

System Dynamics Model for Ventilation effect on COVID-19 transmission

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Context

- COVID-19 is transmissible through air
- Transmissibility is dependent upon, among others, viral concentration in air
- Ventilation has an effect on air viral concentration
- Principal policy focus so far on:
 - Distance guidelines (density, absolute distance)
 - Personal air filters (masks)
 - Generic ventilation guidelines
- Opportunity for
 - Testing scenarios for indoor environments
 - Activity-dependent ventilation (e.g., Restaurants, Classrooms)
 - Identify Operational recommendations
 - Ventilation System Characteristics (Q , pf, RH)
 - Activity type and duration (e.g., number and length of school breaks)

Proposal outline

- **Develop a:**

- Simulation model of relationship between Transmission rate and:
 - Ventilation, activity type and level
- Identify policy levers and their sensitivity
- Apply to specific example cases

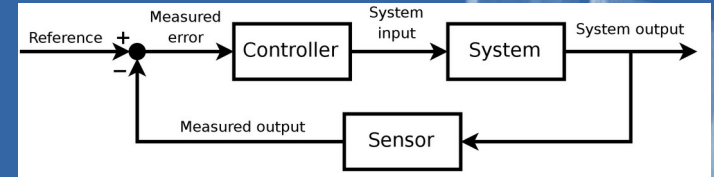
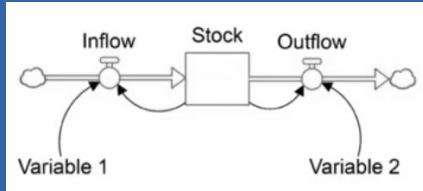
- **In order to:**

- Provide a learning platform with the explicit representation and simulation of:
 - Accumulations (Sources of Inertia)
 - Causal relationships
 - Feedback Loops
 - Exogenous versus
 - Endogenous variables

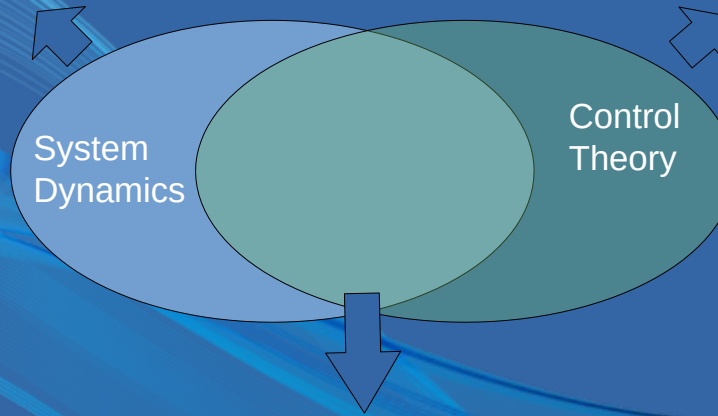
- **Through the use of:**

- System Dynamics Method

System Dynamics versus traditional control



- ✓ Stock and Flow representation
- ✓ States as Accumulations
- ✓ Focus on Relationships
- ✓ Important variables not necessarily quantified



- ✓ Frequency domain analysis
- ✓ Focus on Transfer Function

- ✓ States
- ✓ Dynamic modelling (over time)
- ✓ Polarity (Pos.&Neg.)
- ✓ Feedback (Pos. & Neg.)

COVID-19 Model Equations

$$\frac{dS}{dt} = -\frac{pq}{VA}IS,$$

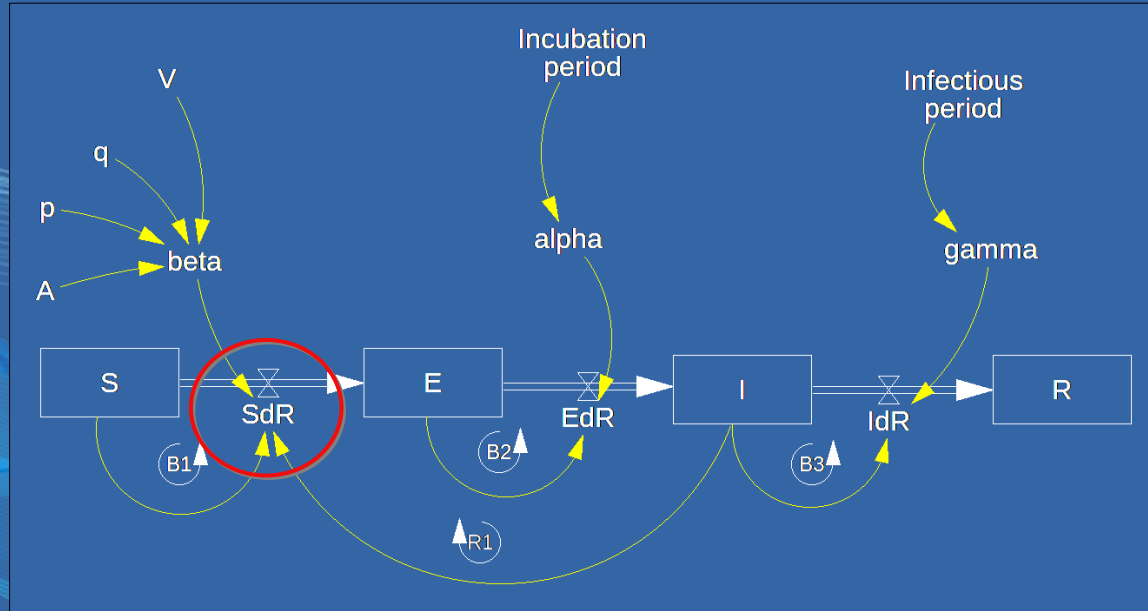
$$\frac{dE}{dt} = \frac{pq}{VA}IS - \alpha E,$$

