

(b)

Let L be the language of the DFA above. How many equivalence classes does \sim_L have? Justify your answer.

from proposition 62 of the book:

Suppose M is a *DFA* whose language is L . if x and y end at the same state of M , then $x \sim_L y$.

In the above DFA, $\{q_0\}$ and $\{q_0, q_1\}$ end in the same states of N so $\{q_0\} \sim_L \{q_0, q_1\}$. The other states have unique output sets so are in their own equivalence classes.

\therefore the number of equivalence classes in \sim_L is 3.