

# CSCI 2021: Basics of Hardware and CPU Architecture

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# Logistics

## Reading Bryant/O'Hallaron

### Ch 4: Architectures

- ▶ Skimming is OK
- ▶ Lecture: high-level coverage

### Ch 6: Memory (Next)

## Goals

- ▶ Circuits that Compute
- ▶ Basics of Processor Arch
- ▶ Pipelining



## Lab / HW 10

- ▶ Time C code using time command
- ▶ Observe strange results that raise questions
- ▶ Answer questions in lecture

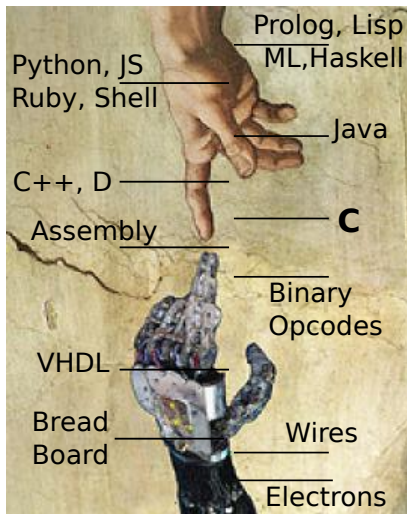
## Project 4

- ▶ Post Next Week
- ▶ Optimization + Performance
- ▶ Use knowledge of Arch / Memory to improve / explain execution speed

# Machines that Compute

- ▶ Humans can perform algorithms, sadly **slow and error-prone**
- ▶ Want a machine which can do this faster with fewer errors
- ▶ Variety of machines have been built over time and technology to implement them has changed rapidly
- ▶ The following are high-level principles that haven't changed much

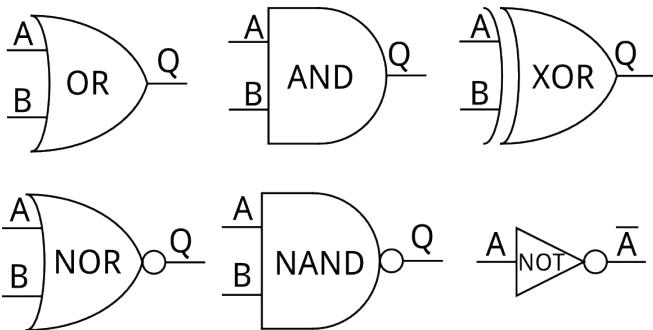
## Pure Abstraction



## Bare Metal

# Logic Gates

- ▶ Abstract physical device that implements a boolean function
- ▶ May be implemented with a variety of components including **transistors**, vacuum tubes, mechanical devices, and [water pressure](#)
- ▶ Physical implementations have many trade-offs: cost, speed, difficulty to manufacture, wetness



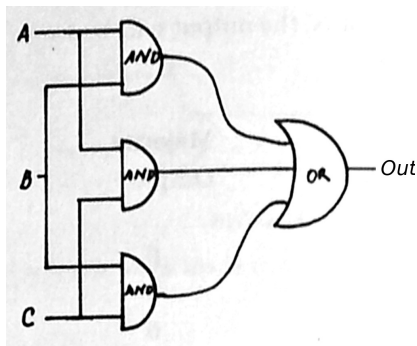
# Combinatorial Circuits

- ▶ Combination of wires/gates with output solely dependent on input
- ▶ No storage of information involved / **stateless**
- ▶ Distinguished from **sequential** circuits which involve storage
- ▶ Can compute any **Boolean functions** of inputs
  - ▶ Set inputs as 0/1
  - ▶ After a delay, outputs will be set accordingly
- ▶ Examples: AND, OR, NOT are obvious

## Exercise: Example Combinatorial Circuit

Calculate the Truth Table for the circuit

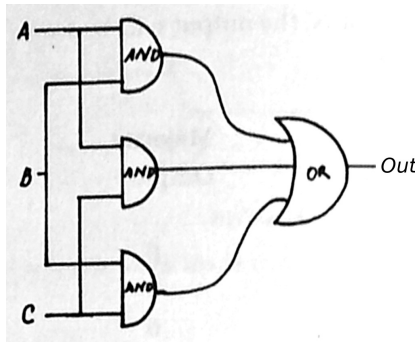
A	B	C	Out
0	0	0	?
0	0	1	?
0	1	0	?
0	1	1	?
1	0	0	?
1	0	1	?
1	1	0	?
1	1	1	?



