

# CMSC216: Memory Systems

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# Logistics

## Assignments

- ▶ Lab10: I/O Redirection + File Statistics
- ▶ HW10: Reading from Files, Directory Traversal
- ▶ P4 Up, Due next week Mon, makeup credit pending

## Reading Bryant/O'Hallaron

Ch	Read?	Topic
Ch 6		<b>The Memory Hierarchy</b>
Ch 6.1	skim	Storage Technologies
Ch 6.2	READ	Locality
Ch 6.3	READ	The Memory Hierarchy
Ch 6.4	opt	Cache Memories
Ch 6.5	READ	Writing Cache Friendly Code
Ch 6.6	skim	Impacts of Cache on Performance
Ch 9		<b>Virtual Memory</b>
Ch 9.1-6	skim	VM Overview, Address Translation
Ch 9.7	opt	Case Study
Ch 9.8	READ	Memory mapping and <code>mmap()</code>
Ch 9.9	READ	Dynamic Memory Allocation
Ch 9.10	opt	Garbage Collection
Ch 9.11	skim	Memory Bugs in C Programs

## Goals

- ▶ Finish I/O discussion: I/O redirection and File attributes
- ▶ Timing Code, Cache vs DRAM Memory, Matrix Layout
- ▶ Permanent Storage Hardware and PROPS!

## Announcements

# Measuring Time in Code

- ▶ Measure CPU time with the standard `clock()` function; measure time difference and convert to seconds
- ▶ Measure Wall (real) time with `gettimeofday()` or related functions; fills struct with info on time of day (duh)

## CPU Time

```
#include <time.h>

clock_t begin, end;
begin = clock(); // current cpu moment

do_something();

end = clock(); // later moment

double cpu_time =
((double) (end-begin)) / CLOCKS_PER_SEC;
```

## Real (Wall) Time

```
#include <sys/time.h>

struct timeval tv1, tv2;
gettimeofday(&tv1, NULL); // early time

do_something();

gettimeofday(&tv2, NULL); // later time

double wall_time =
((tv2.tv_sec-tv1.tv_sec)) +
((tv2.tv_usec-tv1.tv_usec) / 1000000.0);
```

## Exercise: Time and Throughput

Consider the following simple loop to sum elements of an array from `stride_throughput.c`

```
int *data = ...; // global array

int sum_simple(int len, int stride){
    int sum = 0;
    for(int i=0; i<len; i+=stride){
        sum += data[i];
    }
    return sum;
}

int main(){
    ...
    int x1 = sum_simple(n,1);
    int x2 = sum_simple(n,2);
    int x3 = sum_simple(n,3);
    // total time for each stride?
    // throughput for each stride?
}
```

- ▶ Param `stride` controls step size through loop
- ▶ Interested in two features of the `sum_simple()` function:

1. Total Time to complete
2. **Throughput:**

$$\text{Throughput} = \frac{\#Additions}{\text{Seconds}}$$

- ▶ How would one **measure and calculate** these two in a program?
- ▶ As stride increases, **predict** how **Total Time** and **Throughput** change

# Answers: Time and Throughput

## Measuring Time/Throughput

Most interested in CPU time so

```
begin = clock();
sum_simple(length,stride);
end = clock();
cpu_time = ((double) (end-begin))
           / CLOCKS_PER_SEC;

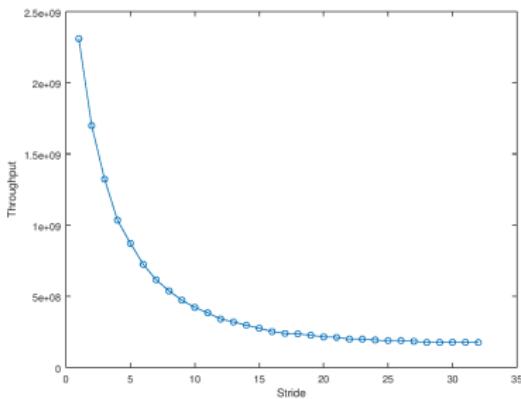
throughput = ((double) length) /
             stride /
             cpu_time;
```

## Time vs Throughput

As stride increases...

- ▶ Time decreases: doing fewer additions (duh)
- ▶ Throughput **decreases**

## Plot of Stride vs Throughput

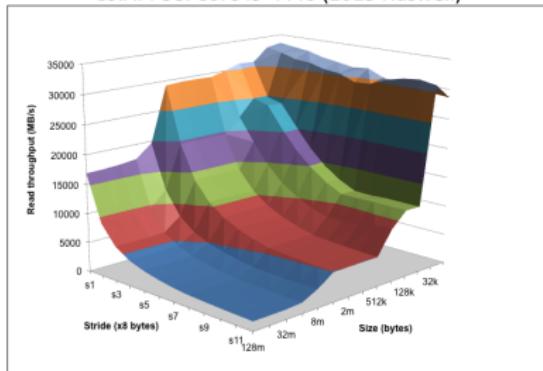


- ▶ Stride = 1: consecutive memory accesses
- ▶ Stride = 16: jumps through memory, more time

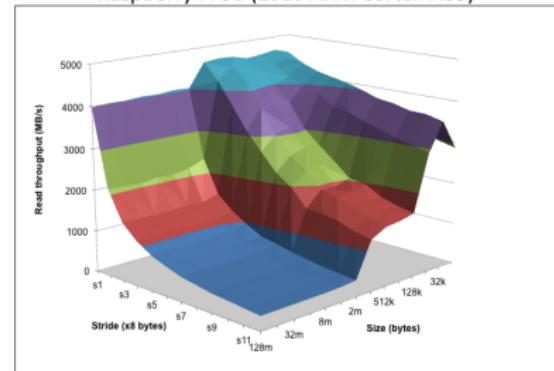
# Memory Mountains from Bryant/O'Hallaron

- ▶ Varying stride for a fixed length leads to decreasing performance, 2D plot
- ▶ Can also vary length for size of array to get a 3D plot
- ▶ Illustrates features of CPU/memory on a system
- ▶ The “Memory Mountain” on the cover of our textbook
- ▶ What **interesting structure** do you see?

