



Artificial Intelligence

Laboratory activity

Name: Fodor, Zsófia and Katona, Áron Group: 30433

Email: fodorzsofi@yahoo.com~katonaaron01@gmail.com

Teaching Assistant: Adrian Groza Adrian.Groza@cs.utcluj.ro





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Chapter 1

A1: Search

1.1 Introduction

Our aim is to implement multiple search algorithms, and compare them with themselves and with the ones that were already discussed: A*, DFS, BFS, UCS.

We chose the following searching strategies:

Uninformed

- Bidirectional Search
- Depth Limited Search
- Iterative Deepening Depth-First Search

Informed

- Iterative Deepening A*
- Recursive Best-First Search

1.2 Bidirectional Search

Bidirectional search simultaneously searches from the start state to the goal state (**forward searching**) and from the goal state to the start state (**backward searching**) hoping that these two searches will meet. The time and space complexity was reduced from $O(b^d)$ to $O(2 * b^{d/2}) = O(b^{d/2}) << O(b^d)$, where b is the branching factor and d is the depth of the shallowest solution.

1.2.1 Implementation

The algorithm uses the **Breadth-First Search policy**, meaning that it takes the shallowest node first. It stops when the forward and backward search intersect. If no solutions is found, than it returns *None*.

We used two sets one representing the explored nodes that are still in the queue and another one, that contains the visited nodes that were popped out of the queue. Entering the while loop, we firstly analyze the forward search. Take the next node from the corresponding queue and if it is not yet visited we put it in the visited set. After we have iterated through the nodes

of the backward search, if there is a meeting point then we return the current path and the path accumulated by the backward search in reverse order.

Next we analyze the backward search the same way as we did for the forward search, the only difference being that we replace each action with its opposite action, we reverse the list containing them and add it to the accumulated path.

The motivation behind using sets is that they are more efficient than lists in verifying whether they contain an arbitrary element.

Source code: Appendix A.2.

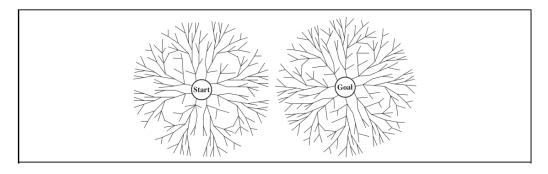


Figure 1.1: Visualization of the bidirectional search algorithm. [1]

1.3 Iterative Deepening Depth-First Search

1.3.1 Depth-Limited Search

The depth-limited search is similar to the depth-first search, with the only difference, that a **depth bound** is added. Thus the algorithm searches for the goal state until the search tree's depth reaches the bound. If the bound is reached, the search backtracks to the parent node and continues searching in the next successor of the parent node. Therefore if there is a path to the goal, whose length is smaller than or equal to the bound, it will be found.

Implementation

To represent the nodes we used the Node class, which is a simple data class whose state, action and cost fields are used. More information about the class can be found in Appendix A.1.

The algorithm is a modified version of the recursive **depth-first search**. At each level of recursion, the function calls itself for all of the successors. The function returns not only the found goal node on success and None on error, but also an additional boolean parameter which specifies whether the search terminated because of a cutoff, or not. In each level of recursion, the limit is decremented. When it reaches 0, the returned cutoff value is true.

Source code: Appendix A.3.

1.3.2 Iterative Deepening Search

The iterative deepening search strategies apply a search algorithm multiple times, with increasing bounds until the goal is reached. The calculation of the bound depends on the applied algorithm. We used the strategy of iterative deepening for the following search algorithms: depth-first search (1.3.3) and A^* (1.4).

1.3.3 Iterative Deepening Depth-First Search

Starting from an initial bound of 0, we call the depth-limited search and verify the returned result. In case a cutoff occurred, we increase the bound by one, and start again the search. If the goal node was found, the path from the start node which ends in the goal node is reconstructed and returned.

The algorithm is complete, because depth-first search, and in particular depth-limited search is guaranteed to find a solution, if the distance to the goal node is inside the bound. The bound is incremented from 0 indefinitely, thus if the solution exists, it will be found.