- Speculate on the “meaning” of this circuit

## Answer: Example Combinatorial Circuit

A	B	C	Out
0	0	0	0
0	0	1	0
0	1	0	0
0	1	1	1
1	0	0	0
1	0	1	1
1	1	0	1
1	1	1	1



A “majority” circuit: Out is 1 when two or more of A,B,C are 1

## Exercise: Comparing Majority-3 Circuits

- ▶ Both upper and lower circuits implement *Majority-3*: Same truth table
- ▶ Which is **better**?
- ▶ What criteria for “better” seems appropriate?

26 THE PATTERN ON THE STONE

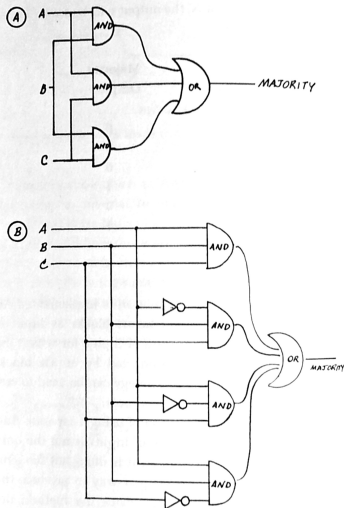


FIGURE 12



## Answer: Comparing “Majority-3” Circuits

Criteria	Upper	Lower
Gate Kinds	2	3
Gate Count	4	8
Gate “Depth”	2	3
“Scalability”	Low	High

- ▶ “Scalability” is not well-defined, roughly how to “scale up” to majority 64
- ▶ Hardware designers spend time trying to design “better” circuits where “better” involves many criteria

26 THE PATTERN ON THE STONE

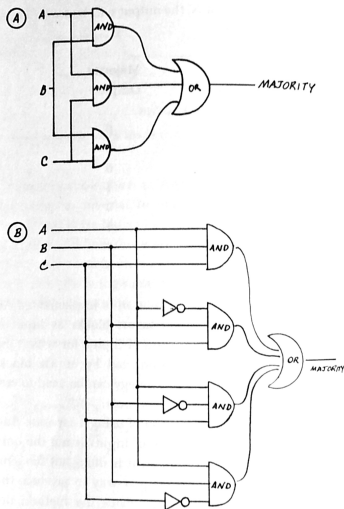
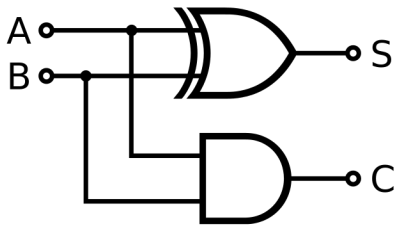


FIGURE 12

# Adders

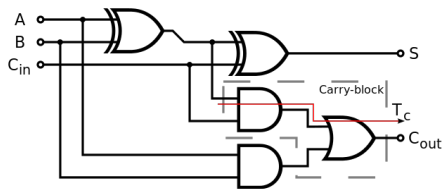
- ▶ Obviously want computers to add stuff
- ▶ An **adder** is a circuit that performs addition

## 1-bit Half Adder



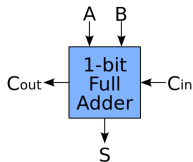
- ▶ “Adds” A and B
- ▶ S is the sum
- ▶ C is the carry
- ▶ Construct a **Truth Table** for the circuit

