# Loss modelling and reserving analytics in R

A hands-on workshop

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## Today's Outline

- Motivation and strategies
- Reserving data structures (part 1)
  - IBNR and RBNS reserve
  - daily and yearly reserving data
- Reserving data structures (part 2)
  - individual and aggregated reserving data
  - runoff triangles
- Claims reserving with triangle
  - chainladder model
  - {ChainLadder} package
  - chainLadder GLM implementation

#### When the chain ladder method fails

- detection tools for triangle stability
- creating homogeneous triangles

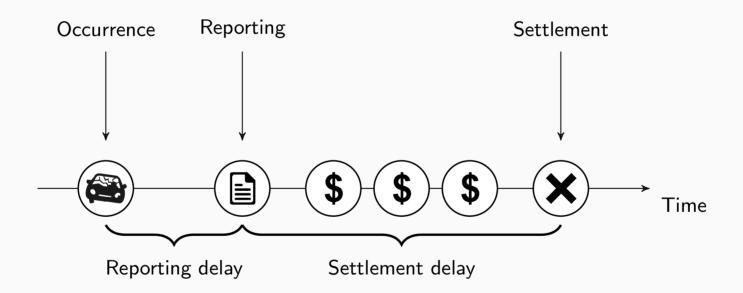
#### Research outlook

- granular reserving methods for predicting the IBNR reserve
- individual reserving methods for predicting the RBNS reserve

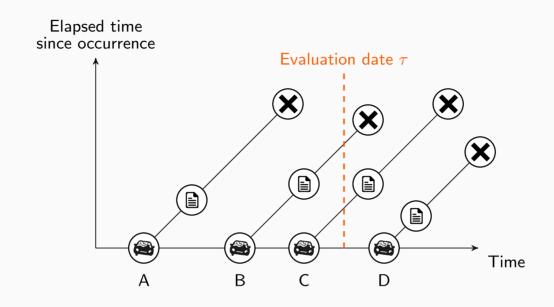
# Motivation and strategies

### Motivation

Insurers observe the **detailed evolution** of **individual claims**.



## Motivation (continued)



Observed claims are **censored** due to **delays** (reporting, settlement) in the claim development process

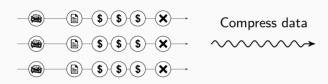
**Reserve**: future costs for claims that occurred in **past exposure periods** (claim B and C)

- RBNS reserve: Reserve for Reported, But Not yet Settled claims (claim B)
- IBNR reserve: Reserve for Incurred, But Not yet Reported claims (claim C)

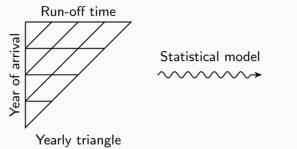
Pricing: all costs for claims that will occur in future insured exposure periods (claim D)

# Three strategies for non-life reserving

#### Aggregate reserving



Individual data

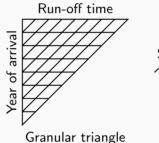




#### Granular reserving



Individual data



Statistical model



Reserve

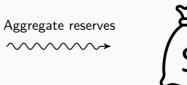
#### Individual reserving



Individual data



Reserve per policy/claim



Reserve

# Three strategies for non-life reserving (continued)

#### Aggregate reserving

First aggregate the past claim history into a **small number of summary statistics**, then predict the total reserve based on these summary statistics.

#### Granular reserving

First aggregate the past claim history into a **large number of summary statistics**, then predict the total reserve based on these summary statistics.

#### Individual reserving

First predict the future costs for **indivudal claims**, then aggregate these individual predictions to predict the total reserve.

#### Data set used in this session

We illustrate reserving analytics based on a **simulated dataset** registering the **detailed development** of 30,000 claims between January 1, 2010 and December 31, 2019.

- Information is available at daily level
- Records correspond to payments made for these claims

The data is stored in a .RData file in the data directory in the course material:

```
# install.packages("rstudioapi")
dir <- dirname(rstudioapi::getActiveDocumentContext()$path)
setwd(dir)
load("data/reserving_data.RData")</pre>
```

```
accident_number accident_date reporting_date settlement_date reporting_delay settlement_delay payment_date payment_size
## 1
                       2012-08-27
                                      2012-09-01
                                                      2012-12-03
                                                                                                   2012-09-01
                                                                                                                    0.0000
## 2
                       2012-08-27
                                      2012-09-01
                                                      2012-12-03
                                                                                                   2012-09-07
                                                                                                                   446.2251
## 3
                       2012-08-27
                                      2012-09-01
                                                      2012-12-03
                                                                                              98 2012-09-18
                                                                                                                   490.1792
## 4
                       2012-08-27
                                      2012-09-01
                                                      2012-12-03
                                                                                                   2012-10-01
                                                                                                                   587.7409
                       2012-08-27
                                      2012-09-01
                                                      2012-12-03
                                                                                                                  1726.0902
                                                                                                    2012-10-19
## 6
                  2 2013-09-20
                                      2013-09-26
                                                      2014-04-06
                                                                                              198 2013-09-26
                                                                                                                    0.0000
```

### Data set used in this session (continued)

Discretize daily dates to yearly indices:

```
date_to_year <- function(date, base_year) {
   year <- as.numeric(format(date, '%Y')) - base_year
}

reserving_data <- reserving_data %>%
   mutate(accident_year = date_to_year(accident_date, 2010),
        reporting_year = date_to_year(reporting_date, 2010),
        payment_year = date_to_year(payment_date, 2010),
        development_year = payment_year - accident_year + 1,
        settlement_year = date_to_year(settlement_date, 2010))
```

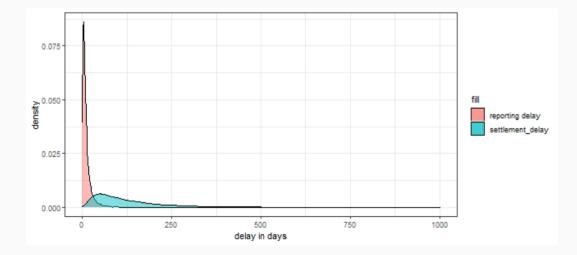
```
accident_number accident_date reporting_date settlement_date reporting_delay settlement_delay payment_date payment_size accident_year reporting_year payment_year
                                       2012-09-01
                                                       2012-12-03
## 1
                        2012-08-27
                                                                                                     2012-09-01
                                                                                                                      0.0000
                                                                                                                     446.2251
## 2
                       2012-08-27
                                       2012-09-01
                                                       2012-12-03
                                                                                                     2012-09-07
## 3
                       2012-08-27
                                       2012-09-01
                                                       2012-12-03
                                                                                                     2012-09-18
                                                                                                                     490.1792
                       2012-08-27
                                       2012-09-01
                                                       2012-12-03
                                                                                                     2012-10-01
                                                                                                                     587.7409
                        2012-08-27
                                       2012-09-01
                                                       2012-12-03
                                                                                                     2012-10-19
                                                                                                                    1726.0902
## 6
                       2013-09-20
                                       2013-09-26
                                                       2014-04-06
                                                                                                     2013-09-26
                                                                                                                      0.0000
    development_year settlement_year
## 1
## 2
## 4
## 5
## 6
```



In this warm up exercise you load the reserving data data set and get some feel for the data.

- 1. Visualize the reporting and settlement delay of claims with a density plot.
- 2. When was the last payment registered in the data set? What do you conclude?
- 3. What is the average number of payments per claim?
- 4. Calculate the number of claims per accident year.

For **Q.1** we plot the density of reporting and settlement delay:



For **Q.2** the last payment was in 2024, i.e. the simulated data is not yet censored!

```
max(reserving_data$payment_date)
## [1] "2024-05-05"
```

For **Q.3** the data set records one row per payment.

```
num_claim <- length(unique(reserving_data$accident_number))
num_payment <- nrow(reserving_data)
num_payment/num_claim</pre>
```

```
## [1] 3.425433
```

At reporting, the data set registers a zero payment for each claim. The average number of non-zero payments per claim is

```
num_payment <- sum(reserving_data$payment_size > 0)
num_payment/num_claim
```

```
## [1] 2.376633
```

For **Q.4** we group the data by accident year and summarise the number of claims.

```
reserving_data %>%
  group_by(accident_year) %>%
  summarise(num_claims = n())
```

```
## # A tibble: 10 x 2
     accident_year num_claims
              <dbl>
                         <int>
##
                         10275
   1
                  0
                         10108
                         10633
                         10295
                         10213
   5
   6
                         10130
                  5
                         10222
   8
                         10069
## 9
                         10261
                  8
## 10
                         10557
                  9
```

The portfolio is stable over time.