CS:APP3e: Core i5-4440 (2013 Haswell)



Raspberry Pi 3B (2016 ARM Cortex-A53)



## CPU vs Memory Speed

- ▶ Early Computing Systems had a CPU Chips and Memory Chips, little if any data storage in the CPU (e.g. no registers)
- ▶ CPU and Memory Chips ran at similar speeds / clock frequencies: CPU would fetch data from Memory, perform arithmetic, store answers back to Memory
- ▶ Engineers found it easier to increase CPU Chip speed than Memory Chip speed: could now perform 100s of arithmetic operations in the time that a single Memory Fetch / Store could take place
- ▶ **Registers and Cache** were developed in response to the growing speed difference between CPU and Memory Chips
- ▶ Registers can be directly controlled by programmers (if the code in Assembly)
- ▶ Cache memory is (mostly) managed by the hardware itself, the **Main Memory System**

# Cache Favors Temporal and Spatial Locality

Hardware folks noticed programmers often write loops like

```
for(int i=0; i<len; i++){  
    sum += array[i];  
}
```

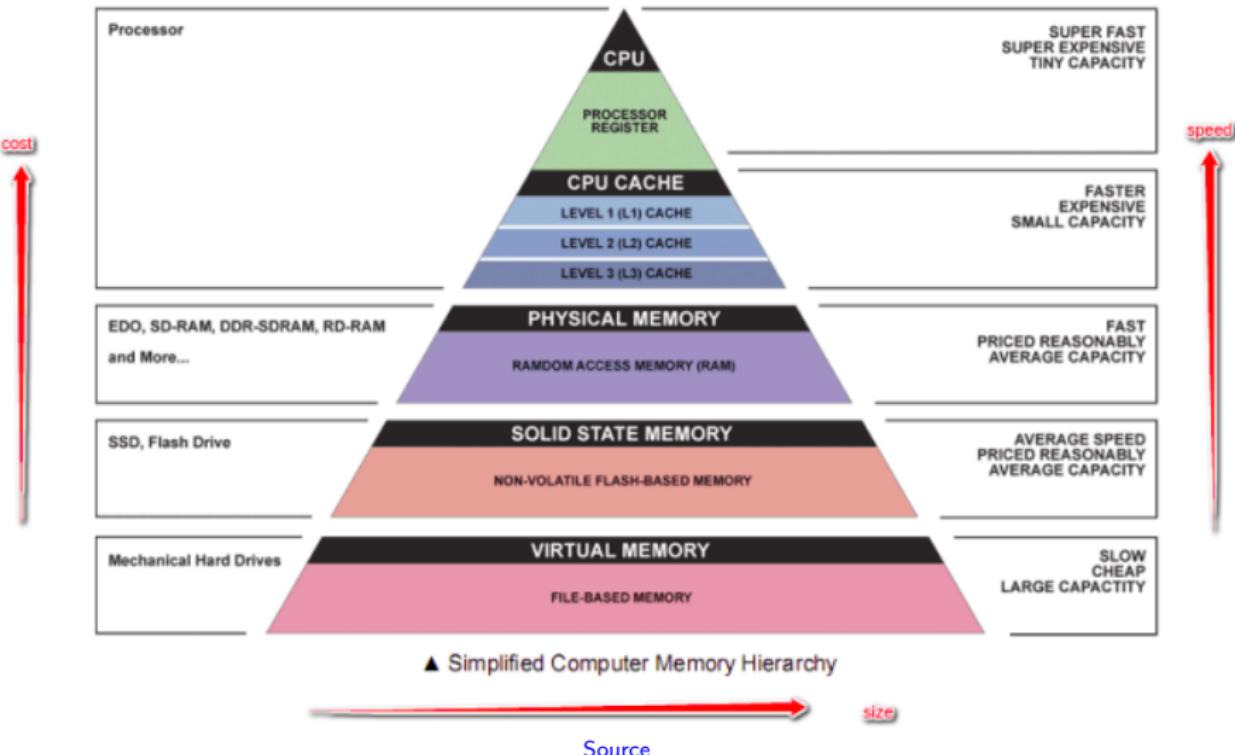
which exhibits two Memory Locality features

1. **Temporal Locality**: memory recently used likely to be used again soon (like `sum` and `i` used in every loop iteration)
2. **Spatial Locality**: nearby addresses to recently used memory likely to be used (like `arr[0]` first then `arr[1], arr[2]`)

Hardware engineers began adding chunks of Memory to CPUs to exploit these code tendencies giving rise to Cache Memory

- ▶ Code that utilizes Cache well will run faster

# The Memory Pyramid



# Numbers Everyone Should Know

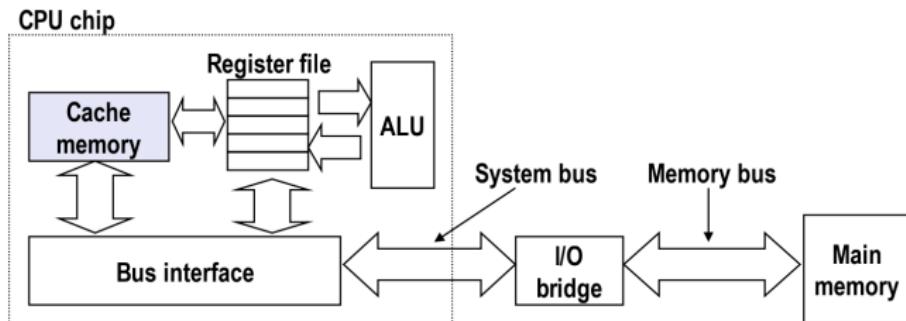
- ▶ “Main Memory” is comprised of many different physical devices that work together and have differing sizes/speeds
- ▶ Accessing memory at #4096 may involve some or all of...
  - ▶ Several Levels of Cache Memory on CPU (SRAM)
  - ▶ DRAM memory on separate chips
  - ▶ Permanent storage (SSDs and HDDs)

Edited Excerpt of [Jeff Dean's](#) talk on data centers.

