

The Welfare Impact of Reemployment Bonuses

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Abstract

This paper investigates the potential of reemployment bonuses, monetary incentives offered to workers who obtain employment, as a means to mitigate the moral hazard in unemployment insurance (UI) while preserving consumption smoothing. Using a dynamic job search model combined with a sufficient statistics approach, I find a substantial positive impact of reemployment bonuses on welfare given the current level of UI benefits. Moreover, using a fully calibrated model, I find that the optimal UI benefit level is higher when reemployment bonuses are incorporated. Compared to the welfare gain achieved by implementing only the optimal level of UI benefits, the optimal combination of UI benefits and reemployment bonuses achieves a 56 percent larger welfare gain.

Keywords: Reemployment bonus; Sufficient statistic approach; Unemployment insurance; Consumption smoothing; Moral hazard

JEL classification: H20, J64, J65

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1 Introduction

Unemployment insurance (UI) is a crucial element of social insurance programs in developed countries, designed to protect workers from income loss during periods of unemployment. However, it is widely acknowledged that UI discourages job search among the unemployed, i.e. moral hazard, which imposes a fiscal burden by increasing government expenditure on UI benefits and reducing income tax revenues. It is a concern not only for economists but also for policymakers. For example, only 20 states in the U.S. have sufficient reserves to sustain a year's worth of UI benefit payments if a recession occurs, posing a threat to the reliability of the current UI system ([White House, 2016](#)). A sustainable UI system requires a policy that encourages job search without impeding the consumption smoothing facilitated by UI.

One potential way to address the issue of moral hazard is reemployment bonuses. Reemployment bonuses are rewards given to unemployed people if they manage to find a job within a certain period. This policy is intended to encourage unemployed individuals to look for jobs more actively, which could help to alleviate the burden on the UI budget. Reemployment bonuses have been tested in the U.S. and implemented in a few other countries.¹ While several studies have found positive effects of these bonuses on labor supply, there has not been much research quantifying their welfare impact or how the government should set reemployment bonuses jointly with UI benefits.

This paper investigates the welfare implications of reemployment bonuses in a dynamic model of consumption, saving, and job search. In the first part, I adopt the sufficient statistic approach and develop a formula to quantify the welfare impact of the first dollar of reemployment bonuses. This formula incorporates several reduced-form parameters and does not need a fully calibrated model. An essential parameter in the formula is the response of unemployment duration to changes in reemployment bonuses. Instead of directly examining exogenous variations in reemployment bonuses that are not widely available, I theoretically establish a link between the labor supply response to reemployment bonuses and the response to UI benefits. This connection allows me to leverage the vast empirical research on the labor supply effects of UI benefits.²

I find that the first dollar of reemployment bonuses has a positive welfare impact by alleviating the moral hazard effect of UI, which is equivalent to a five-dollar increase in lifetime income per person. To facilitate a comparison of this finding with the welfare effects of other existing government programs, I calculate the Marginal Value of Public Funds (MVPF) ([Finkelstein and Hendren 2020](#), [Hendren and Sprung-Keyser 2020](#)). The MVPF of a policy is defined as the ag-

¹Refer to [Meyer \(1995\)](#) for the field experiments in the U.S. Actual implementation of bonus programs in South Korea and Taiwan can be found in [Ahn \(2018\)](#) and [Huang and Yang \(2021\)](#), respectively.

²See [Krueger and Meyer \(2002\)](#) and [Schmieder and Von Wachter \(2016\)](#) for a survey.

gregate willingness to pay for the policy divided by its net cost, and it allows for comparing the cost-effectiveness of various government programs in a unified way. I find that the MVPF of the first dollar of reemployment bonuses exceeds two. This value exceeds the MVPFs observed for many government programs targeted at adults such as unemployment insurance, disability insurance, job training, earned income tax credits, and many others, as documented in [Hendren and Sprung-Keyser \(2020\)](#). This underscores the potential for large welfare improvement through the implementation of reemployment bonuses.

Given the considerable welfare impact of the marginal policy change found above, it would be natural to ask what is the globally optimal joint design of UI benefits and reemployment bonuses and the potential welfare gain it can bring. Addressing such a question, which involves non-marginal policy changes, is beyond the scope of a sufficient statistics approach. Therefore, I fully calibrate the model parameters by matching unemployment durations and elasticities as observed in the data. To highlight the role of reemployment bonuses in the joint design, I initially calculate the optimal level of UI benefits without reemployment bonuses and subsequently examine the jointly optimal policy.

In the absence of reemployment bonuses, I find that optimal UI benefits equate to 18 percent of wages, significantly below typical replacement rates of 50 percent in the U.S., yet still within the range of existing estimates. Relative to a 50 percent replacement rate, this reduction in UI benefits decreases the unemployment rate by 2.4 p.p. while increasing the size of consumption decline upon job loss by 18 p.p. These findings suggest that the moral hazard cost of UI in the calibrated economy is so large that, to maximize welfare, it is necessary to reduce the UI benefit level. This observation is consistent with earlier studies including, for example, [Hansen and Imrohoroglu \(1992\)](#) and [Gruber \(1997\)](#).

Incorporating reemployment bonuses increases the optimal level of UI benefits. Specifically, I find that setting the UI benefit replacement rate to 49 percent, together with reemployment bonuses equivalent to 56 percent of wages, maximizes welfare. This jointly optimal policy maintains an unemployment rate almost as low as the one in the economy with optimal UI benefits alone while preventing significant disruption to consumption smoothing. Consequently, the jointly optimal policy yields a 0.39 percent improvement in welfare in terms of consumption equivalence, which is a 56 percent larger improvement than what the optimal UI benefits alone can achieve.

Related Literature. The concept of reemployment bonuses can be traced back to the 1980s when a series of state-led field experiments revealed that offering lump-sum reemployment bonuses effectively shortened the duration of unemployment ([Woodbury and Spiegelman 1987](#), [Meyer 1995](#), [Robins and Spiegelman 2001](#)). More recent studies by [Ahn \(2018\)](#) and [Huang and Yang \(2021\)](#) have evaluated the impact of reemployment bonuses on unemployment duration in quasi-

experimental settings. Leveraging real policy changes in South Korea and Taiwan, their research demonstrates that reemployment bonuses significantly reduce the unemployment duration among UI recipients. Theoretically, [Hopenhayn and Nicolini \(1997\)](#) study the optimal UI benefit profile in a principal-agent model and show that the optimal contract involves a UI benefit that decreases over time and a wage tax after reemployment that increases over time. In their numerical example, they find that the optimal wage tax can be negative for a worker finding a job quickly enough, suggesting that a negative tax—which can be interpreted as a reemployment bonus—could emerge as a component of the optimal UI design. I build on this work by deriving a sufficient statistic formula that only requires well-established elasticities to quantify the welfare effect of reemployment bonuses.

Methodologically, this paper employs the sufficient statistic approach pioneered by [Baily \(1978\)](#) and [Chetty \(2006\)](#). This approach has been extensively utilized by researchers in examining various aspects of UI. For instance, it has been used to study the optimal level of UI benefits ([Gruber 1997](#), [Chetty 2008](#), [Landaís 2015](#), [Kroft and Notowidigdo 2016](#)), the optimal duration of UI ([Ganong and Noel 2019](#)), and the optimal trajectory of UI benefits ([Kolsrud, Landaís, Nilsson and Spinnewijn 2018](#), [Lindner and Reizer 2020](#)). This approach to welfare evaluation is useful as it requires only a subset of model parameters to be identified. But a welfare formula sometimes requires a variable or a reduced-form parameter that is difficult to obtain, and researchers establish a link between variables that are challenging to measure and those that are more straightforward. For instance, [Chetty \(2008\)](#) approximates the effect of UI on the utility gain from consumption smoothing, which necessitates high-frequency consumption data, by using an estimate of a labor supply response to severance payments. Following a similar logic, [Landaís \(2015\)](#) gauge a labor supply response to UI benefits that vary over time to estimate the utility gain from consumption smoothing. In assessing the welfare impact of reemployment bonuses, I leverage consumption information and a labor supply response to UI benefits to approximate a labor supply response to reemployment bonuses, which is then incorporated into a sufficient statistic formula.

The results from the sufficient statistic approach cannot be extended to cases where policy changes are not marginal due to two reasons. First, the envelope theorem, used to characterize the welfare impact, does not hold for non-marginal policy changes. Second, the formula depends on reduced-form parameters that may not be policy-invariant. Furthermore, it cannot provide direction for the joint design of multiple policy instruments. I supplement my results from the sufficient statistic approach by investigating non-marginal changes in reemployment bonuses through the full calibration of the model. In this vein, [Lentz \(2009\)](#), [Michelacci and Ruffo \(2015\)](#), [Lawson \(2017\)](#), and [Ganong and Noel \(2019\)](#) estimate a partial-equilibrium dynamic model of consumption, saving, and job search to study optimal UI benefit design. While these papers focus on the UI benefit level alone, I study UI benefits together with reemployment bonuses.

2 Model

In this section, I present a dynamic model of consumption, saving, and job search, building upon the framework in [Chetty \(2008\)](#). The primary objective is to analyze the welfare implications of marginal adjustments in reemployment bonuses, relying on a set of reduced-form parameters. This approach offers certain advantages as it does not need a complete specification of the model. For instance, while assuming convexity of the search cost function, I do not specify an exact functional form for it. However, a drawback of this approach is that I cannot quantify the welfare impact of non-marginal policy changes, thereby limiting insights into the globally optimal levels of UI benefits and reemployment bonuses. Later in Section 4, I fully calibrate the baseline model presented in this section to study non-marginal policy changes.

2.1 Environment

Workers in the model are initially unemployed in $t = 1$. Upon becoming employed, they remain employed until the end of the model at period T , which is a standard assumption in the literature and greatly simplifies the problem.³

While unemployed, workers receive UI benefits denoted as b_u for a maximum of T_B periods. Upon finding a job, workers receive reemployment bonuses denoted as b_e . I define the vector $\mathbf{b} = (b_u, b_e)$ to represent these benefit levels. I assume that individuals who find a job before period T_B are eligible to receive b_e until period T_B . For instance, if a worker finds a job in period $\bar{t} < T_B$, the worker receives UI benefits b_u during periods $t = 1, \dots, \bar{t}$ and reemployment bonuses b_e during periods $t = \bar{t} + 1, \dots, T_B$.

In this analysis, I focus on the case where b_u and b_e remain constant over the T_B periods, and T_B is fixed. The government finances UI benefits through taxes denoted as τ , which are collected from each employed worker. The search effort of individuals at time t is denoted as e_t , and I normalize it such that the level of effort e_t is equal to the probability of finding a job. Consequently, the survival probability, which represents the probability of remaining unemployed after searching for a job in period t , is given by $S_t = \prod_{j=1}^t (1 - e_j)$. The expected unemployment duration is defined as $D = \sum_{t=1}^T S_t$, and the expected duration of UI compensation is denoted as $D_B = \sum_{t=1}^{T_B} S_t$.

2.2 Individual Problem

To simplify the analysis, I assume a zero interest rate and no discounting. In each period t , an unemployed individual engages in job search and subsequently determines their consumption level.

³For example, [Chetty \(2008\)](#), [Landais \(2015\)](#), and [Kolsrud et al. \(2018\)](#) adopts the same assumption to get a welfare formula.