## 1-bit Full Adder

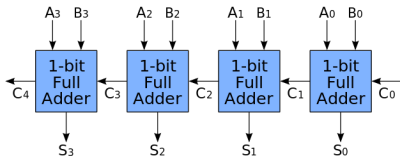


- ▶ “Adds” A, B, and  $C_{in}$
- ▶ S is the sum
- ▶  $C_{out}$  is the carry out
- ▶ Carry In/Out used to string adders together

# Multi-bit Addition

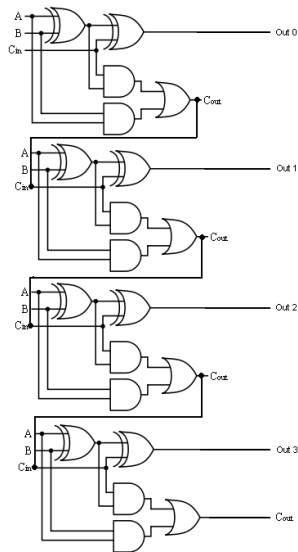


Combine 4 full adders to get a 4-bit ripple carry adder



Easily extends to 32- or 64-bit adders

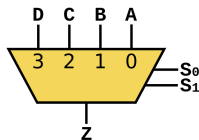
# Full Gate Layout



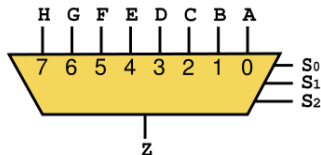
# Multiplexers: MUX

- ▶ Used to “select” output from several inputs
- ▶  $2^N$  Inputs A,B,C,...
- ▶  $N$  selection bits  $S_0, S_1, \dots$
- ▶ Output will be one of inputs “chosen” by selection bits
- ▶ Block diagram is a rectangle or trapezoid with inputs/outputs
- ▶ Will prove useful momentarily

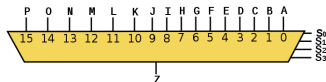
- ▶ 4-to-1 MUX



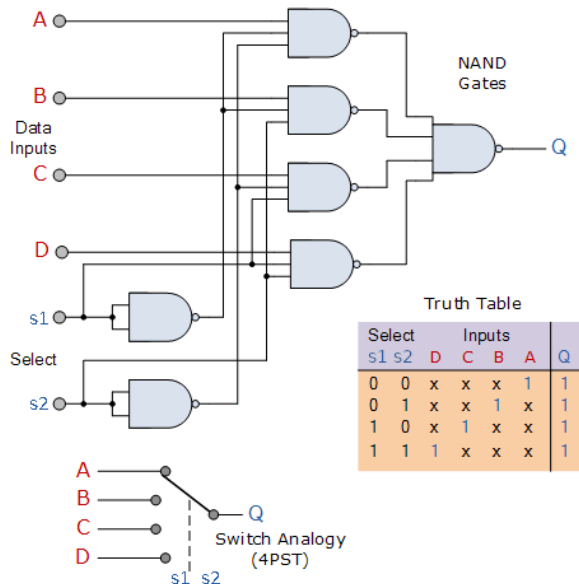
- ▶ 8-to-1 MUX



- ▶ 16-to-1 MUX



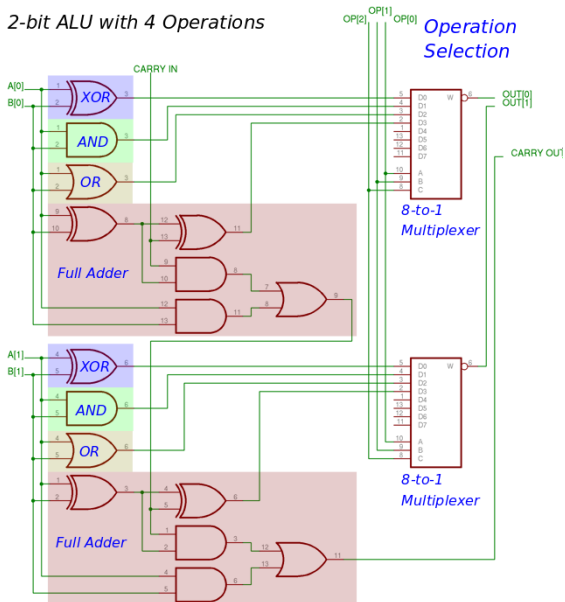
# 4-to-1 Multiplexer Circuit Diagram



- ▶ Variety of ways to design a MUX
- ▶ One shown uses NAND gates exclusively
- ▶ Note output is true when selected input is true

