

We want to design an algorithm for a cryptocurrency startup. We're given two arrays of positive number $N = \{N_1, \dots, N_T\}$ and $W = \{W_1, \dots, W_T\}$ which represent the profits from NorthCoins and WestCoins respectively. Each type of coins requires its own software which takes 1 unit of time to load.

1. First we define several subproblems. Let $\text{ProfitN}(t)$ be the subproblem where the super-computer mines optimally for time intervals 1 to $t - 1$, and mines NorthCoins at time t . Likewise define $\text{ProfitW}(t)$ and $\text{ProfitLoad}(t)$ so that the computer mines WestCoins or loads software at time t , respectively. We order subproblems by increasing t . Let $\text{MaxProfit}(t)$ be the profit if the computer mines optimally for time intervals 1 to $t - 1$.
2. For $t = 1$, then $\text{MaxProfit}(1) = \max(N_1, W_1)$.
For $t = 2$, $\text{MaxProfit}(2) = \max(N_1 + N_2, W_1 + W_2)$.
3. The recurrence relation Let $\text{ProfitSwitch}(t)$

$$\text{MaxProfit}(t) = \max(\text{MaxProfit}(t - 2) + N_t, \text{MaxProfit}(t - 2) + W_t, \text{MaxProfit}(t - 1))$$

4. We prove that the recurrence relation is correct
5. An algorithm for finding a solution to the subproblem
6. An algorithm for finding the optimal solution to the original problem
7. The running time.