

$$(1) d \equiv e^{-1} \pmod{(p-1)(q-1)}$$

$$d = 113$$

$$(2a) c \equiv m^e \pmod{n}$$

$$c = 99$$

$$(b) m \equiv c^d \pmod{n}$$

$$m = 99$$

3,4,5 Bob has a message, m that he wants to encrypt. ^{to Alice} For RSA encryption Alice will need 2 random large numbers, p and q . Let $n = p \cdot q$ and $\phi = (p-1)(q-1)$. She will then choose a number that is co-prime to ϕ $\gcd(e, (p-1)(q-1)) = 1$. She then can compute d using $d \equiv e^{-1} \pmod{(p-1)(q-1)}$. She keeps d as her private key for decryption and she can upload her public key (e, n) to Bob for encryption. Bob can encrypt his message, m , to cipher text, c , using the theorem, $c \equiv m^e \pmod{n}$. Alice can decrypt Bob's cipher-text using her private key, d , and the theorem, $m \equiv c^d \pmod{n}$. Alice did not have to share keys in order to decrypt Bob's message so RSA is valid in not having to share keys.

6, 7, 8 "complexion dimm'd"

⑨ $n = 119143$

$$n = a^2 - b^2$$

$$n = (a+b)(a-b)$$

$$a = \sqrt{119143}$$

$$a = 346$$

$b = \sqrt{346^2 - n}$ b is not a whole number
increase $a+1$ until $b = \sqrt{a^2 - n}$ results
in a whole number

$$a = 352 \quad b = 69$$

$$n = (352 + 69)(352 - 69) = 119143 \checkmark$$

⑩ Given two different cipher texts, $c_1 = m^{e_1}$ and $c_2 = m^{e_2}$ and two numbers, s and t that satisfy $se_1 + te_2 = 1$ then

$$\begin{aligned} c_1 \cdot c_2 &= (m^{e_1})^s + (m^{e_2})^t \\ &= m^{se_1} + m^{te_2} \\ &= m^{se_1 + te_2} \\ &= m^1 \\ &= m \end{aligned}$$

The common modulus attack is correct.