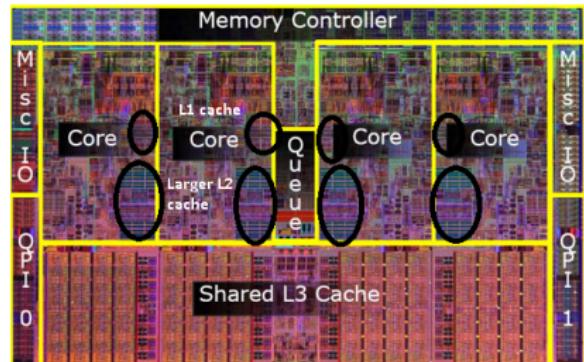
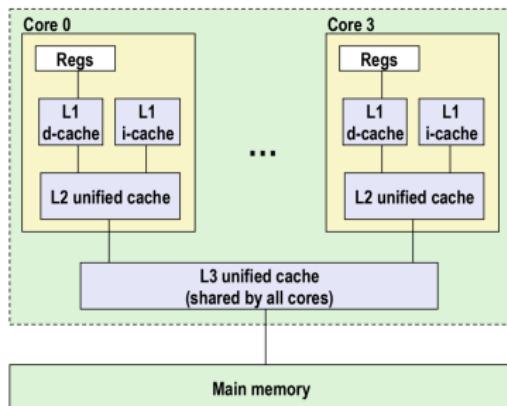
Reference	Time	Analogy
Register	-	Your brain
L1 cache reference	0.5 ns	Your desk
L2 cache reference	7 ns	Neighbor's Desk
DRAM memory reference	100 ns	This Room
Disk seek	10,000,000 ns	Salt Lake City

Big-O Analysis does NOT capture these; proficient programmers do

# Diagrams of Memory Interface and Cache Levels



Source: Bryant/O'Hallaron CS:APP 3rd Ed.



Source: SO "Where exactly L1, L2 and L3 Caches located in computer?"

# Why isn't Everything Cache?

Metric	1985	1990	1995	2000	2005	2010	2015	2015/1985
SRAM \$/MB	2,900	320	256	100	75	60	25	116
SRAM access (ns)	150	35	15	3	2	1.5	1.3	115
DRAM \$/MB	880	100	30	1	0.1	0.06	0.02	44,000
DRAM access (ns)	200	100	70	60	50	40	20	10

Source: Bryant/O'Hallaron CS:APP 3rd Ed., Fig 6.15, pg 603

1 bit SRAM = 6 transistors

1 bit DRAM = 1 transistor + 1 capacitor

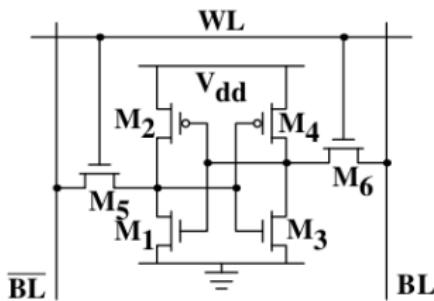


Figure 2.4: 6-T Static RAM

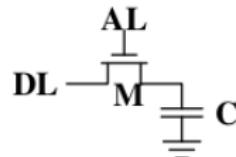
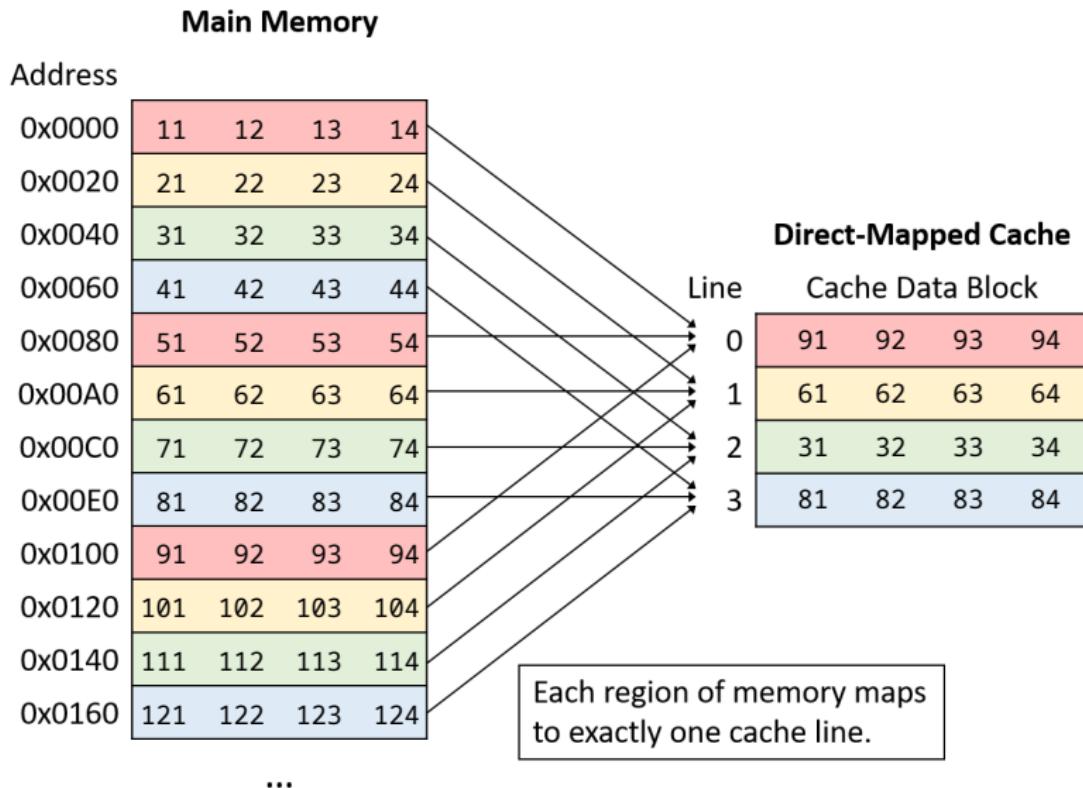


