

Assessing and tracking students' problem solving performances in anchored learning environments

Brian A. Bottge · Enrique Rueda · Jung Min Kwon ·
Timothy Grant · Perry LaRoque

Published online: 20 September 2007

© Association for Educational Communications and Technology 2007

Abstract The purpose of this randomized experiment was to compare the performance of high-, average-, and low-achieving middle school students who were assessed with parallel versions of a computer-based test (CBT) or a paper-pencil test (PPT). Tests delivered in interactive, immersive environments like the CBT may have the advantage of providing teachers with diagnostic tools that can lead to instruction tailored to the needs of students at different achievement levels. To test the feasibility of CBT, students were randomly assigned to the CBT or PPT test conditions to measure what they had learned from an instructional method called enhanced anchored math instruction. Both assessment methods showed that students benefited from instruction and differentiated students by achievement status. The navigation maps generated from the CBT revealed that the low-achieving students were able to navigate the test, spent about the same amount of time solving the subproblems as the more advanced students, and made use of the learning scaffolds.

Keywords Classroom learning · Mathematics · Interactive learning environments · Low achievers · Assessment

Introduction

Government reports such as *What Work Requires of Schools: A SCANS Report for America 2000* (U.S. Department of Labor 1991) and more recent publications (e.g., Gray and Herr 1998; National Center on Education and the Economy 2007; Thornburg 2002; Uchida et al. 1996) stress the importance of workers having a sound foundation in basic skills and

B. A. Bottge (✉)

Department of Special Education and Rehabilitation Counseling, University of Kentucky,
222 Taylor Education Building, Lexington, KY 40506, USA
e-mail: brian.bottge@uky.edu

E. Rueda · J. M. Kwon · T. Grant · P. LaRoque

Wisconsin Center for Education Research, University of Wisconsin – Madison, 1025 W. Johnson St.,
Madison, WI 53706, USA

the ability to use technology to solve important problems. To achieve this level of expertise in math, teachers should provide their students with problem situations that develop their procedural skills (e.g., adding fractions) *as* they work on developing their conceptual understanding (i.e., solving problems that involve rational numbers), a strategy that cognitive science research supports (Rittle-Johnson and Koedinger 2002; Rittle-Johnson et al. 2001). Furthermore, these problems should be presented in authentic-like contexts and align closely with actual work applications (Stone et al. 2006).

Available evidence suggests, however, that many high school students leave school without the ability to solve the kinds of problems required for employment in the contemporary job market (Kirsch et al. 2007; Murnane and Levy 1996). Recent test results seem to support this claim. For example, the 2005 National Assessment of Educational Progress (NAEP; Perie et al. 2005) revealed that 69% of 8th-grade students with disabilities scored below *Basic* performance levels in mathematics compared to 28% of students without disabilities. The problem becomes even worse as students progress to high school when more than one-third (37%) of 12th-grade students score below *Basic*. The NAEP descriptor *Basic* includes both basic foundation skills and the ability to solve problems with diagrams, graphs, and charts using technology tools.

To address this problem, we have studied the effects of a technology-assisted instructional method called Enhanced Anchored Instruction (EAI) for helping adolescents acquire more sophisticated problem solving skills. EAI is based on the concept of anchored instruction originally developed by the Cognition and Technology Group at Vanderbilt (Cognition & Technology Group at Vanderbilt 1990, 1997). Anchored instruction uses a video format to embed complex problems and related subproblems in realistic-looking situations. Students search these learning environments for information that they can use to generate plausible solutions. The visual and auditory format of the video eliminates the need to read and comprehend text, a potential barrier for many students who have difficulty in math *and* reading. In their problem solving groups, students discuss and formulate plausible solutions to problems as teachers carefully monitor their discussions and provide just-in-time guidance as needed. At intervals throughout anchored instruction, teachers model analogous and less complex problems to help students practice emerging skills and deepen their understanding of important concepts.

EAI extends learning beyond the multimedia contexts by having students solve problems embedded in applied projects, such as constructing a skateboard ramp or planning and building a hovercraft. Our previous development work with EAI involved combinations of special education, mathematics, and technology education teachers who collaborated to teach the multimedia-based and applied problems to students of all ability levels, including students with disabilities (e.g., learning disabilities, emotional/behavioral disorders) in middle school (Bottge 1999; Bottge et al. 2002; Bottge et al. 2007a), high school (Bottge and Hasselbring 1993), and alternative school settings (Bottge et al. 2006).

Solving difficult problems such as the ones in EAI requires extraordinary self-management skills (e.g., metacognition and evaluation) (Glasgow 1997; Hannafin et al. 1997; Palinscar 1986; Palinscar and Brown 1984). Although the notion of scaffolding traditionally emphasized the role of dialogue and social interaction with an external source (i.e., a teacher) (Bruner 1975; Vygotsky 1978), scaffolding also refers to the learner's use of internal cognitive tools (Ge and Land 2003). In a technology-supported environment, Hannafin et al. (1999) suggest that students make use of four kinds of scaffolds: (a) conceptual, (b) metacognitive, (c) procedural, and (d) strategic. According to Brush and Saye (2001), *conceptual scaffolds* help students determine what to consider when solving a problem, *metacognitive scaffolds* support students' self-regulation or self-management,

procedural scaffolds assist students with learning how to use resources or tools built into an environment, and *strategic scaffolds* help make students aware of different approaches and techniques for solving problems. The newest of our EAI problems called *Fraction of the Cost* includes all four types of scaffolds.

Although EAI has produced promising findings, two nagging concerns have surfaced in our studies. The first issue has to do with the pencil-paper tests (PPT) we have used to judge whether students had learned the concepts embedded in the EAI problems. We are confident that the constructed response items in the PPT distinguished students who understood the problems from those who did not in recent studies (e.g., Bottge et al. 2007a, b), but some universal design for learning principles (Sireci et al. 2005) that guided development of the EAI were not altogether possible in the PPT format. For example, PPT *did* provide students with pictorial representations and less text for students with reading difficulties thereby giving them more opportunities to understand what the questions were asking, but the static format of PPT did not allow students to interact with the problem contexts (Rose and Meyer 2007). This universal test design principle has been suggested for making tests more accessible for low-achieving students (Dolan and Hall 2001; Hasselbring et al. 2005).

Using the PPT format has also restricted our ability to collect important diagnostic information about students' problem solving behaviors. Although we routinely analyze student performance at the item level and use these results to modify EAI, it was not possible to measure how much time students spent answering items or to what extent they made use of the learning scaffolds. Other investigators (e.g., Puntambekar and Stylianou 2005; Puntambekar et al. 2003) have successfully tracked students' navigation patterns as they worked on problem-solving tasks and being able to collect similar information would provide us with important clues for modifying both the instructional and assessment features of EAI.

To address both these issues, we constructed a computer-based test (CBT) based on universal design principles to map the performance of students *as* they worked on the anchored math problems. The first goal of the study was to assess the comparability of the PPT we had used in previous research to that of the newly created CBT. If the overall performance of students on the CBT matched the performance of students on the PPT across ability levels, we could be reasonably assured of its usefulness in measuring the learning objectives in EAI. We could then set out to accomplish the second goal of tracing the navigation patterns of students to gain a deeper understanding of their problem solving strategies *as* they solved the EAI problems. In line with these goals, the study was conducted to answer three research questions:

1. Does the problem-solving performance differ between students who take a paper-pencil test (PPT) and students who take a computer-based test (CBT)?
2. Does the problem-solving performance differ for low achievers (LA), average achievers (AA), and high achievers (HA) by assessment format (PPT versus CBT)?
3. What are the problem-solving patterns of students on the CBT and how do they compare for students who are low achievers (LA), average achievers (AA), and high achievers (HA) in math?

Method

Participants

All seventh-grade students ($N = 109$) and their two math teachers (MT1, MT2) in one rural middle school in the Midwest participated in the study. Each math teacher taught three

classes. There were 56 boys and 53 females and all of the students were white. Individual Educational Plans indicated that seven students were receiving special education services an average of 43 min for learning disabilities (LD) in math and one student was getting special services in both math and reading. All eight students with LD were included in the general education math classes and received the same instruction as the students without disabilities.

Students in each of the six classes were randomly assigned to either CBT or PPT via an alternate ranks procedure (Dalton and Overall 1977) based results on the state-mandated Wisconsin Knowledge and Concepts Exam (WKCE) math subtest. The WKCE was developed from the *TerraNova* standardized test (CTB/McGraw-Hill 2003) and customized to align with Wisconsin content standards. The test scores of students were ranked from highest to lowest and then grouped into foursomes. The student with the top score in the highest achieving foursome was randomly assigned to either the PPT or CBT group, the second and third students were assigned to the other assessment group, and the fourth student was assigned to the first student's group. This procedure was repeated until students in all foursomes were assigned. Students in the PPT and CBT groups received the same instruction.