# Reserving data structures: daily and yearly data

# From daily to yearly data

Reserves are often calculated based on yearly, aggregated data.

Data aggregation removes the daily noise from the data.

In a first step, we construct a data set that consists of **one record per claim and per development year**. We construct this data set by merging three partial data sets:

- records: empty data set with one record per claim per development year
- claim\_data: data set with one record per claim containing the static claim covariates (e.g. accident year)
- payment\_data: data set containing the total **amount paid per claim and per development year**.

  This data set contains only records for development years with at least one payment.

For records, expand.grid Creates a data.frame with all combinations of accident\_number and development year.

expand.grid creates a data.frame with all possible combinations of the input vectors.

```
expand.grid(A = c(1, 5, 7), B = c(4, 6))

## A B
## 1 1 4
## 2 5 4
## 3 7 4
## 4 1 6
## 5 5 6
## 6 7 6
```

#### head(records)

For claim\_data, we select for each accident\_number the first row in reserving\_data.

```
head(claim_data)
```

```
## # A tibble: 6 x 5
     accident_number accident_year accident_date reporting_year
               <int>
                                                             <dbl:
##
                              <dbl> <date>
## 1
                                  2 2012-08-27
                                  3 2013-09-20
## 2
## 3
                                  5 2015-09-24
## 4
                                  9 2019-01-30
## 5
                                  2 2012-01-07
## 6
                                  8 2018-12-25
```

slice(k) selects the k-th record of a data set

```
df <- data.frame(x = c(1, 2, 3, 4, 5, 6), y = c(1, 1, 1, 2, 2,
df %>% slice(4)

## x y
## 1 4 2
```

In combination with  $group_by$  we can select the k-th record within each group

For payment\_data, we aggregate payments per claim by development\_year.

```
summarise returns one record for each combination of accident_number and development_year in reserving_data.
```

The data set contains no records development years in which no payment was made for a claim!

head(payment\_data)

Merge records, claim\_data and payment\_data into a new data set individual\_data.

```
dim(individual_data)
## [1] 300000 8
```

```
Teft_join combines records in the first (left) with records from the second (right) data set with matching values in the by column.
```

If no match is found in the right data set an NA value is imputed.

```
left <- data.frame(x = c(1, 2, 3), left = 1)
right <- data.frame(x = c(1, 2, 4), right = 1)
left_join(left, right, by = 'x')</pre>
```

```
## x left right
## 1 1 1 1
## 2 2 1 1
## 3 3 1 NA
```

```
head(individual_data, 3)
```

## Censoring the data

The simulated data is not censored, i.e. we observe the full development of all claims that occur before 2019. In practice the available data set is censored and we only observe:

- reported claims
- development information for past calendar years

We censor the data assuming that we observe data until the end of 2019

#### IBNR and RBNS reserves

Reserving models predict the total payments in the unobserved data

```
reserve_actual <- sum(unobserved_data$size)
reserve_actual
## [1] 2468246</pre>
```

Some reserving methods split this reserve in an

- IBNR reserve: a reserve for Incurred, But Not (yet) Reported claims
- RBNS reserve: a reserve for Reported, But Not (yet) Settled claims

```
unobserved_data %>%
mutate(reported = (reporting_year <= 9)) %>%
group_by(reported) %>%
summarise(reserve = sum(size))
```

```
## # A tibble: 2 x 2
## reported reserve
## <lgl> <dbl>
## 1 FALSE 158665.
## 2 TRUE 2309581.
```

# Reserving data structures: individual and aggregated data

# From individual to aggregated data

#### Individual triangle

The data set individual\_data describes the development of individual claims discretised by calendar year.

We can represent the claim characteristics in this data set (settlement, payment, payment size) with **two-dimensional tables** in which the rows represent **individual claims** and columns represent **development years**.

For payment size, this table consists of cells  $U_{k,j}^{\text{size}}$  with  $U_{k,j}^{\text{size}}$  denoting the total amount paid for claim k in development year j.

#### Runoff triangle

Many reserving models go one step further and remove individual claim characteristics by aggregating claims by occurrence year. The data is then represented in a (small) two-dimensional table, the so-called **incremental runoff triangle**.

$$X_{i,j}^{\text{size}} = \sum_{\text{occ.year(k)}=i} U_{k,j}^{\text{size}}.$$

As a result of the Law of Large Numbers (LLN), aggregating data from many claims into runoff triangles **reduces the variance** when all claims are independent realizations from the same distribution.

## From individual to aggregated data (continued)

We construct a runoff triangle by aggregating individual claims by accident\_year.

```
## # A tibble: 10 x 11
    Groups: accident year [10]
                                DY.2
     accident year
                                                    DY.5 DY.6 DY.7 DY.8 DY.9 DY.1
## 1
                 0 4532915. 1739699. 121876. 25952.
                 1 4414954. 1673577. 107415. 19472.
                 2 4786833. 1785616. 149240. 59348. 14858. 4404.
                 3 4653451. 1614053. 127900. 36214. 9301.
                 4 4321019. 1909085. 159247. 49184. 11728.
## 6
                 5 4417129. 1722151. 103907. 65592. 15129.
                 6 4538329. 1718509. 146138. 19248.
                                                             NA
                 7 4578285. 1618201. 77054.
## 9
                 8 4503558. 1756243.
## 10
                 9 4575529.
```

pivot\_wider widens the data set by increasing the number of columns, while decreasing the number of rows.

names\_from: The resulting data set contains a separate column for each unique outcome of this variable.

values\_from: Values from this variable are stored in the

newly created columns.

## From individual to aggregated data (continued)

A more sophisticated function for computing incremental runoff triangles is available in the R code.

```
## [,1] [,2] [,3] [,4] [,5] [,6] [,7] [,8] [,9] [,10]
## [1,] 2264 550 20 5 2 1 1 1 1 0
## [2,] 2269 533 27 5 0 0 0 0 0 NA
## [3,] 2307 557 26 8 3 1 0 0 NA NA
## [4,] 2289 537 23 8 1 0 0 NA NA NA
## [5,] 2239 581 33 8 1 0 NA NA NA NA
## [6,] 2211 532 24 6 3 NA NA NA NA NA
## [7,] 2197 537 30 5 NA NA NA NA NA NA NA
## [8,] 2250 510 18 NA NA NA NA NA NA NA NA
## [9,] 2271 544 NA NA NA NA NA NA NA NA NA
## [10,] 2319 NA NA NA NA NA NA NA NA NA NA
```

Using this function you can easily inspect the reserving data using multiple triangles.

```
[,1] \qquad [,2]
                             [,3]
                                   [,4]
                                                [,5]
                                                         [,6]
                                                                 [,7]
                                                                          [,8]
## [1,] 4532915 1739699 121876.31 25951.66 9304.915 6703.063 9478.77 6217.266
## [2,] 4414954 1673577 107415.07 19472.27
                                                                         0.000
                                                                                  0.000
## [3,] 4786833 1785616 149239.81 59348.18 14857.743 4404.145
                                                                         0.000
## [4,] 4653451 1614053 127900.21 36213.57 9301.109
## [5,] 4321019 1909085 159246.74 49184.25 11727.691
                                                        0.000
## [6,] 4417129 1722151 103906.89 65592.12 15129.218
## [7,] 4538329 1718509 146138.00 19248.11
## [8,] 4578285 1618201 77053.93
                                                           NA
## [9.] 4503558 1756243
                                                           NA
## [10,] 4575529
                               NA
                                                           NA
```

# Cumulative runoff triangles

Cumulative runoff triangles are constructed by computing the cumulative row sum of an incremental runoff triangle, i.e.