# Arithmetic Logic Unit ALU: Select an Operation

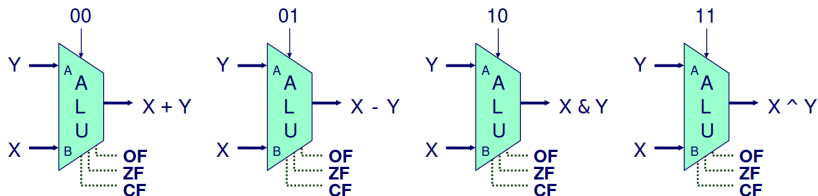
2-bit ALU with 4 Operations



- ▶ Combine some gates, an adder, and a MUX
- ▶ Start having something that looks useful
- ▶ Input for multiple ops like AND, OR, XOR, ADD are **simultaneously** computed
- ▶ Select an “operation” with selection bits, really just selecting which output to pass through

# ALU and FLAGS

- ▶ Block diagram for ALUs are usually a wedge shape
- ▶ Along with arithmetic/logic, ALU usually produces condition codes
  - ▶ ZF: zero flag
  - ▶ OF: overflow flag
  - ▶ SF: sign flag
- ▶ Used in other parts of CPU for conditional jumps/moves



# Hardware Design in the Old Days

- ▶ Hardware design originally done by hand
- ▶ Draw all the gates, transfer it to technical drawing material, peel, send, hope to heaven that nothing gets munged...
- ▶ Required tremendous discipline, still had bugs



*Ted Jenkins remembers working on the first Intel product, the 3101 64-bit RAM. Actually, the first version was only a 63-bit RAM due to a simple error peeling one layer on the rubylith (drawing medium).<sup>1</sup>*

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<sup>1</sup>Andrew Volk, Peter Stoll, Paul Metrovich, "Recollections of Early Chip Development at Intel", Intel Technology Journal Q1, 2001



# Modern Hardware Design: Specification Languages

- ▶ Modern design uses **hardware description languages**
- ▶ Verilog and VHDL pervasive, describe **behavior** of circuit
- ▶ *Synthesis*: convert description to gate layout with constraints like “use only NAND”
- ▶ *Verification*: simulate circuit to ensure correctness
- ▶ The invention of computers greatly accelerated development of better computers

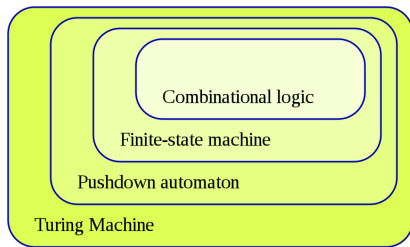
## VHDL for 4-bit ALU $\wedge$ $\&$ $|$ $+$

```
library IEEE;
entity alu is
  Port(A_IN : in signed(3 downto 0);
       B_IN : in signed(3 downto 0);
       OPER : in STD_LOGIC_VECTOR(1 downto 0);
       OUTP : out signed(3 downto 0));
end alu;

architecture Behavioral of alu is
begin
  process(A_IN, B_IN, OPER)
  begin
    case OPER is
      when "00" =>
        OUTP <= A_IN xor B_IN; --XOR gate
      when "01" =>
        OUTP <= A_IN and B_IN; --AND gate
      when "10" =>
        OUTP <= A_IN or B_IN; --OR gate
      when "11" =>
        OUTP <= A_IN + B_IN; --addition
    end case;
  end process;
end Behavioral;
```