The mean scores and standard deviations in normal curve equivalents (NCEs) of students in the PPT and CBT groups were 58.6 ($n = 25$, $SD = 16.8$) and 59.5 ($n = 25$, $SD = 16.3$) for MT1 and 70.7 ($n = 28$, $SD = 19.0$) and 67.9 ($n = 31$, $SD = 20.8$) for MT2. MT2's scores were higher because he taught one class of high-achieving students. Overall NCEs and standard deviations of students taking the PPT or CBT were 65.0 ($n = 53$, $SD = 18.9$) and 64.2 ($n = 56$, $SD = 19.2$), respectively. No significant differences were found between the CBT and PPT comparisons.

The two math teachers were primarily responsible for the instruction. MT1 had a bachelor's degree, was in her third year of teaching, and had taught with EAI the previous year. MT2 was chairperson of the math department, had a master's degree in middle-level education, was beginning his 13th year of teaching, and had taught with EAI the past four years. A special education teacher was on hand to help students with LD who were included in the math classes, but she provided no direct, whole-group instruction. The special education teacher was in her 15th year of teaching, had a master's degree in general education grades 1 through 8, and licensed to teach special education in grades K through 12.

Instructional methods and materials

Instruction involved one EAI problem called *Fraction of the Cost*, which had been integrated into the math curriculum the previous year. MT1 and MT2 assigned 3-to-4 students to problem-solving groups based on whom they thought would work well together. In classes where there were students with LD, one student with LD worked with two or three general education students. At the beginning of each class period, the teachers led students in a 10-min warm-up activity to review concepts they had worked on the previous day and to introduce new material. For the remainder of class, each group worked on a laptop computer, which contained the learning tools (i.e., scaffolds) students could use to help solve each of the subproblems. Teachers circulated from group to group, answering questions and posing new ones. After students solved the video-based anchor, they worked on the hands-on applications.

The authors developed *Fraction of the Cost*, which features three students from a local middle school. Available in Spanish and English, the video was filmed at a local skateboarding store, a garage, and the backyard of a local home. The video opens in a skateboard store and rink, where the students are shown discussing how they can afford to buy materials for building a skateboard ramp. To solve the problem, students need to (a) calculate the percent of money in a savings account and sales tax on a purchase, (b) read a tape measure, (c) convert feet to inches, (d) decipher building plans, (e) construct a table of materials, (f) compute whole numbers and mixed fractions, (g) estimate and compute combinations, and (h) calculate total cost.

Teachers showed *Fraction of the Cost* without interruption the first day and asked students to describe the problems associated with it. Students then worked in small groups to complete their problem-solving packets. To figure out the most economical use of two-by-four ($2'' \times 4''$) lumber in *Fraction of the Cost*, students first needed to identify the lengths of boards shown in the plan. Then they converted these dimensions from feet and inches to inches and calculated several combinations of lengths to maximize their use of the wood available. Once they computed what additional wood was needed, they consulted the store advertisement to decide what to buy. Their final task was to make a materials list to show the total cost of the project. To help solidify students' understanding, the math teachers often led students in brief practice sessions the first 10 min of class. For example, one day the teachers projected on the projector screen four narrow rectangles, which represented two-by-four dimension lumber. Then students were asked to respond to a series of questions about how to convert feet-and-inches to inches. Finally, students calculated the most economical way of cutting the boards.

After students solved the problems posed in *Fraction of the Cost*, they planned and built a rollover cage out of PVC pipe for a hovercraft in a related problem called the *Hovercraft Challenge*. The teacher divided the class into groups of three students, and each group planned how they could make the cage in the most economical way. Once the teacher approved the plans, students worked on measuring, cutting, and assembling. When the cages were complete, they lifted them onto a $4' \times 4'$ plywood platform, which served as the hovercraft base. A leaf blower inserted into the base powered the hovercraft. On the last day of the project, students rode their hovercrafts in relay races up and down the halls of the school. Each teacher taught the video-based and hands-on problems a total of 14 instructional days.

Instrumentation

The CBT and PPT were developed to address the knowledge and concepts in the NCTM standards recommended for students in grades 6–8 (i.e., Numbers and Operations, Measurement, Problem Solving, Communication, and Representation) and both tests contained constructed-response items that measured the concepts in *Fraction of the Cost* (video-based problem) and the *Hovercraft Challenge* (hands-on problem). The total number of points possible for both tests was 38. Internal consistency (Cronbach's coefficient alpha) was .74 for CBT and .73 for PPT. Students in each testing condition could spend a maximum of 80 min taking the test.

Sets of items developed for the PPT were awarded full or partial credit and weighted according to their complexity and the contribution to solving the over-arching problem. The items were grouped into seven clusters, which made it possible to analyze student work at both the item and cluster (concept) levels (Lester and Kroll 1990; Shafer and

Romberg 1999). Prior to its use in this research, the PPT had gone through cycles of refinement in several studies (Bottge et al. 2002; Bottge et al. 2004; Bottge et al. 2001; Bottge et al. 2007b) and was modified based on suggestions from math and assessment specialists (i.e., math teachers, math researchers, test consultants). A previous study showed the concurrent validity correlation coefficient of the PPT was .59 based on pretest scores of the Iowa Tests of Basic Skills (University of Iowa 2001) Problem Solving and Data Interpretation Subtest. This correlation was significant and appears acceptable given that the range of mathematics concepts sampled by the PPT was more restricted than that sampled on the ITBS.

The newly created CBT was designed to measure the same concepts as the PPT, with the additional benefit of providing students a similar level of interactivity they had experienced during EAI. The software included a set of constructed response items and information reservoirs (i.e., scaffolds). The figures representing information for answering items were also similar across tests. The major difference between the tests was the hyperlinks that students taking the CBT could use to access information reservoirs, which contained relevant details for solving the subproblems. The eight hyperlinks consisted of the following: (a) the video-based anchor, (b) schematic plans of a skateboard ramp, (c) a bank statement showing how much money one of the students could spend, (d) a materials list for building the skateboard ramp, (e) a newspaper advertisement from a hardware store, (f) a screen showing the names of the students, (g) navigation assistance about how to operate the markers and ruler, and (h) a tracking feature that helped students monitor their use of the lumber for building the skateboard ramp. Figure 1 shows the information reservoirs.

Cluster comparisons between PPT and CBT

The test consisted of the same seven item clusters as the PPT and the items within clusters were weighted the same. For the most part, the screens in the CBT looked similar to the figures on the PPT although the interactive components of the CBT made it necessary to modify them somewhat. Figures 2 and 3 show the PPT and CBT item clusters, respectively.

Cluster 1 asks how much the kids shown in the video-based problem decide to spend on supplies for building the skateboard ramp. The PPT shows a bank statement next to the question, which the students use to figure out the money Michael can spend. From the video, the students know that the three kids will each spend the same amount (\$19), which they total to \$57. Cluster 1 of the CBT does not show the bank statement alongside the questions. Rather, students need to access the information from the statement and the video located in the information reservoirs. This cluster is worth two points.

Cluster 2 asks students to interpret schematic plans (e.g., 1- and 3-dimensional drawings) of the skateboard ramp shown in the video, indicate the length in feet and inches of each 2×4 -inch board required for building the frame, and then convert these lengths to inches. Students also indicate how many boards of each length are needed. The PPT shows the schematic plans with each part of the skateboard frame labeled in feet and inches. Students complete a table of the required information. The same information is required for the CBT but the plans are not shown next to the table as they are on the PPT. Instead, students must navigate the software to locate the plans. The plans on both assessments are the same except that those on PPT are shaded in black and grays and labeled (e.g., diagonal brace, top side support) whereas the CBT plans are shown in color and not labeled.

Video Help (Anchored Video)



Bank Statement

Michael's Bank Statement

SCU Savere Credit Union	Monthly Statement
Member Number: 524-5896-Tz152	
Your balance last period.....	\$ 120.00
Average daily balance.....	\$ 98.00
Annual percentage yield earned.....	2.91%
Total withdrawals this period.....	\$ 47.00 —
YOUR NEW BALANCE.....	\$ 73.00

Store Advertisement

Smith's Tool
Green Treated Lumber On Sale
Better Quality...We Buy The Lumber Professionals Use From The Finest Mills in North America.

Size	6'	8'	10'
2"x4"	2 ¹⁰	2 ⁴⁹	3 ⁹⁹
2"x6"	3 ⁴⁹	4 ²³	5 ⁹⁹

2 1/2" Frame Screws
5 Pound box.....\$11⁴⁹
3 Pound box.....\$8⁹²

1 5/8" Deck Screws
5 Pound box.....\$7⁸⁹
3 Pound box.....\$4⁶⁶
1 Pound box.....\$2⁸⁹

Prices do not include 5% sales tax.

Navigation Help

Resources VIDEO PLANS STATEMENT AD MATERIALS

Question #5:
Figure out the best use for the lumber in the garage.
Place a marker on the spot you will need to make a cut. Label the pieces by dragging the name from the list.