$$C_{i,j}^{\text{size}} = \sum_{l=1}^{j} X_{i,l}^{\text{size}}.$$

When using a new reserving method, check whether the incremental or cumulative runoff triangle is required!

```
[,1] \qquad [,2]
                             [,3]
                                      [,4]
                                                [,5]
                                                                  [,7]
    [1,] 4532915 1739699 121876.31 25951.66 9304.915 6703.063 9478.77 6217.266 3468.364
    [2,] 4414954 1673577 107415.07 19472.27
                                               0.000
    [3,] 4786833 1785616 149239.81 59348.18 14857.743 4404.145
                                                                          0.000
    [4,] 4653451 1614053 127900.21 36213.57 9301.109
## [5,] 4321019 1909085 159246.74 49184.25 11727.691
   [6,] 4417129 1722151 103906.89 65592.12 15129.218
    [7,] 4538329 1718509 146138.00 19248.11
## [8,] 4578285 1618201 77053.93
## [9,] 4503558 1756243
## [10,] 4575529
```

```
## [,1] [,2] [,3] [,4] [,5] [,6] [,7] [,8] [,9] [,10]
## [1,] 4532915 6272614 6394490 6420442 6429747 6436450 6445929 6452146 6455614 6455614
## [2,] 4414954 6088531 6195946 6215419 6215419 6215419 6215419 6215419 6215419 6215419
## [3,] 4786833 6572449 6721689 6781037 6795895 6800299 6800299 6800299 NA NA
## [4,] 4653451 6267504 6395404 6431618 6440919 6440919 6440919 NA NA NA NA NA
## [5,] 4321019 6230104 6389351 6438535 6450263 6450263 NA NA NA NA NA NA
## [6,] 4417129 6139280 6243187 6308779 6323908 NA NA NA NA NA NA NA
## [7,] 4538329 6256837 6402975 6422224 NA NA NA NA NA NA NA NA NA
## [8,] 4578285 6196486 6273540 NA NA NA NA NA NA NA NA NA
## [9,] 4503558 6259801 NA NA
## [10,] 4575529 NA NA
```

# Claims reserving with triangles

#### Mack chain ladder method

#### Assumptions Mack (1993) chain ladder method:

1. There exist development factors  $f_i$  such that

$$E(C_{i,j+1} \mid C_{i,1}, ..., C_{i,j}) = C_{i,j} \cdot f_j$$
 for  $1 \le i \le 1, 1 \le j \le 1-1$ ,

with 1 the dimension of the runoff triangle.

2. There exist parameters  $\sigma_i$  such that

$$V \ \text{ar}(C_{i,j+1} \mid C_{i,1}, \ldots, C_{i,j}) = C_{i,j} \cdot \sigma_i^2 \quad \text{ for } \quad 1 \leq i \leq l, \, 1 \leq j \leq l-1.$$

3. Occurrence years are independent.

#### Remarks

- Method based on the cumulative triangle!
- Assumption 1. and 2. add an Markov property. Future evolutions of the reserve depend only on the last known situation.

Estimating the **development factors**  $\mathbf{f}_i$ :

$$f^{\hat{}}_{j} = \frac{\sum_{i=1}^{l-j} C_{i,j+1}}{\sum_{i=1}^{l-j} C_{i,j}}.$$

```
triangle <- cumulative_triangle(observed_data, variable = 'size')
l <- nrow(triangle)
f <- rep(0, l-1)

for(j in 1:(l-1)) {
    f[j] <- sum(triangle[1:(l-j), j+1]) / sum(triangle[1:(l-j), j])
}

f</pre>
```

```
## [1] 1.381312 1.019846 1.006146 1.001563 1.000344 1.000366 1.000319 1.000274 1.000000
```

Development factors should converge to 1 for high development years.

Use the development factors to estimate cells in the lower triangle (i+j>1+1):

$$\hat{C}_{i,j} = \hat{C}_{i,j-1} \cdot \hat{f}_{j-1} \quad \text{for} \quad i+j > l+1.$$

```
triangle_completed <- triangle
for(j in 2:l) {
  triangle_completed[l:(l-j+2), j] <- triangle_completed[l:(l-j+2), j-1] * f[j-1]
}</pre>
```

#### Completed cumulative triangle:

#### triangle\_completed

#### Completed incremental triangle:

```
require(ChainLadder)
cum2incr(triangle_completed)
```

```
## [,1] [,2] [,3] [,4] [,5] [,6] [,7] [,8] [,9]
## [1,] 4532915 1739699 121876.31 25951.66 9304.915 6703.063 9478.770 6217.266 3468.36
## [2,] 4414954 1673577 107415.07 19472.27 0.000 0.000 0.000 0.000 0.000 0.000
## [3,] 4786833 1785616 149239.81 59348.18 14857.743 4404.145 0.000 0.000 1861.91
## [4,] 4653451 1614053 127900.21 36213.57 9301.109 0.000 0.000 2057.632 1764.07
## [5,] 4321019 1909085 159246.74 49184.25 11727.691 0.000 2361.270 2061.371 1767.28
## [6,] 4417129 1722151 103906.89 65592.12 15129.218 2172.474 2315.810 2021.685 1733.26
## [7,] 4538329 1718509 146138.00 19248.11 10037.169 2209.697 2355.488 2056.324 1762.95
## [8,] 4578285 1618201 77053.93 38559.90 9865.059 2171.807 2315.098 2021.064 1732.72
## [9,] 4503558 1756243 124232.58 39239.04 10038.809 2210.058 2355.873 2056.660 1763.24
## [10,] 4575529 1744706 125431.95 39617.87 10135.726 2231.395 2378.618 2076.516 1780.26
```

The estimated reserve is the sum of the estimates in the lower half of the incremental runoff triangle.

```
## reserve_cl reserve_actual difference relative_difference_pct
## 1 2205459 2468246 -262787.3 -10.64672
```

These calculations are already implemented in the {ChainLadder} package.

```
require(ChainLadder)
triangle <- cumulative_triangle(observed_data, variable = 'size')
MackChainLadder(triangle)</pre>
```

```
## MackChainLadder(Triangle = triangle)
##
##
        Latest Dev.To.Date Ultimate
                                        IBNR Mack.S.E CV(IBNR)
## 1 6,455,614
                   1.000 6,455,614
## 2 6,215,419
                                               1,243
                   1.000 6,215,419
                                                          Inf
## 3 6,800,299
                   1.000 6,802,161
                                       1,862
                                               3,366 1.8079
     6,440,919
                   0.999 6,444,741
                                       3,822
                                               5,265 1.3777
## 5 6,450,263
                   0.999 6,456,452
                                       6,190
                                              7,483 1.2089
## 6 6,323,908
                   0.999 6,332,152
                                       8,243
                                               8,128 0.9860
     6,422,224
                   0.997 6,440,645
                                      18,422
                                              10,090 0.5477
## 8 6,273,540
                   0.991 6,330,206
                                      56,666
                                              22,280 0.3932
## 9 6,259,801
                   0.972 6,441,698
                                     181,896
                                              35,842 0.1970
## 10 4,575,529
                    0.704 6,503,887 1,928,358 137,089 0.0711
                  Totals
## Latest: 62,217,515.46
## Dev:
                    0.97
## Ultimate: 64,422,974.02
## IBNR:
             2,205,458.56
## Mack.S.E
              148,272.46
## CV(IBNR):
                    0.07
```

Latest: Amount already paid

ultimate : Estimated total amount (= amount paid + reserve)

IBNR: Estimated total reserve, IBNR + RBNS!

Mack.s.e: Estimated standard deviation of the reserve

#### GLM chain ladder method

The chain ladder reserve estimate can also be obtained by assuming a Poisson distribution for the incremental runoff triangle with multiplicative mean, i.e.

```
X_{i,j} \sim POI(\alpha_i \cdot \beta_j), \quad 1 \leq i, j \leq l.
```

```
head(triangle_long)
```

The chain ladder reserve estimate can also be obtained by assuming a Poisson distribution for the incremental runoff triangle with multiplicative mean, i.e.

$$X_{i,j} \sim POI(\alpha_i \cdot \beta_j), \quad 1 \leq i, j \leq l.$$

This Poisson model can be estimated using the glm (Generalized Linear Model) routine in R:

$$\log(E(X_{i,j})) = \log(\alpha_i) + \log(\beta_i).$$

factor: Treat the input as a categorical instead of a numeric variable.

