch 68/5000
Epoch 69/5000
```

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Epoch 70/5000
90000/90000 [=============] - Os 1us/step - loss: 0.0022 - mean_absolute_error:
Epoch 71/5000
90000/90000 [=============] - Os 1us/step - loss: 0.0021 - mean_absolute_error:
Epoch 72/5000
Epoch 73/5000
Epoch 74/5000
90000/90000 [============== ] - Os 1us/step - loss: 0.0020 - mean_absolute_error:
Epoch 75/5000
Epoch 76/5000
Epoch 77/5000
Epoch 78/5000
90000/90000 [=============] - Os 1us/step - loss: 0.0019 - mean_absolute_error:
Epoch 79/5000
Epoch 80/5000
90000/90000 [============== ] - Os 1us/step - loss: 0.0018 - mean_absolute_error:
Epoch 81/5000
90000/90000 [=============] - Os 1us/step - loss: 0.0018 - mean_absolute_error:
Epoch 82/5000
90000/90000 [=============] - Os 1us/step - loss: 0.0018 - mean_absolute_error:
Epoch 83/5000
90000/90000 [=============] - Os 1us/step - loss: 0.0017 - mean_absolute_error:
Epoch 84/5000
90000/90000 [=============] - Os 1us/step - loss: 0.0017 - mean_absolute_error:
Epoch 85/5000
90000/90000 [=============] - Os 1us/step - loss: 0.0017 - mean_absolute_error:
Epoch 86/5000
90000/90000 [============== ] - Os 1us/step - loss: 0.0017 - mean_absolute_error:
Epoch 87/5000
90000/90000 [============== ] - Os 1us/step - loss: 0.0017 - mean_absolute_error:
Epoch 88/5000
Epoch 89/5000
90000/90000 [============== ] - Os 1us/step - loss: 0.0016 - mean_absolute_error:
Epoch 90/5000
90000/90000 [=============] - Os 1us/step - loss: 0.0016 - mean_absolute_error:
Epoch 91/5000
Epoch 92/5000
Epoch 93/5000
90000/90000 [=============] - Os 1us/step - loss: 0.0015 - mean_absolute_error:
```

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90000/90000 [=============] - Os 1us/step - loss: 0.0015 - mean_absolute_error:
Epoch 95/5000
90000/90000 [=============] - Os 1us/step - loss: 0.0015 - mean_absolute_error:
Epoch 96/5000
70000/90000 [===========>...] - ETA: Os - loss: 0.0014 - mean_absolute_error: 0.0066
Epoch 00096: reducing learning rate to 0.0019999999552965165.
90000/90000 [==============] - Os 1us/step - loss: 0.0015 - mean_absolute_error:
Epoch 97/5000
90000/90000 [============== ] - Os 1us/step - loss: 0.0014 - mean_absolute_error:
Epoch 98/5000
90000/90000 [=============] - Os 1us/step - loss: 0.0014 - mean_absolute_error:
Epoch 99/5000
90000/90000 [=============] - Os 1us/step - loss: 0.0014 - mean_absolute_error:
Epoch 100/5000
90000/90000 [=============] - Os 1us/step - loss: 0.0014 - mean_absolute_error:
Epoch 101/5000
90000/90000 [=============] - Os 1us/step - loss: 0.0014 - mean_absolute_error:
Epoch 102/5000
Epoch 103/5000
90000/90000 [============== ] - Os 1us/step - loss: 0.0014 - mean_absolute_error:
Epoch 104/5000
Epoch 105/5000
Epoch 106/5000
75000/90000 [===========>...] - ETA: Os - loss: 0.0012 - mean_absolute_error: 0.005
Epoch 00106: reducing learning rate to 0.0003999999724328518.
90000/90000 [=============] - Os 1us/step - loss: 0.0014 - mean_absolute_error:
Epoch 107/5000
Epoch 108/5000
90000/90000 [============== ] - Os 1us/step - loss: 0.0014 - mean_absolute_error:
Epoch 109/5000
Epoch 110/5000
90000/90000 [============== ] - Os 1us/step - loss: 0.0014 - mean_absolute_error:
Epoch 00110: early stopping
```

Epoch 94/5000

Layer (type)	Output Shape	Param #
main_input (InputLayer)	(5000, 1)	0
hidden_layer1 (Dense)	(5000, 64)	128
hidden_layer2 (Dense)	(5000, 64)	4160
main_output (Dense)	(5000, 1)	65

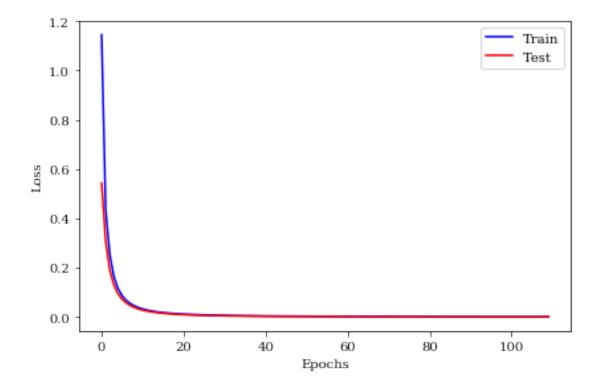
Total params: 4,353 Trainable params: 4,353 Non-trainable params: 0

10000/10000 [=========] - Os 1us/step

Y_mse: 0.001008258246466293

```
In [5]: loss_train = history.history['loss']
    loss_test = history.history['val_loss']
    xplot = list(range(len(loss_train)))

fig = plt.figure(num=2)
    ax = fig.add_subplot(111)
    train = ax.plot(xplot,loss_train,'b-',label='Train')
    test = ax.plot(xplot,loss_test,'r-',label='Test')
    ax.set_xlabel('Epochs')
    ax.set_ylabel('Loss')
    curves = train+test
    labels = [c.get_label() for c in curves]
    ax.legend(curves, labels, loc=0)
    plt.tight_layout()
    plt.savefig('loss' + str(epochs) + 'epochs.pdf')
    plt.show()
```



```
fig = plt.figure(num=3)
ax = fig.add_subplot(111)
y_true = ax.plot(X_pred,Y_pred,'ko',label=r'$Y_{true}$')
y_pred = ax.plot(X_pred,predict,'m*',label=r'$\hat{Y}$')
ax.set_xlabel(r'$X$')
ax.set_ylabel(r'$Y$')
curves = y_true+y_pred
labels = [c.get_label() for c in curves]
ax.legend(curves, labels, loc=0)
plt.tight_layout()
plt.savefig('ypred.pdf')
plt.show()
```