TRACKING

Labels: 12 34 56 78 90 10 12 14 16 18 20

wood left over? ☐

wood left over? ☐

wood left over? ☐

wood left over? ☐

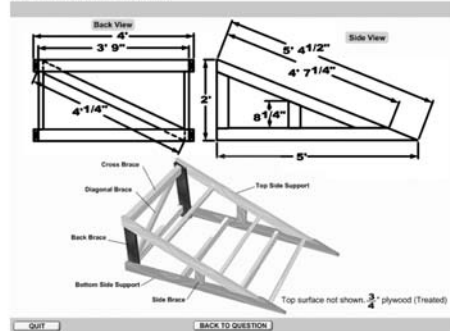
wood left over? ☐

wood left over? ☐

Markers: ☐ Side Brace ☐ Cross Brace ☐ Diagonal Brace ☐ Bottom Side Support ☐ Top Side Support ☐ Back Brace

Navigation: QUIT BACK TO QUESTION NEXT

Schematic Plans



Ramp Materials List

Ramp Material List

- Frame:**
2" x 4" dimension green treated lumber
- Deck:**
Green treated plywood: 4' x 8', 3/4" thick
- Frame screws:**
5 pounds 2 1/2" long
- Deck screws:**
1 pound 1 5/8" long

Who's Who

Resources VIDEO PLANS STATEMENT AD MATERIALS HELP WITH THIS SCREEN

Question #1:
How much money do the students have to spend on this project? Show how you got this information.

Student Name: First Last

WHO IS WHO

Who's Who: Ryan, Michael, Cindy

Navigation: QUIT Questions 1 2 3 4 5 6 7 PREVIOUS NEXT

Tracking Materials Used

This screen will help you keep track of the ramp pieces. Click on the pieces you have already cut. You can go back to the question any time by clicking on the "Back to Question" button

Navigation: QUIT BACK TO QUESTION RESET

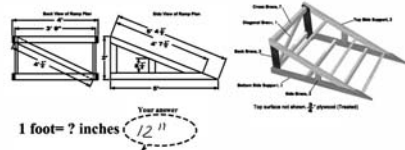
Fig. 1 Information reservoirs in the computer-based test (CBT)

Cluster 2 Interpreting schematic plans

2. Figure out the total number of boards needed to build the ramp. Make sure that your answers are in inches.

-

Work Area

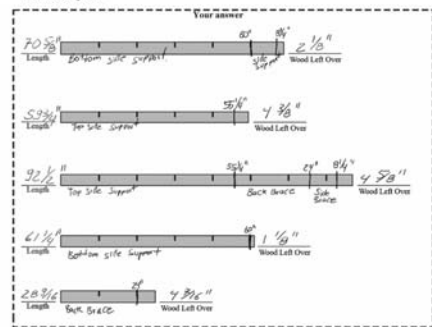
$$\begin{array}{r} 73 \\ -19 \\ \hline 24 \end{array}$$


Your answer			
Quantity	Description	Size in Feet	Size in Inches
2	Sid. Bracs	8 1/2'	80 1/2"
2	Bottom Sidt support	5'	60"
2	Back Braces	2'	24"
1	Diagonal Brace	4' 1 1/4"	48 3/4"
7	Cross Braces	3' 9"	45"
2	top side supports	4' 7 3/4"	55 1/4"

Clusters 4 & 5 Comparing relative lengths and making best use of lumber in garage

4. Label the wood that you found in the garage (drawn below) and show how you would use the wood in your skateboard ramp. Make sure that you show how much wood is left in each piece.


Your answer			
Quantity	Description	Size in Feet	Size in Inches
1	Board	5' 10 $\frac{5}{8}$ "	70 $\frac{5}{8}$ "
1	Board	5' 1 $\frac{1}{4}$ "	61 $\frac{1}{4}$ "
1	Board	4' 11 $\frac{3}{4}$ "	59 $\frac{3}{4}$ "
1	Board	2' 4 $\frac{7}{16}$ "	28 $\frac{7}{16}$ "
1	Board	7' 8 $\frac{1}{2}$ "	92 $\frac{1}{2}$ "



Cluster 7 Computing total cost


6. How much does it cost to build the ramp?

10 foot 2×4 's = _____ inches



8 foot 2×4 's = 96 inches

Cross brace



Cross brace

Cross brace

Cross brace

Cross brace

Cross brace

Wale


Wale

Wale

Wale

Wale

6 foot 2×4 's = _____ inches



Skateboard Ramp Materials List

Frame:
 4 × 6 dimension green treated lumber

Deck:
 1/2" dimension green treated plywood 4' x 8', 3/4" thick

Frame screws:
 4 pounds 3 1/2" long

Deck screws:
 1 pound 1 5/8" long

Your answer		
Quantity	Measure	Cost
4	8 foot 2x4"	\$9.36
1	5 pounds 2 1/2" long	\$11.43
1	1 pound 1 5/8" long	\$2.83
1	green treated plywood 48x8' x 3/4" thick	\$29.45
	Subtotal	\$53.79
	Tax	\$2.69
	Total	\$56.48

However, there is a tracking feature on the CBT that enables students to keep track of the boards they have accounted for. This cluster of items is worth a total of six points.

 Springer

Cluster 2 Interpreting schematic plans

[Resources](#)
[Plans](#)
[Statements](#)
[AD](#)
[Materials](#)
[Help With This Screen](#)

Question #2: Student Name: First _____ Last _____

Figure out the total number and lengths of boards Cindy, Ryan and Michael need to build the ramp.

Description	Length of Each Board in feet and inches	Length of Each Board in inches	Quantity (how many)
Cross Brace	3' 9"	45"	7
Diagonal Brace	4 1/4"	48 1/4"	1
Bottom Side Support	5'	60"	2
Back Brace	2'	24"	2
Side Brace	8 1/4"	8 1/4"	2
Top Side Support	4' 7"	55 1/4"	2


[Quit](#)
[Questions](#)
[1](#)
[2](#)
[3](#)
[4](#)
[5](#)
[6](#)
[7](#)
[Previous](#)
[Next](#)


Cluster 4 Comparing relative lengths


[Resources](#)
[VIDEO](#)
[PLANS](#)
[STATEMENT](#)
[AD](#)
[MATERIALS](#)
[HELP WITH THIS SCREEN](#)


Question #4: Student Name: First Last


Drag the corresponding wood piece to the correct measurement.

$28\frac{1}{4}$


$61\frac{1}{4}$


$92\frac{1}{2}$


$59\frac{3}{4}$


$70\frac{5}{8}$


Cluster 6 Figuring out how much wood to buy

RESOURCES VIDEO PLANS STATEMENT AD MATERIALS HELP WITH THIS SCREEN

Question #8: Student Name: First Last

Place the marker where you need to make a cut. Label the pieces by dragging the name from the "Parts Labels" box. Indicate in the white box how many inches are left over

TRACKING

Top Table Support

wood left over? 36"

Cross Brace

wood left over? 6"

Crate Brace

wood left over?

wood left over?

wood left over?

wood left over?

Parts Labels

- Side Brace
- Cross Brace
- Diagonal Brace
- Bottom Side Support
- Top Side Support
- Back Brace

Markers

Lumber Store

Click to Buy

- 10" Lumber
- 8" Lumber
- 6" Lumber

1 2 3 4 5 6 7 8 9 10 11 12

inches

Questions 1 2 3 4 5 6 7

PREVIOUS NEXT

Fig. 3 Item clusters in the computer-based test (CBT)

the best use of this wood before deciding how much new wood they need to buy. Both the PPT and CBT versions require students to read a tape measure to an eighth of an inch and to record the lengths in inches. The CBT also asks students to match relative lengths of the 2×4 s to the lengths shown on the tape measure. This cluster is worth three points.

Cluster 4 on the CBT asks students to transfer the five lengths from cluster 3 to a table showing representations of 2×4 s. Students have to label 2×4 s shown in the table according to their relative lengths. This cluster is shown together with cluster 5 on the PPT. Since this group of items does not call for students to use computation skills, the cluster is worth only two points.

Cluster 5 items are worth a total of 10 points, because they are especially important for solving the overall problem. On both the PPT and CBT, students are to indicate the most economical lengths to cut the 2×4 s for building the ramp frame. This work involves adding combinations of wood in such a way as to waste as little wood as possible. To figure out the correct combinations, students must accurately add mixed numbers. They must also indicate how much of each board is left over after cutting the wood, which involves subtracting mixed numbers. In addition, students must label each piece they cut with the part of the ramp frame shown in the schematic drawing. On the PPT, students show the combinations and label them with their pencil. On the CBT, students show where to cut the boards by dragging markers to the appropriate places on each board. The CBT also provides students with a virtual ruler they can use to doublecheck the lengths of the wood they have cut. This cluster is worth a total of 10 points.

Cluster 6 is worth six points and the items are similar to those in cluster 5 because students are to show the most economical use of *new* wood they need to buy for building the rest of the ramp after making use of the wood in the garage. Students are to indicate where they would cut 6-foot, 8-foot, or 10-foot lengths of 2×4 s they would purchase from the lumberyard and correctly label them. As in cluster 5, the students who take the PPT are to use a pencil to show where they would cut the wood and label the piece with the part of the ramp. On the CBT, students are required drag the marker to the cut points and move the correct ramp labels onto the boards.