The algorithm is optimal for unit action costs, because if no solution was found for bound b, the length of the shortest path from the start node to the goal node is at least b+1, and if there is any solution with length b+1, all of them are optimal solutions, and one of them will be found by the depth-limited search.

Source code: Appendix A.4.

1.4 Iterative Deepening A* Search

Iterative deepening is a preferred algorithm when we have a larger search state space than the one that can fit in memory and the depth of our solution is not known.

Iterative Deepening A* is similar to A* the difference being that we do not keep all reached states in memory, at a cost of visiting some states multiple times. It is a very frequently used algorithm for problems that do not fit in memory, as stated above.

1.4.1 Implementation

The idea behind the algorithm was that we search the node with the lowest combined cost and heuristic first (f = g + h). The algorithm is limiting the size of the frontier by using this calculated f value as a bound.

We used a set in which we stored the visited nodes. Searching in sets is faster than searching in lists, that is why we chose set. Besides this set, we used a list called path, that stored for each node its state, the action that needs to be performed to get there from the previous node and the cost.

We have a utility function that we call repeatedly until the returned value is either a very large number (∞) or the *None* state and we change the value of the bound to the returned value if none of these conditions is satisfied.

The utility function begins with taking the last element from the path, computing the f value of this element and comparing it to the bound. If it is larger than the bound, we return the f value. If the state of the node is the goal state, it means we reached our goal, so we return the *None* state. If none of these conditions are fulfilled, then we iterate through each child of the current node, add it to the visited set and to the path list, then we call the utility function on it. We make the adjustments according to the returned value of this call, remove the node from the visited list and the path. Lastly we return the minimum value which represents the minimum cost of all values that exceeded the current bound.

1.4.2 Remarks

This algorithm was actually easy to implement after we understood the idea behind it.

Comparing the number of expanded nodes we can see that it is much larger than for the A* algorithm, because of the fact that we do not keep all reached states in memory risking the fact that we might visit some nodes more than once.

1.5 Recursive Best-First Search

The recursive best-first search, similarly to the depth-limited search (1.3.1), searches for the deepest node first, but stops after surpassing a bound. But in this case the bound is placed on the f-value of a node, instead of its depth.

The f-value of a node is the maximum between the f-value of its parent and the cost of reaching the node + the heuristic, i.e. $f(n) = max\{g(n) + h(n), f(n.parent)\}$. When a branch of the search is cut off because the limit on the f-value, while backtracking, the f-value of a parent node will be updated with the f-value of its child. This way, the f-value of a node will become a more and more accurate estimation of the true cost of reaching the goal node from it.

This algorithm uses the principle of best-first searching. It only expands the node with the smallest f-value. If the node is on the current searching branch, than it will be expanded, otherwise the search tree backtracks to the level of the node with the smallest f-value. Therefore at each level of recursion we take the first two successors with the lowest f-value, call the search for the best option, and supply the bound as the f-limit of the alternative successor. This is repeated until the solution is found, or until the f-value of the best node will become greater than the f-limit. Thus it always considers a best and an alternative path, and switches between them, if the alternative path becomes the best one, in terms of lowest f-value.

The advantage of this algorithm is that it uses linear space: used for storing the nodes along the search path, and also the sibling of each node. The disadvantage is that it regenerates already visited nodes, which could happen very frequently. Thus it trades speed for storage.

For the implementation the Node class (A.1) was used for storing the nodes, and a priority queue was used for obtaining the best successor of a node. The recursive function returns the result and None, if the goal node was found. If the goal was not found, it returns None and the f-value of the deepest node reached before surpassing the limit.

Source code: Appendix A.6.

1.6 Comparison

Consider b the branching factor and d the depth of the shallowest solution.

1.6.1 Bidirectional Search vs Breadth-First Search

As stated in chapter 1.2, the bidirectional search reduces the size of the frontier and the running time from $O(b^d)$ to $O(b^{d/2})$. To find a solution with length d, the two frontiers contain in the worst case only the nodes with the depth d/2 from either nodes. Thus both the space and the running time is reduced.

However the implementation of the bidirectional search is difficult if the actions cannot be reversed fast. E.g. North \leftrightarrow South.