#### summary(fit)

```
##
## glm(formula = size ~ factor(occ.year) + factor(dev.year), family = poisson(link = log
      data = triangle_long)
##
## Deviance Residuals:
                       Median
## -139.185 -64.152
                      -4.062
                                38.541 132.371
## Coefficients:
                    Estimate Std. Error z value Pr(>|z|)
                     1.533e+01 4.029e-04 38048.572 < 2e-16 ***
## (Intercept)
## factor(occ.year)2 -3.792e-02 5.620e-04 -67.473 < 2e-16 ***
## factor(occ.year)3 5.229e-02 5.495e-04
                                           95.155 < 2e-16 ***
## factor(occ.year)4 -1.686e-03 5.570e-04 -3.027 0.002472 **
## factor(occ.year)5 1.298e-04 5.568e-04
                                          0.233 0.815596
## factor(occ.year)6 -1.931e-02 5.596e-04
                                          -34.510 < 2e-16 ***
## factor(occ.year)7 -2.322e-03 5.574e-04
                                           -4.165 3.12e-05 ***
## factor(occ.year)8 -1.962e-02 5.608e-04
                                          -34.979 < 2e-16 ***
## factor(occ.year)9 -2.158e-03 5.615e-04
                                           -3.843 0.000121 ***
## factor(occ.year)10 7.450e-03 6.171e-04
                                          12.072 < 2e-16 ***
## factor(dev.year)2 -9.641e-01 2.982e-04 -3233.538 < 2e-16 ***
## factor(dev.year)3 -3.597e+00 1.017e-03 -3537.016 < 2e-16 ***
## factor(dev.year)4 -4.749e+00 1.915e-03 -2480.500 < 2e-16 ***
                                                                             33 / 66
## factor(dev.year)5 -6.112e+00 4.076e-03 -1499.723 < 2e-16 ***
```

#### GLM chain ladder method

#### Predict the cells in the lower triangle

```
## # A tibble: 10 x 11
     occ.year
                                                 DY.5 DY.6 DY.7 DY.8 DY.9
                 <dbl>
                                  <dbl> <dbl> <dbl> <dbl> <dbl> <dbl> <dbl> <dbl> <
            1 4532915. 1739699. 121876. 25952. 9305. 6703. 9479. 6217. 3468. 0
## 2
            2 4414954. 1673577. 107415. 19472.
            3 4786833. 1785616. 149240. 59348. 14858. 4404.
            4 4653451. 1614053. 127900. 36214. 9301.
                                                               0 2058. 1764. 0.000247
## 5
            5 4321019. 1909085. 159247. 49184. 11728.
                                                         0 2361. 2061. 1767. 0.000248
            6 4417129, 1722151, 103907, 65592, 15129, 2172, 2316, 2022, 1733, 0.000243
            7 4538329. 1718509. 146138. 19248. 10037. 2210. 2355. 2056. 1763. 0.000247
## 8
            8 4578285. 1618201. 77054. 38560. 9865. 2172. 2315. 2021. 1733. 0.000243
            9 4503558, 1756243, 124233, 39239, 10039, 2210, 2356, 2057, 1763, 0.000247
## 10
           10 4575529. 1744706. 125432. 39618. 10136. 2231. 2379. 2077. 1780. 0.000250
```

#### Compute the reserve

```
reserve_glm <- sum(triangle_long$size[lower_triangle])
reserve_glm
## [1] 2205459</pre>
```



In certain lines of business, the **Corona pandemic** and social distancing measures have **reduced claim frequency**.

The R script contains code to simulate a 50% reduction in claim frequency in the months March, April and May of 2019. The new data sets are named <code>observed\_data\_covid</code> and <code>unobserved\_data\_covid</code>.

In this exercise you will investigate the effect of this reduction in claim frequency on the accuracy of the chain ladder method.

- 1. Compute the actual reserve from the covid data set.
- 2. Estimate the reserve using the chain ladder method from the {ChainLadder} package.
- 3. Compute the difference between the estimated and actual reserve. How many standard deviations is this error?

For **Q.1** we compute the actual reserve from the unobserved data.

```
reserve_covid_actual <- sum(unobserved_data_covid$size)
reserve_covid_actual
## [1] 2389277</pre>
```

The reserve is smaller since less claims have occurred in the past. However, the difference is small since many claims from these months have already settled.

```
c(reserve_actual, reserve_covid_actual)
## [1] 2468246 2389277
```

The effect on the amount already paid is larger.

```
c(already_paid_no_covid = sum(observed_data$size),
  already_paid_covid = sum(observed_data_covid$size))
```

```
## already_paid_no_covid
## 62217515 61504837
```

For **Q.2** we appy the chain ladder method to the cumulative runoff triangle.

```
## MackChainLadder(Triangle = triangle)
        Latest Dev.To.Date Ultimate
##
                                         IBNR Mack, S.E CV(IBNR)
## 1 6,455,614
                    1.000 6,455,614
## 2 6,215,419
                    1.000 6,215,419
                                                1,243
                                                           Inf
## 3 6,800,299
                    1.000 6,802,161
                                        1,862
                                                3,366
                                                        1.8079
## 4 6,440,919
                    0.999 6,444,741
                                       3,822
                                                5,265
                                                        1.3777
## 5 6,450,263
                    0.999 6,456,452
                                                7,483
                                                       1.2089
                                        6,190
## 6 6,323,908
                    0.999 6,332,152
                                                8,128 0.9860
                                       8,243
## 7 6,422,224
                    0.997 6,440,645
                                               10,090
                                                        0.5477
                                      18,422
## 8 6,273,540
                    0.991 6,330,206
                                      56,666
                                               22,280
                                                        0.3932
## 9 6,259,801
                    0.972 6,441,698
                                      181,896
                                               35,842 0.1970
## 10 3.862.850
                    0.704 5,490,850 1,628,000 124,951 0.0768
##
                   Totals
## Latest: 61.504.836.84
## Dev:
                     0.97
## Ultimate: 63,409,936.76
## IBNR:
             1,905,099.93
## Mack.S.E
               136,795.35
## CV(IBNR):
```

For **Q.3** we compute the prediction error of the chain ladder method.

```
## error pct_error std.dev
## 484177.34 20.26 3.54
```

The reduction in claim frequency in the months March, April and May has reduced the accuracy of the chain ladder method.

#### Actual triangle:

```
[,1] [,2]
                              [,3]
                                      [,4]
                                                 [,5]
                                                          [,6]
                                                                   [,7]
    [2,] 4414954 1673577 107415.07 19472.27
                                                0.000
                                                         0.000
                                                                  0.000
                                                                           0.000
                                                                                    0.00
   [3,] 4786833 1785616 149239.81 59348.18 14857.743 4404.145
                                                                  0.000
                                                                           0.000
                                                                                    0.00
## [4,] 4653451 1614053 127900.21 36213.57 9301.109
                                                                  0.000
                                                                           0.000
                                                                                    0.00
   [5,] 4321019 1909085 159246.74 49184.25 11727.691
                                                         0.000 8367.837 1250.830
                                                                                    0.00
    [6,] 4417129 1722151 103906.89 65592.12 15129.218
                                                                  0.000
                                                                           0.000
   [7,] 4538329 1718509 146138.00 19248.11 8206.603 1255.568
                                                                  0.000
                                                                           0.000
## [8,] 4578285 1618201 77053.93 20586.47 4744.763
                                                                  0.000
                                                                           0.000
                                                                                    0.00
## [9,] 4503558 1756243 153002.08 50348.72 10709.289 4574.275
                                                                  0.000
                                                                           0.000
## [10,] 3862850 1801338 214885.47 77394.80 26305.781 6306.792
                                                                  0.000
                                                                           0.000
```