Cluster 7 asks students to complete a materials list using all the relevant from their calculations. In addition to indicating the screws, the 2×4 lumber, and plywood decking they need to buy, they compute the total cost of the project, including sales tax. On the PPT, the materials list (not the quantities) and the store advertisement are shown on the same page as the item. On the CBT, students must access the information reservoirs to retrieve the information for the expense table (e.g., plans, store ad). This cluster is worth nine points.

Research design

The study was conducted on two levels. The first level consisted of a randomized pretest–posttest design that assessed the performance of students who took the CBT compared to students who took the PPT after all students had been taught with EAI. Specifically, the purpose was to assess whether students at three levels of math achievement (i.e., high, average, and low) would demonstrate the same or different levels of understanding on the CBT compared with PPT. Students were matched on math ability based on a standardized measure and then assigned to either the CBT or PPT assessment group. Before and after instruction with EAI, students in both groups took either the CBT or PPT.

A second objective was to trace the search-path maps of six students who were classified as high achievers, average achievers, and low achievers by their teachers. The students were video-recorded while they were taking the CBT pretest and posttest. One camera was positioned in front of the students to record their facial and body movements. The other camera was connected to the computer monitor to record the student's on-screen activity. The on-screen video was captured, digitized, and compressed into 14.25 GB in MPEG-1 encoding format and then merged into video analysis software called *vPrism*. The software enabled us to determine the navigations students made through the CBT along with the frequency of visits and the amount of time students at the cluster questions, information reservoirs, and help screens.

Implementation fidelity

Several methods converged to help ensure that the instruction and assessment procedures were followed. Both teachers had taught EAI in previous years and participated in controlled intervention studies using the *Fraction of the Cost* problem. One of the math teachers (MT2) had helped write the lesson plans and had conducted two training sessions with teachers from other school districts on implementing EAI in general education and special education settings. The math teachers had common planning times when they discussed their instructional plans. In addition, research staff observed classroom practices on several occasions. Finally, members of the research staff were on hand throughout the testing process, both at pretest and posttest, to observe and video record students as they took the PPT and CBT. The implementation data showed that procedures were followed as planned except in one instance when the special education teacher was observed pointing to items on the paper of one student with LD who was taking the PPT. It is unclear how much help this student actually received from the special education teachers or what effect this may have had on the overall score. She was not present during the CBT testing and students with disabilities took the test as planned.

Results

Overall comparisons

Prior to conducting the analyses, the two groups of students that had been randomly assigned to CBT or PPT based on their WKCE scores were stratified into groups of high achievers (HA), average achievers (AA), or low achievers (LA). The lowest-achieving 25% and highest-achieving 25% students were considered LA and HA, respectively. Overall means and standard deviations (reported as NCEs) were 39.7 for LA ($n = 26$, $SD = 12.9$), 65.2 for AA ($n = 57$, $SD = 6.9$), and 88.0 for HA ($n = 26$, $SD = 26$). No differences were found in student performance between teachers within achievement for LA, $t(24) = -0.681$, $p = .502$ ($n = 9$ [MT1], $n = 17$ [MT2]) or for AA, $t(55) = 0.635$, $p = .528$ ($n = 31$ [MT1], $n = 26$ [MT2]). There was a difference between teachers for HA, $t(24) = 2.181$, $p = .039$ ($n = 19$ [MT1], $n = 7$ [MT2]) but there were no overall differences because half the students from each of the teacher's classes was randomly assigned to one or the other test condition (see "Participants" section).

Table 1 shows descriptive information of the HA, AA, and LA students who took PPT or CBT. The data were analyzed in a 3 (HA, AA, LA) \times 2 (PPT, CBT) ANOVA with time

Table 1 Means and standard deviations overall and by ability level

Group	Paper–pencil test		Computer-based test	
	<i>n</i>	<i>M (SD)</i>	<i>n</i>	<i>M (SD)</i>
Overall	53		56	
Pretest		13.6 (6.6)		15.1 (6.2)
Posttest		31.8 (7.1)		31.5 (6.4)
High achievers	13		13	
Pretest		14.6 (9.1)		21.4 (4.1)
Posttest		35.1 (4.7)		35.2 (3.6)
Average achievers	26		31	
Pretest		14.9 (5.1)		14.9 (4.8)
Posttest		34.4 (4.1)		32.6 (3.9)
Low achievers	14		12	
Pretest		10.0 (5.4)		8.6 (4.5)
Posttest		24.1 (7.6)		24.4 (8.7)

of test (pretest, posttest) as the repeated measure. Results indicated a main effect for achievement level, $F(2,103) = 39.15$, $p < .001$, $\eta^2 = .43$, and for time of test, $F(1,103) = 603.40$, $p < .001$, $\eta^2 = .85$. Post-hoc comparisons showed that HA students outscored AA students, and AA students outscored LA students. There were no other significant main effects or interactions. A summary of results is provided in Table 2.

Item cluster comparisons

In addition to comparing overall test scores, we analyzed item cluster scores to gather a more complete understanding of student performances. Because the maximum score for

Table 2 Analysis of variance results for overall test scores

	<i>df</i>	<i>F</i>	<i>p</i>	η^2
Main effects				
Ability	2,103	39.15	<.001	0.43
Time of test	1,103	603.40	<.001	0.85
Test format	1,103	0.59	0.443	–
Two-way interactions				
Ability by time of test	2,103	2.68	0.073	–
Ability by test format	2,103	2.46	0.090	–
Time of test by test format	1,103	3.01	0.086	–
Three-way interaction				
Ability by format by time	2,103	2.54	0.840	–

each cluster was small (range = 2–10 points), the clusters were analyzed with non-parametric techniques. The Mann–Whitney test compared performances of students by test format (PPT vs. CBT) whereas the Kruskal–Wallis test compared performances of students by achievement group (HA, AA, LA). The large sample approximations of these tests were used for the tests of two-way interactions while exact tests were used for the three-way interaction due to small group sizes. The Holm procedure was used to control family wide Type I error rate to 0.05. Table 3 shows the CBT and PPT item cluster scores on the CBT and PPT for each ability group.

Performance between test format within ability group

At posttest, there were no significant differences between PPT and CBT. At pretest, however, results showed three clusters where CBT students outscored PPT students: cluster 3 ($Z = 3.012$, $p = .003$), cluster 4 ($Z = 3.594$, $p < .001$), and cluster 5 ($Z = 3.752$, $p < .001$). Much of this difference can be attributed to the HA students who scored higher on the CBT than on the PPT in cluster 2 ($Z = 3.021$, $p = .003$), cluster 4 ($Z = 2.726$, $p = .006$), and cluster 5 ($Z = 2.808$, $p = .005$). This trend is reversed in cluster 7 where the PPT students outscored the CBT students ($Z = 5.08$, $p < .001$).

Performance between ability groups within test format

Differences between achievement levels were studied within each cluster for test format and testing time using the Kruskal–Wallis test and the Holm Method with Shaffer logic to protect against inflation of the Type I error rate. The four families compared were PPT at pretest, PPT at posttest, CBT at pretest, and CBT at posttest.

On the PPT pretest, there were no differences between achievement groups. However, on the CBT pretest, there were differences in cluster 1 ($\chi^2(2) = 14.412$, $p = 0.001$), cluster 2 ($\chi^2(2) = 21.961$, $p < 0.001$), and cluster 5 ($\chi^2(2) = 20.536$, $p < 0.001$). There was more variability in posttest performance on the both the PPT and CBT. On the PPT posttest, there were differences in three clusters: Cluster 1 ($\chi^2(2) = 17.564$, $p < 0.001$), Cluster 5 ($\chi^2(2) = 18.592$, $p < 0.001$), and Cluster 6 ($\chi^2(2) = 10.627$, $p = 0.005$). Subsequent pair wise comparisons using exact Mann–Whitney tests revealed that HA and AA students outscored LA students in clusters 1 and 5. In cluster 6, AA students scored higher than LA students. On the CBT posttest there were three clusters for which there were significant differences between achievement groups: Cluster 2 ($\chi^2(2) = 11.209$, $p = 0.004$), Cluster 5 ($\chi^2(2) = 11.884$, $p = 0.003$), and Cluster 6 ($\chi^2(2) = 8.867$, $p = 0.010$). In all three clusters, HA outperformed LA. However, there were no significant differences between LA and AA scores on any of the seven clusters.

