Exploration of Multiple Treatments on the Metabolic Efficiency of the Mitochondria

Dom Fenoglio, Brian Kim, Kathleen Zhang

1 Background

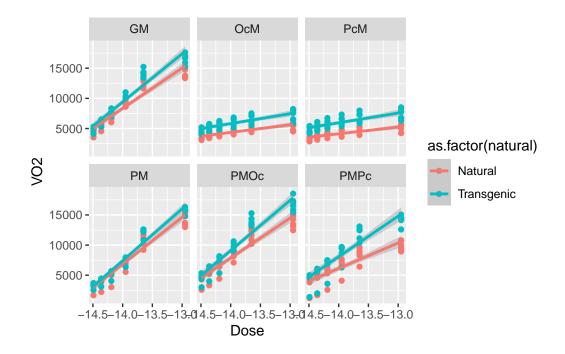
The mitochondria are considered the "powerhouse" of the cell, responsible for generating the cell's usable energy through oxidative phosphorylation, a process necessary for all biological processes, particularly in high-demand organs such as the heart, brain, and muscles. Their proper function is critical for overall health, as disruptions to their function are associated with various health issues, such as cancer, heart disease, and Alzheimer's.

One way to examine mitochondrial function is by using the multiplexed assay platform, a laboratory method that allows researchers to measure multiple dimensions of mitochondrial activity across different substrates and energy demand conditions. By measuring respiration rates under different combinations of substrates across different experimental settings, such as genetic background and dose, researchers hope to better understand these effects on the metabolic and functional phenotypes of mitochondria.

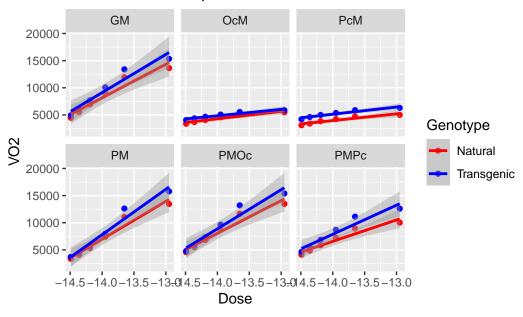
The main motivation for our analysis is to quantitatively test hypotheses about genetic changes on mitochondrial efficiency and energy production, and whether there is evidence that genotype effects (transgenic vs. natural mice) depend on substrate and/or dose. By building a modeling framework, we hope to determine how mitochondrial efficiency varies by substrate, genotype, and dose while capturing both fixed and random sources of variation.

- 2 Exploratory Data Analysis
- 3 Modeling
- 4 Analysis
- 5 Conclusion and Future Work
- 6 Appendix

