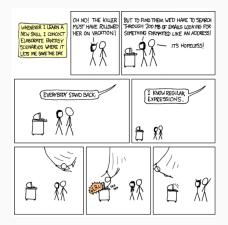
Games, graphs, and machines



Stars and cats

Alphabet $\Sigma=\{0,1\}.$ Languages $L=\{0\}$ and $\mathit{M}=\{1,11,111,1111,\cdots\}.$

- 1. LM =
- 2. ML =
- 3. $L^* =$
- 4. $M^* =$
- 5. $L^*M =$

man grep

REGULAR EXPRESSIONS

A regular expression is a pattern that describes a set of strings. Regular expressions are constructed analogously to arithmetic expressions, by using various operators to combine smaller expressions...

Character Classes and Bracket Expressions

A bracket expression is a list of characters enclosed by [and]...

Anchoring

The caret ^ and the dollar sign \$ are meta-characters...

The Backslash Character and Special Expressions

The symbols < and > respectively match the empty string...

Repetition

- ? The preceding item is optional and matched at most once.
- The preceding item will be matched zero or more times.
- + The preceding item will be matched one or more times.
- {n} The preceding item is matched exactly n times.
- {n,} The preceding item is matched n or more times.
- $\{\mbox{,m}\}$ The preceding item is matched at most m times. This is a GNU extension.
- $\{n,m\}$ The preceding item is matched at least n times, but not more than m times.

Concatenation

Two regular expressions may be concatenated; ...

Alternation

Two regular expressions may be joined by the infix operator |;...

Our regexps

- Ø
 - ϵ
 - (
 - .
- Concatenation ab alternation a|b star a*.

Regular expressions

Explicitly write the language described by the regexp.

- 1. 01*
- 2. (0|1)*
- 3. (01)*
- $4. \ 00^*10^*0$

Building regexps

Find regular expressions that describe the following languages.

- 1. Ø
- 2. $\{\epsilon\}$
- 3. $\{0,00,000,\cdots\}$
- 4. $\{w \mid w \text{ starts with 0 and ends with 1}\}$