Time in clusters and navigation maps

A total of six students' navigations were mapped (2 HA, 2 AA, 2LA). Table 4 shows the proportion of time students spent on the item clusters compared to information reservoirs. Math composite scores on the standardized WKCE test in percentile ranks were 82 and 83 for the HA students, 56 and 61 for the AA students, and 22 and 12 for the LA students. Both of the LA students were receiving special education services for LD. All students

Table 3 Item cluster performances of high-achieving (HA), average-achieving (AA), and low-achieving (LA) Students

	PPT (<i>n</i> = 53)					CBT (<i>n</i> = 56)				
	PRE		POST		Overall	PRE		POST		Overall
	<i>X</i>	<i>SD</i>	<i>X</i>	<i>SD</i>		<i>X</i>	<i>SD</i>	<i>X</i>	<i>SD</i>	
<i>Cluster 1 (Total = 2)</i>										
HA	1.77	.60	2.00	.00	1.89	1.92	.28	2.00	.00	1.96
AA	1.38	.75	1.81	.57	1.60	1.48	.57	1.94	.25	1.71
LA	1.21	.97	1.21	.70	1.21	.83	.83	1.50	.67	1.17
Overall	1.43	.80	1.70	.61	1.57	1.45	.69	1.86	.40	1.66
			HA = AA			HA > AA				
			HA > LA			HA > LA				
			AA > LA			AA = LA				
<i>Cluster 2 (Total = 6)</i>										
HA	3.54	2.37	5.92	2.78	4.73	5.77	.44	6.00	.00	5.89
AA	3.81	2.12	5.77	.51	4.79	4.52	1.34	5.81	.40	5.17
LA	2.64	2.41	5.07	1.59	3.86	2.08	2.07	4.17	2.29	3.13
Overall	3.43	2.27	5.62	.95	4.53	4.29	1.87	5.50	1.28	4.90
						HA > AA		HA = AA		
						HA > LA		HA > LA		
						AA > LA		AA = LA		
<i>Cluster 3 (Total = 3)</i>										
HA	2.26	1.20	3.00	.00	2.63	3.00	.00	3.00	.00	3.00
AA	2.86	.60	2.95	.16	2.91	2.96	.21	2.98	.11	2.97
LA	2.10	1.24	2.79	.80	2.45	2.70	.87	3.00	.00	2.85
Overall	2.51	1.01	2.92	.42	2.72	2.91	.43	2.99	.08	2.95
<i>Cluster 4 (Total = 2)</i>										
HA	1.15	.99	2.00	.00	1.58	2.00	.00	2.00	.00	2.00
AA	1.73	.67	2.00	.00	1.87	1.94	.36	2.00	.00	1.97
LA	1.14	.95	1.57	.85	1.36	1.75	.62	2.00	.00	1.88
Overall	1.43	.87	1.89	.47	1.66	1.91	.39	2.00	.00	1.96
<i>Cluster 5 (Total = 10)</i>										
HA	3.00	4.26	9.38	.77	6.19	7.54	2.82	9.31	.85	8.43
AA	1.62	2.48	9.19	1.39	5.41	3.42	3.09	8.29	1.95	5.86
LA	.57	1.65	4.43	3.57	2.50	1.17	2.04	5.33	3.17	3.25
Overall	1.68	2.93	7.98	2.98	4.83	3.89	3.56	7.89	2.50	5.89
			HA = AA			HA > AA		HA = AA		
			HA > LA			HA > LA		HA > LA		
			AA > LA			AA = LA		AA = LA		
<i>Cluster 6 (Total = 6)</i>										
HA	1.54	1.81	5.23	1.69	3.39	1.15	1.77	5.38	1.19	3.27
AA	1.08	1.55	5.38	1.06	3.23	.35	.71	4.68	1.33	2.52
LA	.21	.80	3.50	2.14	1.86	.00	.00	3.50	2.02	1.75
Overall	.96	1.52	4.85	1.74	2.91	.46	1.06	4.59	1.58	2.53

Table 3 continued

PPT (<i>n</i> = 53)						CBT (<i>n</i> = 56)					
PRE			POST		Overall	PRE		POST		Overall	
<i>X</i>	<i>SD</i>	<i>X</i>	<i>SD</i>	<i>X</i>		<i>SD</i>	<i>X</i>	<i>SD</i>			
								HA = AA			
								HA = LA			
								AA > LA			
<i>Cluster 7 (Total = 9)</i>											
HA	1.38	2.36	7.54	2.60	4.46	.00	.00	7.54	2.60	3.77	
AA	2.42	2.66	7.31	2.28	4.87	.26	1.44	6.90	2.43	3.58	
LA	2.14	2.35	5.5	2.65	3.82	.08	.29	4.92	2.94	2.50	
Overall	2.09	2.50	6.89	2.55	4.49	.16	1.07	6.63	2.70	3.40	
<i>TOTAL (Total = 38)</i>											
	13.55	6.61	31.84	7.06	22.70	15.08	6.22	31.45	6.42	23.27	

Type I error rate controlled for each family, PPT Pre, PPT Post, CBT Pre, and CBT Post

The = in the group comparisons indicates that there is not a significant difference

Table 4 Proportion of time students spent in item clusters and information reservoirs

Student	Pretest				Posttest			
	Score		Proportion of time		Score		Proportion of time	
			Item clusters	Information reservoirs			Item clusters	Information reservoirs
High achievers								
Student 1	15	.85		.15	28	.76		.24
Student 2	18	.55		.45	31	.87		.13
Average achievers								
Student 3	11	.76		.24	29	.81		.19
Student 4	16	.62		.38	29	.89		.11
Low achievers								
Student 5	5	.61		.39	13	.75		.25
Student 6	6	.66		.34	17	.71		.29

except one (HA student) spent more time on item clusters at posttest than at pretest possibly indicating they had less need for the learning scaffolds following instruction and could immediately turn their attention to problem solving.

Table 5 shows the proportion of time the six students spent in each item cluster and the points they earned at pretest and posttest. The students, regardless of ability level, spent most of their item on the most critical items for solving the overall problem. The LA students spent more than one-third of their time in cluster 2, which requires students to “read” the schematic plan, construct a table that includes labels and dimensions of each part of the plan, and convert from feet and inches to inches. All four of the HA and AA students received full credit on this posttest item whereas the two LA students earned five points and two points. Students also spent a large portion of their time on cluster 5 where they are asked to figure out the most economical way of cutting the 2×4 s in the garage.

Table 5 Percentage of time spent in individual clusters for selected students

Item Cluster	Student 1 (HA)		Student 2 (HA)		Student 3 (AA)		Student 4 (AA)		Student 5 (LA)		Student 6 (LA)	
	Pre	Post	Pre	Post	Pre	Post	Pre	Post	Pre	Post	Pre	Post
1	0.76	8.74	9.42	1.69	4.58	10.01	8.56	4.13	16.51	9.32	10.38	5.01
4 pts.	(1)	(2)	(2)	(2)	(0)	(2)	(2)	(2)	(0)	(1)	(1)	(2)
2	22.94	17.29	11.27	33.77	20.81	12.10	22.19	28.96	29.92	38.72	23.32	35.21
6 pts.	(3)	(6)	(3)	(6)	(6)	(6)	(4)	(6)	(0)	(2)	(0)	(5)
3	12.62	8.48	8.56	4.48	9.74	5.71	15.01	5.26	10.93	15.47	9.44	11.89
3 pts.	(3)	(3)	(3)	(3)	(3)	(3)	(3)	(3)	(3)	(3)	(3)	(3)
4	2.84	2.37	4.03	2.84	1.62	1.60	3.31	1.94	2.75	4.87	2.19	2.57
2 pts.	(2)	(2)	(2)	(2)	(2)	(2)	(2)	(2)	(2)	(2)	(2)	(2)
5	43.22	38.31	44.64	30.66	37.11	34.52	50.58	54.17	18.96	30.90	27.68	25.10
10 pts.	(5)	(9)	(6)	(9)	(0)	(9)	(5)	(8)	(0)	(5)	(0)	(4)
6	17.09	20.20	22.07	16.01	4.58	19.47	0.36	5.40	12.53	0.23	24.73	14.79
6 pts.	(1)	(6)	(2)	(5)	(0)	(6)	(0)	(4)	(0)	(0)	(0)	(1)
7	0.54	4.61	0.00	10.55	21.55	16.60	0.00	0.14	8.39	0.48	2.27	5.43
9 pts.	(0)	(0)	(0)	(4)	(0)	(9)	(0)	(4)	(0)	(0)	(0)	(0)
Total	100	100	100	100	100	100	100	100	100	100	100	100
38 pts.	(15)	(28)	(18)	(31)	(11)	(29)	(16)	(29)	(5)	(13)	(6)	(17)

Numbers in parentheses () indicate obtained scores

The HA and AA students were quite successful on this item cluster whereas the LA students earned about half the points. All six students received full credit for clusters 3 and 4, which involved reading a tape measure and matching the lengths of boards to the dimensions. However, students did poorly on clusters 6 and 7, possibly because they ran out of time.