Optimal consumption of employed workers. If a worker is employed in period t with assets A_t , the value function is defined as

$$V_{s,t}^E(A_t; b_e, \tau) = \max_{A_{t+1} \geq L} U(A_t - A_{t+1} + y_{e,s,t}) + V_{s,t+1}^E(A_{t+1}; b_e, \tau). \quad (1)$$

Here, s represents the period in which the worker finds the job, A_t denotes the asset level at the start of period t , and L represents the exogenous liquidity constraint. The income of workers who find a job in period s , denoted as $y_{e,s,t}$, is given by $y_{e,s,t} = w_{s,t} - \tau + b_e$ for $t \leq T_B$, and $y_{e,t} = w_{s,t} - \tau$ for $t > T_B$. The wage $w_{s,t}$ may depend on s to capture the potential impact of unemployment duration on future wages. I assume that wages are non-random and deterministic, but allowing for stochastic wages does not change results as I discuss later. The utility function $U(\cdot)$ is assumed to be twice-differentiable, strictly increasing, and strictly concave on \mathbb{R}_+ .

Note that the value of an employed worker depend on reemployment bonuses b_e but not on UI benefits b_u since the worker stays employed once getting a job.

Optimal consumption of unemployed workers. If an unemployed worker with asset A_t does not find a job at the start of period t , the value function is given by

$$V_t^U(A_t; \mathbf{b}, \tau) = \max_{A_{t+1} \geq L} U(A_t - A_{t+1} + y_{u,t}) + V_{t+1}(A_{t+1}; \mathbf{b}, \tau), \quad (2)$$

where $y_{u,t}$ represents the income for unemployed workers, which is determined by $y_{u,t} = \bar{y} + b_u$ if $t \leq T_B$, and $y_{u,t} = \bar{y}$ otherwise. The parameter \bar{y} represents an additional income source that does not impact the government budget. For instance, it can account for the income of other family members or informal transfers from parents. The term $V_{t+1}(\cdot)$ in the second part of the equation denotes the expected value at the beginning of period $t + 1$ before initiating a job search.

In contrast to the value function of an employed worker, the value function of an unemployed worker depends on both UI benefits b_u and reemployment bonuses b_e .

Optimal search effort. The value function of an unemployed worker with asset level A_t at the beginning of each period, before initiating a job search, is given by

$$V_t(A_t; \mathbf{b}, \tau) = \max_{e_t \in [0,1]} e_t V_{t,t}^E(A_t; b_e, \tau) + (1 - e_t) V_t^U(A_t; \mathbf{b}, \tau) - \psi(e_t), \quad (3)$$

where $\psi(\cdot)$ represents the disutility of search effort. The function $\psi(\cdot)$ is twice-differentiable, strictly increasing, and strictly convex on the interval $(0, 1)$. I impose the conditions $\psi'(0) = 0$ and $\lim_{e \rightarrow 1} \psi(e) = +\infty$ to ensure an interior solution. $V_t^U(\cdot)$ may not be concave due to the presence of $V_{t+1}(\cdot)$ in the second term of Equation (2). I assume that $V_t^U(\cdot)$ is concave under plausible

parameter values, as assumed in [Chetty \(2008\)](#).

The optimal level of search effort is determined by solving the following first-order condition

$$\psi'(e_t(A_t; \mathbf{b}, \tau)) = V_{t,t}^E(A_t; b_e, \tau) - V_t^U(A_t; \mathbf{b}, \tau). \quad (4)$$

Given that $\psi(\cdot)$ is a convex function, the left-hand side of the equation is increasing in e_t . This implies that individuals exert greater search effort when the value of employment is higher and exert less search effort when the value of unemployment is higher. Consequently, an increase in UI benefits b_u , which makes remaining unemployed more valuable, leads to a decrease in search effort. Conversely, more generous reemployment bonuses b_e incentivize higher search effort by increasing the value of being employed.

2.3 Government Problem

In this subsection, I derive a formula for assessing the welfare impact of a marginal change in b_e . To evaluate this impact, let $W(\mathbf{b})$ represent the value of unemployed individuals at the beginning of the model as a function of UI benefits b_u and reemployment bonuses b_e subject to the budget constraint. Specifically, given the initial assets A_1 , I define

$$W(\mathbf{b}) = V_1(A_1; \mathbf{b}, \tau(\mathbf{b})) \quad \text{where} \quad \tau(\mathbf{b}) = \frac{D_B b_u + (T_B - D_B) b_e}{T - D}. \quad (5)$$

Here, $\tau(\mathbf{b})$ represents the budget-balancing level of taxes as a function of UI benefits b_u and reemployment bonuses b_e . The government's objective is to determine the optimal UI benefits b_u and reemployment bonuses b_e that maximize the welfare measure $W(\mathbf{b})$. In this section, I do not solve the problem to obtain a globally optimal policy. Instead, I analyze the welfare impact of a marginal increase in b_e from the current level of $b_e = 0$.

The government budget constraint can be expressed as

$$[T - D(\mathbf{b}, \tau)]\tau(\mathbf{b}) = D_B(\mathbf{b}, \tau)b_u + [T_B - D_B(\mathbf{b}, \tau)]b_e. \quad (6)$$

The impact of providing reemployment bonuses is given by

$$\begin{aligned} \frac{\partial \tau(\mathbf{b})}{\partial b_e} &= \underbrace{\frac{T_B - D_B(\mathbf{b}, \tau(\mathbf{b}))}{T - D(\mathbf{b}, \tau(\mathbf{b}))}}_{\text{Mechanical Impact}} \\ &\quad + \underbrace{\frac{1}{T - D(\mathbf{b}, \tau(\mathbf{b}))} \left[\frac{dD_B(\mathbf{b}, \tau(\mathbf{b}))}{db_e} (b_u - b_e) + \frac{dD(\mathbf{b}, \tau(\mathbf{b}))}{db_e} \tau(\mathbf{b}) \right]}_{\text{Behavioral Impact}}, \end{aligned} \quad (7)$$

where $\frac{dD_B(\mathbf{b}, \tau(\mathbf{b}))}{db_e}$ and $\frac{dD(\mathbf{b}, \tau(\mathbf{b}))}{db_e}$ are the response of D_B and D to a balanced-budget increase in b_e , which includes the effect of the change in τ needed to finance the increase in b_e . The first term captures the increase in taxes required to fund reemployment bonuses in the absence of any response from unemployed workers, referred to as the mechanical impact. The second term shows that the response of unemployed workers has an impact on the budget through a change in unemployment duration, which I refer to as the behavioral impact. If a budget-balance increase in reemployment bonuses induces shorter unemployment duration (i.e., $\frac{dD_B}{db_e} < 0$ and $\frac{dD}{db_e} < 0$), the increase in taxes is less than the mechanical cost of the policy change.

Reemployment bonuses also affect consumption after reemployment. Taking that into account as well, the following proposition characterizes the welfare impact of the marginal change in reemployment bonuses b_e given UI benefits b_u .

Proposition 1. *The welfare impact of the marginal increase in reemployment bonuses b_e is given by*

$$\frac{\partial W(\mathbf{b})}{\partial b_e} \bigg/ \frac{\partial V_1}{\partial w} = \frac{T_B - D_B}{T - D} \left[\frac{MU_{e,T_B} - MU_{e,T}}{MU_{e,T}} - \frac{dD_B}{db_e} \frac{b_u - b_e}{T_B - D_B} - \frac{dD}{db_e} \frac{\tau(\mathbf{b})}{T_B - D_B} \right], \quad (8)$$

where $D = D(b, \tau(b))$, $D_B = D_B(\mathbf{b}, \tau(\mathbf{b}))$, and $MU_{e,t}$ is given by

$$MU_{e,t} = \sum_{k=1}^t \frac{1 - S_k}{t - D_B} \mathbb{E}_s[U'(c_{e,s,k})] \quad \text{for } t = T_B, T. \quad (9)$$

Proof. See Appendix A.2. □

To obtain a money metric for assessing the welfare impact, I normalize $\frac{\partial W(\mathbf{b})}{\partial b_e}$ by the welfare gain resulting from a permanent increase in wages $\frac{\partial V_1}{\partial w}$. $MU_{e,t}$ is the weighted average of marginal utilities of consumption during employment, where the weights are proportional to the probability that an individual is employed in period t . This expectation is computed by considering all possible histories that lead to the state where a person is employed in period t .⁴

The interpretation of formula (8) is as follows. The first term in the bracket captures the redistributive effect of the policy change, which arises from intertemporal transfers associated with the increase in reemployment bonuses b_e and the corresponding rise in taxes τ . Note that individuals can receive b_e for a maximum of T_B periods while they pay taxes until the end of the model period T . This difference generates transfers across periods. The second and third terms represent the welfare gain resulting from the behavioral impact of reemployment bonuses, corresponding to the second term in equation (7).

The sign of the first term can be theoretically positive or negative, depending on the underlying income processes. On the one hand, since $MU_{e,T}$ assigns weights to workers who find a job later,

⁴The precise expression of $\mathbb{E}_s[U'(c_{e,s,k})]$ is provided in equation (42) in Appendix A.2.

$MU_{e,T}$ should be larger than MU_{e,T_B} to the extent that human capital losses during unemployment lead to consumption losses after reemployment. On the other hand, $MU_{e,T}$ also assigns weights to workers who have been employed for a longer period after reemployment. If these workers accumulate human capital and experience increased consumption, $MU_{e,T}$ should be smaller than MU_{e,T_B} .

3 Empirical Implementation

3.1 Inferring the Response to Reemployment Bonuses from the Response to UI benefits

One crucial parameter in the formula is the response of unemployment duration to reemployment bonuses. Instead of attempting to directly estimate this parameter by seeking exogenous policy variations, I theoretically establish a connection between the labor supply response to UI benefits and the labor supply response to reemployment bonuses. This connection allows me to leverage the vast empirical literature on the labor supply response to UI, as documented in [Krueger and Meyer \(2002\)](#) and [Schmieder and Von Wachter \(2016\)](#).

Recall that the first-order condition for search effort is given by:

$$\psi'(e_t(A_t; \mathbf{b}, \tau)) = V_{t,t}^E(A_t; b_e, \tau) - V_t^U(A_t; \mathbf{b}, \tau). \quad (4)$$

By differentiating both sides of the equation with respect to either b_u or b_e for $t \leq T_B$, I obtain:

$$\frac{\partial e_t}{\partial b_u} = \frac{-\frac{\partial V_t^U(A_t; \mathbf{b}, \tau)}{\partial b_u}}{\psi''(e_t)}, \quad (10)$$

$$\frac{\partial e_t}{\partial b_e} = \frac{\frac{\partial V_{t,t}^E(A_t; b_e, \tau)}{\partial b_e} - \frac{\partial V_t^U(A_t; \mathbf{b}, \tau)}{\partial b_e}}{\psi''(e_t)}. \quad (11)$$

Note that the response of search effort to UI benefits b_u and reemployment bonuses b_e both depend on the curvature of the search cost function $\psi''(\cdot)$. By rearranging the equations, I obtain the following relationship:

$$\frac{\partial e_t}{\partial b_e} = \frac{\partial e_t}{\partial b_u} \times \frac{\frac{\partial V_{t,t}^E(A_t; b_e, \tau)}{\partial b_e} - \frac{\partial V_t^U(A_t; \mathbf{b}, \tau)}{\partial b_u}}{-\frac{\partial V_t^U(A_t; \mathbf{b}, \tau)}{\partial b_u}}. \quad (12)$$

The left-hand side represents the response of search effort to reemployment bonuses, while the right-hand side represents the response of search effort to UI benefits multiplied by a correction

term. The correction term accounts for the ratio of the marginal values of reemployment bonuses and UI benefits, which depend on the marginal utility of consumption.