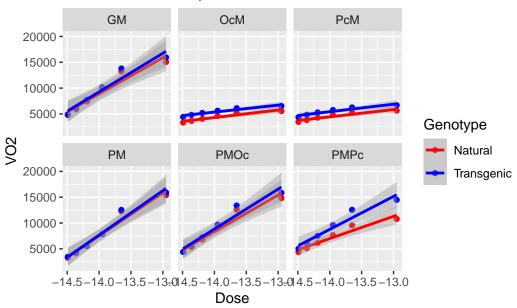
Exploratory Data Analysis



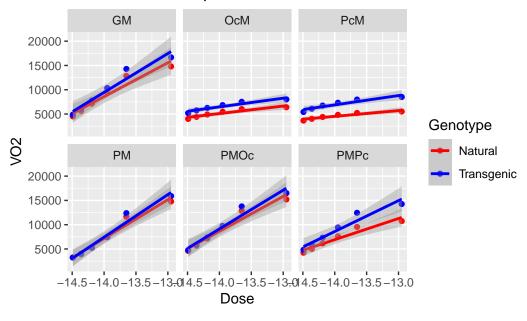
VO2 vs. Dose for pair 1



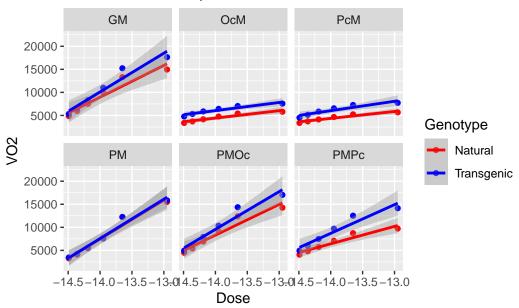
VO2 vs. Dose for pair 2



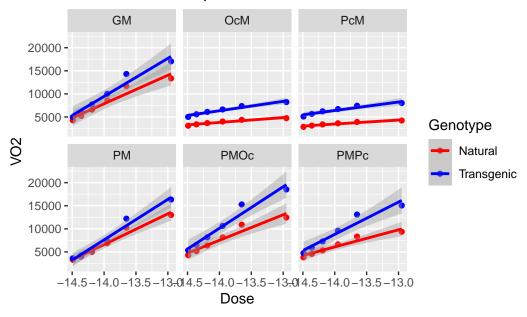
VO2 vs. Dose for pair 3



VO2 vs. Dose for pair 4



VO2 vs. Dose for pair 5



VO2 vs. Dose for pair 6

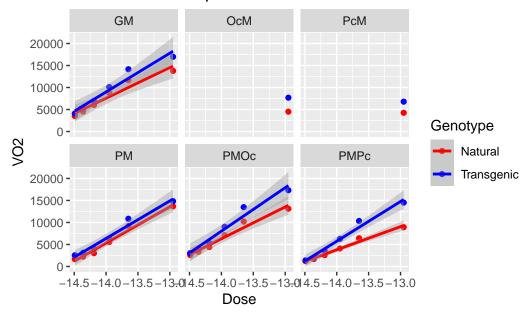


Table 1: Model comparison using AIC and Adjusted \mathbb{R}^2

Model	df	AIC	$Adjusted_R2$
Amino Acids	8	7439.921	0.721

Modeling

Call:

lm(formula = VO2 ~ Substrate:natural + Dose:natural:Substrate,
 data = data)

Residuals:

Min 1Q Median 3Q Max -3254.1 -370.8 186.2 536.4 1727.3

Coefficients: (1 not defined because of singularities)

	Estimate	Std. Error	t value	Pr(> t)
(Intercept)	138201.0	7230.7	19.113	< 2e-16 ***
SubstrateGM:naturalNatural	5077.4	10225.7	0.497	0.619863
SubstrateOcM:naturalNatural	-104126.4	10724.8	-9.709	< 2e-16 ***
SubstratePcM:naturalNatural	-107896.1	10724.8	-10.060	< 2e-16 ***
SubstratePM:naturalNatural	3735.0	10225.7	0.365	0.715163
SubstratePMOc:naturalNatural	-2949.2	10225.7	-0.288	0.773223
SubstratePMPc:naturalNatural	-49273.5	10225.7	-4.819	2.25e-06 ***
SubstrateGM:naturalTransgenic	27374.7	10225.7	2.677	0.007815 **
SubstrateOcM:naturalTransgenic	-99396.5	10724.8	-9.268	< 2e-16 ***
SubstratePcM:naturalTransgenic	-95812.6	10724.8	-8.934	< 2e-16 ***
SubstratePM:naturalTransgenic	14409.0	10225.7	1.409	0.159790
SubstratePMOc:naturalTransgenic	27257.2	10225.7	2.666	0.008081 **
SubstratePMPc:naturalTransgenic	NA	NA	NA	NA
bubbilatelii C.iiatulalilaiibgeiilC	IVA	11/11	1471	1111
SubstrateGM: naturalNatural: Dose	9596.5	511.7		
9			18.755	
SubstrateGM:naturalNatural:Dose	9596.5	511.7	18.755 3.766	< 2e-16 ***
SubstrateGM:naturalNatural:Dose SubstrateOcM:naturalNatural:Dose	9596.5 2110.8	511.7 560.5	18.755 3.766 3.317	< 2e-16 *** 0.000198 *** 0.001015 **
SubstrateGM:naturalNatural:Dose SubstrateOcM:naturalNatural:Dose SubstratePcM:naturalNatural:Dose	9596.5 2110.8 1859.4	511.7 560.5 560.5	18.755 3.766 3.317 18.806	< 2e-16 *** 0.000198 *** 0.001015 ** < 2e-16 ***
SubstrateGM:naturalNatural:Dose SubstrateOcM:naturalNatural:Dose SubstratePcM:naturalNatural:Dose SubstratePM:naturalNatural:Dose	9596.5 2110.8 1859.4 9622.6	511.7 560.5 560.5 511.7	18.755 3.766 3.317 18.806 17.714	< 2e-16 *** 0.000198 *** 0.001015 ** < 2e-16 *** < 2e-16 ***
SubstrateGM:naturalNatural:Dose SubstrateOcM:naturalNatural:Dose SubstratePcM:naturalNatural:Dose SubstratePM:naturalNatural:Dose SubstratePMOc:naturalNatural:Dose	9596.5 2110.8 1859.4 9622.6 9064.0	511.7 560.5 560.5 511.7	18.755 3.766 3.317 18.806 17.714 11.511	< 2e-16 *** 0.000198 *** 0.001015 ** < 2e-16 *** < 2e-16 ***
SubstrateGM:naturalNatural:Dose SubstrateOcM:naturalNatural:Dose SubstratePcM:naturalNatural:Dose SubstratePM:naturalNatural:Dose SubstratePMOc:naturalNatural:Dose SubstratePMPc:naturalNatural:Dose	9596.5 2110.8 1859.4 9622.6 9064.0 5889.9	511.7 560.5 560.5 511.7 511.7	18.755 3.766 3.317 18.806 17.714 11.511 21.713	< 2e-16 *** 0.000198 *** 0.001015 ** < 2e-16 *** < 2e-16 ***
SubstrateGM:naturalNatural:Dose SubstrateOcM:naturalNatural:Dose SubstratePcM:naturalNatural:Dose SubstratePM:naturalNatural:Dose SubstratePMOc:naturalNatural:Dose SubstratePMPc:naturalNatural:Dose SubstrateGM:naturalTransgenic:Dose	9596.5 2110.8 1859.4 9622.6 9064.0 5889.9 11110.1	511.7 560.5 560.5 511.7 511.7 511.7	18.755 3.766 3.317 18.806 17.714 11.511 21.713 4.186	< 2e-16 *** 0.000198 *** 0.001015 ** < 2e-16 *** < 2e-16 *** < 2e-16 ***
SubstrateGM:naturalNatural:Dose SubstrateOcM:naturalNatural:Dose SubstratePcM:naturalNatural:Dose SubstratePM:naturalNatural:Dose SubstratePMOc:naturalNatural:Dose SubstratePMPc:naturalNatural:Dose SubstrateGM:naturalTransgenic:Dose SubstrateOcM:naturalTransgenic:Dose	9596.5 2110.8 1859.4 9622.6 9064.0 5889.9 11110.1 2346.2	511.7 560.5 560.5 511.7 511.7 511.7 560.5	18.755 3.766 3.317 18.806 17.714 11.511 21.713 4.186 4.618	< 2e-16 *** 0.000198 *** 0.001015 ** < 2e-16 *** < 2e-16 *** < 2e-16 *** < 2e-16 *** 5.64e-06 ***
SubstrateGM:naturalNatural:Dose SubstrateOcM:naturalNatural:Dose SubstratePcM:naturalNatural:Dose SubstratePM:naturalNatural:Dose SubstratePMOc:naturalNatural:Dose SubstratePMPc:naturalNatural:Dose SubstrateGM:naturalTransgenic:Dose SubstrateOcM:naturalTransgenic:Dose SubstratePcM:naturalTransgenic:Dose	9596.5 2110.8 1859.4 9622.6 9064.0 5889.9 11110.1 2346.2 2588.6	511.7 560.5 560.5 511.7 511.7 511.7 560.5	18.755 3.766 3.317 18.806 17.714 11.511 21.713 4.186 4.618 20.219	<pre>< 2e-16 *** 0.000198 *** 0.001015 ** < 2e-16 *** < 2e-16 ***</pre>

```
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
```