Figures 4–7 show the CBT screens and the navigation routes of one HA student and one LA student at pretest and posttest. The HA and LA student scored 15 and 6 on the pretest and 33 and 19 on the posttest, respectively. The boxes along the top and the bottom of the figure show the information reservoirs (e.g., video, plans, tracking, who's who); those in the center of the page show the item clusters. The lines between the boxes represent the number of navigations students made between test locations with the thicker lines indicating more frequent visits. The actual frequencies to and from each location are provided in parentheses. On the HA student pretest, the heaviest traffic was between the skateboard ramp plans and between questions 5 and 6, which asked the student to cut the lumber in the appropriate lengths thereby wasting as little wood as possible. The student also used the tracking feature of the program to help her remember which parts of the ramp she had already "built". Her posttest map differed from her pretest map somewhat because she went directly from question 2 to question 5 without having to rely on the support screens. She also traveled frequently to the last item where she summarized her solution to the problem.

The LA student traveled many times during the pretest between the ramp plans and item cluster 2, which asked him to complete a table with the lengths and quantity of wood required for each part of the ramp. He also made use of the help button, but he rarely went to questions 5 and 6. However, on the posttest he spent more time working on the difficult items of the assessment and his search map grew more similar to that of the HA student. His map also suggests that he realized he needed to access information from the schematic plans, bank statement, and the store ad for answering item cluster 7.

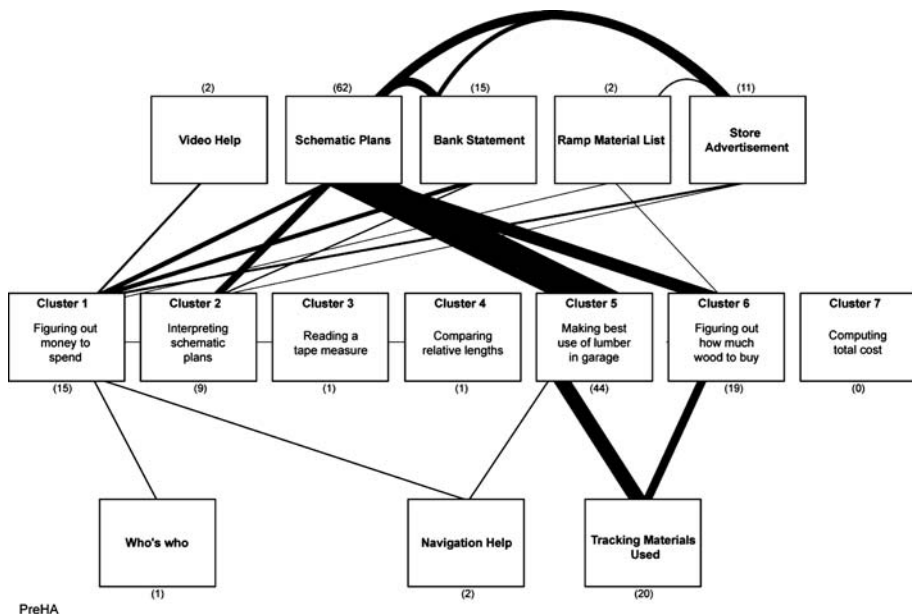


Fig. 4 Navigation map of high-achieving student on the computer-based pretest

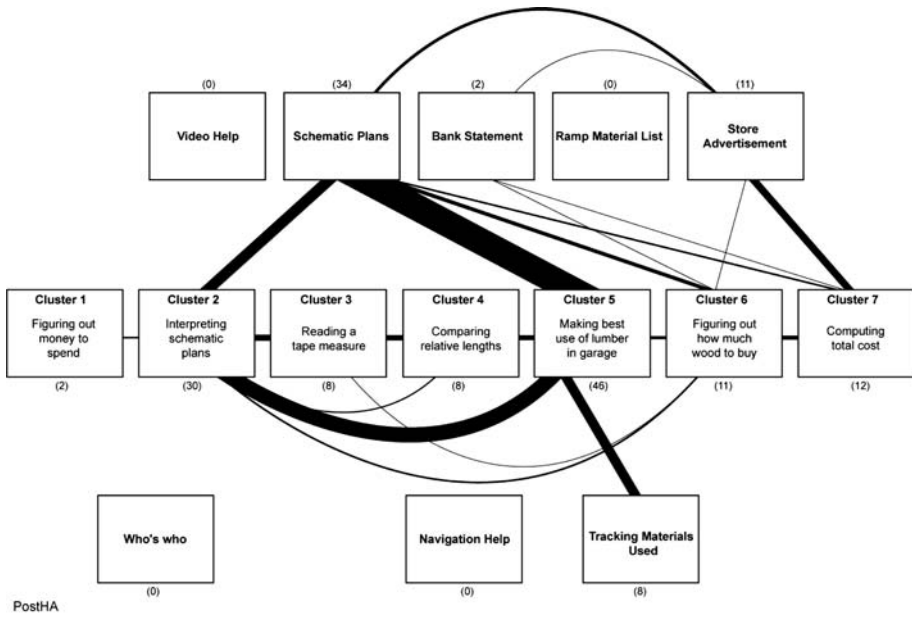


Fig. 5 Navigation map of high-achieving student on the computer-based posttest

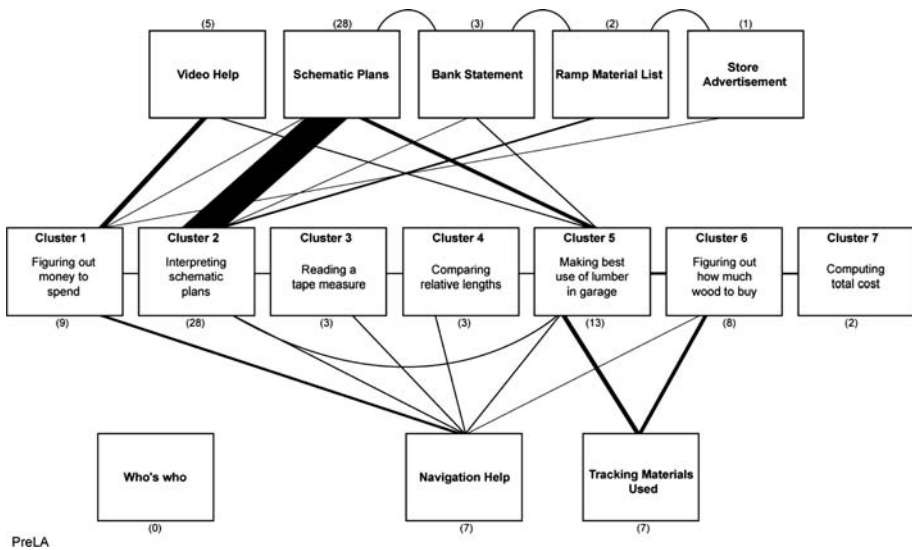


Fig. 6 Navigation map of low-achieving student on the computer-based pretest

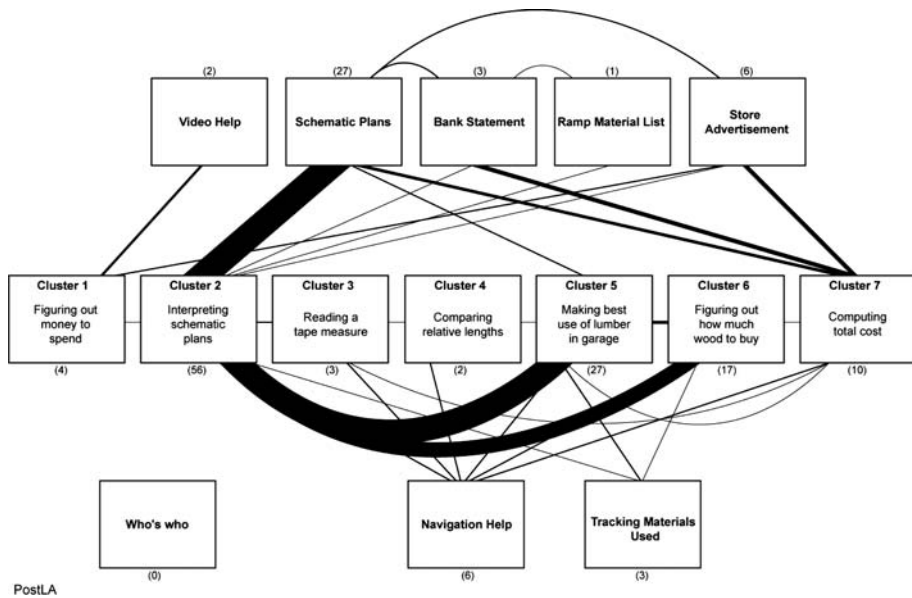


Fig. 7 Navigation map of low-achieving student on the computer-based posttest

Anecdotal findings

Observers were on hand to watch students as they took the PPT and CBT pretest and posttest. The following informal findings were noted. First, students in the CBT condition worked for the entire class time on the pretest and the posttest. Although students taking the CBT did not score higher than students in the PPT condition overall, it was evident that the multimedia format of the test genuinely interested the students. Many students taking the PPT also worked for most of the time but several students appeared to stop early, either because they were finished or they could do no more. Second, the students who took the CBT asked very few questions about how to navigate the program. This was unexpected because the application was new to students. Students explored the CBT as though it was an instructional tool rather than an assessment tool.