1.6.2 Iterative Deepening Depth-First Search

vs Depth-First Search: The depth-first search does not find always the optimal solution, and may not find any solution even if it exists in the graph. However the iterative deepening version is optimal and complete, because each path is considered in increasing order of depth.

vs Breadth-First Search: The running time has the same $O(b^d)$ complexity. For the iterative deepening depth-first search the space complexity is reduced from $O(b^d)$ to O(bd), because

the deepest node is taken first. However because of the iterative deepening, the number of expanded nodes is higher.

1.6.3 Iterative Deepening A* vs A*

Iterative Deepening A* is similar to A* the difference being that we do not keep all reached states in memory, at a cost of visiting some states multiple times. It is a very frequently used algorithm for problems that do not fit in memory.

1.6.4 Recursive Best-First Search

vs A*: RBFS uses only linear space, but suffers from frequently regenerating the nodes. Given enough time it could solve those problems that could not be solved by A* because of running out of memory.

vs Iterative Deepening A* The two algorithms are solutions for the same problem of reducing the size of the frontier of A*. Both suffer from revisiting and regenerating nodes. However the RBFS is slightly more efficient, because of storing more information that the other one, thus increasing the speed.

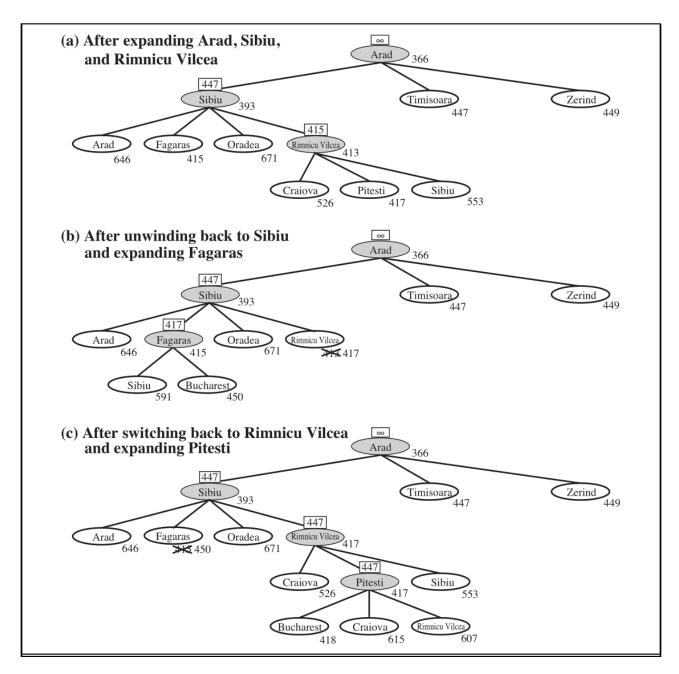


Figure 1.2: Finding a path from Arad to Bucharest by using recursive best-first search. The number above a node is its f-limit, and the number on the right of it is its f-value. The searching branch was switched two times. [1]

Bibliography

[1] Stuart Russell and Peter Norvig. Solving problems by searching. In *Artificial Intelligence:* A Modern Approach, chapter 3, pages 63–105. Pearson, 4 edition, 2020.

Appendix A

Source Code: Search

The code snippets below are from search.py.

A.1 Nodes

To represent the search nodes, we used different strategies across the various search algorithms. In some cases we used tuples containing the state, the action and the cumulative cost of a node, while in other cases we used the Node class defined below.

In the latter case, we stored in a node a reference to its parent. This information is used for reconstructing the path from the start node to the goal node, in the reconstructPath(node) method.

```
class Node:
68
      Node used for search algorithms.
69
70
71
      def __init__(self, state, action, cost, parent, f=0):
72
73
           state: (x,y) coordinates
          action: direction from Directions of game.py
75
           cost: cost of reaching the node
76
           parent: parent node
78
           f: the backed-up f-value
79
           self.state = state
80
           self.action = action
81
           self.cost = cost
82
           self.parent = parent
83
           self.f = f
```

Listing A.1: The Node class

```
def reconstructPath(node):
    """

Reconstructs a path, whose end node is given as a parameter, by
    iterating through the parent references.

node: search node, instance of Node
    """

if not node:
    return None
```

```
path = []

while node.parent is not None:

path = path + [node.action]

node = node.parent

path.reverse()

return path
```

Listing A.2: Method for reconstructing the path from the start to the goal node.