The equation above is about search effort e_t . However, what I can observe is unemployment duration D . To translate the relationship above into the one in terms of unemployment duration in a tractable way, I impose several assumptions regarding the evolution of consumption. These assumptions are listed below:

Assumption. (A.1) *Consumption after finding a job does not depend on s and t , i.e., $c_{e,s,t} = c_e$.*

(A.2) *Finding a job does not decrease consumption, i.e., $c_e \geq c_{u,t}$.*

(A.3) *Consumption during unemployment does not increase over time, i.e., $c_{u,t} \leq c_{u,t-1}$.*

It is worth emphasizing that all of these assumptions are either common or empirically supported. Assumption (A.1) is reasonable for an approximation when the impact of unemployment on lifetime income is negligible. This assumption is commonly made in research that derives a welfare formula for UI benefits (e.g. [Chetty 2008](#), [Kroft and Notowidigdo 2016](#)). Moreover, [Chetty \(2008\)](#) provides simulation results demonstrating that this approximation has a negligible impact on the evaluated welfare. The remaining assumptions (A.2)-(A.3), while intuitively reasonable, also gain empirical support from studies examining consumption patterns such as [Ganong and Noel \(2019\)](#).

With these assumptions, I am now able to use the relationship between the response of *search effort* to UI benefits and reemployment benefits in equation (12) to establish the link between the response of *unemployment duration* to UI benefits and reemployment bonuses.

Proposition 2. *Suppose assumptions (A.1)-(A.3) are satisfied. Then, the response of the expected UI-compensated unemployment spells D_B to a change in reemployment bonuses b_e is bounded as follows:*

$$\underline{M}_{T_B} \frac{\partial D_B(\mathbf{b}, \tau)}{\partial b_u} \leq -\frac{\partial D_B(\mathbf{b}, \tau)}{\partial b_e} \leq \overline{M}_{T_B} \frac{\partial D_B(\mathbf{b}, \tau)}{\partial b_u}, \quad (13)$$

where

$$\overline{M}_{T_B} = \frac{U'(c_e)}{U'(c_{u,1})}, \quad \underline{M}_{T_B} = \frac{U'(c_e)}{U'(c_{u,T_B})}.$$

Proof. See Appendix [A.3](#). □

The proposition establishes the upper and lower bounds for the labor supply response to reemployment bonuses. The bounds depend on the response to UI benefits and the marginal rate of substitution between consumption during periods of employment and unemployment. As previously discussed, the labor supply response to either policy is influenced by the curvature of the job-search disutility function, making the response to UI benefits a useful quantity in inferring the

response to reemployment bonuses. However, certain adjustments are needed given that UI benefits influence consumption during unemployment, while reemployment bonuses impact consumption during employment. For instance, if consumption during employment significantly exceeds consumption during unemployment, the concave utility function implies that offering reemployment bonuses exerts a smaller impact on the net value of employment than UI benefits do. The marginal rate of substitution does the adjustment.

Remark 1. The bounds established in Proposition 2 are derived based on partial derivatives and do not account for the effects of changes in taxes associated with changes in reemployment bonuses. However, the welfare formula (8) relies on total derivatives. It is important to note that:

$$\frac{dD_B(\mathbf{b}, \tau(\mathbf{b}))}{db_e} = \frac{\partial D_B(\mathbf{b}, \tau(\mathbf{b}))}{\partial b_e} + \frac{\partial D_B(\mathbf{b}, \tau)}{\partial \tau} \Big|_{\tau=\tau(\mathbf{b})} \times \frac{\partial \tau(\mathbf{b})}{\partial b_e}, \quad (14)$$

$$\frac{dD(\mathbf{b}, \tau(\mathbf{b}))}{db_e} = \frac{\partial D(\mathbf{b}, \tau(\mathbf{b}))}{\partial b_e} + \frac{\partial D(\mathbf{b}, \tau)}{\partial \tau} \Big|_{\tau=\tau(\mathbf{b})} \times \frac{\partial \tau(\mathbf{b})}{\partial b_e}. \quad (15)$$

When the tax changes associated with reemployment bonuses are large, the difference between the total derivatives and the partial derivatives becomes significant. However, in practice, this term is likely to be small due to the fact that reemployment bonuses are typically provided to a small fraction of the overall employed population. Following Chetty (2008) and Kolsrud et al. (2018), I ignore the difference between the partial and total impact of policy changes on expected unemployment duration. Nevertheless, it is worth examining the impact of ignoring the difference between the total derivatives and the partial derivatives. I use the fully calibrated model in Section 4 and find that using the partial derivatives leads to the overestimation of the welfare impact by two percent. Throughout this section, I use $\frac{\partial D}{\partial b_e}$ and $\frac{\partial D_B}{\partial b_e}$ as approximations for $\frac{dD}{db_e}$ and $\frac{dD_B}{db_e}$, respectively.

Remark 2. In this remaining part of the section, I use the lower limit outlined in Proposition 2 to obtain the minimum potential impact on welfare by reemployment bonuses. Notably, even with the lower bound, I find a substantial improvement in welfare as I show later. However, it is worth examining the extent of the disparity between the lower and upper bounds. To illustrate this, recognize that the only difference between these bounds comes from the difference between \underline{M}_{T_B} and \overline{M}_{T_B} . By computing their ratio, I obtain

$$\frac{\overline{M}_{T_B}}{\underline{M}_{T_B}} = \frac{U'(c_{u,T_B})}{U'(c_{u,1})}. \quad (16)$$

Table 1: Parameters for the Welfare Evaluation of the Marginal Change in b_e

Parameter	Description	Value
u	Fraction of periods being unemployed	0.054
D	Expected unemployment duration (weeks)	24.3
D_B	Expected UI-compensated unemployment duration (weeks)	15.8
η_{D_B, b_u}	Elasticity of D_B with respect to UI benefits	0.53

Note: D , D_B , and η_{D_B, b_u} are directly taken from [Chetty \(2008\)](#). The paper also reports $\sigma = \frac{T-D}{T} = 0.946$, which implies that $u = 1 - \sigma = 0.054$.

Table 2: Welfare Impact of the Marginal Increase in b_e

c_u/c_e	$\gamma = 1$	$\gamma = 2$	$\gamma = 3$
0.85	0.017	0.014	0.012
0.90	0.018	0.016	0.014
0.95	0.019	0.018	0.017

Note: This table reports the welfare impact of the marginal increase in reemployment bonuses b_e from zero. The first column reports the consumption ratio $c_{u, T_B}/c_e$ used in the evaluation. The second to the fourth columns report $\frac{\partial W(b)}{\partial b_e} / \frac{\partial V_1}{\partial w}$ under different values of CRRA parameters γ . The unit of measure is the marginal value of a permanent increase in wages.

Assuming a CRRA utility function with a risk aversion parameter of γ , this simplifies to

$$\frac{\bar{M}_{T_B}}{\underline{M}_{T_B}} = \left(\frac{c_{u,1}}{c_{u, T_B}} \right)^\gamma. \quad (17)$$

The right-hand side can be obtained by comparing the consumption level immediately after a job loss, $c_{u,1}$, and that of T_B weeks into unemployment—typically a 26-week period. [Ganong and Noel \(2019\)](#) document unemployed workers’ consumption trajectory on a monthly basis. They find a sharp decline in consumption following the onset of unemployment, which then keeps decreasing only gradually until the expiration of UI benefits. Consequently, $c_{u,1}$ is not much higher than c_{u, T_B} . Indeed, a comparison of consumption during the first month of UI benefit receipt and the final month, as illustrated in Figure 2 of [Ganong and Noel \(2019\)](#), suggests that $c_{u,1}$ is higher than c_{u, T_B} by approximately five percent. Given this consumption pattern, equation (17) implies that the upper boundary exceeds the lower one by a factor of $(1.05)^\gamma$. For a plausible parameter choice of $\gamma = 2$, for instance, the upper bound is approximately 10 percent higher than the lower bound.

3.2 Evaluating the Welfare Impact

Proposition 1 in the previous section gives the welfare impact of providing reemployment bonuses. I replace the response to reemployment bonuses with the response to UI benefits using Proposition 2, and evaluate it at $b_e = 0$. Then, I obtain a lower bound on the welfare impact of the provision of reemployment bonuses that can be evaluated by readily available reduced-form parameters.

Corollary 1. *Suppose that assumptions (A.1)-(A.3) are satisfied. Then the welfare impact of the marginal increase in reemployment bonuses b_e from zero is given by*

$$\frac{\partial W(\mathbf{b})}{\partial b_e} \bigg/ \frac{\partial V_1}{\partial w} \geq \frac{u}{1-u} \frac{D_B}{D} \underline{M}_{T_B} \eta_{D_B, b_u}, \quad \text{where} \quad \eta_{D_B, b_u} = \frac{dD_B}{db_u} \frac{b_u}{D_B} \text{ and } u = \frac{D}{T}. \quad (18)$$

Proof. See Appendix A.4. □

Note that η_{D_B, b_u} represents the elasticity of expected UI-compensated duration with respect to UI benefits, while u corresponds to the fraction of periods during which an individual is expected to be unemployed.

The evaluation of the formula requires the following five parameters: u , D , D_B , \underline{M}_{T_B} , and η_{D_B, b_u} . As for the parameters other than \underline{M}_{T_B} , I use the values reported in Chetty (2008), as summarized in Table 1. The remaining parameter to be determined is \underline{M}_{T_B} . Assuming a constant relative risk aversion (CRRA) utility function of the form $U(c) = \frac{c^{1-\gamma}}{1-\gamma}$, I obtain

$$\underline{M}_{T_B} = \left(\frac{c_{u, T_B}}{c_e} \right)^\gamma. \quad (19)$$

I can pin it down by comparing consumption without job loss with consumption of T_B weeks into unemployment. Again, I rely on Ganong and Noel (2019) to determine this consumption ratio. They document that consumption just before UI expiration is about 10 percent lower than consumption before job loss. Assuming that consumption would be constant if job loss does not happen. Then, $c_{u, T_B}/c_e \approx 0.9$.

In Table 2, I report the welfare impact of reemployment bonuses for various values for $c_{u, T_B}/c_e$ including the one corresponding to the estimate in Ganong and Noel (2019). I also choose a range of values for the CRRA parameter γ due to the lack of consensus in the literature regarding its precise value. The first column displays the consumption ratio ($c_{u, T_B}/c_e$) used in the evaluation. The second to fourth columns show the welfare gain measured in units of the marginal gain from a permanent increase in wages ($\frac{\partial V}{\partial w}$). The table reveals that the welfare impact increases with the consumption ratio (c_u/c_e) and decreases with the CRRA parameter (γ). This pattern arises because, with other parameters held constant, a larger consumption ratio or a lower CRRA parameter results

Table 3: MVPFs of the Marginal Increase in b_e

c_u/c_e	$\gamma = 1$	$\gamma = 2$	$\gamma = 3$
0.85	3.31	2.46	2.02
0.90	3.83	2.99	2.49
0.95	4.54	3.86	3.38

Note: This table presents the Marginal Value of Public Funds (MVPF) of the marginal increase in reemployment bonuses b_e from zero. The first column indicates the consumption ratio $c_{u,T_B}/c_e$ used in the evaluation. The second to fourth columns report the MVPFs under different values of CRRA parameter γ .

in a larger value of \underline{M}_{T_B} in equation (19). Consequently, this implies a larger labor supply response, as evident in equation (13).

Even in the most conservative case where $c_{u,T_B}/c_e = 0.85$ and $\gamma = 3$, the first dollar of reemployment bonuses yields a welfare impact equivalent to a permanent increase of 1.2 cents in weekly earnings. To aggregate this impact over a lifetime, I assume $T = 450$ based on the calculation $u = \frac{D}{T}$, where $u = 0.054$ and $D = 24.3$ from Table 1. Under this assumption, the welfare impact is equivalent to a $0.012 \times (450 - 24.3) = 5.1$ dollar increase in lifetime income per person.