Discussion

The purpose of this randomized experiment was twofold. First, we compared two methods (CBT or PPT) of assessing the math skills of HA, AA, and LA students after they had been taught with EAI. Second, we used the CBT to gain a deeper understanding of students' problem solving performance as they navigated between item clusters and information reservoirs. This information could be used in future work to revise test items on both tests, provide more adaptive navigation routes for low-achieving students on the CBT, and identify what kind of learning scaffolds are needed in both the instructional and assessment software.

Related to the first purpose, the results showed there were no differences between assessment methods (CBT or PPT) for total test score within the three achievement levels. Although some studies comparing pencil-paper and computer test formats have shown one

testing condition superior to the other (e.g., DeAngelis 2000; Federico 1989; Hargreaves et al. 2004; Mazzeo et al. 1991), other studies have found no differences between testing conditions (Andersson et al. 2003; Clariana and Wallace 2002; Mason et al. 2001; Schaeffer et al. 1993). Each achievement group scored significantly higher on the posttest than they did on the pretest, an indication that students, regardless of ability level, profited from EAI. Inspection of performances on specific items revealed HA students scored higher than the other achievement groups on three item clusters on the CBT pretest, an indication that these students were able to use the information reservoirs to figure some problems prior to instruction. These differences were diminished and, in fact, disappeared in some cases between the AA and LA groups on the CBT posttest. Two item clusters (i.e., 2 and 5) seemed to account for most of the differences in total scores between achievement groups. Solving these groups of items correctly was key to figuring out solutions to the other test items.

Analyses of the students' navigation patterns through the CBT provided clues about the problem solving behaviors of students at the three achievement levels. Although LA students scored lower than the AA students and the HA students on the CBT overall, their navigation maps were quite similar. That is, the LA students spent most of their time answering clusters of items that were central to solving the overall problem in *Fraction of the Cost*. They also accessed the information reservoirs to search for the relevant information for helping them construct a useful strategy, although the HA student did not seem to need them as much as the LA student during the posttest.

Implications

These results suggest that the newly developed CBT is a viable method for assessing students' problem solving ability on complex problems such as the EAI problem, *Fraction of the Cost*. The pathways between items and information reservoirs seemed easily navigable for each group of students, including students with LD. Prior to conducting the study, ease of navigation was a concern because the students had not been exposed to the test architecture. Although the screens were similar to those students had encountered during instruction, they had not been taught how to access them. On both the CBT and PPT, we attempted to reduce the potential for overloading students' working memory by limiting text and integrating graphics (Clark and Mayer 2003; Mayer 2001). Overload was reduced on the CBT by carefully paying attention to anticipated student movements through the software. The static visual representations on the PPT had been refined over the course of several previous studies so students could readily understand the intent of the items without compromising the complex nature of the concepts tested by the items (Rose and Meyer 2007).

Based on these findings, the multimedia format of the CBT seems to carry with it several advantages. First, the content of the CBT is complex and aligns with the movement to extend "basic" skills beyond procedural competency advocated by teacher groups (e.g., National Council of Teachers of Mathematics 2000), by employer groups (e.g., National Center on Education and the Economy 2007), and in government legislation (e.g., No Child Left Behind Act of 2001). The CBT requires students to actively engage in solving a complex problem for which there are several related subproblems. Most students, even those with learning disabilities, were able to navigate the assessment space of the CBT. In fact, observers reported that all of the students worked continuously through the class period on the CBT.

The second advantage of the CBT is the diagnostic information it provides. Having the ability to trace students' movements to and from items and scaffolds furnishes important information on whether the students are paying attention to the most critical subproblems, the time students spend answering these items, and the scaffolds students make use of for helping them understand the problem. These interactions are complex but are made more visible by the tracking features used with the software. The problems embedded in *Fraction of the Cost* are considered to be highly interactive because the overall problem cannot be solved without all the elements being processed together. The use of learning scaffolds in the form of story contexts, visual representations, and other interactive tools can help students reduce the cognitive load imposed by this interactivity (Clark and Mayer 2003; Mousavi et al. 1995; Rittle-Johnson and Koedinger 2005; Mayer and Moreno 2003). Knowing where in the learning and assessment process overload happens may lead to more accessible designs of both instructional and assessment tools.

Although the results show promise for using CBT formats, the conclusions that can be drawn from the findings are somewhat limited. First, the rural school from which the students were drawn was relatively high performing and not diverse. In addition, the average achievement levels within the ability groups were quite high and it is not clear whether similar results would have been obtained with a lower-achieving or more heterogeneous student population. Second, it was not possible to generate the strategic maps of more than six students because of the constraints imposed by the data collection procedures. The search maps were generated post-hoc in a labor-intensive process, which involved tracking and recording each movement of the student's cursor. In future research, the software will generate these maps automatically for all students in the class providing us with more confidence in our findings.

Despite these limitations, this research provides a first step in developing multimedia-based assessments that can match the contextualized nature of the authentic-like problems used in EAI. The accommodations afforded by more flexible test formats may have the potential to more adequately probe deeper understandings of students with poor language skills (e.g., receptive in the form of reading and expressive in the form of writing). The impact of such work is likely to provide clues about how to more appropriately measure the understanding of secondary school students where research on test accommodations is especially lacking (Sireci et al. 2005).

In future research, we expect to merge interactive assessments as used in this study with interactive instructional tools to provide both ongoing formative measures of skills to help teachers individualize instruction and summative assessments to evaluate the overall effectiveness of instructional practices. Our objective will be to collect information from the CBT to explore changes in students' mathematical abilities that may have contributed to differences in their test performance over time. In a recent study of EAI (Cho et al. 2007), the response patterns of low-achieving, average-achieving, and high-achieving students on a criterion-referenced problem-solving test were compared using mixture item response theory (IRT) models (Baker 1992; Baker and Kim 2004; Hambleton et al. 1991; Lord 1980). The results suggested that latent class membership reflected a clear change in ability from pretest to posttest. That is, many of the students who were considered low achieving on the basis of standardized, curriculum-aligned pretests joined the average-achieving students at posttest. Using the CBT format will enable us to map the individual student's performances on each item to more completely understand how these changes occur.

Acknowledgements The research reported in this article was supported by a grant from the U. S. Department of Education, Institute of Education Sciences Cognition and Student Learning (CASL) Program, Award No. R305H040032. Any opinions, findings, or conclusions are those of the authors and do not necessarily reflect the views of the supporting agency.

References

- Andersson, G., Kaldo-Sandstrom, V., Strom, L., & Stromgren, T. (2003). Internet administration of the Hospital Anxiety and Depression Scale in a sample of tinnitus patients. *Journal of Psychosomatic Research*, 55, 259–262.
- Baker, F. B. (1992). *Item response theory: Parameter estimation techniques*. New York: Marcel Dekker.
- Baker, F. B., & Kim, S. H. (2004). *Item response theory: Parameter estimation techniques* (2nd ed.). New York: Marcel Dekker.
- Bottge, B. A. (1999). Effects of contextualized math instruction on problem solving of average and below-average achieving students. *Journal of Special Education*, 33, 81–92.
- Bottge, B. A., & Hasselbring, T. S. (1993). A comparison of two approaches for teaching complex, authentic mathematics problems to adolescents in remedial math classes. *Exceptional Children*, 59, 556–566.
- Bottge, B. A., Heinrichs, M., Chan, S., & Serlin, R. (2001). Anchoring adolescents' understanding of math concepts in rich problem-solving environments. *Remedial and Special Education*, 22, 299–314.
- Bottge, B. A., Heinrichs, M., Mehta, Z., & Hung, Y. (2002). Weighing the benefits of anchored math instruction for students with disabilities in general education classes. *The Journal of Special Education*, 35, 186–200.
- Bottge, B. A., Rueda, E., LaRoque, P. T., Serlin, R. C., & Kwon, J. (2007a). Integrating reform-oriented math instruction in special education settings. *Learning Disabilities Research & Practice*, 22, 96–109.
- Bottge, B. A., Rueda, E., Serlin, R. C., Hung, Y., & Kwon, J. (2007b). Shrinking achievement differences with anchored math problems: Challenges and possibilities. *The Journal of Special Education*, 41, 31–49.
- Bottge, B., Rueda, E., & Skivington, M. (2006). Situating math instruction in rich problem-solving contexts: Effects on adolescents with challenging behaviors. *Behavioral Disorders*, 31, 394–407.
- Bruner, J. S. (1975). The ontogenesis of speech acts. *Journal of Child Language*, 2, 1–40.
- Brush, T., & Saye, J. (2001). The use of embedded scaffolds with hypermedia-supported student-centered learning. *Journal of Multimedia and Hypermedia*, 10, 333–356.
- Cho, S., Cohen, A., Kim, S., & Bottge, B. (2007). *Latent transition analysis with a mixture response theory measurement model*. Paper to be presented at the National Council on Measurement in Education Annual Conference, Chicago, IL.
- Clariana, R., & Wallace, P. (2002). Paper-based versus computer-based assessment: Key factors associated with the test mode effect. *British Journal of Educational Technology*, 33, 593–602.
- Clark, R. C., & Mayer, R. E. (2003). *E-Learning and the science of instruction*. Hoboken, NJ: John Wiley & Sons, Inc.
- Cognition, Technology Group at Vanderbilt (1990). Anchored instruction and its relationship to situated cognition. *Educational Researcher*, 19(3), 2–10.
- Cognition, Technology Group at Vanderbilt (1997). *The Jasper Project: Lessons in curriculum, instruction, assessment, and professional development*. Mahwah, NJ: Erlbaum.
- CTB McGraw-Hill (2003). *TerraNova Comprehensive Tests of Basic Skills*. Monterey, CA.
- Dalton, S., & Overall, J. E. (1977). Nonrandom assignment in ANCOVA: The alternate ranks design. *Journal of Experimental Education*, 46, 58–62.
- DeAngelis, S. (2000). Equivalency of computer-based and paper-and-pencil testing. *Journal of Allied Health*, 29(3), 21–29.
- Dolan, R. P., & Hall, T. E. (2001). Universal design for learning: Implications for large-scale assessment. *IDA Perspectives*, 27(4), 22–25.
- Federico, P. A. (1989). Computer-based and paper-based measurement of recognition (Research Report No. NPRDC-TR-89-7): Navy Personnel Research and Development Centre Report.
- Ge, X., & Land, S. M. (2003). Scaffolding students' problem-solving processes in an ill-structured task using question prompts and peer interactions. *Educational Technology Research and Development*, 51(1), 21–38.
- Glasgow, N. (1997). *New curriculum for new times: A guide to student-centered, problem-based learning*. Thousand Oaks, CA: Corwin.
- Gray, K. C., & Herr, E. L. (1998). *Workforce education: The basics*. Boston: Allyn and Bacon.