### Predicted triangle:

```
dev
         4532915 1739699 121876.31 25951.66 9304.915 6703.063 9478.770 6217.266 3468.
##
       3 4786833 1785616 149239.81 59348.18 14857.743 4404.145
                                                                  0.000
##
       4 4653451 1614053 127900.21 36213.57 9301.109
                                                         0.000
                                                                  0.000 2057.632 1764.0
##
       5 4321019 1909085 159246.74 49184.25 11727.691
                                                         0.000 2361.270 2061.371 1767.2
##
##
       7 4538329 1718509 146138.00 19248.11 10037.169 2209.697 2355.488 2056.324 1762.9
##
                          77053.93 38559.90 9865.059 2171.807 2315.098 2021.064 1732.7
##
       9 4503558 1756243 124232.58 39239.04 10038.809 2210.058 2355.873 2056.660 1763.2
##
       10 3862850 1472953 105894.83 33447.04 8556.998 1883.835 2008.127 1753.080 1502.9
```

## When the chain ladder method fails

The chain ladder method assumes that claims from all occurrence years follow the **same development pattern**. We construct various triangles to assess this assumption:

Number of open claims begin at the start of the year:

```
triangle_open <- incremental_triangle(
  observed_data_covid %>%
    mutate(open = calendar_year <= settlement_year),
  variable = 'open')
triangle_open</pre>
```

```
## [,1] [,2] [,3] [,4] [,5] [,6] [,7] [,8] [,9] [,10]
## [1,] 2933 802 37 7 2 1 1 1 1 0
## [2,] 2886 756 34 6 1 0 0 0 0 NA
## [3,] 3000 790 41 9 5 2 0 0 NA NA
## [4,] 2937 791 28 8 2 1 0 NA NA NA
## [5,] 2908 795 44 9 2 1 NA NA NA NA NA
## [6,] 2862 770 34 7 3 NA NA NA NA NA NA
## [7,] 2866 788 39 7 NA NA NA NA NA NA NA
## [8,] 2862 744 25 NA NA NA NA NA NA NA NA
## [9,] 2867 772 NA NA NA NA NA NA NA NA
## [10,] 2573 NA NA NA NA NA NA NA NA NA
```

### Settlement probability:

```
triangle_settlement <- incremental_triangle(
  observed_data_covid %>%
    mutate(settlement = calendar_year == settlement_year),
  variable = 'settlement')

triangle_settlement / triangle_open
```

```
## [,1] [,2] [,3] [,4] [,5] [,6] [,7] [,8] [,9] [,10]
## [1,] 0.7565632 0.9538653 0.8108108 0.7142857 0.5 0 0 0 0 1 NaN
## [2,] 0.7723493 0.9550265 0.8235294 0.8333333 1.0 NaN NaN NaN NaN NAN NA
## [3,] 0.7640000 0.9481013 0.7804878 0.44444444 0.6 1 NaN NaN NA NA NA
## [4,] 0.7647259 0.9646018 0.7142857 0.7500000 0.5 1 NaN NA NA NA NA
## [5,] 0.7568776 0.9446541 0.7954545 0.7777778 0.5 0 NA NA NA NA NA
## [6,] 0.7641509 0.9558442 0.7941176 0.5714286 1.0 NA NA NA NA NA NA
## [7,] 0.7616888 0.9505076 0.8205128 0.5714286 NA NA NA NA NA NA NA
## [8,] 0.7672956 0.9663978 0.7600000 NA NA NA NA NA NA NA NA
## [9,] 0.7697942 0.9572539 NA NA NA NA NA NA NA NA NA NA
## [10,] 0.7298873 NA NA NA NA NA NA NA NA NA NA
```

The percentage of settled claims is lower in the last accident year. Indicating that more claims are still open 39 / 66

The chain ladder method assumes that claims from all occurrence years follow the **same development pattern**. We construct various triangles to assess this assumption:

Percentage of open claims for which a payment is made.

```
triangle_payment <- incremental_triangle(
  observed_data_covid,
  variable = 'payment')
triangle_payment / triangle_open</pre>
```

```
## [,1] [,2] [,3] [,4] [,5] [,6] [,7] [,8] [,9] [,10]
## [1,] 0.7719059 0.6857855 0.5405405 0.7142857 1.0 1.0 1 1 1 NaN
## [2,] 0.7862093 0.7050265 0.7941176 0.8333333 0.0 NaN NaN NaN NaN NAN NA
## [3,] 0.7690000 0.7050633 0.6341463 0.8888889 0.6 0.5 NaN NaN NA NA NA
## [4,] 0.7793667 0.6788875 0.8214286 1.0000000 0.5 0.0 NaN NA NA NA NA
## [5,] 0.7699450 0.7308176 0.7500000 0.8888889 0.5 0.0 NA NA NA NA NA
## [6,] 0.7725367 0.6909091 0.7058824 0.8571429 1.0 NA NA NA NA NA NA
## [7,] 0.7665736 0.6814721 0.7692308 0.7142857 NA NA NA NA NA NA NA
## [8,] 0.7861635 0.6854839 0.7200000 NA NA NA NA NA NA NA NA
## [9,] 0.7921172 0.7046632 NA NA NA NA NA NA NA NA NA NA
## [10,] 0.7765255 NA NA NA NA NA NA NA NA NA NA
```

Average amount paid given a payment is made.

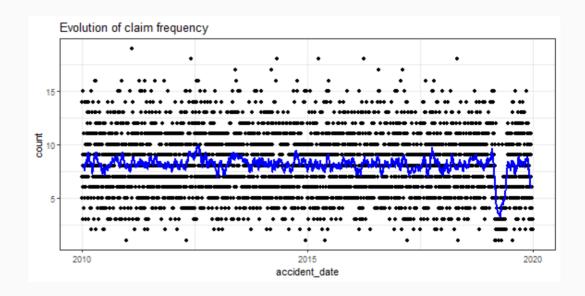
```
triangle_size <- incremental_triangle(
  observed_data_covid,
  variable = 'size')

triangle_size / triangle_payment</pre>
```

```
## [1,] 2002.171 3163.090 6093.815 5190.332 4652.457 6703.063 9478.77 6217.266 3468.3
## [2.] 1945.771 3139.920 3978.336 3894.454
                                                                            NaN
## [3,] 2074.917 3205.774 5739.993 7418.522 4952.581 4404.145
                                                                   NaN
                                                                            NaN
## [4,] 2032.962 3005.686 5560.879 4526.696 9301.109
                                                                   NaN
                                                                             NΑ
## [5,] 1929.888 3285.860 4825.659 6148.031 11727.691
## [6,] 1997.797 3237.126 4329.454 10932.020 5043.073
                                                                    NA
                                                                             NA
## [7,] 2065.694 3200.202 4871.267 3849.622
                                                            NΑ
                                                                    NΑ
                                                                             NΑ
## [8,] 2034.793 3172.943 4280.774
## [9,] 1983.073 3228.389
                                                            NA
                                                                    NA
                                                                             NA
## [10,] 1933.359
                                          NA
                                                            NA
                                                                    NA
                                                                             NΑ
```

The chain ladder method assumes that claims from all occurrence years follow the **same development pattern**. Inspecting the (granular) daily data:

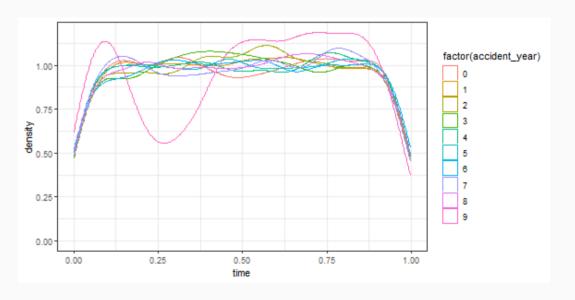
```
claims covid <- observed data covid %>%
  group by(accident number) %>%
  slice(1) %>%
 ungroup()
occ intensity <- claims covid %>%
  group by(accident date) %>%
  summarise(count = n())
require(zoo)
occ_intensity$moving_average <-</pre>
  rollmean(occ_intensity$count, 30, na.pad = TRUE)
ggplot(occ_intensity) +
 theme_bw() +
  geom_point(aes(x = accident_date, y = count)) +
  geom_line(aes(x = accident_date, y = moving_average),
            size = 1, color = 'blue') +
  ggtitle('Evolution of claim frequency')
```



The moving average indicates a period with decreased claim frequency in 2019

The chain ladder method assumes that claims from all occurrence years follow the **same development pattern**. Inspecting the (granular) daily data:

Density of when claims occur within each accident year. The chain ladder method works best when the densities look similar for all accident years.