Figure 2.5: 1-T Dynamic RAM

"What Every Programmer Should Know About Memory" by Ulrich Drepper, Red Hat, Inc.

# Diagram of Direct Mapped Cache



Source: Dive into Systems dot org, with modifications

# How big is your cache? Check Linux System special Files

## lscpu Utility

Handy Linux program that summarizes info on CPU(s)

```
> lscpu
Architecture: x86_64
CPU op-mode(s): 32-bit, 64-bit
Byte Order: Little Endian
Address sizes: 36 bits physical,
                48 bits virtual
CPU(s):        4
Vendor ID:    GenuineIntel
CPU family:   6
Model:        58
Model name:   Intel(R) Core(TM)
                i7-3667U CPU @ 2.00GHz
...
L1d cache:    64 KiB
L1i cache:    64 KiB
L2 cache:    512 KiB
L3 cache:    4 MiB
Vulnerability Meltdown: Mitigation; ...
Vulnerability Spectre v1: Mitigation ...
...
```

## Detailed Hardware Info

Files under /sys/devices/... show hardware info (caches)

```
> cd /sys/devices/system/cpu/cpu0/cache/
> ls
index0  index1  index2  index3 ...
> ls index0/
number_of_sets  type  level  size
ways_of_associativity ...
> cd index0
> cat level type number_* ways_* size
1 Data 64 8 32K
> cd ../index1
> cat level type number_* ways_* size
1 Instruction 64 8 32K
> cd ../index3
> cat level type number_* ways_* size
3 Unified 8192 20 10240K
```

## Exercise: 2D Arrays

- ▶ Several ways to construct “2D” arrays in C
- ▶ All must *embed* a 2D construct into 1-dimensional memory
- ▶ Consider the 2 styles below: how will the picture of memory look different?

```
// REPEATED MALLOC
// allocate
int rows=100, cols=30;
int **mat =
    malloc(rows * sizeof(int*));

for(int i=0; i<rows; i++){
    mat[i] = malloc(cols*sizeof(int));
}

// do work
mat[i][j] = ...

// free memory
for(int i=0; i<rows; i++){
    free(mat[i]);
}
free(mat);
```

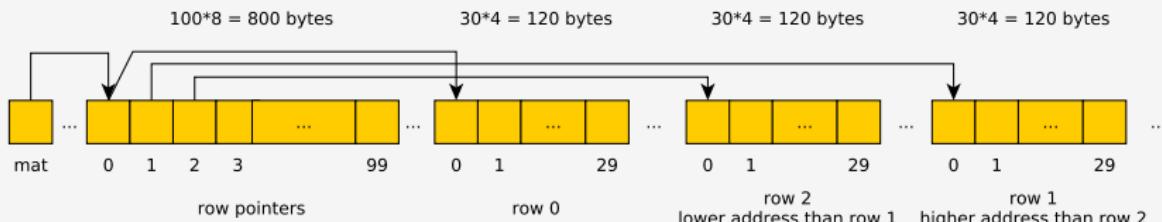
```
// TWO MALLOCs
// allocate
int rows=100, cols=30;
int **mat =
    malloc(rows * sizeof(int*));
int *data =
    malloc(rows*cols*sizeof(int));
for(int i=0; i<rows; i++){
    mat[i] = data+i*cols;
}

// do work
mat[i][j] = ...

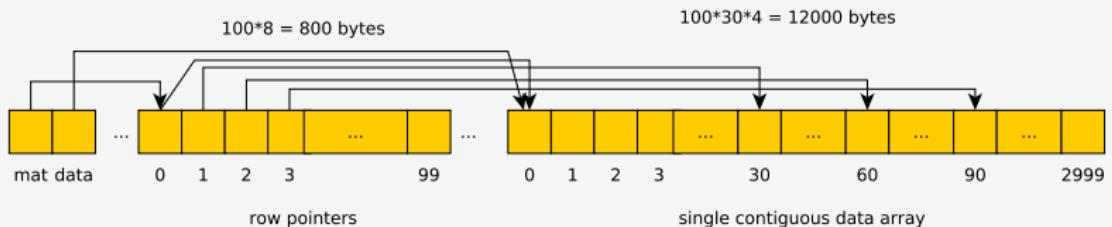
// free memory
free(data);
free(mat);
```

# Answer: 2D Arrays

## Repeated Mallocs



## Two Mallocs



# Single Malloc Matrices

Somewhat common to use a 1D array as a 2D matrix as in

```
int *matrix =
    malloc(rows*cols*sizeof(int));

int i=5, j=20;
int elem_ij = matrix[ i*cols + j ]; // retrieve element i,j
```

HWs / Labs / P4 will use this technique along with some structs and macros to make it more readable:

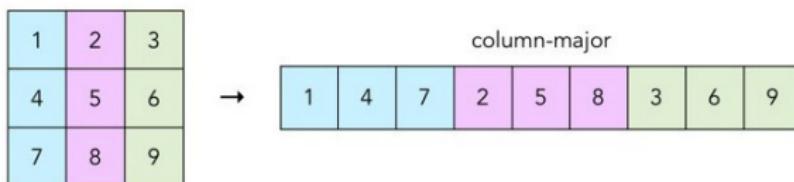
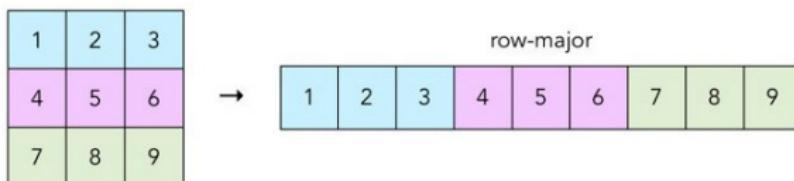
```
matrix_t mat;
matrix_init(&mat, rows, cols);

int elij = MGET(mat,i,j);
// elij = mat.data[ mat.cols*i + j ]

MSET(mat,i,j, 55);
// mat.data[ mat.cols*i + j ] = 55;
```

## Aside: Row-Major vs Col-Major Layout

- ▶ Many languages use **Row-Major** order for 2D arrays/lists
  - ▶ C, Java, Python, Ocaml,...
  - ▶  $\text{mat}[i]$  is a contiguous row,  $\text{mat}[i][j]$  is an element
- ▶ Numerically-oriented languages use **Column-Major** order
  - ▶ Fortran, Matlab/Octave, R, Ocaml (?)...
  - ▶  $\text{mat}[j]$  is a contiguous **column**,  $\text{mat}[i][j]$  is an element
- ▶ Being aware of language convention can increase efficiency



Source: The Craft of Coding

## Exercise: Matrix Summing

- ▶ How are the two codes below different?
- ▶ Are they doing the same number of operations?
- ▶ Which will run faster?

```
int sumR = 0;  
for(int i=0; i<rows; i++){  
    for(int j=0; j<cols; j++){  
        sumR += mat[i][j];  
    }  
}
```

```
int sumC = 0;  
for(int j=0; j<cols; j++){  
    for(int i=0; i<rows; i++){  
        sumC += mat[i][j];  
    }  
}
```

## Answer: Matrix Summing

- ▶ Show timing in `matrix_timing.c`
- ▶ `sumR` faster than `sumC`: caching effects
- ▶ Discuss timing functions used to determine duration of runs

```
> gcc -Og matrix_timing.c
```

```
> a.out 50000 10000
```

```
sumR: 1711656320 row-wise CPU time: 0.265 sec, Wall time: 0.265  
sumC: 1711656320 col-wise CPU time: 1.307 sec, Wall time: 1.307
```

- ▶ `sumR` runs about 6 times faster than `sumC`
- ▶ Understanding why requires knowledge of the memory hierarchy and cache behavior

## (Optional) Tools to Measure Performance: perf

- ▶ The Linux `perf` tool is useful to measure performance of an entire program
- ▶ Shows variety of statistics tracked by the kernel about things like memory performance
- ▶ **Examine** examples involving the `matrix_timing` program: `sumR` vs `sumC`
- ▶ **Determine** statistics that explain the performance gap between these two?

## (Optional Exercise): perf on sumR vs sumC

What stats below might explain the performance difference?

```
> perf stat $perfopts ./matrix_timing 8000 4000 row ## RUN sumR ROW SUMMING
sumR: 1227611136 row-wise CPU time: 0.019 sec, Wall time: 0.019
```

Performance counter stats for './matrix_timing 8000 4000 row':		%SAMPLED
135,161,407	cycles:u	(45.27%)
417,889,646	instructions:u # 3.09 insn per cycle	(56.22%)
56,413,529	L1-dcache-loads:u	(55.96%)
3,843,602	L1-dcache-load-misses:u # 6.81% of all L1-dcache hits	(50.41%)
28,153,429	L1-dcache-stores:u	(47.42%)
125	L1-icache-load-misses:u	(44.77%)
3,473,211	cache-references:u # last level of cache	(56.22%)
1,161,006	cache-misses:u # 33.427 % of all cache refs	(56.22%)

```
> perf stat $perfopts ./matrix_timing 8000 4000 col # RUN sumC COLUMN SUMMING
sumC: 1227611136 col-wise CPU time: 0.086 sec, Wall time: 0.086
```

Performance counter stats for './matrix_timing 8000 4000 col':		%SAMPLED
372,203,024	cycles:u	(40.60%)
404,821,793	instructions:u # 1.09 insn per cycle	(57.23%)
61,990,626	L1-dcache-loads:u	(60.21%)
39,281,370	L1-dcache-load-misses:u # 63.37% of all L1-dcache hits	(45.66%)
23,886,332	L1-dcache-stores:u	(43.24%)
2,486	L1-icache-load-misses:u	(40.82%)
32,582,656	cache-references:u # last level of cache	(59.38%)
1,894,514	cache-misses:u # 5.814 % of all cache refs	(60.38%)

## Answers: perf stats for sumR vs sumC, what's striking?

### Observations

- ▶ Similar number of instructions between row/col versions
- ▶ #cycles lower for row version → higher insn per cycle
- ▶ **L1-dcache-misses**: marked difference between row/col version
- ▶ **Last Level Cache Refs** : many, many more in col version
- ▶ Col version: much time spent waiting for memory system to feed in data to the processor

