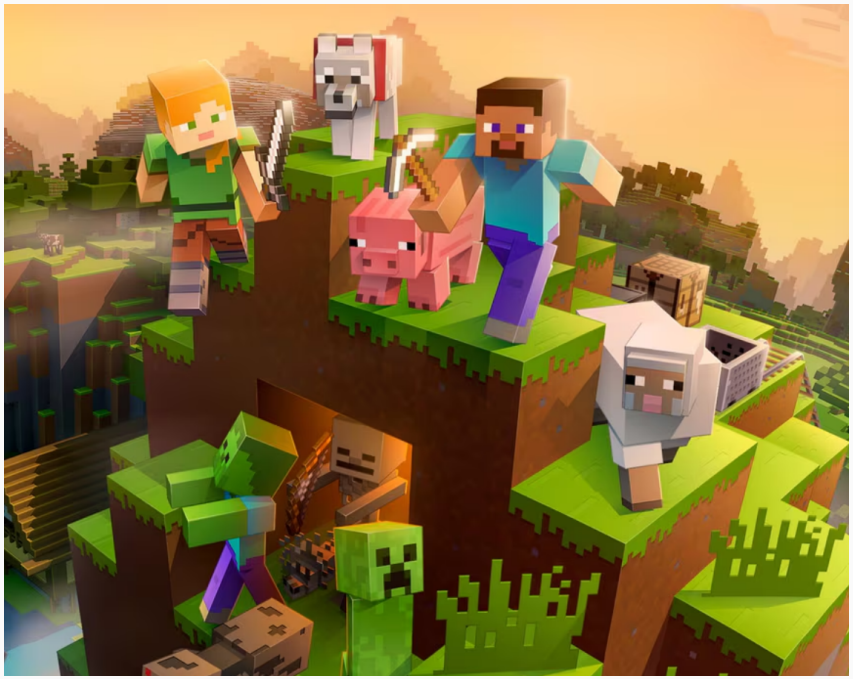
Games, graphs, and machines



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Poset chomp

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1. Interpret *Chomp* as the Poset Chomp of a poset.
2. Interpret Nim$(2, 3)$ as the Poset Chomp of a poset.

Divisor poset chomp

Let S be the divisor poset of 30 excluding the number 1. Is PosetChomp(S) an N-game or a P-game?

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Let S be the divisor poset of 30 excluding the number 1. Is PosetChomp(S) an N-game or a P-game? What is the winning move?

Adding

Let S be the divisor poset of 30 excluding the number 1. Is $\mathsf{PosetChomp}(\mathsf{S}) + \mathsf{Nim}(4, 4)$ an N-game or P-game?

N+P is P; P+P is P

Theorem

1. $N + P = P$
2. $P + P = P$

N+N could be either!

Find an example where an N-game + an N-game is a P game.

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Find an example where an N-game + an N-game is an N game.