A.2 Bidirectional Search

```
def bidirectionalSearch(problem):
229
       Simultaneously searches from both the start and the goal positions.
230
       Stops when the two frontiers intersect.
231
       The shallowest node is taken first (BFS).
233
234
235
       forward = util.Queue()
       start = problem.getStartState()
       exploredForward = {start}
237
       forward.push((start, []))
238
239
       backward = util.Queue()
       goal = problem.goal
241
       exploredBackward = {goal}
242
       backward.push((goal, []))
243
244
       visitedForward = set()
245
       visitedBackwards = set()
246
       while not forward.isEmpty() and not backward.isEmpty():
248
249
           # Forward searching
250
251
           currentNode, currentActions = forward.pop()
252
           if currentNode not in visitedForward:
253
                visitedForward.add(currentNode)
254
                if currentNode in exploredBackward:
256
                    while not backward.isEmpty():
                        node, actions = backward.pop()
257
                        if node == currentNode:
258
                             solution = currentActions + actions.reverse()
                             return solution
260
261
                for (childState, childAction, childCost) in problem.
262
      getSuccessors(currentNode):
                    forward.push((childState, currentActions + [childAction]))
263
                    exploredForward.add(childState)
264
265
266
           # Backward searching
           currentNode, currentActions = backward.pop()
267
268
           if currentNode not in visitedBackwards:
269
                visitedBackwards.add(currentNode)
271
                if currentNode in exploredForward:
272
```

```
274
                    while not forward.isEmpty():
                        node, actions = forward.pop()
                        if node == currentNode:
276
                             backwardActions = [reverseAction(action) for action
27
      in currentActions]
                             backwardActions.reverse()
278
                             solution = actions + backwardActions
279
                             return solution
280
281
                for (childState, childAction, childCost) in problem.
      getSuccessors(currentNode):
                    backward.push((childState, currentActions + [childAction]))
283
                    exploredBackward.add(childState)
284
       return None
285
286
   def reverseAction(action):
       """Changes the action to its inverse."""
289
290
       if action == 'North':
291
           return 'South'
       elif action == 'South':
293
           return 'North'
       elif action == 'West':
295
           return 'East'
296
297
           return 'West'
298
```

search.py

A.3 Depth Limited Search

```
depthLimitedSearch(problem, limit):
366
367
       Search the deepest nodes in the search tree first. The search depth is
368
      limited by the given parameter.
369
       returns a (node, cutoff) tuple:
370
       - node is the goal node containing reference to its parent.
372
        cutoff is True if no solution was found in the given limit, False
      otherwise.
       0.00
373
374
       start_node = Node(problem.getStartState(), None, 0, None)
375
       visited = {start_node.state}
376
       return recursiveDLS(problem, visited, start_node, limit)
377
378
379
   def recursiveDLS(problem, visited, node, limit):
380
381
382
       Helper function for depthLimitedSearch(problem, limit).
383
       returns a (node, cutoff) tuple:
384
       - node: the goal node containing reference to its parent, or False if no
385
       solution was found.
       - cutoff: True if no solution was found in the given limit, False
386
      otherwise.
```

```
if problem.isGoalState(node.state):
           return node, False
390
       if limit == 0:
391
           return None, True
       cutoff_occurred = False
394
       for child_state, child_action, child_cost in problem.getSuccessors(node.
395
      state):
           if child_state not in visited:
396
397
                child = Node(child_state, child_action, child_cost, node)
398
                visited.add(child_state)
400
                (result, cutoff) = recursiveDLS(problem, visited, child, limit -
401
       1)
                visited.remove(child_state)
403
                if cutoff:
404
                    cutoff_occurred = True
405
                elif result:
                    return result, False
407
408
       if cutoff_occurred:
409
410
           return None, True
411
           return None, False
412
```

search.py

A.4 Iterative Deepening Depth-First Search

```
def iterativeDeepeningSearch(problem):
416
417
       Search the deepest nodes in the search tree first. The search depth is
418
      limited, but the limit is increased in each
       iteration.
419
420
       returns:
       - node: the goal node containing reference to its parent, or False if no
422
       solution was found.
423
424
       depth = 0
425
       while True:
426
           (result, cutoff) = depthLimitedSearch(problem, depth)
           if not cutoff:
428
                return reconstructPath(result)
429
           depth += 1
```