$$\frac{dI}{dt} = \alpha E - \gamma I,$$

$$\frac{dR}{dt} = \gamma I,$$

$$S + I + E + R = N,$$

Model Source: Noakes, C.J., Beggs, C.B., Sleight, P.A. and Kerr, K.G., 2006. Modelling the transmission of airborne infections in enclosed spaces. *Epidemiology & Infection*, 134(5), pp.1082-1091.



$$SdR = \text{beta} \cdot S \cdot I$$

$$\frac{dS}{dt} = -\beta(t)SI$$

$$\beta(t) = Q_b C(t) c_i p_m$$

$$C(t) = \frac{P}{Q} (1 - e^{-\lambda_a t})$$

System Dynamics representation of SEIR Model

Differential Equations

$$\frac{dS}{dt} = -\frac{pq}{VA} IS,$$

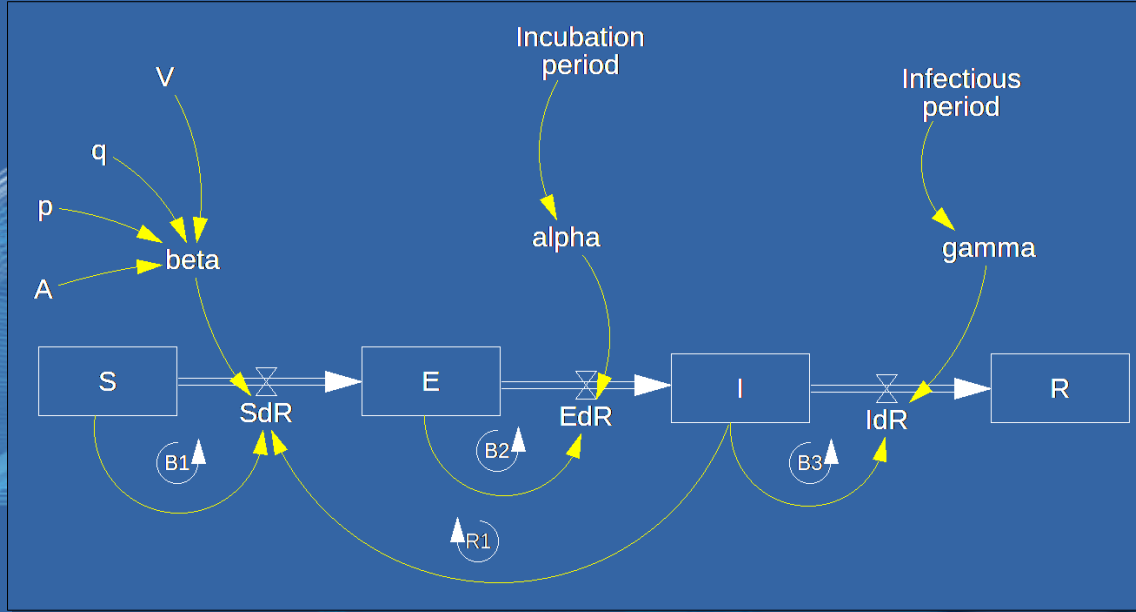
$$\frac{dE}{dt} = \frac{pq}{VA} IS - \alpha E,$$

$$\frac{dI}{dt} = \alpha E - \gamma I,$$

$$\frac{dR}{dt} = \gamma I,$$

$$S + I + E + R = N,$$

Model Representation



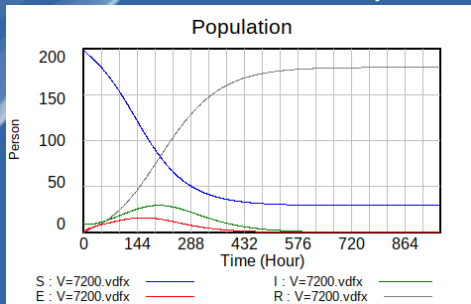
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Dynamic Simulation