3.3 Comparison to Historical Policy Changes in the U.S.

To facilitate a comparison of the finding above with the welfare effects of other existing government programs, I calculate the Marginal Value of Public Funds (MVPF) as introduced by [Hendren and Sprung-Keyser \(2020\)](#). The MVPF of a policy is defined as the aggregated willingness to pay for the policy divided by the net cost to the government.⁵ This notion provides a unified framework for assessing the impacts of government policies on social welfare. I keep making the same assumptions (A.1)-(A.3) as before. The willingness to pay for a \$1 increase in reemployment bonuses b_e is given by

$$WTP_e = T_B - D_B. \quad (20)$$

The net cost of this policy change is given by

$$\begin{aligned} Net\ Cost_e &= (T - D) \frac{\partial \tau(\mathbf{b})}{\partial b_e} \\ &= (T_B - D_B)(1 + FE_e), \end{aligned} \quad (21)$$

where

$$FE_e = \frac{1}{T_B - D_B} \left[\frac{dD_B}{db_e} (b_u - b_e) + \frac{dD}{db_e} \tau \right]. \quad (22)$$

⁵Since the model in this paper assumes no ex-ante heterogeneity, there is no distinction between the aggregated willingness to pay and that of an individual.

Here, FE_e represents the fiscal externality due to the behavioral response of unemployed people. To quantify the welfare impact of the first dollar of reemployment bonuses, evaluating FE_e at the point $b_e = 0$ yields

$$FE_e = \frac{u_B}{1 - u_B} \frac{dD_B}{db_e} \frac{b_u}{D_B} + \frac{u_B}{1 - u_B} \frac{u}{1 - u} \frac{dD}{db_e} \frac{b_u}{D}, \quad (23)$$

where $u_B = \frac{D_B}{T_B}$. Using Proposition 2 and the fact that the second term is positive, I get

$$FE_e \leq -\frac{u_B}{1 - u_B} M_{T_B} \eta_{D_B, b_u}. \quad (24)$$

Note that FE_e is negative, implying that the net cost is less than 1. The lower bound on the MVPF is given by

$$MVPF_e = \frac{WTP_e}{Net\ Cost_e} \geq \frac{1}{1 - \frac{u_B}{1 - u_B} M_{T_B} \eta_{D_B, b_u}}. \quad (25)$$

The last column of Table 3 shows that the MVPF of the proposed policy change exceeds two even in a conservative case where $c_{u, T_B}/c_e = 0.85$ and $\gamma = 3$. This result is remarkable as [Hendren and Sprung-Keyser \(2020\)](#) reports MVPFs of 133 historical policy changes in the U.S. and most policies targeting adults have MVPFs below two.

For comparison purposes, I also calculate the MVPF of unemployment insurance (UI) derived from my model. A detailed derivation can be found in Appendix A.5. The MVPF of the marginal increase in UI benefits b_u is approximately given by

$$MVPF_u \approx \frac{1 + \gamma \frac{c_e - c_u}{c_e}}{1 + \frac{1}{1 - u} \eta_{D_B, b_u}}. \quad (26)$$

This expression can be interpreted as follows: The willingness to pay for an additional dollar of UI benefits in the numerator depends on the relative difference between the marginal utility of consumption during unemployment and employment, which, in the case of CRRA utility, can be approximated by the consumption drop upon unemployment multiplied by the risk aversion parameter γ as shown in the numerator above. If consumption declines more significantly upon unemployment, individuals place a higher value on additional UI benefits. On the other hand, the net cost of an additional dollar of UI benefits depends on the moral hazard impact of UI, which can be captured by the elasticity of insured duration with respect to UI benefits.

Suppose I have $\gamma = 2.0$ and a consumption drop upon unemployment of 10 percent. Then, the MVPF of the marginal increase in UI benefits is approximately given by

$$MVPF_u \approx \frac{1 + 2 \times 0.1}{1 + \frac{1}{1 - 0.054} \times 0.053} \approx 0.77, \quad (27)$$

Table 4: Sensitivity of MVPF to η_{D_B, b_u}

Study	η_{D_B, b_u}	$\gamma = 1$	MVPF	
			$\gamma = 2$	$\gamma = 3$
Moffitt (1985)	0.36	2.01	1.82	1.68
Solon (1985)	0.10	1.16	1.14	1.13
Katz and Meyer (1990)	0.80	∞	∞	10.35
Meyer and Mok (2007)	0.12-0.60	1.2-6.12	1.18-4.95	1.16-3.10
Landais (2015)	0.29	1.68	1.57	1.49
Kroft and Notowidigdo (2016)	0.63	8.22	4.77	3.47
Card, Johnston, Leung, Mas and Pei (2015)	0.38-1.21	2.13- ∞	1.91- ∞	1.75- ∞

Note: This table shows the estimated elasticity of insured duration with respect to UI benefits for a collection of studies surveyed in Schmieder and Von Wachter (2016) and shows the MVPFs computed based on those elasticities.

which falls within the range of MVPFs of UI reported in Hendren and Sprung-Keyser (2020).

This observation highlights the inverse relationship between the large MVPFs of the marginal increase in reemployment bonuses reported in Table 3 and the low MVPF of the marginal increase in UI benefits above. The small MVPF of UI benefits is primarily driven by the significant moral hazard cost associated with UI, which outweighs the consumption smoothing gain. This substantial moral hazard cost arises from the large response of unemployment spells to UI benefits. As demonstrated in Proposition 2, this large labor supply response to UI generosity translates into a corresponding large labor supply response to reemployment bonuses to the extent that it is driven by the curvature of the search disutility function. Consequently, the government can achieve substantial reductions in UI spending by encouraging job search through reemployment bonuses, leading to a welfare gain through tax reductions.

3.4 Discussion

The baseline model analyzed so far is highly stylized, and it is important to acknowledge that the model may not capture some important realistic features. In this subsection, I provide a comprehensive discussion on the robustness of the analysis as well as its limitations.

Sensitivity to the elasticity parameter. One advantage of my approach, which connects the response of unemployment duration to reemployment bonuses and the response to UI benefits, is that I can utilize the extensive research on labor supply responses to UI benefits. In this section, I calculate the MVPFs for reemployment bonuses again, applying estimation results from several other studies.

Table 4 outlines the estimated elasticities from a collection of studies using U.S. data, reviewed in Schmieder and Von Wachter (2016). It also shows the MVPFs of reemployment bonuses determined using these elasticities. For studies like Solon (1985) with smaller estimated elasticities, the

MVPF ranges from 1.13-1.16 depending on the risk aversion parameter γ . While this is significantly smaller than the figures discussed earlier in this section, it still exceeds 1, suggesting that the policy provides welfare benefits greater than one dollar for each dollar of government expenditure. Conversely, for studies with larger estimated elasticities, the MVPF's denominator turns negative. In these cases, I define the MVPF as infinity, following [Hendren and Sprung-Keyser \(2020\)](#). An infinite MVPF indicates that the labor supply response to reemployment bonuses is so substantial that the significant reduction in UI benefit spending allows the reemployment bonus policy to fund itself.

State dependencies of marginal utility of consumption. In Proposition 2, the marginal utilities $U'(c_{u,t})$ and $U'(c_{e,t,t})$ play a crucial role in connecting the estimable quantity $\frac{\partial D_B}{\partial b_u}$ to what needs to be obtained $\frac{\partial D_B}{\partial b_e}$. So far, I have assumed that the marginal utilities of consumption do not directly depend on employment status as commonly assumed. However, they might depend on employment status for a few reasons. For instance, if consumption and leisure are not separable, the true marginal rate of substitution should deviate from what I have used in Proposition 2. Let $U_u(c)$ denote utility from consumption while unemployed and $U_e(c)$ denote utility from consumption while employed. [Ziliak and Kniesner \(2005\)](#) estimate a utility function in which consumption and leisure are not separable, and find that consumption and leisure are direct substitutes. This implies that the marginal utility of consumption is higher during periods of employment, i.e., $U'_u(c) < U'_e(c)$. Importantly, under this condition, Proposition 2 provides a conservative estimate of the lower bound since I have $\frac{U'_u(c_{e,t,t})}{U'_u(c_{u,t})} < \frac{U'_e(c_{e,t,t})}{U'_u(c_{u,t})}$, which in turn leads to a conservative estimate of the welfare impact of reemployment bonuses.

Another possibility is that unemployed individuals have more time to devote to shopping and home production, allowing them to achieve the same level of utility with a lower level of *expenditure*, as discussed by [\(Aguiar and Hurst, 2007\)](#).⁶ For example, suppose a person is busy while employed and often dines out to save time. If this person becomes unemployed, they have more free time and can spend it on cooking to save money. Let c represent expenditure and \tilde{c} represent consumption (as the output of time and expenditure). It is likely that $\frac{c_e}{c_u} > \frac{\tilde{c}_e}{\tilde{c}_u}$. This implies that the marginal rate of substitution between *consumption* while employed and while unemployed would be greater than the marginal rate of substitution between *expenditure* while employed and while unemployed, which is used in the proposition. Once again, this leads to a conservative estimate of the lower bound for the response of unemployment duration, which in turn leads to a conservative estimate of the welfare impact of reemployment bonuses.

⁶Here, consumption and expenditure are distinct concepts. Consumption is considered to be the output produced by utilizing time and market goods (expenditure) as inputs. See [Becker \(1965\)](#) and [Aguiar and Hurst \(2005\)](#).

Heterogeneity. While the model presented in this section does not assume heterogeneity among unemployed individuals, unemployed people in reality would exhibit heterogeneity, particularly in terms of their liquidity, as discussed by (Chetty, 2008). However, incorporating heterogeneity into the model does not affect the formulation of the formula. By redefining welfare as $W(\mathbf{b}) = \int V_1(A_1(\omega), \omega; b, \tau(\mathbf{b})) dF(\omega)$, where $V_1(A_1(\omega), \omega; \mathbf{b}, \tau(\mathbf{b}))$ represents the value of an individual and $F(\omega)$ denotes the distribution of individuals, the resulting formula remains the same as equation (8), except that the marginal utilities need to be integrated with respect to $F(\omega)$. A detailed derivation of the formula in the presence of heterogeneity is in Appendix B.1.

Uncertainty in wage offers. In many studies that analyze the job search behavior of unemployed individuals, it is commonly assumed that stochastic wage offers are drawn from a distribution, as discussed by (McCall, 1970). While incorporating this assumption introduces a reservation wage (R_t) as an additional choice variable in the model, the envelope theorem suggests that the response of reservation wages to reemployment bonuses does not have a first-order impact on individual values. Furthermore, the effect of the response of reservation wages on the government budget is captured by $\frac{dD}{db_e}$ in equation (8). Consequently, the presence of uncertainty in wage offers does not alter the welfare formula. A more rigorous treatment of this issue is in Appendix B.2.

Ex-ante savings response. The preceding analysis has focused on the problem that arises after individuals experience a job loss, disregarding the possibility that individuals may respond to policy changes even before losing their jobs. For instance, a more generous unemployment insurance (UI) policy could lead to reduced precautionary savings, as discussed by Engen et al. (Engen and Gruber, 2001). However, given that the policy change is marginal, the ex-ante response does not have an impact on the analysis presented in this section due to the envelope condition. Although changes in reemployment bonuses (b_e) may influence pre-job loss asset choices, what is crucial for the welfare calculation is the direct impact of reemployment bonuses (b_e) on utility and the externality through the government budget constraint. Other effects resulting from individual choices cancel out due to the first-order conditions of the agent's optimization problem.