Residual standard error: 839.7 on 316 degrees of freedom (20 observations deleted due to missingness)

Multiple R-squared: 0.9233, Adjusted R-squared: 0.9177 F-statistic: 165.4 on 23 and 316 DF, p-value: < 2.2e-16

Call:

lm(formula = VO2 ~ natural * Dose * Substrate, data = data)

Residuals:

Min 1Q Median 3Q Max -3254.1 -370.8 186.2 536.4 1727.3

Coefficients:

	Estimate	Std. Error	t value	Pr(> t)	
(Intercept)	143278.42	7230.68	19.815	< 2e-16	***
naturalTransgenic	22297.32	10225.72	2.181	0.0300	*
Dose	9596.47	511.68	18.755	< 2e-16	***
SubstrateOcM	-109203.79	10724.83	-10.182	< 2e-16	***
SubstratePcM	-112973.48	10724.83	-10.534	< 2e-16	***
SubstratePM	-1342.39	10225.72	-0.131	0.8956	
SubstratePMOc	-8026.61	10225.72	-0.785	0.4331	
SubstratePMPc	-54350.93	10225.72	-5.315	2.02e-07	***
naturalTransgenic:Dose	1513.62	723.63	2.092	0.0373	*
naturalTransgenic:SubstrateOcM	-17567.40	15167.20	-1.158	0.2476	
naturalTransgenic:SubstratePcM	-10213.84	15167.20	-0.673	0.5012	
naturalTransgenic:SubstratePM	-11623.31	14461.35	-0.804	0.4221	
naturalTransgenic:SubstratePMOc	7909.05	14461.35	0.547	0.5848	
naturalTransgenic:SubstratePMPc	26976.20	14461.35	1.865	0.0631	
Dose:SubstrateOcM	-7485.71	758.95	-9.863	< 2e-16	***
Dose:SubstratePcM	-7737.11	758.95	-10.195	< 2e-16	***
Dose:SubstratePM	26.09	723.63	0.036	0.9713	
Dose:SubstratePMOc	-532.46	723.63	-0.736	0.4624	
Dose:SubstratePMPc	-3706.61	723.63	-5.122	5.26e-07	***
naturalTransgenic:Dose:SubstrateOcM	-1278.14	1073.31	-1.191	0.2346	
naturalTransgenic:Dose:SubstratePcM	-784.42	1073.31	-0.731	0.4654	
naturalTransgenic:Dose:SubstratePM	-790.30	1023.37	-0.772	0.4405	
naturalTransgenic:Dose:SubstratePMOc	550.68	1023.37	0.538	0.5909	
naturalTransgenic:Dose:SubstratePMPc	1854.02	1023.37	1.812	0.0710	

Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

Residual standard error: 839.7 on 316 degrees of freedom (20 observations deleted due to missingness)

Multiple R-squared: 0.9233, Adjusted R-squared: 0.9177 F-statistic: 165.4 on 23 and 316 DF, p-value: < 2.2e-16

Call:

lm(formula = VO2 ~ Substrate - 1, data = data)

Residuals:

Min 1Q Median 3Q Max -5366.1 -1939.5 -445.7 1327.1 7567.6

Coefficients:

	Estimate Std.	Error t	value	Pr(> t)	
${\tt SubstrateGM}$	8155.9	346.4	23.55	<2e-16	***
${\tt SubstrateOcM}$	4955.3	379.4	13.06	<2e-16	***
${\tt SubstratePcM}$	4926.5	379.4	12.98	<2e-16	***
${\tt SubstratePM}$	6215.9	346.4	17.95	<2e-16	***
${\tt SubstratePMOc}$	7716.4	346.4	22.28	<2e-16	***
${\tt SubstratePMPc}$	6563.2	346.4	18.95	<2e-16	***

Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1

Residual standard error: 2683 on 334 degrees of freedom

(20 observations deleted due to missingness)

Multiple R-squared: 0.8611, Adjusted R-squared: 0.8586 F-statistic: 345.1 on 6 and 334 DF, p-value: < 2.2e-16

Linear mixed model fit by REML. t-tests use Satterthwaite's method [lmerModLmerTest]

Formula: VO2 ~ natural * Dose * Substrate + (1 | pair)

Data: data

REML criterion at convergence: 4979.4

Scaled residuals:

Min 1Q Median 3Q Max -3.09075 -0.64782 0.02403 0.63668 3.05598

Random effects:

Groups Name Variance Std.Dev.
pair (Intercept) 582983 763.5
Residual 322707 568.1
Number of obs: 340, groups: pair, 6

Fixed effects:

11104 0110000.		~		_
		Std. Error		t value
(Intercept)	143278.42	4901.42	313.21	29.232
naturalTransgenic	22297.32	6917.62	310.97	3.223
Dose	9596.47	346.15	310.97	27.724
SubstrateOcM	-109503.46	7255.28	310.97	-15.093
SubstratePcM	-113273.15	7255.28	310.97	-15.613
SubstratePM	-1342.39	6917.62	310.97	-0.194
SubstratePMOc	-8026.61	6917.62	310.97	-1.160
SubstratePMPc	-54350.93	6917.62	310.97	-7.857
naturalTransgenic:Dose	1513.62	489.53	310.97	3.092
naturalTransgenic:SubstrateOcM	-17567.40	10260.49	310.97	-1.712
naturalTransgenic:SubstratePcM	-10213.84	10260.49	310.97	-0.995
naturalTransgenic:SubstratePM	-11623.31	9782.99	310.97	-1.188
naturalTransgenic:SubstratePMOc	7909.05	9782.99	310.97	0.808
naturalTransgenic:SubstratePMPc	26976.20	9782.99	310.97	2.757
Dose:SubstrateOcM	-7485.71	513.42	310.97	-14.580
Dose:SubstratePcM	-7737.11	513.42	310.97	-15.070
Dose:SubstratePM	26.09	489.53	310.97	0.053
Dose:SubstratePMOc	-532.46	489.53	310.97	-1.088
Dose:SubstratePMPc	-3706.61	489.53	310.97	-7.572
naturalTransgenic:Dose:SubstrateOcM	-1278.14	726.09	310.97	-1.760
naturalTransgenic:Dose:SubstratePcM	-784.42	726.09	310.97	-1.080
naturalTransgenic:Dose:SubstratePM	-790.30	692.30	310.97	-1.142
$\verb naturalTransgenic:Dose:SubstratePMOc \\$	550.68	692.30	310.97	0.795
$\verb naturalTransgenic:Dose:SubstratePMPc \\$	1854.02	692.30	310.97	2.678
	Pr(> t)			