# Combinatorial vs Sequential Circuits

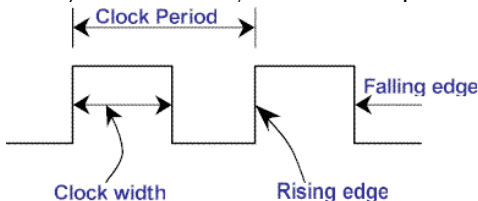
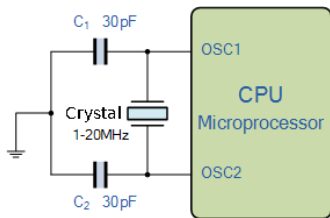
- ▶ Combinatorial circuits can do lots of things BUT don't constitute a complete programming system
- ▶ Need to represent **state**: store values, make future values depend on past state
- ▶ **Sequential circuits** introduce the notion of time and state to allow actual computation
- ▶ Most actual machines are state machines in some class like push-down automata or Turing machines (studied in 2011 and 4011)



*The class of problems that can be solved grows with more powerful machines.*

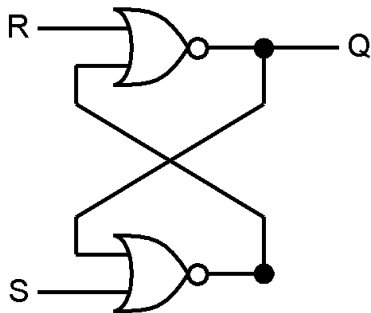
## Clock Circuits

- ▶ To move beyond combinatorial circuits, need a way to measure time
- ▶ A **Clock Circuit** does this
- ▶ Provides an oscillating signal of high/low voltages at a fixed frequency
- ▶ Physical device: often **quartz crystal** which contracts when voltage is applied (*electrostriction*), expands when released
- ▶ Manufactured to have different periods/frequencies
- ▶ Circuitry attached to crystal causes oscillation at crystal's resonant frequency; circuitry can increase/decrease output frequency



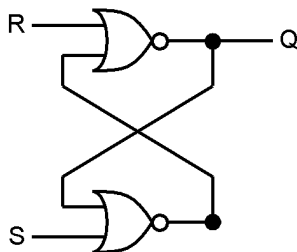
## A Strange Circuit: SR Latch

- ▶ This one should **bug you** a little - why?
- ▶ Try computing a Truth Table for it...



# A Strange Circuit: SR Latch

- ▶ SR Latch uses **feedback to store one bit** which is output as Q
- ▶ Truth Tables less relevant than **State Transition Table**
- ▶ Shows what the next state will be based on previous state
- ▶ Inputs and Outputs
  - ▶ S is for “SET”
  - ▶ R is for “RESET”
  - ▶ Q is current stored value
  - ▶  $Q_{next}$  is new stored value



State Transition Table

S	R	$Q_{next}$	Action
0	0	Q	hold state
0	1	0	reset
1	0	1	set
1	1	X	not allowed

# Storage via Latches $\approx$ Flip-Flops

Specific combinations of latches yield the following nice properties

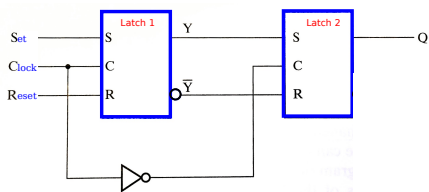
- ▶ Store a bit of information so long as power is supplied (not shown in diagrams)
- ▶ Constantly output the stored bit
- ▶ Change the bit on certain inputs
- ▶ **Only change stored bit** during the rising edge of an input signal - **the clock tick**
- ▶ Often referred to as a **Flip Flop**, commonly a *rising edge flip-flop*<sup>2</sup>
- ▶ Latches/Flip Flops can serve as a basis **registers**

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<sup>2</sup>There is no agreement on whether latches and flip-flops are the same or different so take care to understand context if going deeper. Relation above is adopted from some textbooks on digital design.