The occurrence intensity in accident year 9 deviates from the other accident years.

## Fixing the chain ladder method

Improve the performance of the chain ladder method by making the data more homogeneous:

- **Group** claims by:
  - claim characteristics, e.g. separate triangle for fire and water related claims in home insurance.
  - occurrence time within a calendar year
- Omit:
  - deviating years/cells, especially if they occurred long ago
- **Adjust** for:
  - inflation

The appropriate method(s) depend on the data inspection from the previous slides.

## Fixing the chain ladder method (continued)

### Applied to the **covid data set**:

- claim frequency has changed in the months March, April, May
- only 2019, accident year 9, is affected

As 2019 is a recent calendar year, we cannot omit accident year 9 from the data.

We improve homogeneity in the data by splitting claims in two groups:

- group A: claims that have occurred in March, April or May
- group B: claims that have not occurred in March, April or May

```
observed_data_covid <- observed_data_covid %>%
  mutate(occurrence_month = as.numeric(format(accident_date, '%m')))
observed_data_covidA <- observed_data_covid %>%
  filter(occurrence_month %in% c(3, 4, 5))
observed_data_covidB <- observed_data_covid %>%
  filter(!(occurrence_month %in% c(3, 4, 5)))
```



In this exercise you compute the chain ladder reserve for claims in group A and B.

- 1. Choose data set A or B and analyse the stability of the chosen data set using some of the presented detection tools.
- 2. Compute the chain ladder reserve for group A and B separately.

  Combine these estimates to obtain an estimate for the total reserve.
- 3. Compare the new reserve estimate with the estimate obtained earlier using the chain ladder method without splitting the data.
- 4. Compute the standard error of the reserve estimate using the formula

$$\sigma^2 = \sigma_A^2 + \sigma_B^2.$$

For Q.1, analysing the stability of data set A.

#### Number of open claims begin dev.year:

```
triangle_open <- incremental_triangle(
  observed_data_covidA %>%
    mutate(open = calendar_year <= settlement_year),
  variable = 'open')
triangle_open</pre>
```

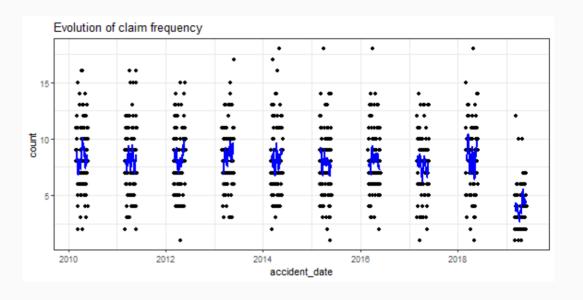
```
## [,1] [,2] [,3] [,4] [,5] [,6] [,7] [,8] [,9] [,10]
## [1,] 775 53 7 1 1 0 0 0 0 0
## [2,] 748 38 0 0 0 0 0 0 0 NA
## [3,] 773 47 5 1 1 0 0 0 NA NA
## [4,] 781 52 3 0 0 0 0 NA NA NA
## [5,] 757 63 7 2 1 0 NA NA NA NA
## [6,] 730 38 5 1 1 NA NA NA NA NA
## [7,] 750 59 2 1 NA NA NA NA NA NA
## [8,] 704 51 8 NA NA NA NA NA NA NA
## [9,] 770 40 NA NA NA NA NA NA NA NA
## [10,] 367 NA NA NA NA NA NA NA NA NA
```

### Settlement probability:

```
triangle_settlement <- incremental_triangle(
  observed_data_covidA %>%
    mutate(settlement = calendar_year == settlement_year),
  variable = 'settlement')
triangle_settlement / triangle_open
```

### For Q.1, analysing the stability of data set A.

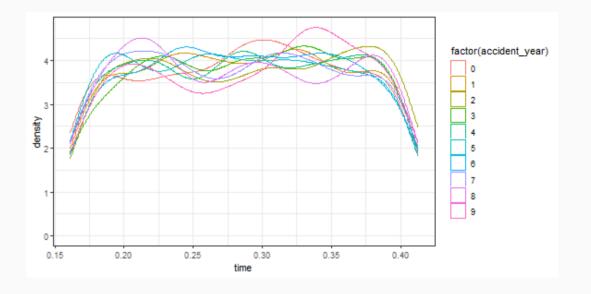
```
claims_covidA <- observed_data_covidA %>%
  group_by(accident_number) %>%
  slice(1) %>%
 ungroup()
occ intensity <- claims covidA %>%
  group_by(accident_date, accident_year) %>%
  summarise(count = n())
require(zoo)
occ_intensity <- occ_intensity %>%
  group_by(accident_year) %>%
 mutate(moving_average = rollmean(count, 14, na.pad = TRUE))
ggplot(occ_intensity) +
  theme_bw() +
  geom_point(aes(x = accident_date, y = count)) +
  geom_line(aes(x = accident_date, y = moving_average),
            size = 1, color = 'blue') +
  ggtitle('Evolution of claim frequency')
```



We compute moving averages within each accident year.

Otherwise rollmean would naively assume that May 31, 2010 is followed by March 1, 2011.

### For **Q.1**, analysing the stability of data set A.



All densities have a similar, indicating that within each accident year the distributon of when claims occur is the same.

For Q.1, analysing the stability of data set B.

#### Number of open claims begin at the start of the year:

```
triangle_open <- incremental_triangle(
  observed_data_covidB %>%
    mutate(open = calendar_year <= settlement_year),
  variable = 'open')
triangle_open</pre>
```

```
## [,1] [,2] [,3] [,4] [,5] [,6] [,7] [,8] [,9] [,10]
## [1,] 2158 749 30 6 1 1 1 1 1 0
## [2,] 2138 718 34 6 1 0 0 0 0 NA
## [3,] 2227 743 36 8 4 2 0 0 NA NA
## [4,] 2156 739 25 8 2 1 0 NA NA NA
## [5,] 2151 732 37 7 1 1 NA NA NA NA NA
## [6,] 2132 732 29 6 2 NA NA NA NA NA
## [7,] 2116 729 37 6 NA NA NA NA NA NA
## [8,] 2158 693 17 NA NA NA NA NA NA NA NA
## [9,] 2097 732 NA NA NA NA NA NA NA NA
## [10,] 2206 NA NA NA NA NA NA NA NA NA
```

### Settlement probability:

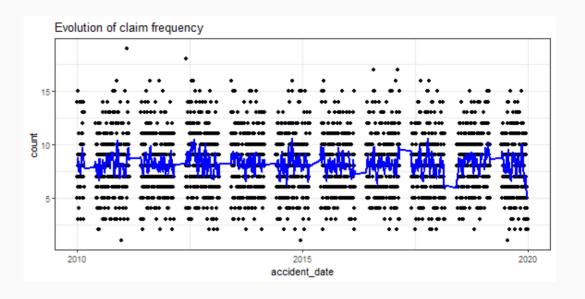
```
triangle_settlement <- incremental_triangle(
  observed_data_covidB %>%
    mutate(settlement = calendar_year == settlement_year),
    variable = 'settlement')

triangle_settlement / triangle_open
```

```
[,2]
                               [,3]
## [1,] 0.6936979 0.9599466 0.8000000 0.8333333 0.0
## [2,] 0.7104771 0.9526462 0.8235294 0.8333333 1.0 NaN NaN
## [3,] 0.7031881 0.9515478 0.7777778 0.5000000 0.5 1 NaN
## [4,] 0.7036178 0.9661705 0.6800000 0.7500000 0.5
## [5,] 0.7006044 0.9494536 0.8108108 0.8571429 0.0
## [6,] 0.7012195 0.9603825 0.7931034 0.6666667 1.0
## [7,] 0.7051040 0.9492455 0.8378378 0.6666667
## [8,] 0.7150139 0.9754690 0.8235294
                                              NA NA
## [9,] 0.7043395 0.9617486
                                              NA
                                                   NA
## [10,] 0.6940163
                       NA
                                          NA NA NA NA NA
```