(Intercept) < 2e-16 *** naturalTransgenic 0.00140 ** Dose < 2e-16 *** SubstrateOcM < 2e-16 *** SubstratePcM < 2e-16 *** SubstratePM 0.84626 SubstratePMOc 0.24681 ${\tt SubstratePMPc}$ 6.48e-14 *** naturalTransgenic:Dose 0.00217 ** naturalTransgenic:SubstrateOcM 0.08787 .

```
naturalTransgenic:SubstratePcM
                                      0.32029
naturalTransgenic:SubstratePM
                                      0.23570
naturalTransgenic:SubstratePMOc
                                      0.41945
naturalTransgenic:SubstratePMPc
                                      0.00617 **
Dose:SubstrateOcM
                                      < 2e-16 ***
Dose:SubstratePcM
                                      < 2e-16 ***
Dose:SubstratePM
                                      0.95753
Dose:SubstratePMOc
                                      0.27757
Dose:SubstratePMPc
                                     4.23e-13 ***
naturalTransgenic:Dose:SubstrateOcM
                                      0.07934 .
naturalTransgenic:Dose:SubstratePcM
                                      0.28083
naturalTransgenic:Dose:SubstratePM
                                      0.25451
naturalTransgenic:Dose:SubstratePMOc 0.42697
naturalTransgenic:Dose:SubstratePMPc 0.00780 **
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

Correlation matrix not shown by default, as p = 24 > 12.
Use print(x, correlation=TRUE) or
 vcov(x) if you need it

Type III Analysis of Variance Table with Satterthwaite's method

Sum Sq	Mean Sq	${\tt NumDF}$	DenDF	F value	Pr(>F)
17606539	17606539	1	310.97	54.5589	1.397e-12
1517357360	1517357360	1	310.97	4701.9667	< 2.2e-16
380517369	76103474	5	310.97	235.8284	< 2.2e-16
15683854	15683854	1	310.97	48.6009	1.886e-11
8560933	1712187	5	310.97	5.3057	0.0001077
362539320	72507864	5	310.97	224.6864	< 2.2e-16
8399558	1679912	5	310.97	5.2057	0.0001323
	17606539 1517357360 380517369 15683854 8560933 362539320	17606539 17606539 1517357360 1517357360 380517369 76103474 15683854 15683854 8560933 1712187 362539320 72507864	17606539 17606539 1 1517357360 1517357360 1 380517369 76103474 5 15683854 15683854 1 8560933 1712187 5 362539320 72507864 5	17606539 17606539 1 310.97 1517357360 1517357360 1 310.97 380517369 76103474 5 310.97 15683854 15683854 1 310.97 8560933 1712187 5 310.97 362539320 72507864 5 310.97	17606539 17606539 1 310.97 54.5589 1517357360 1517357360 1 310.97 4701.9667 380517369 76103474 5 310.97 235.8284 15683854 15683854 1 310.97 48.6009 8560933 1712187 5 310.97 5.3057 362539320 72507864 5 310.97 224.6864

natural ***
Dose ***
Substrate ***
natural:Dose ***
natural:Substrate ***
natural:Dose:Substrate ***

Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1