Additional fiscal externalities. In the context of UI, fiscal externalities stem from heightened expenditure on UI benefits and a contraction in tax revenue due to extended unemployment durations caused by worker moral hazard. In my model, I assume that all the taxes derived from the employed workers are spent on UI benefits for unemployed individuals. However, in reality, the government uses taxes collected from employed workers for other programs, such as Social Security and Medicare. Consequently, the reduction in tax revenue provoked by UI-induced extended unemployment results in additional welfare costs (Lawson, 2017). The same argument suggests

Table 5: List of Parameters

Parameter	Description	Value	Target
Externally set			
γ	Coefficient of relative risk aversion	2.0	Michelacci and Ruffo (2015)
r	Interest rate	0	
β	Discount factor	1	
A_1	Initial asset (relative to weekly wage)	5.16	Median asset in the SIPP (Chetty, 2008)
T	Time length of the model (weeks)	450	Unemployment rate of 5.4% (Chetty, 2008)
L	Liquidity constraint	0.0	
Internally estimated			
θ	Utility cost of search: weight	378.6	Avg. unemployment duration of 24.3 weeks
ξ	Utility cost of search: convexity	0.020	Elasticity of duration w.r.t. UI of 0.53
\bar{y}	Nonlabor income	0.512	Consumption loss upon job loss of 10%

that, when accounting for such additional fiscal externalities, reemployment bonuses could generate a larger welfare gain by facilitating the government's collection of taxes for other programs.

4 Optimal Policy in the Calibrated Economy

Based on the sufficient statistic approach, the analysis in the previous section shows the potential for welfare improvement in the current UI system. Given the large welfare gain from the first dollar of reemployment bonuses, it would be natural to ask what is the globally optimal reemployment bonuses and how UI benefits should be adjusted to reemployment bonuses. By fully calibrating the model, I numerically solve for the optimal combination of UI benefits and reemployment bonuses that maximizes welfare.

4.1 Quantitative Specification

I specify the utility from consumption $U(c)$ and the disutility from job search $\psi(e)$ as

$$U(c) = \frac{c^{1-\gamma}}{1-\gamma}, \quad \psi(e) = \theta \frac{e^{1+\xi}}{1+\xi}, \quad (28)$$

where γ represents the coefficient of relative risk aversion, θ is the weight on the utility cost of job search, and ξ is the parameter governing the convexity of the utility cost of job search.

I use $\gamma = 2.0$ for the coefficient of relative risk aversion, which is a standard value in the literature (e.g. [Michelacci and Ruffo 2015](#)). As before, I keep assuming $r = 0$ and $\beta = 1$. I normalize wages to be 1. I set the initial asset A_1 to the median asset in the Survey of Income

Table 6: Comparison of Baseline Economy with Economy under Optimal Policy

	Baseline	Optimal UI	Optimal Joint
Unemployment rate (%)	5.38	2.94	3.41
Consumption drop (%)	10.03	27.76	14.18
UI spending	8.69	2.23	5.17
RB spending	0.00	0.00	8.61
Welfare gain (%)	0.00	0.25	0.39
Policy parameters:			
UI benefit	0.50	0.18	0.49
Reemployment bonus	0.00	0.00	0.56

Note: UI refers to unemployment insurance. RB refers to reemployment bonuses. Welfare gain is measured in a welfare-equivalent increase in consumption.

and Program Participation (SIPP) reported by [Chetty \(2008\)](#).⁷ Time length of the model is set to $T = 450$ weeks so that the unemployment rate in the model $u = \frac{D}{T}$ is 5.4% where $D = 24.3$ is targeted in the estimation. The borrowing limit is set to $L = 0$. UI benefits and reemployment bonuses in the baseline are set to $b_u = 0.5$ and $b_e = 0$. Since wages are normalized to 1, $b_u = 0.5$ represents the replacement rate of 50%.

The remaining parameters (θ, ξ, \bar{y}) are determined by matching several data moments. The weight on job search disutility θ directly influences the amount of effort an unemployed worker puts forth. I target the average unemployment duration $D = 24.3$ to pin down θ . The curvature ξ is informed by the responsiveness of a worker's job search effort to a change in the relative value of employment versus unemployment. In particular, I determine ξ by targeting the elasticity of compensated unemployment duration with respect to UI benefits $\eta_{D_B, b_u} = 0.53$. Lastly, nonlabor income \bar{y} affects consumption decline upon a job loss. I determine \bar{y} by targeting a 10 percent consumption loss upon unemployment. Specifically, I calculate the consumption drop by $(c_{u, T_B} - c_e)/c_e$ where c_{u, T_B} is the consumption level of an unemployed worker after $T_B = 26$ weeks while c_e is the consumption level that realizes if a worker never loses a job.⁸ Table 5 summarizes all the parameters.

4.2 Optimal Joint Design of UI Benefits and Reemployment Bonuses

With the calibrated model, I numerically solve the following optimization problem.

$$\max_{b_u, b_e} W(\mathbf{b}) = V_1(A_1; \mathbf{b}, \tau(\mathbf{b})) \quad \text{where} \quad \tau(\mathbf{b}) = \frac{D_B b_u + (T_B - D_B) b_e}{T - D}. \quad (29)$$

The objective function is the value function in the initial period where the tax $\tau(\mathbf{b})$ satisfies the government budget constraint.

First, I discuss the case where the government can choose only UI benefits. The first column in Table 6 represents the baseline economy. The second column in the same table corresponds to the case where only b_u is chosen to maximize welfare and b_e is fixed at zero. The optimal UI benefit level in the calibrated economy is 18% of weekly wages. Although this value is lower than what many other papers suggest, it still falls within the range of existing estimates (e.g., Hansen and Imrohoroglu 1992, Gruber 1997). Consequently, the unemployment rate decreases from 5.38% in the baseline case to 2.94% in this counterfactual. The government spending on UI benefits goes down. Each unemployed worker receives UI benefits equivalent to 8.69 weeks of wages on average in the baseline, whereas, in the counterfactual economy, this number decreases to 2.23. At the expense of the lower spending on UI benefits, unemployed workers experience a much larger decline in consumption of 28% compared to 10% in the baseline. Overall, workers in the counterfactual economy experience a 0.25% increase in welfare in terms of consumption equivalence. In other words, workers would be indifferent between the baseline economy and the counterfactual economy if their consumption in the baseline economy increased by 0.25%.

The third column of the same table presents the outcomes in an economy where both b_u and b_e are optimally chosen. The optimal combination of UI benefits and reemployment bonuses is determined to be $(b_u, b_e) = (0.49, 0.56)$. This finding suggests that the baseline UI benefit level of 0.5 in the economy happens to be close to the optimal level when the government also provides reemployment bonuses equivalent to 56% of weekly wages. It is worth noting that the optimal policy sets b_u close to b_e , resulting in a situation where an unemployed worker receives almost the same amount of benefits regardless of whether the worker finds a job or not. This effectively addresses the moral hazard associated with the provision of UI benefits. In this counterfactual scenario, the unemployment rate decreases significantly to 3.41%, compared to the 5.38% observed in the baseline economy. Despite the low unemployment rate, the decline in consumption upon job loss is 14%, only slightly lower than the 10% experienced in the baseline economy. Welfare

⁷Using the SIPP, Chetty (2008) reports the median annual wage of unemployed people before job loss is \$17,780 and median liquid wealth is \$1,763. Since weekly wages are normalized to 1 in the model, I choose initial asset $A_1 = (\$17,780/52\text{weeks})/\$1,763 \approx 5.16$.

⁸Here, c_e is constant because $(1+r)\beta = 1$ and there is no uncertainty.

increases by 0.39%, suggesting that incorporating reemployment bonuses into the UI system has a quantitatively large impact on welfare.

5 Conclusion

This paper studies the welfare impact of reemployment bonuses as a way to address moral hazard inherent in the UI system. Using a dynamic model of consumption, saving, and job search, I derived a formula that quantifies the welfare impact of the first dollar of reemployment bonuses. By leveraging the existing estimates of the response of unemployment duration to changes in UI benefits, I evaluated the welfare formula and found that this initial one-dollar increase in reemployment bonuses leads to a welfare improvement equivalent to a lifetime income increase of \$5.1. When evaluating the welfare impact using the Marginal Value of Public Funds (MVPF), I found that this impact exceeds many historical policy changes documented in the work of [Hendren and Sprung-Keyser \(2020\)](#).

Additionally, by fully calibrating the model, I extended the analysis to examine non-marginal policy changes. I found that the current UI benefit level, amounting to 50 percent of wages, is nearly optimal when complemented by the provision of reemployment bonuses equivalent to 56 percent of wages. This combination effectively mitigates moral hazard while ensuring consumption smoothing.

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Online Appendix (Not for Publication)

Appendix A Proofs

A.1 Properties of Job Search Effort

Here, I discuss how unemployed workers respond to a change in UI benefits or reemployment bonuses through their search effort. The optimal level of search effort is determined by solving the following first-order condition

$$\psi'(e_t(A_t; \mathbf{b}, \tau)) = V_{t,t}^E(A_t; b_e, \tau) - V_t^U(A_t; \mathbf{b}, \tau). \quad (4)$$

For periods before UI expiration $t \leq T_B$, I have

$$\frac{\partial e_t}{\partial b_u} = \frac{-\frac{\partial V_t^U(A_t; \mathbf{b}, \tau)}{\partial b_u}}{\psi''(e_t)}, \quad (30)$$

$$\frac{\partial e_t}{\partial b_e} = \frac{\frac{\partial V_{t,t}^E(A_t; b_e, \tau)}{\partial b_e} - \frac{\partial V_t^U(A_t; \mathbf{b}, \tau)}{\partial b_e}}{\psi''(e_t)}. \quad (31)$$

The partial derivatives of the value functions are

$$\frac{\partial V_t^U(A_t; \mathbf{b}, \tau)}{\partial b_u} = U'(c_{u,t}) + \sum_{k=t+1}^{T_B} S_{k|t+1} U'(c_{u,k}), \quad (32)$$

$$\frac{\partial V_{t,t}^E(A_t; b_e, \tau)}{\partial b_e} = \sum_{j=t}^{T_B} U'(c_{e,t,j}), \quad (33)$$

$$\frac{\partial V_t^U(A_t; \mathbf{b}, \tau)}{\partial b_e} = e_{t+1} \frac{\partial V_{t+1,t+1}^E(A_{t+1}; b_e, \tau)}{\partial b_e} + (1 - e_{t+1}) \frac{\partial V_{t+1}^U(A_{t+1}; \mathbf{b}, \tau)}{\partial b_e} \quad (34)$$

where $c_{u,k}$ represents the consumption of unemployed individuals in period k , $c_{e,t,k}$ represents the consumption of employed individuals in period k who find a job in period t , and $S_{k|t+1} = \prod_{j=t+1}^k (1 - e_j)$ denotes the probability of remaining unemployed at the end of period k , given that the individual was unemployed at the beginning of period $t + 1$. None of these expressions depend on the worker's response in consumption (e.g. $\frac{\partial c_{u,t}}{\partial b_u}$) or in search effort (e.g. $\frac{\partial e_t}{\partial b_u}$) since the envelope theorem implies that they cancel out in first-order conditions.

The right-hand side of equation (30) is negative, implying that search effort is decreasing in UI benefits b_u . For search effort to be increasing in reemployment bonuses, I need to show $\frac{\partial V_{t,t}^E(A_t; b_e, \tau)}{\partial b_e} - \frac{\partial V_t^U(A_t; \mathbf{b}, \tau)}{\partial b_e} > 0$. I prove it below under an additional assumption that $c_{e,s,t} = c_e$ for

$s, t \leq T_B$. This assumption is reasonable as an approximation unless the worker is constrained by liquidity and experiences rapid wage growth after reemployment. Based on this, equation (31) implies that the partial derivative $\frac{\partial e_t}{\partial b_e}$ turns out to be positive, and hence search effort is expected to increase with higher reemployment bonuses b_e .