### For **Q.1**, analysing the stability of data set B.

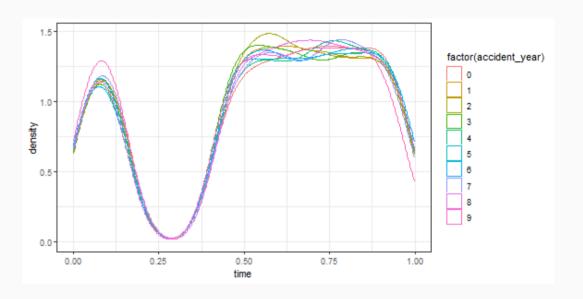
```
claims covidB <- observed data covidB %>%
  group_by(accident_number) %>%
  slice(1) %>%
 ungroup()
occ_intensity <- claims_covidB %>%
  group_by(accident_date, accident_year) %>%
  summarise(count = n())
require(zoo)
occ_intensity <- occ_intensity %>%
  group_by(accident_year) %>%
 mutate(moving average = rollmean(count, 14, na.pad = TRUE))
ggplot(occ_intensity) +
  theme_bw() +
  geom_point(aes(x = accident_date, y = count)) +
  geom_line(aes(x = accident_date, y = moving_average),
            size = 1, color = 'blue') +
  ggtitle('Evolution of claim frequency')
```

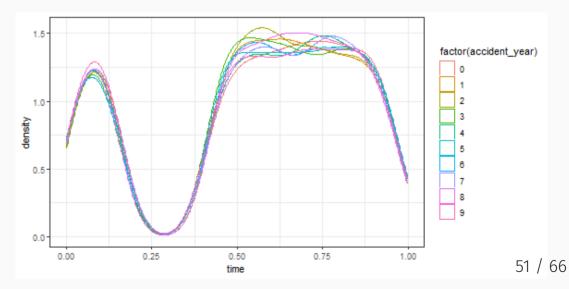


Claim frequency is stable over all accident years. No sudden jumps/decreases.

For Q.1, analysing the stability of data set B.

Since we only observe reported claims, we observe less claims from recent accident years around the end of the year. Correct for this by filtering claims that are reported in the year of occurrence.





### For **Q.2** computing the chain ladder reserve

```
## Warning in Mack.S.E(CL[["Models"]], FullTriangle, est.sigma = est.sigma, : Informatic
## '5-6', '6-7', '7-8', '8-9'
```

```
## MackChainLadder(Triangle = triangleA)
##
##
        Latest Dev.To.Date Ultimate
                                         IBNR Mack.S.E CV(IBNR)
## 1 1,619,982
                     1.000 1,619,982 0.00e+00 0.00e+00
## 2 1,528,185
                    1.000 1,528,185 0.00e+00 1.44e-13
                                                            Inf
## 3 1,608,274
                    1.000 1,608,274 -4.66e-10 3.54e-10 -0.761
## 4 1,671,348
                    1.000 1,671,348 -4.66e-10 3.64e-10
                                                         -0.781
                    1.000 1,684,656 -4.66e-10 3.66e-10
## 5 1.684.656
                                                         -0.785
## 6 1,470,984
                    1.000 1,470,984 -4.66e-10 4.23e-10
                                                         -0.908
## 7 1,640,175
                     0.999 1,641,391 1.22e+03 2.38e+03
                                                          1.962
## 8 1,666,274
                     0.996 1,672,544 6.27e+03 4.74e+03
                                                          0.756
## 9 1,615,375
                     0.987 1,636,318 2.09e+04 1.18e+04
                                                          0.561
                     0.893 811,877 8.70e+04 3.14e+04
## 10 724,846
                                                          0.361
##
##
                   Totals
## Latest: 15,230,099.47
## Dev:
                     0.99
## Ultimate: 15,345,559.70
## IBNR:
               115,460.23
## Mack.S.E
                34,373.24
## CV(IBNR):
                    0.30
```

```
## MackChainLadder(Triangle = triangleB)
##
##
        Latest Dev.To.Date Ultimate
                                        IBNR Mack.S.E CV(IBNR)
## 1 4,835,633
                    1.000 4,835,633
                                                          NaN
## 2 4,687,234
                    1.000 4,687,234
                                                1,212
                                                          Inf
## 3 5,192,025
                                                3,398
                    1.000 5,193,916
                                        1,892
                                                       1.7965
## 4 4,769,571
                    0.999 4,773,326
                                                5,225
                                       3,755
                                                       1.3914
## 5 4,765,606
                                                7,422 1.2219
                    0.999 4,771,681
                                        6,074
## 6 4,852,924
                    0.998 4,861,338
                                                8,249 0.9803
                                       8,414
## 7 4,782,048
                    0.996 4,799,125
                                                       0.5675
                                       17,077
                                                9,690
## 8 4,607,266
                    0.989 4,656,956
                                      49,690
                                               19,630 0.3950
## 9 4,644,426
                    0.967 4,804,801
                                     160.374
                                               39.868 0.2486
## 10 3,138,005
                    0.640 4,902,249 1,764,244 132,487 0.0751
##
                   Totals
## Latest: 46,274,737.36
## Dev:
## Ultimate: 48,286,257.75
## IBNR:
             2,011,520.39
## Mack.S.E
               144,671,48
## CV(IBNR):
                    0.07
```

#### For Q.3, we combine the estimated reserves from A and B

```
ultimateA <- sum(cum2incr(clA$FullTriangle))
already_paidA <- sum(cum2incr(clA$Triangle), na.rm = TRUE)
reserveA <- ultimateA - already_paidA

ultimateB <- sum(cum2incr(clB$FullTriangle))
already_paidB <- sum(cum2incr(clB$Triangle), na.rm = TRUE)
reserveB <- ultimateB - already_paidB

reserve_covid_cl_split <- reserveA + reserveB

c(reserve_actual = reserve_covid_actual,
    reserve_cl = reserve_covid_cl,
    reserve_cl_split = reserve_covid_cl_split)</pre>
```

```
## reserve_actual reserve_cl reserve_cl_split
## 2389277 1905100 2126981
```

Splitting the data results in a more accurate reserve estimate.

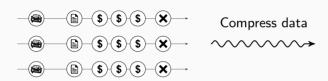
### For Q.4, we evaluate the relative performance of the model

|           | chain ladder | chain ladder split |
|-----------|--------------|--------------------|
| error     | -484177.34   | -262296.65         |
| sigma     | 136795.35    | 148698.88          |
| pct_error | -20.26       | -10.98             |
| std.dev   | -3.54        | -1.76              |

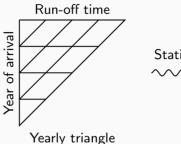
# Research outlook

### Research outlook

### Aggregate reserving



Individual data

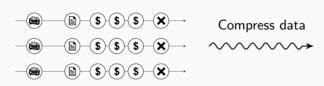


Statistical model



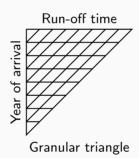
Reserve

### Granular reserving



Individual data

Individual data



Statistical model



Reserve

### Individual reserving



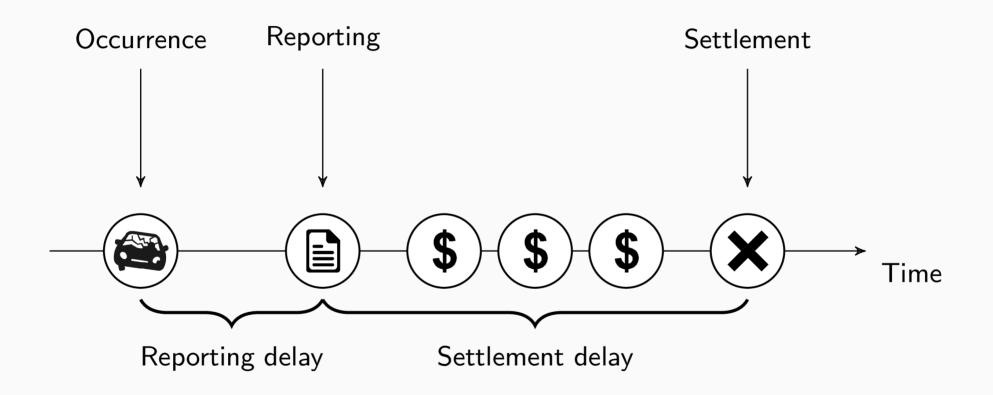
44444 44444 44444 Aggregate reserves



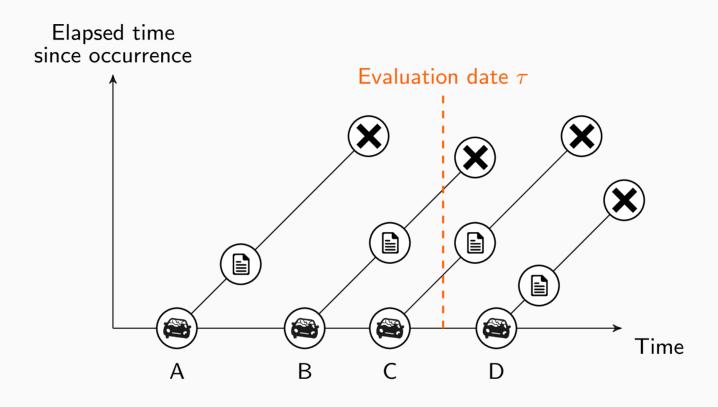
Reserve per policy/claim

Reserve

## Development of a individual claims



## Development of a individual claims (continued)



Observed claims are **censored** due to **delays** (reporting, settlement) in the claim development process