```
refitting model(s) with ML (instead of REML)
Data: data
Models:
lmm2: VO2 ~ Dose * Substrate + (1 | pair)
lmm1: VO2 ~ natural * Dose * Substrate + (1 | pair)
                 BIC logLik deviance Chisq Df Pr(>Chisq)
            AIC
      14 5632.8 5686.4 -2802.4
                                 5604.8
lmm1
     26 5332.5 5432.0 -2640.2 5280.5 324.39 12 < 2.2e-16 ***
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
Likelihood ratio test
Model 1: VO2 ~ natural * Dose * Substrate + (1 | pair)
Model 2: VO2 ~ Dose * Substrate + (1 | pair)
 #Df LogLik Df Chisq Pr(>Chisq)
1 26 -2489.7
2 14 -2724.9 -12 470.45 < 2.2e-16 ***
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
boundary (singular) fit: see help('isSingular')
# R2 for Mixed Models
  Conditional R2: 0.965
    Marginal R2: 0.901
boundary (singular) fit: see help('isSingular')
# Intraclass Correlation Coefficient
    Adjusted ICC: 0.644
  Unadjusted ICC: 0.064
Call:
lm(formula = VO2 ~ natural * Dose * Substrate, data = data)
```

Residuals:

Min 1Q Median 3Q Max -3254.1 -370.8 186.2 536.4 1727.3

Coefficients:

	Estimate	${\tt Std.} \ {\tt Error}$	t value	Pr(> t)	
(Intercept)	143278.42	7230.68	19.815	< 2e-16	***
naturalTransgenic	22297.32	10225.72	2.181	0.0300	*
Dose	9596.47	511.68	18.755	< 2e-16	***
SubstrateOcM	-109203.79	10724.83	-10.182	< 2e-16	***
SubstratePcM	-112973.48	10724.83	-10.534	< 2e-16	***
SubstratePM	-1342.39	10225.72	-0.131	0.8956	
SubstratePMOc	-8026.61	10225.72	-0.785	0.4331	
SubstratePMPc	-54350.93	10225.72	-5.315	2.02e-07	***
naturalTransgenic:Dose	1513.62	723.63	2.092	0.0373	*
naturalTransgenic:SubstrateOcM	-17567.40	15167.20	-1.158	0.2476	
naturalTransgenic:SubstratePcM	-10213.84	15167.20	-0.673	0.5012	
naturalTransgenic:SubstratePM	-11623.31	14461.35	-0.804	0.4221	
naturalTransgenic:SubstratePMOc	7909.05	14461.35	0.547	0.5848	
naturalTransgenic:SubstratePMPc	26976.20	14461.35	1.865	0.0631	•
Dose:SubstrateOcM	-7485.71	758.95	-9.863	< 2e-16	***
Dose:SubstratePcM	-7737.11	758.95	-10.195	< 2e-16	***
Dose:SubstratePM	26.09	723.63	0.036	0.9713	
Dose:SubstratePMOc	-532.46	723.63	-0.736	0.4624	
Dose:SubstratePMPc	-3706.61	723.63	-5.122	5.26e-07	***
$\verb naturalTransgenic:Dose:SubstrateOcM \\$	-1278.14	1073.31	-1.191	0.2346	
$\verb naturalTransgenic:Dose:SubstratePcM \\$	-784.42	1073.31	-0.731	0.4654	
naturalTransgenic:Dose:SubstratePM	-790.30	1023.37	-0.772	0.4405	
$\verb naturalTransgenic:Dose:SubstratePMOc \\$	550.68	1023.37	0.538	0.5909	
$\verb naturalTransgenic:Dose:SubstratePMPc \\$	1854.02	1023.37	1.812	0.0710	•

Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1

Residual standard error: 839.7 on 316 degrees of freedom

(20 observations deleted due to missingness)

Multiple R-squared: 0.9233, Adjusted R-squared: 0.9177 F-statistic: 165.4 on 23 and 316 DF, p-value: < 2.2e-16

Warning in modelUpdate(objects[[i - 1]], objects[[i]]): original model was of class "lmerModLmerTest", updated model is of class "lm"

Likelihood ratio test

```
Model 1: VO2 ~ natural * Dose * Substrate + (1 | pair)

Model 2: VO2 ~ natural * Dose * Substrate

#Df LogLik Df Chisq Pr(>Chisq)