Now, I show that $\frac{\partial V_{t,t}^E(A_t; b_e, \tau)}{\partial b_e} - \frac{\partial V_t^U(A_t; \mathbf{b}, \tau)}{\partial b_e} > 0$. First, let $S_{K|k} = \prod_{j=k}^K (1 - e_j)$ denote the probability of staying unemployed at the end of period K conditional on being unemployed at the beginning of period k . For notational brevity, I suppress the dependence of the value functions on A_t, \mathbf{b} and τ below. Note that

$$\begin{aligned} \frac{\partial V_{t,t}^E}{\partial b_e} - \frac{\partial V_t^U}{\partial b_e} &= \frac{\partial V_{t,t}^E}{\partial b_e} - \left[e_{t+1} \frac{\partial V_{t+1,t+1}^E}{\partial b_e} + (1 - e_{t+1}) \frac{\partial V_{t+1}^U}{\partial b_e} \right] \\ &= \frac{\partial V_{t,t}^E}{\partial b_e} - \frac{\partial V_{t+1,t+1}^E}{\partial b_e} + (1 - e_{t+1}) \left[\frac{\partial V_{t+1,t+1}^E}{\partial b_e} - \frac{\partial V_{t+1}^U}{\partial b_e} \right], \end{aligned} \quad (35)$$

where I have

$$\frac{\partial V_{t,t}^E}{\partial b_e} = \sum_{j=t}^{T_B} U'(c_{e,t,j}) \quad (36)$$

due to the envelope theorem. Therefore, the first two terms in the second line of equation (35) are

$$\frac{\partial V_{t,t}^E}{\partial b_e} - \frac{\partial V_{t+1,t+1}^E(A_{t+1})}{\partial b_e} = U'(c_{e,t,t}) + \sum_{j=t+1}^{T_B} [U'(c_{e,t,j}) - U'(c_{e,t+1,j})]. \quad (37)$$

Now I impose an approximation assumption that $c_{e,s,t} = c_e$ for $s, t \leq T_B$. Then the expression reduces down to

$$\frac{\partial V_{t,t}^E}{\partial b_e} - \frac{\partial V_t^U}{\partial b_e} = U'(c_e) + \sum_{k=t+1}^{T_B} S_{k|t+1} U'(c_e), \quad (38)$$

which is positive since the marginal utility is always positive.

A.2 Proof of Proposition 1

Proof. Remember that the welfare function $W(\mathbf{b})$ is defined as $W(\mathbf{b}) = V_1(A_1; b, \tau(\mathbf{b}))$ given A_1 where $\tau(\mathbf{b})$ is the budget-balancing taxes. Differentiating this with respect to wage subsidies b_e yields

$$\frac{\partial W(\mathbf{b})}{\partial b_e} = \frac{\partial V_1}{\partial b_e} + \frac{\partial V_1}{\partial \tau} \frac{\partial \tau(\mathbf{b})}{\partial b_e}. \quad (39)$$

Exploiting the envelope conditions from individual's optimization problem, I have

$$\begin{aligned}
\frac{\partial V_1}{\partial b_e} &= e_1 \frac{\partial V_1^E}{\partial b_e} + (1 - e_1) \frac{\partial V_1^U}{\partial b_e} \\
&= e_1 \sum_{t=1}^{T_B} U'(c_{e,1,t}) + S_1 e_2 \sum_{t=2}^{T_B} U'(c_{e,2,t}) + \cdots + S_{T_B-1} e_{T_B} U'(c_{e,T_B,T_B}) \\
&= e_1 U'(c_{e,1,1}) + \sum_{t=1}^2 S_{t-1} e_t U'(c_{e,t,T_B}) + \cdots + \sum_{t=1}^{T_B} S_{t-1} e_t U'(c_{e,t,T_B}),
\end{aligned} \tag{40}$$

where $S_0 = 1$. Note that $\sum_{t=1}^j S_{t-1} e_t = 1 - S_j$. I obtain

$$\frac{\partial V_1}{\partial b_e} = \sum_{t=1}^{T_B} (1 - S_t) \mathbb{E}_s[U'(c_{e,s,t})], \tag{41}$$

where

$$\mathbb{E}_s[U'(c_{e,s,t})] = \sum_{s=1}^t \kappa_s U'(c_{e,s,t}) \quad \text{where} \quad \kappa_s = \frac{S_{s-1} e_s}{1 - S_t}. \tag{42}$$

Similarly, I obtain

$$\frac{\partial V_1}{\partial \tau} = - \sum_{t=1}^T (1 - S_t) \mathbb{E}_s[U'(c_{e,s,t})].$$

Recall that the government budget constraint is given by

$$(T - D)\tau(\mathbf{b}) = D_B b_u + (T_B - D_B) b_e. \tag{43}$$

Differentiating this with respect to b_e yields

$$(T - D) \frac{\partial \tau(\mathbf{b})}{\partial b_e} - \frac{dD}{db_e} \tau(\mathbf{b}) = T_B - D_B + \frac{dD_B}{db_e} (b_u - b_e). \tag{44}$$

Arranging terms, I obtain

$$\frac{\partial \tau(\mathbf{b})}{\partial b_e} = \frac{T_B - D_B}{T - D} \left[1 + \frac{dD_B}{db_e} \frac{b_u - b_e}{T_B - D_B} + \frac{dD}{db_e} \frac{\tau(\mathbf{b})}{T_B - D_B} \right]. \tag{45}$$

To get a money metric of the welfare impact of wage subsidies, I normalize $\frac{\partial W(\mathbf{b})}{\partial b_e}$ by the welfare gain from permanently increasing wages by \$1, i.e., $\frac{\partial V_1}{\partial w}$. Note that $\frac{\partial V_1}{\partial w} = -\frac{\partial V_1}{\partial \tau}$. Then, I

have

$$\begin{aligned} \frac{\partial W(\mathbf{b})}{\partial b_e} \bigg/ \frac{\partial V_1}{\partial w} &= \frac{\frac{\partial V_1}{\partial b_e}}{-\frac{\partial V_1}{\partial \tau}} - \frac{\partial \tau(\mathbf{b})}{\partial b_e} \\ &= \frac{T_B - D_B}{T - D} \left[\frac{MU_{e,T_B} - MU_{e,T}}{MU_{e,T}} - \frac{dD_B}{db_e} \frac{b_u - b_e}{T_B - D_B} - \frac{dD}{db_e} \frac{\tau(\mathbf{b})}{T_B - D_B} \right], \end{aligned} \quad (46)$$

where $MU_{e,t}$ is given by

$$MU_{e,t} = \sum_{k=1}^t \frac{1 - S_k}{t - D_B} \mathbb{E}_s[U'(c_{e,s,k})] \quad \text{for } t = T_B, T. \quad (47)$$

□

A.3 Proof of Proposition 2

Proof. Let $t \leq T_B$. In Appendix A.1, I obtained

$$\frac{\partial e_t}{\partial b_u} = \frac{-\frac{\partial V_t^U}{\partial b_u}}{\psi''(e_t)}, \quad (30)$$

$$\frac{\partial e_t}{\partial b_e} = \frac{\frac{\partial V_{t,t}^E}{\partial b_e} - \frac{\partial V_t^U}{\partial b_e}}{\psi''(e_t)}. \quad (31)$$

and

$$\frac{\partial V_t^U}{\partial b_u} = U'(c_{u,t}) + \sum_{k=t+1}^{T_B} S_{k|t+1} U'(c_{u,k}), \quad (32)$$

$$\frac{\partial V_{t,t}^E}{\partial b_e} - \frac{\partial V_t^U}{\partial b_e} = U'(c_e) + \sum_{k=t+1}^{T_B} S_{k|t+1} U'(c_e). \quad (38)$$

Now I define

$$\mu_{u,t} = U'(c_{u,t}) + \sum_{k=t+1}^{T_B} S_{k|t+1} U'(c_{u,k}), \quad (48)$$

$$\mu_{e,t} = U'(c_e) + \sum_{k=t+1}^{T_B} S_{k|t+1} U'(c_e). \quad (49)$$

Then the first-order condition for job search effort can be written as

$$\frac{\partial e_t}{\partial b_e} = -\frac{\mu_{e,t}}{\mu_{u,t}} \frac{\partial e_t}{\partial b_u}. \quad (50)$$

This can be rewritten as

$$\frac{\partial(1-e_t)}{\partial b_e} = -\frac{\mu_{e,t}}{\mu_{u,t}} \frac{\partial(1-e_t)}{\partial b_u}. \quad (51)$$

First, I calculate $\frac{\partial S_t}{\partial b_e}$. Remember that $S_t = \prod_{j=1}^t (1-e_j)$. Using the equation above, I have

$$\begin{aligned} \frac{\partial S_t}{\partial b_e} &= \frac{\partial}{\partial b_e} \prod_{j=1}^t (1-e_j) \\ &= \sum_{k=1}^t \frac{\partial(1-e_k)}{\partial b_e} \prod_{j \neq k} (1-e_j) \\ &= -\sum_{k=1}^t \frac{\mu_{e,k}}{\mu_{u,k}} \frac{\partial(1-e_k)}{\partial b_u} \prod_{\tilde{i} \neq k} (1-e_{\tilde{i}}), \end{aligned} \quad (52)$$

where the last equality comes from equation (51). Recall that compensated unemployment duration D_B is defined as $D_B = \sum_{t=1}^{T_B} S_t$. Therefore, I have

$$\begin{aligned} \frac{\partial D_B}{\partial b_e} &= \sum_{t=1}^{T_B} \frac{\partial S_t}{\partial b_e} \\ &= -\sum_{t=1}^{T_B} \left[\sum_{k=1}^t \frac{\mu_{e,k}}{\mu_{u,k}} \frac{\partial(1-e_k)}{\partial b_u} \prod_{\tilde{i} \neq k} (1-e_{\tilde{i}}) \right]. \end{aligned} \quad (53)$$

Now, I compute a bound on $\frac{\mu_{e,t}}{\mu_{u,t}}$. Using assumption (A.3), i.e., $c_{u,t} \leq c_{u,t-1}$, I obtain

$$\begin{aligned} \frac{\mu_{e,t}}{\mu_{u,t}} &= \frac{U'(c_e) + \sum_{k=t+1}^{T_B} S_{k|t+1} U'(c_e)}{U'(c_{u,t}) + \sum_{k=t+1}^{T_B} S_{k|t+1} U'(c_{u,k})} \\ &\geq \frac{[1 + \sum_{k=t+1}^{T_B} S_{k|t+1}] U'(c_e)}{[1 + \sum_{k=t+1}^{T_B} S_{k|t+1}] U'(c_{u,T_B})} \\ &= \frac{U'(c_e)}{U'(c_{u,T_B})}. \end{aligned} \quad (54)$$

Using the assumptions (A.2) $c_{u,t} \leq c_e$ and (A.3) $c_{u,t} \geq c_{u,t+1}$, I also have

$$\begin{aligned} \frac{\mu_{e,t}}{\mu_{u,t}} &= \frac{U'(c_e) + \sum_{k=t+1}^{T_B} S_{k|t+1} U'(c_e)}{U'(c_{u,t}) + \sum_{k=t+1}^{T_B} S_{k|t+1} U'(c_{u,k})} \\ &\leq \frac{U'(c_e)}{U'(c_{u,t})} \\ &\leq \frac{U'(c_e)}{U'(c_{u,1})}. \end{aligned} \quad (55)$$

Define

$$\overline{M}_{T_B} = \frac{U'(c_e)}{U'(c_{u,1})} \quad \underline{M}_{T_B} = \frac{U'(c_e)}{U'(c_{u,T_B})}. \quad (56)$$

