

## Homework 1 - Cpts 223

$$1. \frac{2}{N} < 37 < \sqrt{N} < N < N \log(\log(N)) < N \log N < N \log^2 N \\ < N^{1.5} < N^2 < N^2 \log N < N^4 < 2^{(N/2)} < 2^N$$

$$2. \begin{aligned} O(N) &\rightarrow \left(\frac{35}{20}\right) 100 = \boxed{175} \\ O(N + \log N) &\rightarrow \left(\frac{35}{20 \log 20}\right) 100 \log 100 = \boxed{455.2} \\ O(N^3) &\rightarrow \left(\frac{35}{20^3}\right) 100^3 = \boxed{4375} \\ O(2^N) &\rightarrow \left(\frac{35}{2^{20}}\right) 2^{100} = \boxed{42 \cdot 10^{24}} \end{aligned}$$

(There is no #3)

$$4. a. \begin{aligned} f(n) &= f(n-1) + 3 \rightarrow \boxed{O(n)} \\ g(n) &= 1 + 2(n+1) + 2n + 1 = 4n + 4 \rightarrow \boxed{O(n)} \end{aligned}$$

b. max depth = 5,  $f(5)$

$$\boxed{f(n) = O(n) ; g(n) = O(1)}$$

c. int h(int n)

```
{
  if (n <= 1)
  {
    return n;
```

```
}
```

```
else
```

```
{
```

```
  return h(n-1) + h(n-2)
```

```
}
```

time complexity =

$$h(n) = O(1)$$

$$5. \begin{aligned} \text{runs } \frac{n}{2}, \text{ if } n \text{ is odd} &\rightarrow \frac{n}{2} + 1 \\ \text{if } n \text{ is even} &\rightarrow \frac{n}{2} \end{aligned} \left. \vphantom{\begin{aligned} \text{runs } \frac{n}{2}, \text{ if } n \text{ is odd} \\ \text{if } n \text{ is even} \end{aligned}} \right\} \boxed{O\left(\frac{n}{2}\right)}$$

7.  $T(n) = O(n)$

6. 1. Input  $n$ .

2. Declare variables:

$a=1, b=2, c=3, d=4, e=5, f=6, g=7, h=8, i=9, x=1$   
 $count=0, k=1;$

3. Get remainder of product.

4. Do-while loop runs.

5. Check if remainder is equal to integer and add 1 to count.

6. Repeat steps 3-5 until  $count = 10$ .

7. Display  $k$ .

```
while (x != 0)
{
    int p = k * n;
    int r = p % 10;
    do {
        if (r == a)
        {
            a--;
            if (a == -1) { k++; }
        }
        if (r == b)
        {
            b = b - r;
            if (b == 0) { k++; }
        }
        // repeats above until i
    } while (r != 0);
    if (k == 10)
    {
        x = 0;
        // print k
    }
    p = p / 10;
    r = r % 10;
} while (r != 0);
```

7. a. 1. input  $n$

2. check if  $n \% 2 == 0$ . If so,  $n$  is even.

3. else,  $n$  is odd.

$$T(n) = O(1)$$

b. 1. input  $n$

2. for  $i = 0$  to length

3. if ( $n = \text{element at } i$ )

4. element is found

5. else, element was not found

$$T(n) = O(n)$$

c. 1.  $s = \text{list}[0]$

2. for  $i = 0$  to length

3. if ( $s > \text{list}[i]$ )

4.  $s = \text{list}[i]$

5. Once loop is done, return  $s$ .

$$T(n) = O(n)$$

e. ~~1~~ 1. check length of list 1

2. repeat 1 for list 2

3. if (length 1 == length 2)

4. for  $i = 0$  to length 1

5. if ( $a[i] == b[i]$ )

6. if all are equal, then lists are the same

7. else not.

8. else, length of list is not equal

$$T(n) = O(n)$$

d. same as e, without steps 1, 2, 3, and 8

$$T(n) = O(n^2)$$



e. 1. `node search( root, n )`

2. if `root == Null` or `root->data == n`, return `root`.

3. if `root->data < n`, return `search( root->right, n )`

4. return `search( root->left, n )`

8. `cp` → copy files / directories

`rm` → removes ---

`mkdir` → make directory

`ssh` → provide secure, encrypted connection

`g++` → GNU C++ compiler

`scp` → copy / transfer files across hosts

9. `argc` → number of arguments passed (non-neg)

`argv[]` → points to each argument passed to the program

Both are command line arguments