

RBE500: Foundations of Robotics

Week 10 : Joint Control

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Introduction

The purpose of this week's assignment was to practice and learn sampling methods in order to obtain an optimal mobile plan path. In this assignment, we were tasked with creating our own binary occupancy space. Using this space, the RRT sampling method of obtaining an optimal path was used. This is a very popular and useful method of sampling and branching out within the workspace for the purpose of discovering the best paths to the desired position.

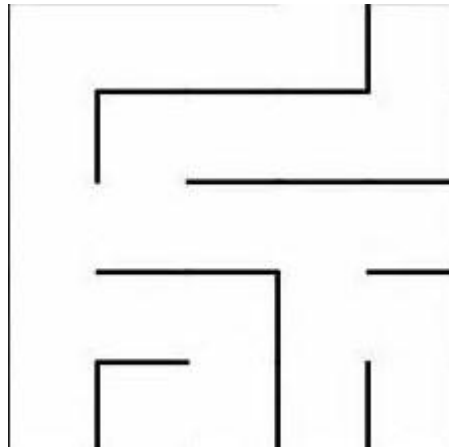


Figure 1 - Image used to create the pathmap

Methods and Results

For this assignment, I used two MATLAB source codes, to develop my solution.

First I used MATLAB's `binaryOccupancyMap` function to turn an RGB image of a maze into a binary image or mask that I can use to differentiate the free space and occupied space in my submission.

In order to accomplish this I needed to :

Create a state space.

```
clc; clear;
```

```
ss = stateSpaceSE2;
```

Create an occupancyMap-based state validator using the created state space.

```
sv = validatorOccupancyMap(ss);
```

Create an occupancy map from an image

```
%load exampleMaps  
image = imread('C:\Users\thomm\Documents\KATHIA\ez_ez.png');
```

Convert to grayscale and then black and white image based on given threshold value.

```
grayimage = rgb2gray(image);  
bwimage = grayimage < 150;
```

Use black and white image as matrix input for binary occupancy grid.

```
gridy = binaryOccupancyMap(bwimage);  
  
map = gridy;  
sv.Map = map;
```

Set validation distance for the validator.

```
sv.ValidationDistance = 0.05;
```

Update state space bounds to be the same as map limits.

```
ss.StateBounds = [map.XWorldLimits; map.YWorldLimits; [-pi pi]];
```

Create the path planner and increase max connection distance.

```
planner = plannerRRT(ss,sv);  
planner.MaxConnectionDistance = 0.5;
```

Set the start and goal states.

```
start = [50,200, 0];  
goal = [200,50,0];
```

Plan a path with default settings.

```
rng(100,'twister'); % for repeatable result  
[pthObj,solnInfo] = plan(planner,start,goal);
```

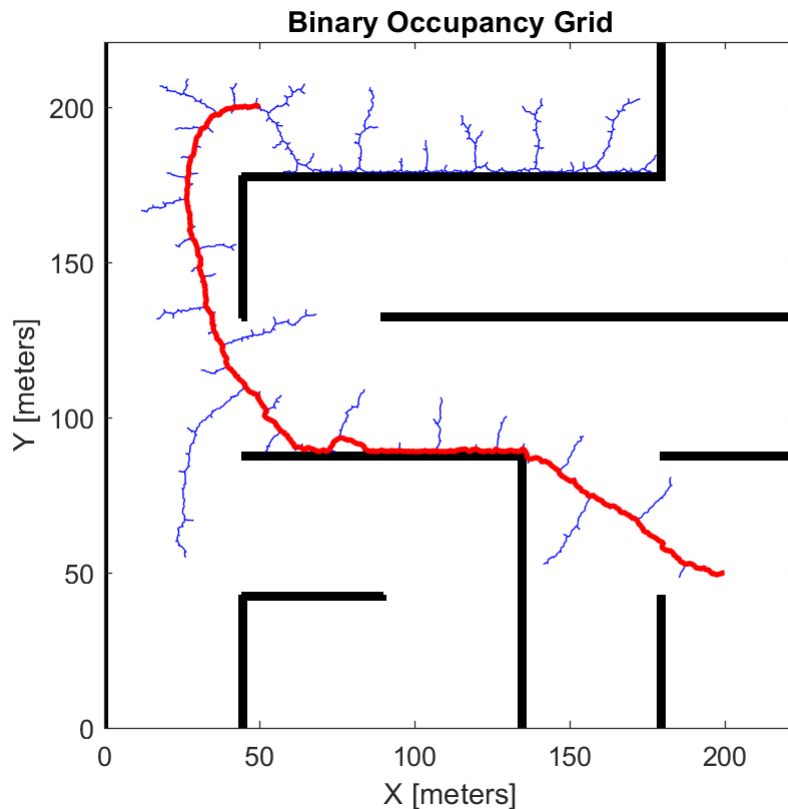
Visualize the results.

```
show(map)  
hold on
```

```

plot(solnInfo.TreeData(:,1),solnInfo.TreeData(:,2),'b-'); % tree expansion
plot(pthObj.States(:,1),pthObj.States(:,2),'r-','LineWidth',2) % draw path
hold off

```



Now graphing of Δx , Δy and $\Delta \theta$.

