

$$\left. \begin{aligned} \cdot \dot{q} &= f[q, p] \\ \cdot \dot{p} &= g[q, p] \end{aligned} \right\} \begin{aligned} \cdot \dot{q}[q_0, p_0] &= f[q_0, p_0] = 0 \\ \cdot \dot{p}[q_0, p_0] &= g[q_0, p_0] = 0 \end{aligned} \quad \left. \begin{aligned} (p_0, q_0) &:= \\ \text{punto fijo.} \end{aligned} \right\}$$

$$\cdot \delta \dot{q} = \frac{d}{dt} [\delta q] = \frac{\partial f}{\partial q}[q_0, p_0] \delta q + \frac{\partial f}{\partial p}[q_0, p_0] \delta p + \dots$$

$$\cdot \delta \dot{p} = \frac{d}{dt} [\delta p] = \frac{\partial g}{\partial q}[q_0, p_0] \delta q + \frac{\partial g}{\partial p}[q_0, p_0] \delta p + \dots$$

$$\rightarrow \frac{d}{dt} \begin{bmatrix} \delta q \\ \delta p \end{bmatrix} = \underbrace{\begin{bmatrix} \frac{\partial f}{\partial q}[q_0, p_0] & \frac{\partial f}{\partial p}[q_0, p_0] \\ \frac{\partial g}{\partial q}[q_0, p_0] & \frac{\partial g}{\partial p}[q_0, p_0] \end{bmatrix}}_M \underbrace{\begin{bmatrix} \delta q \\ \delta p \end{bmatrix}}_E$$

$$\Rightarrow \frac{d\bar{E}}{dt} = M\bar{E} \rightarrow \bar{E} = c_1 \bar{D}_1 e^{\lambda_1 t} + c_2 \bar{D}_2 e^{\lambda_2 t}$$

\*  $\bar{D}_i$  = autovectores  
\*  $\lambda_i$  = autovalores.

$$\left. \begin{aligned} \textcircled{b} \cdot x^2 &= 2x - y = 0 \Rightarrow y = 2x \Rightarrow \boxed{y = 0} \\ \cdot y^2 &= x + 2y = 0 \Rightarrow x + 4x = 0 \Rightarrow \boxed{x = 0} \end{aligned} \right\} \text{puntos fijos.}$$

$$\cdot x = 2xt - yt + x_0$$

$$\cdot y = xt + 2yt + y_0$$

$$M = \begin{bmatrix} 2 & -1 \\ 1 & 2 \end{bmatrix}$$

$$\cdot x = -i c_1 e^{(2-i)t} + c_2 [1+i] e^{(2+i)t}$$

$$\cdot y = c_1 e^{(2-i)t} + c_2 e^{(2+i)t}$$

$$\rightarrow \bar{D}_1 = \begin{bmatrix} -i \\ 1 \end{bmatrix} ; \lambda_1 = 2-i$$

$$\rightarrow \bar{D}_2 = \begin{bmatrix} i \\ 1 \end{bmatrix} ; \lambda_2 = 2+i$$