- Hambelton, R. K., Swaminathan, H., & Rogers, H. J. (1991). *Fundamentals of item response theory*. Newbury Park, CA: Sage.
- Hannafin, M. J., Hill, J., & Land, S. (1997). Student-centered learning and interactive multimedia: Status, issues, and implications. *Contemporary Education*, 68(2), 94–99.
- Hannafin, M., Land, S., & Oliver, K. (1999). Open learning environments: Foundations, methods, and models. In C. M. Reigeluth (Ed.), *Instructional design theories and models: A new paradigm of instructional theory* (pp. 115–140). Mahwah, NJ: Erlbaum.
- Hargreaves, M., Shorrocks-Taylor, D., Swinnerton, B., Tait, K., & Threlfall, J. (2004). Computer or paper? That is the question: does the medium in which assessment questions are presented affect children's performance in mathematics? *Educational Research*, 46(1), 29–42.
- Hasselbring, T. S., Lewis, P., & Bausch, M. E. (2005). Assessing students with disabilities: Moving assessment forward through universal design. *Insight*, 5, 1–16.
- Kirsch, I., Braun, H., & Sum, A. (2007). *America's perfect storm: Three forces changing our nation's future*. Princeton, NJ: Educational Testing Service.
- Lester, J., & Kroll, D. L. (1990). *Assessing student growth in mathematical problem solving: Assessing higher order thinking in mathematics*. Washington, DC: American Association for the Advancement of Science.
- Lord, F. N. (1980). *Applications of item response theory to practical testing problems*. Mahwah, NJ: Erlbaum.
- Mason, B. J., Patry, M., & Bernstein, D. J. (2001). An examination of the equivalence between non-adaptive computer-based and traditional testing. *Journal of Educational Computing Research*, 24(1), 29–39.
- Mayer, R. E. (2001). *Multi-media learning*. New York: Cambridge University Press.
- Mayer, R. E., & Moreno, R. (2003). Nine ways to reduce cognitive load in multimedia learning. *Educational Psychology*, 38(1), 43–52.
- Mazzeo, J., Druesne, B., Raffeld, P., Checketts, K. T., & Muhlstein, E. (1991). *Comparability of computer and paper-and-pencil scores for two CLEP general examinations* (ETS Report No. RR-92-14). Princeton, NJ: Educational Testing Service.
- Mousavi, S. Y., Low, R., & Sweller, J. (1995). Reducing cognitive load by mixing auditory and visual presentation modes. *Journal of Educational Psychology*, 87, 319–334.
- Murnane, R. J., & Levy, F. (1996). *Teaching the new basic skills*. New York, NY: The Free Press.
- National Center on Education, the Economy (2007). *Tough choices or tough times: The report of the new commission on the skills of the American workforce*. Washington, DC.
- National Council of Teachers of Mathematics (2000). *Principles and standards for school mathematics*. Reston, VA: Author.
- No Child Left Behind Act of 2001, Pub. L. No. 107–110, 115 Stat. 1425 (2002).
- Palincsar, A. S. (1986). The role of dialogue in providing scaffolded instruction. *Educational Psychologist*, 21, 73–98.
- Palincsar, A. S., & Brown, A. L. (1984). Reciprocal teaching of comprehension-fostering and comprehension-monitoring activities. *Cognition and Instruction*, 1, 117–175.
- Perie, M., Grigg, W., & Dion, G. (2005). *The Nation's Report Card: Mathematics 2005* (NCES 2006-453). U. S. Department of Education. National Center for Education Statistics. Washington, DC: Government Printing Office.
- Puntambekar, S., & Stylianou, A. (2005). Designing navigation support in hypertext systems based on navigation patterns. *Instructional Science*, 33, 451–481.
- Puntambekar, S., Stylianou, A., & Hubscher, R. (2003). Improving navigation and learning in hypertext environments with navigable concept maps. *Human-Computer Interaction*, 18, 395–428.
- Rittle-Johnson, B., & Koedinger, K. R. (2005). Designing knowledge scaffolds to support mathematical problem solving. *Cognition and Instruction*, 23, 313–349.
- Rittle-Johnson, B., Siegler, R. S., & Alibali, M. W. (2001). Developing conceptual understanding and procedural skill in mathematics: An iterative process. *Journal of Educational Psychology*, 93, 346–362.
- Rose, D. H., & Meyer, A. (2007). Teaching every student in the digital age: Universal design for learning. Retrieved February 2, 2007 from: <http://www.cast.org/teachingeverystudent/ideas/tes/>
- Schaeffer, G., Reese, C. M., Steffen, M., McKinley, R. L., & Mills, C. N. (1993). *Field test of a computer-bases GRE general test* (Report No. ETS-RR-93-07). Princeton, NJ: Educational Testing Service.
- Shafer, M. C., & Romberg, T. A. (1999). Assessment in classrooms that promote understanding. In E. Fennema & T. A. Romberg (Eds.), *Mathematics classrooms that promote understanding* (pp. 159–184). Mahwah, NJ: Erlbaum.
- Sireci, S. G., Scarpatti, S. E., & Shuhong, L. (2005). Test accommodations for students with disabilities: An analysis of the interaction hypothesis. *Review of Educational Research*, 75, 475–490.

- Stone, J. R., Alfeld, C., Pearson, D., Lewis, M. V., & Jensen, S. (2006). *Building academic skills in context: Testing the value of enhanced math learning in CTE*. Minneapolis: University of Minnesota.
- Thornburg, D. (2002). *The new basics: Education and the future of work in the telematic age*. Alexandria, VA: Association for Supervision and Curriculum Development.
- Uchida, D., Cetron, M., & Mckenzie, F. (1996). *Preparing students for the 21st century*. Arlington, VA: American Association of School Administrators.
- University of Iowa (2001). *The Iowa Tests of Basic Skills (ITBS)*. Itasca, IL: Riverside Publishing.
- U.S. Department of Labor (1991). *What work requires of schools: A SCANS report for America*. Washington, DC: Author.
- Vygotsky, L. S. (1978). *Mind in society*. Cambridge, MA: Harvard University Press.

Brian A. Bottge Brian A. Bottge is the William T. Bryan Endowed Chair in Special Education in the Department of Special Education and Rehabilitation Counseling at the University of Kentucky. His research focuses on using multimedia and hands-on learning applications for improving the problem-solving skills of low-achieving students in mathematics.

Enrique Rueda Enrique Rueda is Associate Researcher at the Wisconsin Center for Education Research at the University of Wisconsin-Madison. Mr. Rueda is a multimedia artist and develops curricula that integrate digital media into the process of learning/teaching mathematics.

Jung Min Kwon Jung Min Kwon is working on her doctoral degree in the Department of Rehabilitation Psychology and Special Education at the University of Wisconsin-Madison. Her research interests center on using technology in special education to promote authentic learning.

Timothy Grant Timothy Grant is working on his doctoral degree in the Department of Educational Psychology at the University of Wisconsin-Madison. His research interests include hierarchical linear modeling and Bayesian methods.

Perry LaRoque Perry T. LaRoque completed his PhD in Special Education from the Department of Rehabilitation Psychology and Special Education. His research interests involve adolescent deviance and the effects of peer group orientation on school conduct.