- ▶ Sensitivity
- ▶ Phase Diagrams

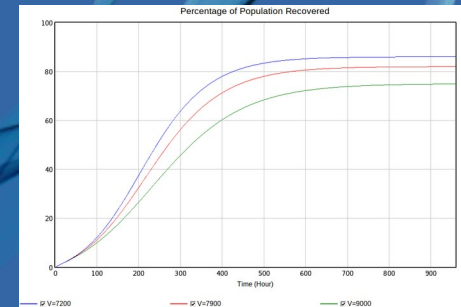
Variable	Name
S	Susceptible
E	Exposed
I	Infected
R	Recovered
V	Room Volume
A	Ventilation Rate
q	Quanta production
p	Pulmonary Ventilation rate

SEIR dynamics



Explicit Representation of

- ▶ Accumulations (Inertia)
- ▶ Causal Relationships
- ▶ Exogenous vs Endogenous Variables
- ▶ Feedback Loop visibility (R,B)



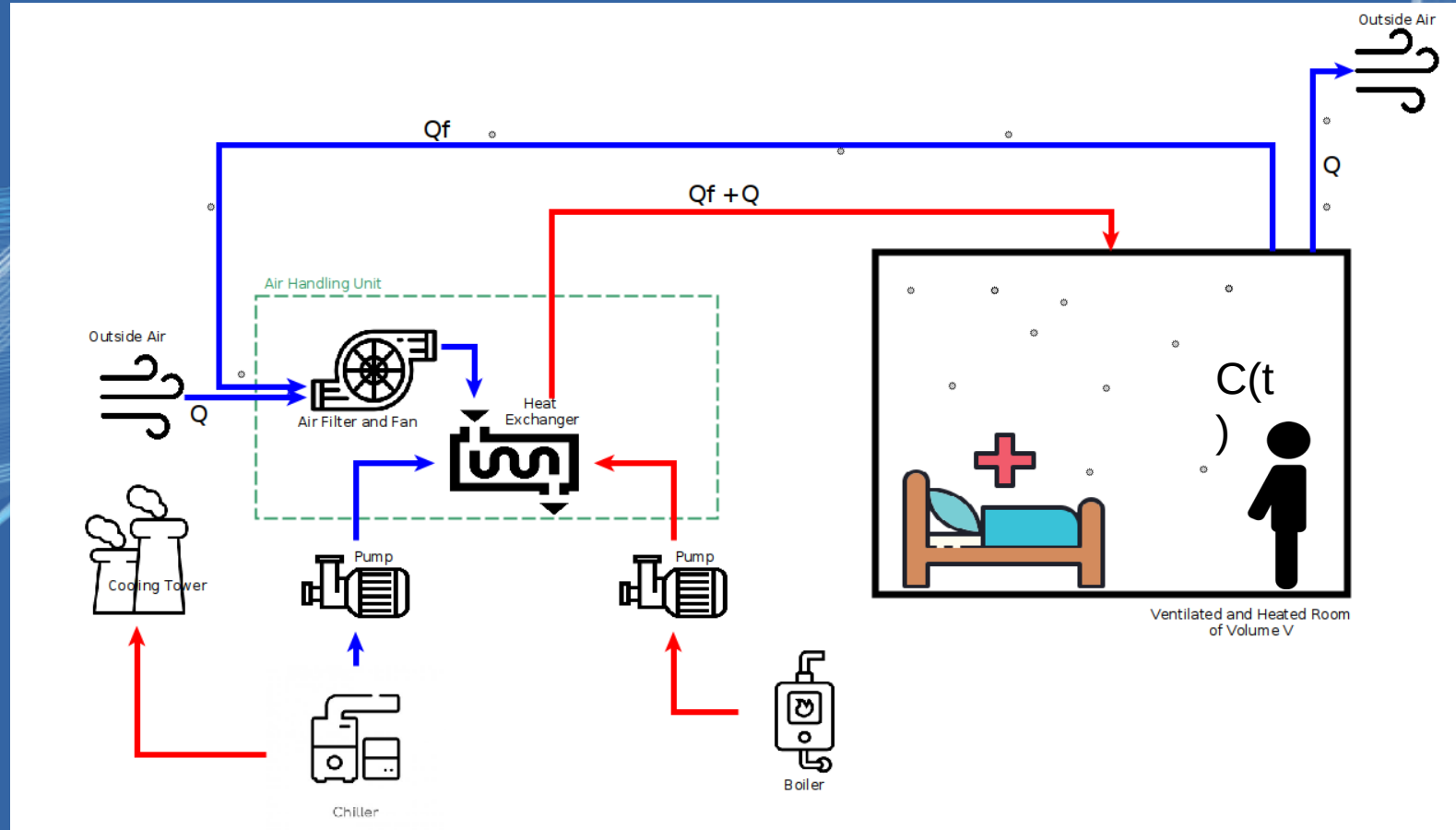
Sensitivity Analysis:
Percentage of Population Recovered
with different room Volumes, 7200,
7900 and 9000 m³

The background is a solid blue color. Overlaid on this are several abstract, flowing, wavy lines in various shades of blue, ranging from light to dark. These lines create a sense of movement and depth, resembling liquid or smoke. The lines are most prominent on the left and right sides, framing the central text.