Then, I obtain

$$\begin{aligned} -\frac{\partial D_B}{\partial b_e} &= \sum_{t=1}^{T_B} \left[\sum_{k=1}^t \frac{\mu_{e,k}}{\mu_{u,k}} \frac{\partial(1-e_k)}{\partial b_u} \prod_{\tilde{i} \neq k} (1-e_j) \right] \\ &\leq \sum_{t=1}^{T_B} \left[\sum_{k=1}^t \overline{M}_{T_B} \frac{\partial(1-e_k)}{\partial b_u} \prod_{\tilde{i} \neq k} (1-e_j) \right] \\ &= \overline{M}_{T_B} \sum_{t=1}^{T_B} \left[\sum_{k=1}^t \frac{\partial(1-e_k)}{\partial b_u} \prod_{\tilde{i} \neq k} (1-e_j) \right] \\ &= \overline{M}_{T_B} \sum_{t=1}^{T_B} \frac{\partial S_t}{\partial b_u} \\ &= \overline{M}_{T_B} \frac{\partial D_B}{\partial b_u}. \end{aligned} \quad (57)$$

In the same way, I can show that

$$-\frac{\partial D_B}{\partial b_e} \geq \underline{M}_{T_B} \frac{\partial D_B}{\partial b_u}. \quad (58)$$

Combining these, I obtain

$$\underline{M}_{T_B} \frac{\partial D_B}{\partial b_u} \leq -\frac{\partial D_B}{\partial b_e} \leq \overline{M}_{T_B} \frac{\partial D_B}{\partial b_u}. \quad (59)$$

□

A.4 Proof of Corollary 1

Proof. From Appendix A.2, remember that

$$\frac{\partial W(\mathbf{b})}{\partial b_e} \bigg/ \frac{\partial V_1}{\partial w} = \frac{T_B - D_B}{T - D} \left[\frac{MU_{e,T_B} - MU_{e,T}}{MU_{e,T}} - \frac{dD_B}{db_e} \frac{b_u - b_e}{T_B - D_B} - \frac{dD}{db_e} \frac{\tau(\mathbf{b})}{T_B - D_B} \right]. \quad (60)$$

Evaluating this at $b_e = 0$ yields

$$\frac{\partial W(\mathbf{b})}{\partial b_e} \bigg/ \frac{\partial V_1}{\partial w} = \frac{T_B - D_B}{T - D} \left[\frac{MU_{e,T_B} - MU_{e,T}}{MU_{e,T}} - \frac{dD_B}{db_e} \frac{b_u}{T_B - D_B} - \frac{dD}{db_e} \frac{D_B b_u}{(T_B - D_B)^2} \right]. \quad (61)$$

Assumption (A.1) implies $MU_{e,T_B} = MU_{e,T}$, so the first term in the bracket disappears. Using Proposition 2, which requires assumptions (A.1)-(A.3), I obtain

$$\begin{aligned} \frac{\partial W(\mathbf{b})}{\partial b_e} \bigg/ \frac{\partial V_1}{\partial w} &= -\frac{T_B - D_B}{T - D} \left[\frac{dD_B}{db_e} \frac{b_u}{T_B - D_B} + \frac{dD}{db_e} \frac{D_B b_u}{(T_B - D_B)^2} \right] \\ &\geq \frac{T_B - D_B}{T - D} \left[\frac{dD_B}{db_u} \frac{b_u}{D_B} \frac{D_B}{T_B - D_B} \underline{M}_{T_B} + \frac{dD}{db_u} \frac{b_u}{D} \frac{D_B D}{(T_B - D_B)^2} \underline{M}_T \right] \\ &= \frac{T_B - D_B}{T - D} \left[\eta_{D_B, b_u} \frac{D_B}{T_B - D_B} \underline{M}_{T_B} + \eta_{D, b_u} \frac{D_B D}{(T_B - D_B)^2} \underline{M}_T \right]. \end{aligned} \quad (62)$$

Since $\underline{M}_T = U'(c_e)/U'(c_{u,T}) \geq 0$ and $\eta_{D, b_u} \geq 0$, arranging terms yields

$$\frac{\partial W(\mathbf{b})}{\partial b_e} \bigg/ \frac{\partial V_1}{\partial w} \geq \frac{u}{1-u} \frac{D_B}{D} \underline{M}_{T_B} \eta_{D_B, b_u}, \quad (63)$$

where $u = \frac{D}{T}$ is the fraction of periods during which a person is expected to be unemployed. \square

A.5 Derivation of MVPF of the Marginal Increase in UI Benefits

The willingness to pay for a marginal increase in UI benefits b_u in terms of dollars during employment is given by

$$\begin{aligned} WTP &= \frac{\partial V_1}{\partial b_u} \bigg/ \frac{\partial V_1}{\partial w} \\ &= D_B \frac{MU_{u,T_B} - MU_{e,T}}{MU_{e,T}}, \end{aligned} \quad (64)$$

where MU_{u,T_B} and $MU_{e,T}$ are the marginal utilities of consumption averaged over time:

$$MU_{u,T_B} = \sum_{t=1}^{T_B} \frac{S_t}{D_B} U'(c_{u,t}), \quad MU_{e,T} = \sum_{t=1}^T \frac{1 - S_t}{T - D_B} \mathbb{E}_s[U'(c_{e,s,t})]. \quad (65)$$

Since it is difficult to track individual-level consumption at a week/month frequency over time, many papers just assume that $c_{u,t}$ and $c_{e,s,t}$ do not depend on t or s (Chetty 2009, Hendren and Sprung-Keyser 2020). Rigorously computing the willingness to pay for UI is beyond the scope of paper, and I simply let $c_{u,t} = c_u$ and $c_{e,s,t} = c_e$. Assuming CRRA utility $U(c) = \frac{c^{1-\gamma}}{1-\gamma}$, I obtain

$$WTP = D_B \frac{c_u^{-\gamma} - c_e^{-\gamma}}{c_e^{-\gamma}} \approx D_B \left(1 + \gamma \frac{c_e - c_u}{c_e} \right), \quad (66)$$

where I take the first-order approximation with respect to c_e around c_u .

The net cost of a marginal increase in UI benefits b_u is given by

$$\begin{aligned} Net\ Cost &= (T - D) \frac{\partial \tau(\mathbf{b})}{\partial b_u} \\ &= D_B (1 + FE_u), \end{aligned} \quad (67)$$

where $FE_u = \frac{1}{D_B} \left[\frac{dD_B}{db_u} (b_u - b_e) + \frac{dD}{db_e} \tau \right]$ represents the fiscal externality due to the behavioral response of unemployment people. Evaluating FE_u at the point $b_e = 0$ yields

$$\begin{aligned} FE_u &= \frac{1}{D_B} \left[\frac{dD_B}{db_u} b_u + \frac{dD}{db_u} \tau \right] \\ &= \eta_{D_B, b_u} + \eta_{D, b_u} \frac{u}{1-u}. \end{aligned} \quad (68)$$

Following Chetty (2008), I assume that $\eta_{D_B, b_u} = \eta_{D, b_u}$. Then, I obtain $FE_u = \frac{1}{1-u} \eta_{D_B, b_u}$. Combining these, I obtain

$$MVPF \approx \frac{1 + \gamma \frac{c_e - c_u}{c_e}}{1 + \frac{1}{1-u} \eta_{D_B, b_u}}. \quad (69)$$

Appendix B Extensions

B.1 Heterogeneity

The model in the main text assumes homogeneous individuals. In this subsection, I assume that individuals are heterogeneous in many respects including utility functions, income processes, initial assets, and liquidity constraints. I show that the welfare formula is almost unchanged in the presence of heterogeneity although additional conditions are required.

I begin by rewriting individual problems that account for individual heterogeneity. I assume that individuals are heterogeneous and each individual is indexed by $\theta \in \Theta$. If individual θ is

employed at a period t with asset A_t , the value function is given by

$$V_{s,t}^E(A_t, \theta) = \max_{A_{t+1} \geq L(\theta)} U(A_t - A_{t+1} + y_{e,s,t}(\theta); \theta) + V_{s,t+1}^E(A_{t+1}, \theta), \quad (70)$$

where the utility function U directly depends on θ . The liquidity constraint L and income y also depend on θ . More precisely, income is given by

$$y_{e,s,t}(\theta) = \begin{cases} w_{e,s,t}(\theta) + b_e & \text{if } t \leq T_B, \\ w_{e,s,t}(\theta) & \text{if } t > T_B, \end{cases} \quad (71)$$

where $w_{e,s,t}(\theta)$ is non-stochastic earnings for individual θ .

If individual θ with asset A_t does not find a job at the beginning of a period t , the value function is given by

$$V_t^U(A_t, \theta) = \max_{A_{t+1} \geq L(\theta)} U(A_t - A_{t+1} + y_{u,t}(\theta); \theta) + V_{t+1}(A_{t+1}, \theta), \quad (72)$$

where income is given by

$$y_{u,t}(\theta) = \begin{cases} y_{u,t}(\theta) + b_e & \text{if } t \leq T_B, \\ y_{u,t}(\theta) & \text{if } t > T_B, \end{cases} \quad (73)$$

where $y_{u,t}(\theta)$ is non-stochastic non-labor income for individual θ . The value function of unemployed individual θ with asset A_t at the beginning of each period before searching for a job is given by

$$V_t(A_t, \theta) = \max_{e_t \in [0,1]} e_t V_{t,t}^E(A_t, \theta) + (1 - e_t) V_t^U(A_t, \theta) - \psi(e_t; \theta), \quad (74)$$

where the disutility of job search ψ directly depends on θ . Let $e_t(\theta)$ be the search effort of individual θ at time t . I define a survival probability, expected unemployed duration, and expected insured duration for each individual as follows:

$$S_t(\theta) = \prod_{s=1}^t (1 - e_s(\theta)), \quad (75)$$

$$D(\theta) = \sum_{t=1}^T S_t(\theta), \quad (76)$$

$$D_B(\theta) = \sum_{t=1}^{T_B} S_t(\theta). \quad (77)$$

The government budget constraint is given by

$$(T - \bar{D})\tau = \bar{D}_B b_u + (T_B - \bar{D}_B) b_e, \quad (78)$$

where

$$\bar{D} = \int_{\theta \in \Theta} D(\theta) dF(\theta), \quad (79)$$

$$\bar{D}_B = \int_{\theta \in \Theta} D_B(\theta) dF(\theta). \quad (80)$$

Let $\tau(\mathbf{b})$ be the tax as a function of UI benefits and wage subsidies b implied by the budget constraint above. I define the welfare function $W(\mathbf{b})$ as

$$W(\mathbf{b}) = \int_{\theta \in \Theta} V_1(A_1(\theta), \theta; b, \tau(\mathbf{b})) dF(\theta), \quad (81)$$

where F is the distribution of θ in the population and $A_1(\theta)$ is the initial asset exogenously given to individual θ . Here I make the value function explicitly depend on the government policy (b, τ) . My objective here is to characterize $\frac{\partial W(\mathbf{b})}{\partial b_e}$.