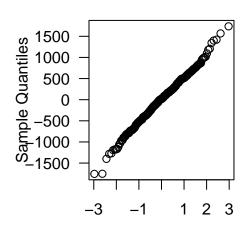
1 26 -2489.7

2 25 -2759.2 -1 539.1 < 2.2e-16 ***
---

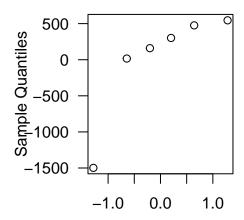
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
```

Residuals

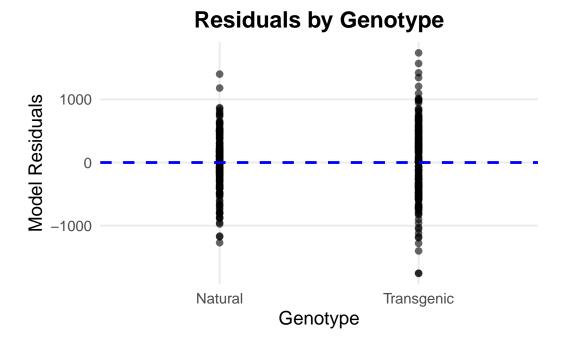
Random Effects

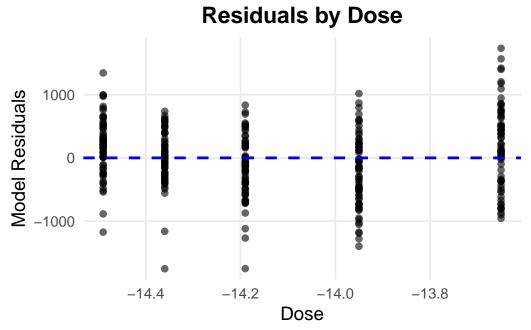


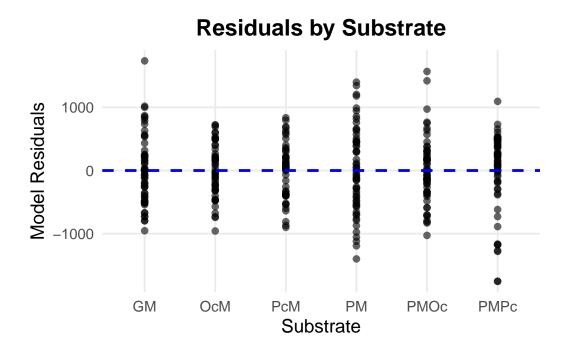


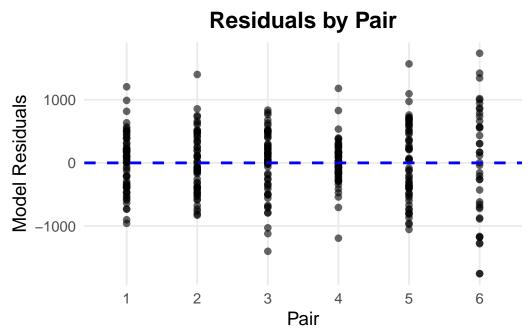


Theoretical Quantiles

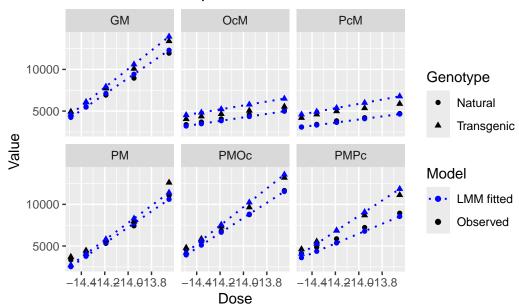




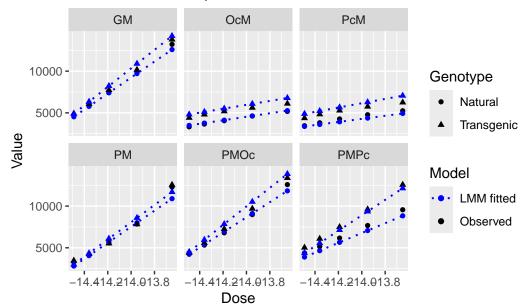




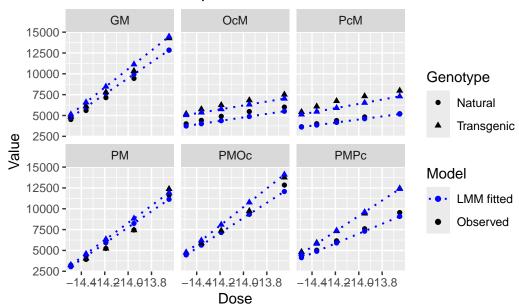
VO2 vs. Dose for pair 1



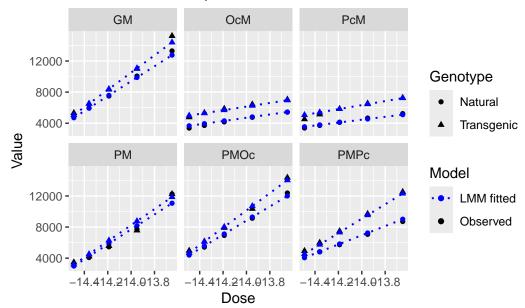
VO2 vs. Dose for pair 2



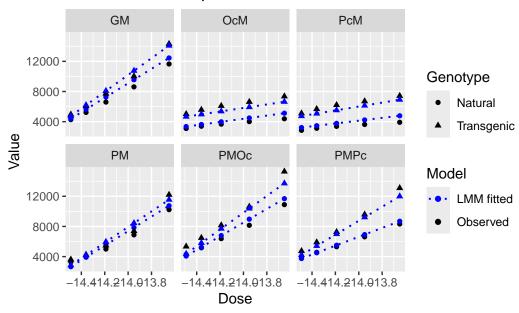