Application Example:

Let's go to VENSIM

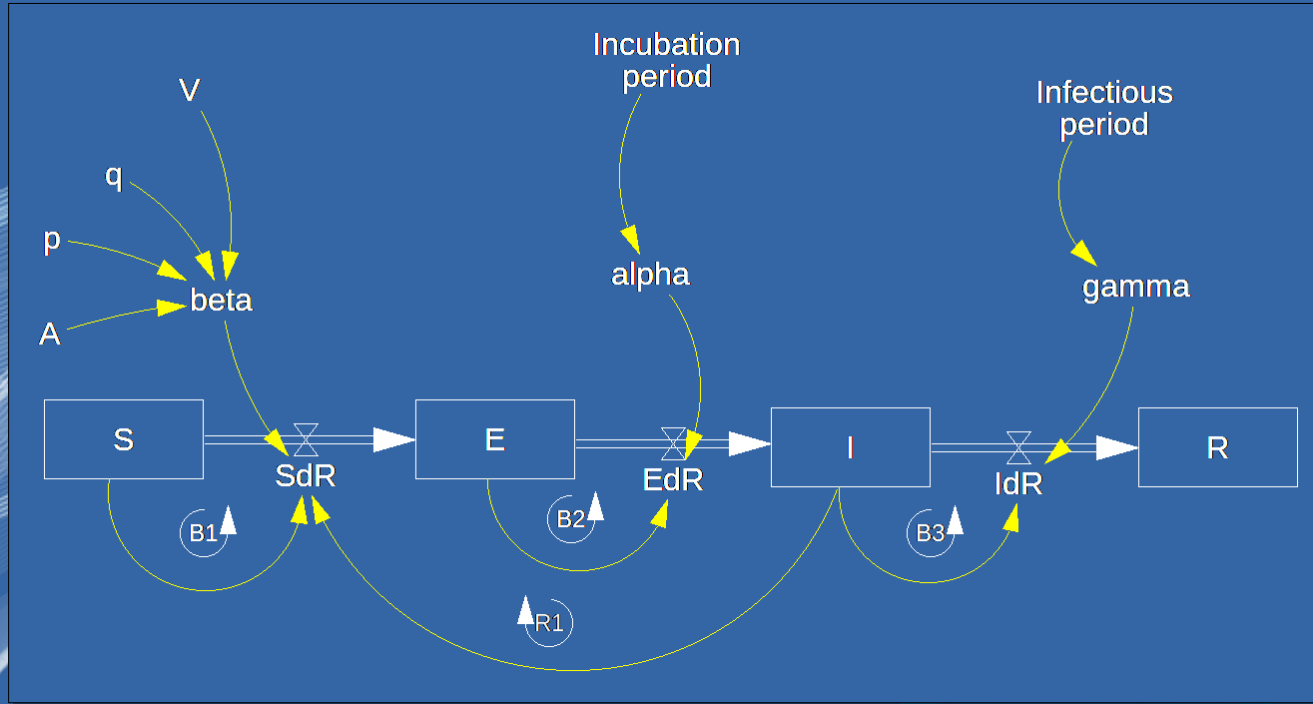
Ventilation : Simple Ventilation System



The background is a solid blue color. Overlaid on this are several abstract, flowing, wavy lines in various shades of blue, ranging from light to dark. These lines create a sense of movement and depth, with some appearing as thin, wispy streaks and others as thicker, more defined waves. The lines generally flow from the left side towards the right, with some curving upwards and others downwards.

Thank you

Model with all Variable names



Variable	Name
S	Susceptible
E	Exposed
I	Infected
R	Recovered
V	Room Volume
A	Ventilation Rate
q	Quanta Production
p	Pulmonary Ventilation Rate
SdR	Susceptible decrease Rate
EdR	Exposed decrease Rate
IdR	Infected decrease Rate
Bx	Balancing Loops
Rx	Reinforcing Loops



COMPLETE: Model with all
Variable names

Presentation



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● PhD, Operations Management, DTU

- System Dynamics Modelling for:
 - Supply Systems
 - Stock fluctuations
 - Bullwhip effects & Hoarding
 - Cyber-resilience
 - Healthcare
 - Compliance Behaviour of Diabetes patients
 - Return patients to Emergency care



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- System Dynamics Modelling for:
 - Healthcare
 - Return patients to Emergency care
 - Policy analysis for COVID-19 Spread