### Notes

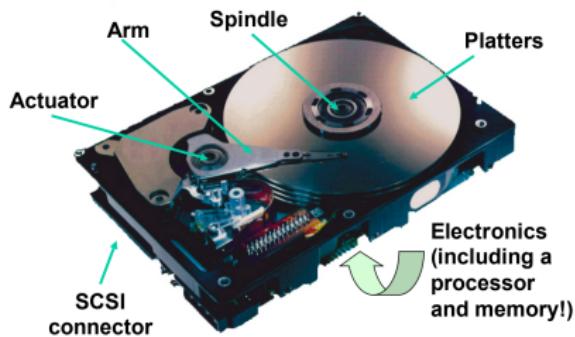
- ▶ The right-side percentages like (50.41%) indicate how much of the time this feature is measured; some items can't be monitored all the time.
- ▶ Specific perf invocation is in  
`10-memory-systems-code/measure-cache.sh`

## Flavors of Permanent Storage

- ▶ Have discussed a variety of fast memories which are **small**
- ▶ At the bottom of the pyramid are **disks**: slow but **large** memories, may contain copies of what is in higher parts of memory pyramid
- ▶ These are **persistent**: when powered off, they retain information
- ▶ Permanent storage often referred to as a “drive”
- ▶ Comes in many variants but these 3 are worth knowing about in the modern era
  1. Rotating Disk Drive
  2. Solid State Drive
  3. Magnetic Tape Drive
- ▶ Surveyed in the slides that follow

# Ye Olde Rotating Disk

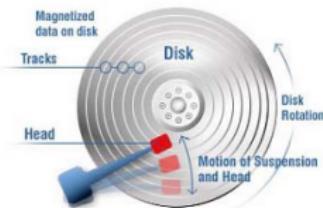
- ▶ Store bits “permanently” as magnetized areas on special platters
- ▶ Magnetic disks: moving parts → slow
- ▶ Cheap per GB of space



*Image courtesy of Seagate Technology*

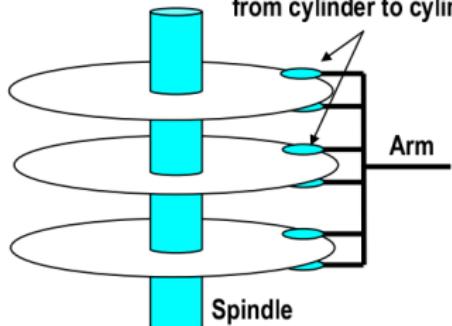
Source: CS:APP Slides

HARD DRIVE DATA READ & WRITE OPERATION MOTION DIAGRAM



Source: Realtechs.net

Read/write heads  
move in unison  
from cylinder to cylinder



Source: CS:APP Slides

# Rotating Disk Drive Features of Interest

## Measures of Quality

- ▶ Capacity: bigger is usually better
- ▶ Seek Time: delay before a head assembly reaches an arbitrary track of the disk that contains data
- ▶ Rotational Latency: time for disk to spin around to correct position; faster rotation → lower Latency
- ▶ Transfer Rate: once correct read/write position is found, how fast data moves between disk and RAM

## Sequential vs Random Access

Due to the rotational nature of Magnetic Disks...

- ▶ Sequential reads/writes comparatively FAST
- ▶ Random reads/writes comparatively very SLOW

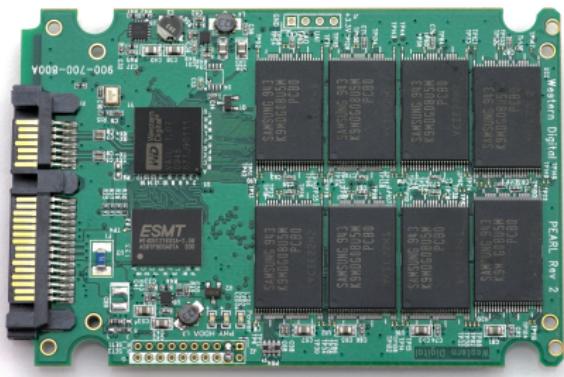
# Solid State Drives

- ▶ No moving parts → speed
- ▶ Most use “flash” memory, non-volatile circuitry
- ▶ Major drawback: limited number of **writes**, disk wears out eventually
- ▶ Reads faster than writes
- ▶ Sequential somewhat faster than random access
- ▶ **Expensive:**

*A 1TB internal 2.5-inch hard drive costs between \$40 and \$50, but as of this writing, an SSD of the same capacity and form factor starts at \$250. That translates into*

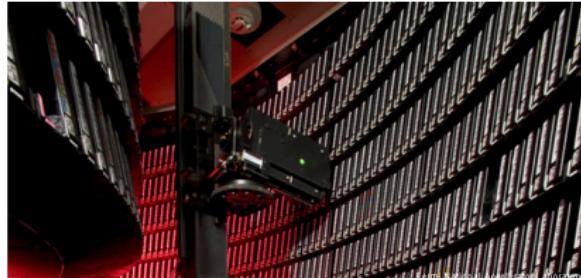
- 4 to 5 cents/GB for HDD
- 25 cents/GB for the SSD.