VO2 vs. Dose for pair 3



VO2 vs. Dose for pair 4

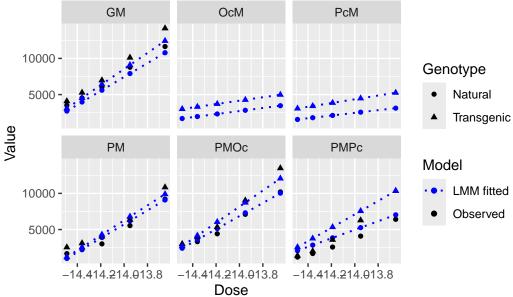


VO2 vs. Dose for pair 5

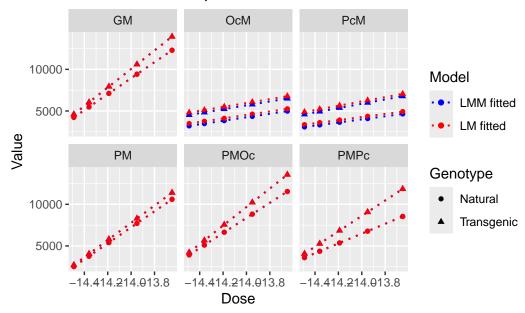


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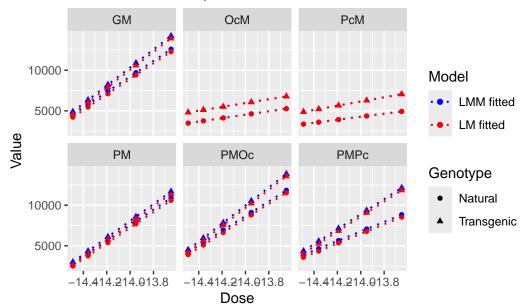




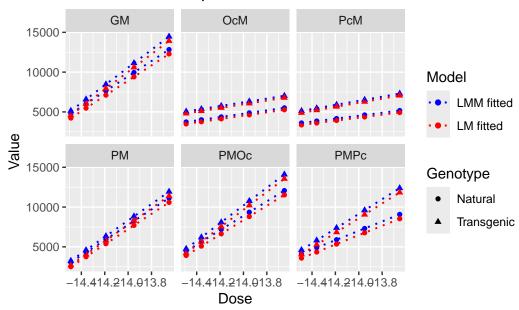
VO2 vs. Dose for pair 1



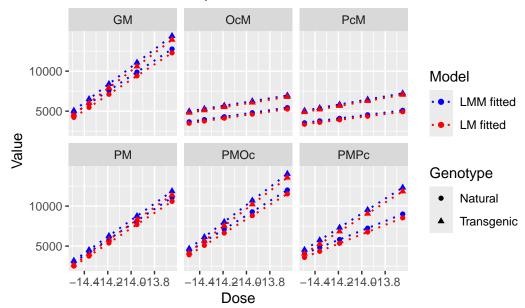
VO2 vs. Dose for pair 2



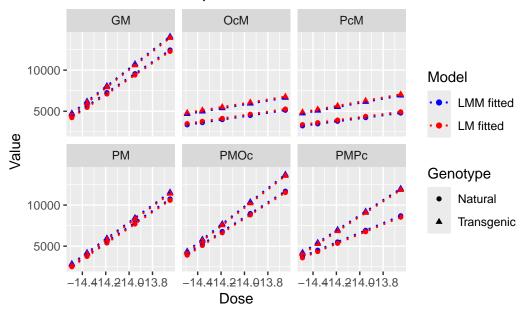
VO2 vs. Dose for pair 3



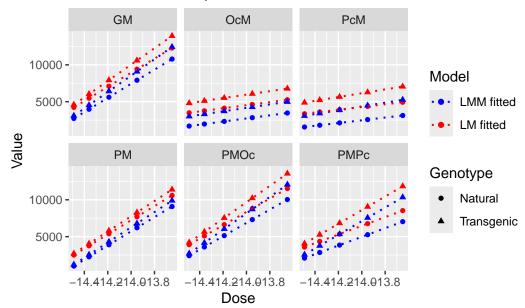
VO2 vs. Dose for pair 4



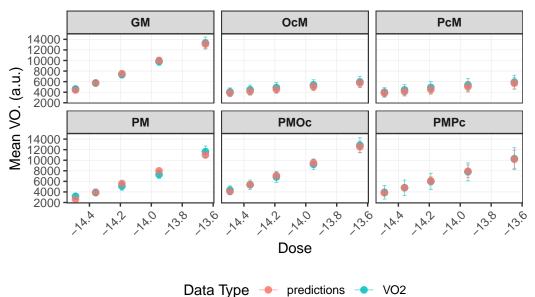
VO2 vs. Dose for pair 5



VO2 vs. Dose for pair 6



Dose vs. Mean VO.



Predictions vs. Observed VO.