IBNR reserve: future costs for claims that occurred, but are not yet reported (claim B)

RBNS reserve: future costs for claims that are reported, but are not yet settled (claim C)

Pricing: all costs for claims that will occur in future insured exposure periods (claim D)

### The IBNR reserve

Following a frequency-severity decomposition, the IBNR reserve is the product of the expected **number of unreported claims** times the **expected severity per claim**.

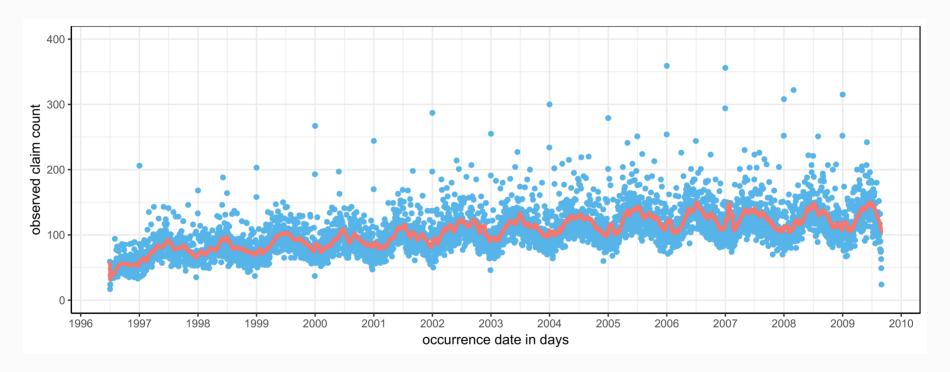
- Insurance pricing covers the estimation of claim severity for new claims
- Reserving methods focus on predicting the number of unreported claims.

### Our work on the topic:

- "Modeling the number of hidden events subject to observation delay". Jonas Crevecoeur, Katrien Antonio and Roel Verbelen. (2019). European Journal of Operational Research.
- "Modeling the occurrence of events subject to a reporting delay via an EM algorithm". Roel Verbelen, Katrien Antonio, Gerda Claeskens and Jonas Crevecoeur. (2019). Submitted.

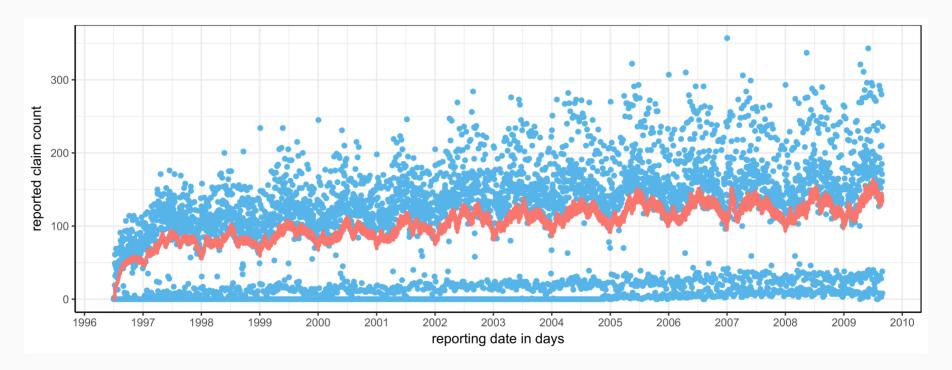
# The IBNR reserve (continued)

Number of observed claim occurrences per day



# The IBNR reserve (continued)

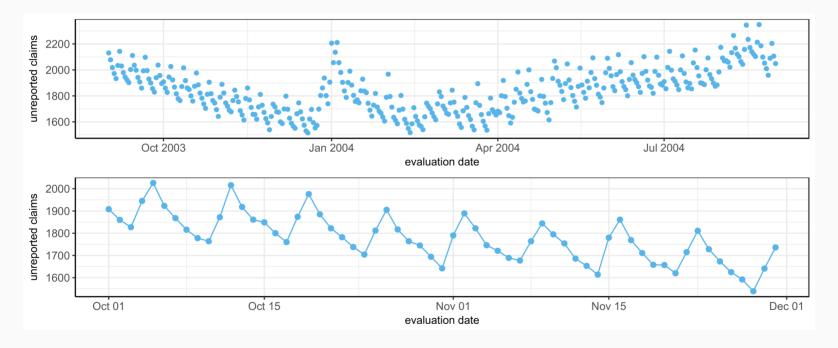
Number of reported claims per day



Almost no claims are reported on Saturdays, Sundays and holidays.

## The IBNR reserve (continued)

Total number of unreported claims on each day, i.e. the number of claims that occur before the evaluation date, but are reported afterwards.



The number of unreported claims increases during the weekend (+10% on sunday) and around the end of the year (+30%).

### The RBNS reserve

Predict the future costs of individual, reported claims.

### Our work on the topic:

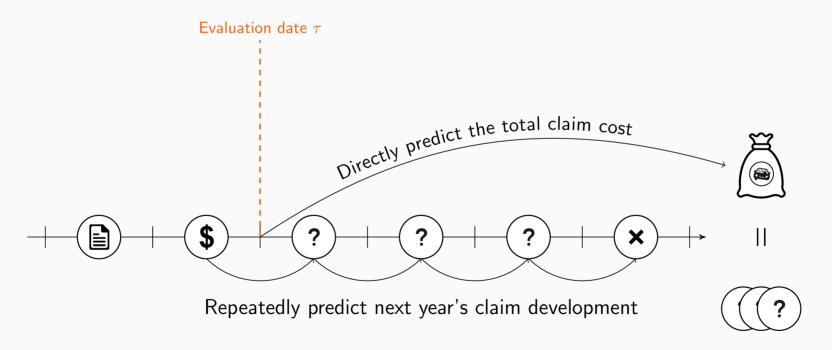
- "A hierarchical reserving model for non-life insurance claims". Jonas Crevecoeur and Katrien Antonio. (2020). Sumbitted.
- "Bridging the gap between pricing and reserving with an occurrence and development model for non-life insurance claims". Katrien Antonio and Jonas Crevecoeur. (2020). Working paper.

Methods implemented in the R package {hirem}, Hierarchical reserving models, available on GitHub.

## The RBNS reserve (continued)

The hierarchical model is based on two key ideas:

1. Model the development of indiviudal claim in discrete time (steps of one year) using the observed development in previous years.



## The RBNS reserve (continued)

The hierarchical model is based on **two key ideas**:

- 1. Model the development of indiviudal claim in discrete time (steps of one year) using the observed development in previous years.
- 2. Focus on all events registered over the lifetime of a claim

Common events registered over the lifetime of a claim:

- settlement
- payments
- initial incurred / changes in the incurred
- involvement lawyer

### These events are **dependent**:

- if a claim is **settled**, there will be no **payments** in the future
- large **payments** are more likely when the outstanding **reserve** is large

## Implementation in the {hirem} package

Implementation readily available from the {hirem} package on GitHub. Events are added to the model as **layers**.

## Thanks!

Slides created with the R package xaringan.

Course material available via

https://github.com/katrienantonio/workshop-loss-reserv-fraud-2020