Differentiating the welfare function with respect to b_e yields

$$\frac{\partial W(\mathbf{b})}{\partial b_e} = \int_{\theta \in \Theta} \left[\frac{\partial V_1(A_1(\theta), \theta; b, \tau)}{\partial b_e} + \frac{\partial V_1(A_1(\theta), \theta; b, \tau)}{\partial \tau} \frac{\partial \tau(\mathbf{b})}{\partial b_e} \right] dF(\theta). \quad (82)$$

The same calculation as in the proof of Proposition 1 implies

$$\frac{\partial V_1(A_1(\theta), \theta; b, \tau)}{\partial b_e} = \sum_{t=1}^{T_B} (1 - S_t(\theta)) \mathbb{E}_{s, \theta} [U'(c_{e,s,t}(\theta); \theta)], \quad (83)$$

$$\frac{\partial V_1(A_1(\theta), \theta; b, \tau)}{\partial \tau} = - \sum_{t=1}^T (1 - S_t(\theta)) \mathbb{E}_{s, \theta} [U'(c_{e,s,t}(\theta); \theta)], \quad (84)$$

where

$$\mathbb{E}_{s, \theta} [U'(c_{e,s,t}(\theta); \theta)] = \sum_{s=1}^t \frac{S_{s-1}(\theta) e_s(\theta)}{1 - S_t(\theta)} U'(c_{e,s,t}(\theta); \theta). \quad (85)$$

The budgetary impact of wage subsidies is given by

$$\frac{\partial \tau(\mathbf{b})}{\partial b_e} = \frac{T_B - \bar{D}_B}{T - \bar{D}} \left[1 + \frac{d\bar{D}_B}{db_e} \frac{b_u - b_e}{T_B - \bar{D}_B} + \frac{d\bar{D}}{db_e} \frac{\tau(\mathbf{b})}{T_B - \bar{D}_B} \right]. \quad (86)$$

To get a money metric of the welfare impact of wage subsidies, I normalize $\frac{\partial W(\mathbf{b})}{\partial b_e}$ by the average welfare gain from permanently increasing wages by \$1, i.e., $\int \frac{\partial V_1}{\partial w} dF(\theta)$. Note that $\frac{\partial V_1}{\partial w} =$

$-\frac{\partial V_1}{\partial \tau}$. Then, I have

$$\begin{aligned} \frac{\frac{\partial W(\mathbf{b})}{\partial b_e}}{\int_{\theta \in \Theta} \frac{\partial V_1}{\partial w} dF(\theta)} &= \frac{\int_{\theta \in \Theta} \frac{\partial V_1(A_1(\theta), \theta; b, \tau)}{\partial b_e} dF(\theta)}{-\int_{\theta \in \Theta} \frac{\partial V_1(A_1(\theta), \theta; b, \tau)}{\partial \tau} dF(\theta)} - \frac{\partial \tau(\mathbf{b})}{\partial b_e} \\ &= \frac{T_B - \bar{D}_B}{T - \bar{D}} \left[\frac{\overline{MU}_{e, T_B} - \overline{MU}_{e, T}}{\overline{MU}_{e, T}} - \frac{d\bar{D}_B}{db_e} \frac{b_u - b_e}{T_B - \bar{D}_B} - \frac{d\bar{D}}{db_e} \frac{\tau(\mathbf{b})}{T_B - \bar{D}_B} \right], \end{aligned} \quad (87)$$

where $\overline{MU}_{e, t}$ is given by

$$\overline{MU}_{e, t} = \int_{\theta \in \Theta} \sum_{k=1}^t \frac{1 - S_k(\theta)}{t - \bar{D}_B} \mathbb{E}_{s, \theta} [U'(c_{e, s, k}(\theta); \theta)] dF(\theta) \quad \text{for } t = T_B, T. \quad (88)$$

How is this formula in the presence of heterogeneity different from the formula (8) that is derived under the assumption that individuals are homogeneous? One difference is that the average marginal utility $MU_{e, t}$ in equation (8) is now replaced by $\overline{MU}_{e, t}$ which is $MU_{e, t}$ averaged over individuals. Another difference is that the expected unemployment duration D and the expected insured duration D_B are also replaced by the ones averaged over individuals \bar{D} and \bar{D}_B .

Now I evaluate the formula at $b_e = 0$, and in addition, I impose the assumption (A.1). Then, I obtain

$$\frac{\frac{\partial W(\mathbf{b})}{\partial b_e}}{\int_{\theta \in \Theta} \frac{\partial V_1}{\partial w} dF(\theta)} = -\frac{T_B - \bar{D}_B}{T - \bar{D}} \left[\frac{d\bar{D}_B}{db_e} \frac{b_u}{T_B - \bar{D}_B} + \frac{d\bar{D}}{db_e} \frac{\bar{D}_B b_u}{(T_B - \bar{D}_B)^2} \right]. \quad (89)$$

Proposition 2 cannot be directly applied to \bar{D}_B . Instead, I have

$$\frac{\partial \bar{D}_B}{\partial b_e} = \int_{\theta \in \Theta} \frac{\partial D_B(\theta)}{\partial b_e} dF(\theta), \quad (90)$$

which implies

$$\int_{\theta \in \Theta} \underline{M}_{T_B}(\theta) \frac{\partial D_B(\theta)}{\partial b_u} dF(\theta) \leq -\frac{\partial \bar{D}_B}{\partial b_e} \leq \int_{\theta \in \Theta} \bar{M}_{T_B}(\theta) \frac{\partial D_B(\theta)}{\partial b_u} dF(\theta), \quad (91)$$

where

$$\bar{M}_{T_B}(\theta) = \frac{U'(c_e(\theta); \theta)}{U'(c_{u, 1}(\theta); \theta)}, \quad \underline{M}_{T_B}(\theta) = \frac{U'(c_e(\theta); \theta)}{U'(c_{u, T_B}(\theta); \theta)}. \quad (92)$$

If the heterogeneity in the population is such that $\underline{M}_{T_B}(\theta)$ and $\bar{M}_{T_B}(\theta)$ are independent of $\frac{\partial D_B(\theta)}{\partial b_u}$, then the inequality simplifies to

$$\int_{\theta \in \Theta} \underline{M}_{T_B}(\theta) dF(\theta) \frac{\partial \bar{D}_B(\theta)}{\partial b_u} \leq -\frac{\partial \bar{D}_B}{\partial b_e} \leq \int_{\theta \in \Theta} \bar{M}_{T_B}(\theta) dF(\theta) \frac{\partial \bar{D}_B(\theta)}{\partial b_u}. \quad (93)$$

As in Corollary 1, let $\underline{M}_T = 0$. Then, arranging terms yields

$$\frac{\frac{\partial W(\mathbf{b})}{\partial b_e}}{\int_{\theta \in \Theta} \frac{\partial V_1}{\partial w} dF(\theta)} \geq \frac{u}{1-u} \frac{\bar{D}_B}{\bar{D}} \eta_{\bar{D}_B, b_u} \int_{\theta \in \Theta} \underline{M}_{T_B} dF(\theta), \quad (94)$$

where $u = \frac{\bar{D}}{T}$ is the fraction of periods during which a person is expected to be unemployed, and $\eta_{\bar{D}_B, b_u}$ is the elasticity of insured duration with respect to UI benefits. For the parameters $(u, \bar{D}_B, \bar{D}, \eta_{\bar{D}_B, b_u})$, the same parameter values can be used as in Table 1. The remaining thing to be determined is $\int_{\theta \in \Theta} \underline{M}_{T_B} dF(\theta)$. If the utility for consumption is homogeneous (i.e., $U(c; \theta) = U(c)$) and is given by CRRA function, then

$$\int_{\theta \in \Theta} \underline{M}_{T_B} dF(\theta) = \int_{\theta \in \Theta} \left(\frac{c_{u, T_B}(\theta)}{c_e(\theta)} \right)^\gamma dF(\theta). \quad (95)$$

If CRRA parameter is $\gamma \geq 1$, which is a standard assumption, then Jensen's inequality implies

$$\int_{\theta \in \Theta} \underline{M}_{T_B} dF(\theta) \geq \left[\int_{\theta \in \Theta} \frac{c_{u, T_B}(\theta)}{c_e(\theta)} dF(\theta) \right]^\gamma, \quad (96)$$

where the expression inside the bracket is the average consumption due to unemployment. Together with assumption (A.4), I obtain

$$\begin{aligned} \frac{\frac{\partial W(\mathbf{b})}{\partial b_e}}{\int_{\theta \in \Theta} \frac{\partial V_1}{\partial w} dF(\theta)} &\geq \frac{u}{1-u} \frac{\bar{D}_B}{\bar{D}} \eta_{\bar{D}_B, b_u} \left[\int_{\theta \in \Theta} \frac{c_{u, T_B}(\theta)}{c_0(\theta)} dF(\theta) \right]^\gamma \\ &\approx \frac{u}{1-u} \frac{\bar{D}_B}{\bar{D}} \eta_{\bar{D}_B, b_u} \left[\frac{\int_{\theta} c_{u, T_B}(\theta) dF(\theta)}{\int_{\theta} c_0(\theta) dF(\theta)} \right]^\gamma, \end{aligned} \quad (97)$$

where the second line is based on the first-order approximation around the averages of $c_{u, T_B}(\theta)$ and $c_e(\theta)$ in the population. As in Section 3, the last term can be computed based on high-frequency average consumption profile reported in, for example, [Ganong and Noel \(2019\)](#). The resulting welfare impact is the same as in Section 3.

B.2 Stochastic Wage Offers

The discussion here mostly follows [Chetty \(2008\)](#) except that I differentiate the welfare function with respect to wage subsidies instead of UI benefits. As before, individuals exert search effort e_t but this time I assume that conditional on getting a job offer, the wage offer is stochastic and follows a distribution F_w . If individuals are employed at a period t with asset A_t and wage w , their

value function is given by

$$V_{s,t}^E(A_t, w) = \max_{A_{t+1} \geq L} U(A_t - A_{t+1} + y_{e,s,t}) + V_{s,t+1}^E(A_{t+1}, w), \quad (98)$$

where income is given by

$$y_{e,s,t} = \begin{cases} w + b_e & \text{if } t \leq T_B, \\ w & \text{if } t > T_B. \end{cases} \quad (99)$$

If individuals with asset A_t does not find a job at the beginning of a period t , their value function is given by

$$V_t^U(A_t) = \max_{A_{t+1} \geq L} U(A_t - A_{t+1} + y_{u,t}) + V_{t+1}(A_{t+1}), \quad (100)$$

where $y_{u,t}$ is the same as in the main text.

Now consider the search decision of individuals. Individuals follow a reservation wage policy. Letting R_t be the reservation wage at t , the value function of unemployed people with asset A_t at the beginning of each period before searching for a job is given by

$$V_t(A_t) = \max_{e_t \in [0,1], R_t} e_t \Pr(w \geq R_t) \mathbb{E}[V_t^E(A_t, w) | w \geq R_t] + (1 - e_t \Pr(w \geq R_t)) V_t^U(A_t; b, \tau) - \psi(e_t). \quad (101)$$

This optimization problem is different from the one in the main text in that individuals now can choose the reservation wage R_t in addition to the search effort e_t .

As in the main text, I define the welfare function as $W(\mathbf{b}) = V_1(A_1; b, \tau(\mathbf{b}))$ given A_1 . Differentiating this with respect to wage subsidies b_e yields

$$\frac{\partial W(\mathbf{b})}{\partial b_e} = \frac{\partial V_1}{\partial b_e} + \frac{\partial V_1}{\partial \tau} \frac{\partial \tau(\mathbf{b})}{\partial b_e}. \quad (102)$$

Exploiting the envelope conditions from individual's optimization problem, I have

$$\frac{\partial V_1}{\partial b_e} = e_1 \Pr(w \geq R_1) \frac{\partial \mathbb{E} V_1^E}{\partial b_e} + (1 - e_1 \Pr(w \geq R_1)) \frac{\partial V_1^U}{\partial b_e}. \quad (103)$$

By defining a survival probability as $S_t = \prod_{j=1}^t [1 - e_j \Pr(w \geq R_j)]$, the same calculation as in Appendix A.2 yields

$$\frac{\partial V_1}{\partial b_e} = \sum_{t=1}^{T_B} (1 - S_t) \mathbb{E}_s[U'(c_{e,s,t})], \quad \frac{\partial V_1}{\partial \tau} = - \sum_{t=1}^T (1 - S_t) \mathbb{E}_s[U'(c_{e,s,t})]. \quad (104)$$

This is exactly the same as the case where wage offers are not stochastic except that the survival probability is now redefined so that it reflects the probability that an offered wage is above the

reservation wage. Introducing stochastic wage offers into the model does not change the welfare formula because the additional variable R_t shows up in the formula only through the survival probability S_t . Since the government budget constraint is not affected by the introduction of stochastic wage offers, the formula for the welfare impact of the marginal change in b_e in the presence of stochastic wage offers is the same as the one in the main text.