Reactivity Coefficients

$$\begin{split} \frac{\partial \rho}{\partial t} &= +\rho_o \delta(t) + \alpha_{T_F} \frac{\partial T_F}{\partial t} U(t) \\ \int\limits_{-\infty}^t \frac{\partial \rho}{\partial s} ds &= \int\limits_{-\infty}^t \rho_o \delta(s) ds + \int\limits_{-\infty}^t \alpha_{T_F} \frac{\partial T_F}{\partial s} \ U(s) \ ds \\ \int\limits_{-\infty}^t \frac{\partial \rho}{\partial s} ds &= \rho_o U(t) + \int\limits_0^t \alpha_{T_F} \frac{\partial T_F}{\partial s} ds \\ \int\limits_{\rho(-\infty)}^{\rho(t)} d(\rho(s)) &= \rho_o U(t) + \alpha_{T_F} \int\limits_{T_F(0)}^{T_F(t)} d(T_F(s)) \\ \rho(t) - \rho(-\infty) &= \rho_o U(t) + \alpha_{T_F} (T_F(t) - T_F(0)) \\ \rho(t) &= \rho_o + \alpha_{T_F} ((T_F(t) - T_F(0)) \end{split}$$