To do this I took the navpath object produced by the plan function and plotted the differential of its 3 outputs and against the step size.

This plot displays the change in direction per step size, which is the velocity of the system. Δx and Δy are linear velocities and $\Delta \theta$ is the angular velocity.

```

pathobj=pthObj % navpath object

```

```

pathobj =
  navPath with properties:

    StateSpace: [1x1 stateSpaceSE2]
      States: [647x3 double]
    NumStates: 647

```

```

figure
% delta x
%plot3(diff(pathobj.States(:,1)), diff(pathobj.States(:,2)), diff(pathobj.States(:,3)))
plot(diff(pathobj.States(:,1)));

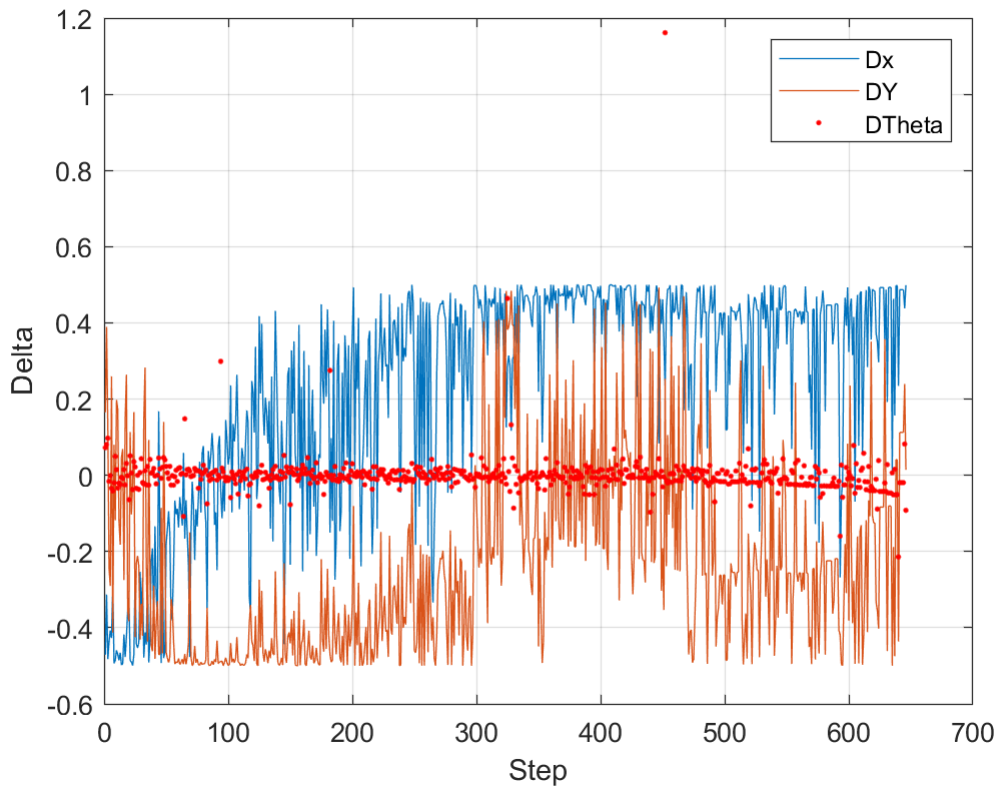
```

```

hold on
plot( diff(pathobj.States(:,2)));
hold on
plot(diff(pathobj.States(:,3)), '.r');
%hold on
%plot(diff(waypoints(:,1)),diff( waypoints(:,2)), ".r", "MarkerSize", 20);
grid on;

hold off
legend( 'Dx', 'DY', 'DTheta')
ylabel( 'Delta')
xlabel( 'Step')

```



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Discussion

This assignment involved using RRT, a sampling trial and error computational methods in order to obtain the most optimal path between the desired start and end position. While doing this assignment it was very interesting to manipulate the different parameters involved with RRT and then visualizing these changes by analyzing the resulting "optimal" path. While doing the first portion of this assignment I found that having a small validation and small connection distance produces the most straightforward and shortest path. Also while playing around with different work spaces, I found that smaller workspaces tend to have a better result.

The second portion of this assignment involved analyzing the differentials of the x and y position and the differential of theta of the system. In order to do this, I plotted these differentials on the same plot in order to better compare them. In the plot the differentials are plotted against a step, therefore the plot is showing velocity of x, y and theta. Looking at the plot it looks like the angle theta did not change much it was relatively stable, this was to be expected as the path produced by the algorithm did not involve a great amount of turn or angles. The x and y position differentials differ about the same.

All in all this was an interesting and short assignment. I really enjoyed learning and getting practice with the RRT method. It was interesting and very rewarding to see the parameters that affect the length of the optimal path.

References

(1) Spong et al. (2020). *Robot Modeling and Control* (2nd Edition). Wiley.