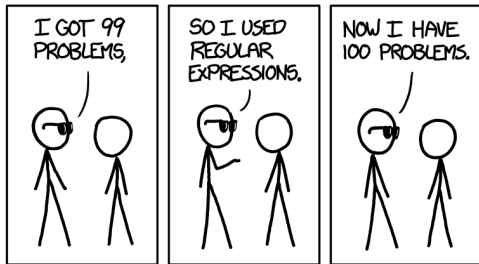


Games, graphs, and machines



September 20, 2024

A regex

Let L be the language on $\{0, 1\}$ consisting of w that contain an even number of 0s. Can you construct a regex that describes L ?

An automaton

Let M be the language on $\{0, 1\}$ consisting of w that contain an even number of 1s. Last time, we constructed an automaton that describes L (and similarly M). Construct automata that describe $L \cup M$ and $L \cap M$.

A generalisation

Given two languages L and M described by automata A and B , construct automata that describe $L \cup M$ and $L \cap M$.

Regexes again?

Returning to L (even 0s) and M (even 1s), construct regexes that describe $L \cup M$ and $L \cap M$.

Regexes again?

Returning to L (even 0s) and M (even 1s), construct regexes that describe $L \cup M$ and $L \cap M$.

For $L \cap M$:

$$(0(11)^*0 \mid (1 \mid 0(11)^*10)(0(0 \mid 1(11)^*10))^*(1 \mid 01(11)^*0))^*$$

Regexes and automaton are equivalent

Theorem Any language that can be described by a regex can also be described by an automaton, and vice-versa.

Better machines?

Searching for truth?

Let $L =$ (Mathematical) statements that are true. Is there an automaton (or a Turing machine) that describes L ?

The true reason why [no one] has succeeded in finding an unsolvable problem is, in my opinion, that there is no unsolvable problem. [...] We must know. We shall know!

– David Hilbert (1930)