*PC Magazine, “SSD vs HDD” by Tom Brant and Joel Santo Domingo March 26, 2018*

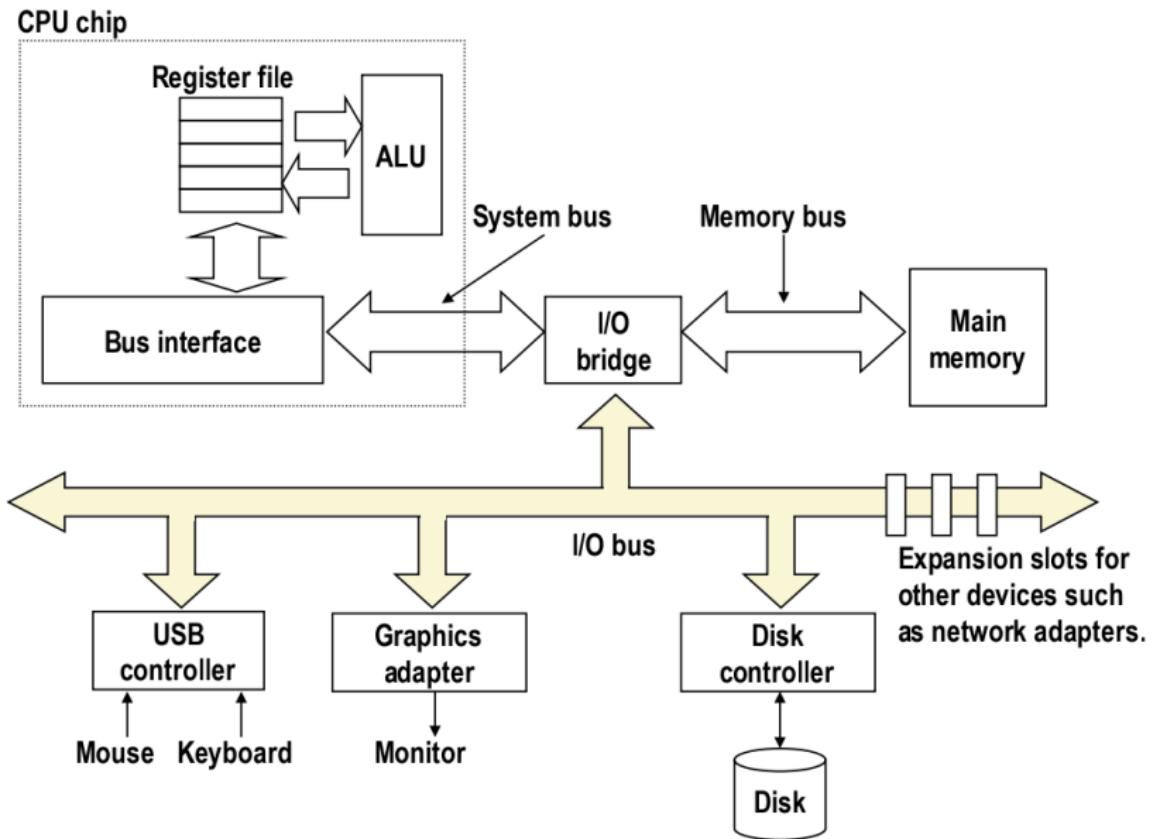


# Tape Drives

- ▶ Slowest yet: store bits as magnetic field on a piece of “tape” a la 1980’s cassette tape / video recorder 
- ▶ Extremely cheap per GB so mostly used in backup systems
- ▶ Ex: CSELabs does nightly backups of home directories, recoverable from tape at request to Operator



# The I/O System Connects CPU and Peripherals



# Terminology

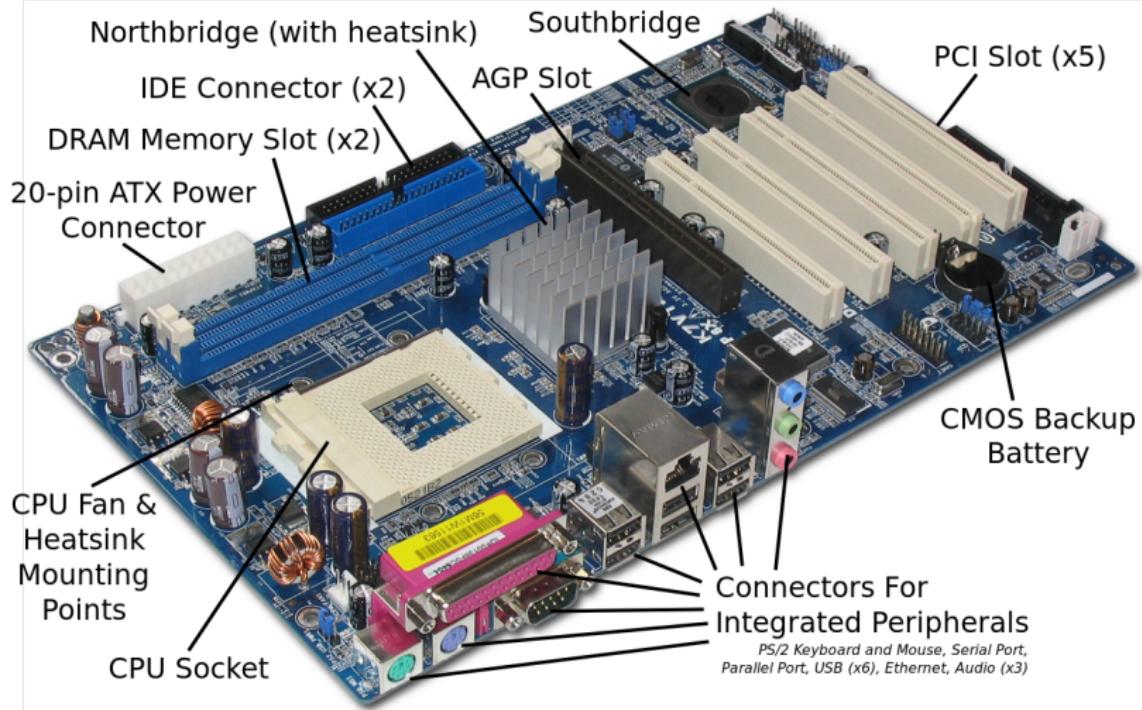
**Bus** A collection of wires which allow communication between parts of the computer. May be serial (single wire) or parallel (several wires), must have a communication protocol over it.