search.py

A.5 Iterative Deepening A*

```
def iterativeDeepeningAStarSearch(problem, heuristic=nullHeuristic):
433
434
       Search the node that has the lowest combined cost and heuristic first.
435
      It differs from A* by limiting the size of
       the frontier, using a bound on the f value.
436
437
438
       start = problem.getStartState()
439
       bound = heuristic(start, problem)
440
       path = [(start, None, 0)]
441
       visited = {start}
442
443
       while True:
444
           t = iterativeDeepeningAStarSearchUtil(problem, heuristic, path,
445
      visited, bound)
446
447
           if t is None:
               return [action for (state, action, cost) in path if action is
448
      not None]
           if t == sys.maxint:
449
                return None
451
           bound = t
452
453
   def iterativeDeepeningAStarSearchUtil(problem, heuristic, path, visited,
455
      bound):
       0.00
456
       Utility function for iterativeDeepeningAStarSearch.
457
       Returns the minimum cost of all values that exceeded the current bound.
458
       0.00
459
       state, action, cost = path[-1]
460
       f = cost + heuristic(state, problem)
462
       if f > bound:
463
           return f
       if problem.isGoalState(state):
465
           return None
466
467
       min = sys.maxint
468
469
       for child_state, child_action, child_cost in problem.getSuccessors(state
470
      ):
           if child_state not in visited:
                visited.add(child_state)
472
                path.append((child_state, child_action, child_cost + cost))
473
474
                t = iterativeDeepeningAStarSearchUtil(problem, heuristic, path,
475
      visited, bound)
476
                if t is None:
                    return None
                if t < min:
479
                    min = t
480
481
                path.pop()
482
                visited.remove(child_state)
483
484
485
       return min
```

A.6 Recursive Best-First Search

```
def recursiveBestFirstSearch(problem, heuristic=nullHeuristic):
301
302
       Similarly to the DFS, search the deepest nodes in the search tree first,
       but uses the f_limit variable to keep
       track of the f values. The f value is the largest reached g(n) + h(n)
304
      value upon one path after the search is
       stopped because of the f_limit. This f values is backed up to the parent
305
       of a node upon backtracking. The f_limit of
       the best child path is the f value of the best alternative path.
306
       returns:
308
        \cdot node: the goal node containing reference to its parent, or False if no
309
       solution was found.
       start_node = Node(problem.getStartState(), None, 0, None)
311
       start_node.f = 0
312
       visited = {start_node.state}
313
       result, _ = RBFS(problem, heuristic, visited, start_node, float('inf'))
315
       return reconstructPath(result)
316
317
318
   def RBFS(problem, heuristic, visited, node, f_limit):
319
320
       Helper function of recursiveBestFirstSearch(problem, heuristic).
321
322
       returns:
323
       - node: the goal node containing reference to its parent, or None if no
324
      solution was found.
       - f-cost: the f value obtained on the path.
325
326
327
       if problem.isGoalState(node.state):
           return node, None
329
330
       successors = util.PriorityQueueWithFunction(lambda n: n.f)
331
332
       for child_state, child_action, child_cost in problem.getSuccessors(node.
333
      state):
           if child_state not in visited:
334
               path_cost = child_cost + node.cost
               child_f = max(path_cost + heuristic(child_state, problem), node.
336
      f)
               child = Node(child_state, child_action, path_cost, node, child_f
337
      )
               successors.push(child)
338
339
       if successors.isEmpty():
340
           return None, float('inf')
341
342
       while True:
343
344
           best = successors.pop()
345
```

```
if best.f > f_limit:
346
347
                return None, best.f
348
           if successors.isEmpty():
349
                alternative_f = float('inf')
350
351
           else:
                alternative = successors.pop()
352
                alternative_f = alternative.f
353
                successors.push(alternative)
355
           visited.add(best.state)
356
           result, best.f = RBFS(problem, heuristic, visited, best, min(f_limit)
357
      , alternative_f))
           visited.remove(best.state)
358
359
           if result:
360
                return result, best.f
362
           successors.push(best)
363
```

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