**Bus Speed** Frequency of the clock signal on a particular bus, usually different between components/buses requiring interface chips  
CPU Frequency > Memory Bus > I/O Bus

**Interface/Bridge** Computing chips that manage communications across the bus possibly routing signals to correct part of the computer and adapting to differing speeds of components

**Motherboard** A printed circuit board connects to connect CPU to RAM chips and peripherals. Has buses present on it to allow communication between parts. *Form factor* dictates which components can be handled.

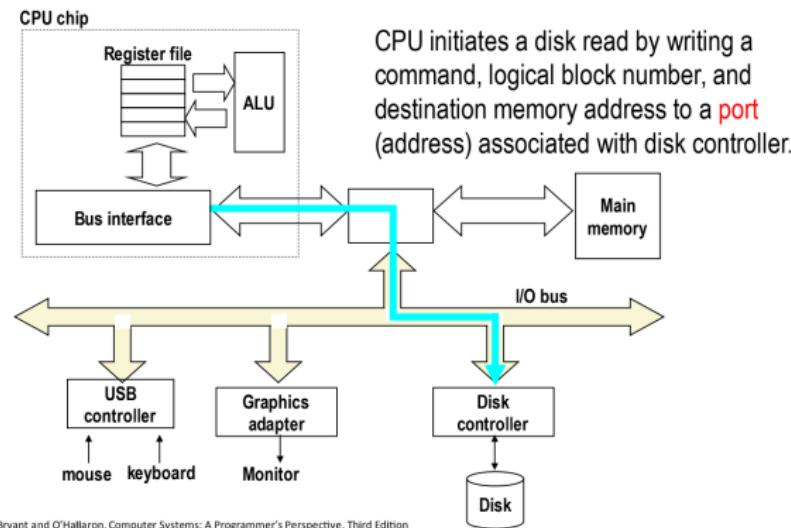
# The Motherboard



Picture Source: Wikipedia  
Live Props Courtesy of Free Geek Minneapolis

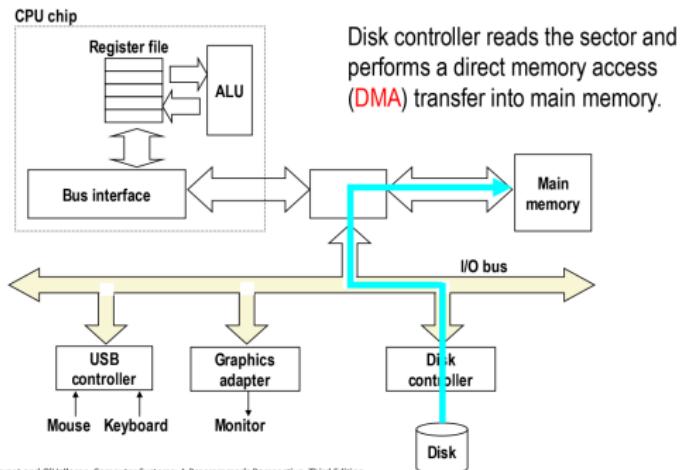
# Memory Mapped I/O

- ▶ Modern systems are a collection of devices and microprocessors
- ▶ CPU usually uses **memory mapped I/O**: read/write certain memory addresses translated to communication with devices on I/O bus



# Direct Memory Access

- ▶ Communication received by *other* microprocessors like a Disk Controller or Memory Management Unit (MMU)
- ▶ Other controllers may talk: Disk Controller loads data directly into Main Memory via **direct memory access**

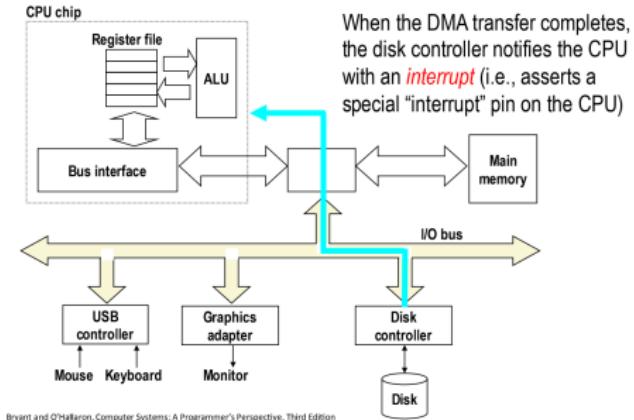


# Interrupts and I/O

Recall access times

Place	Time
L1 cache	0.5 ns
RAM	100 ns
Disk	10,000,000 ns

- ▶ While running Program X, CPU reads an int from disk into %rax
- ▶ Communicates to disk controller to read from file
- ▶ Rather than wait, OS puts Program X to “sleep”, starts running program Y



Bryant and O'Hallaron, Computer Systems: A Programmer's Perspective, Third Edition

- ▶ When disk controller completes read, signals the CPU via an **interrupt**, electrical signals indicating an event
- ▶ OS handles interrupt, schedules Program X as “ready to run”

## Interrupts from Outside and Inside

- ▶ Examples of events that generate interrupts
  - ▶ Integer divide by 0
  - ▶ I/O Operation complete
  - ▶ Memory address not in RAM (Page Fault)
  - ▶ User generated: x86 instruction int 80
- ▶ Interrupts are mainly the business of the Operating System
- ▶ Usually cause generating program to immediately transfer control to the OS for handling
- ▶ When building your own OS, must write “interrupt handlers” to deal with above situations
  - ▶ Divide by 0: **signal** program usually terminating it
  - ▶ I/O Complete: schedule requesting program to run
  - ▶ Page Fault: sleep program until page loaded
  - ▶ User generated: perform system call
- ▶ User-level programs will sometimes get a little access to interrupts via **signals**, a topic in many OS classes