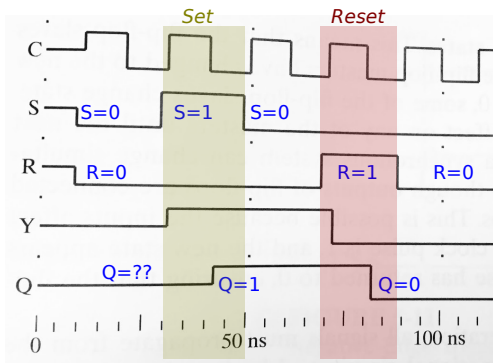
## Example: Master Slave SR Flip-Flop and Timing

- Shows how a flip-flop (combination of two latches) stores a bit
- Set to 1:  $S=1, R=0$
- Set to 0:  $S=0, R=1$



### State Transition Table

S	R	$Q_{\text{next}}$	Action
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0	1	0	reset
1	0	1	set
1	1	X	not allowed

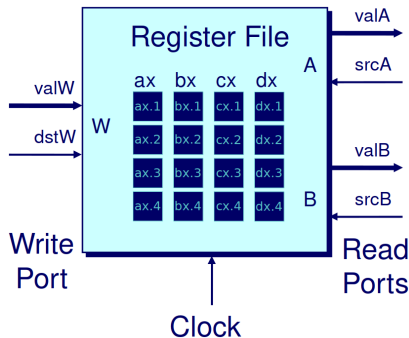


# Registers: a form of Static RAM (SRAM)

- ▶ Combine 4 flip-flops (each storing one bit) and one has an 4-bit **register**: circuitry that holds a changeable multi-bit quantity
- ▶ Combine more flip-flops to get larger registers, 8- 16- 32- 64-bit
- ▶ Combine several registers with some access control circuitry (multiplexers) and one has a **register file** containing `%rax %rbx ... %r15`

Typical register file allows simultaneous

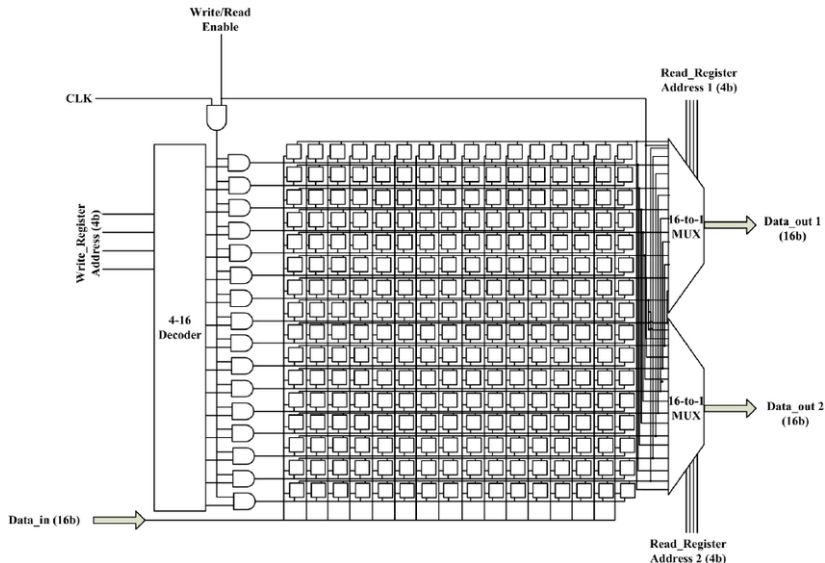
- ▶ read from two regs
- ▶ write to one reg



*Register File with 4 registers, each with 4 bits*



# Register File with 16 Regs X 16 Bits + I/O



Source: Mostafa Khatib "Aging Analysis of Datapath Sub-blocks Based on CET Map Model for Negative Bias Temperature Instability (NBTI)", Masters of Science Thesis, Center for Materials and Microsystems, Trento, Italy  
January 2014

# Other Registers/CPU Memory of Note (SRAM)

## Instruction Memory/Cache

Fast access to binary opcodes of program text

## Program Counter (rip)

Position in instruction memory

## Intermediate Results

For internal communication between different parts of the CPU to facilitate pipelining, usually accessible in assembly language

## Some Memory Caches

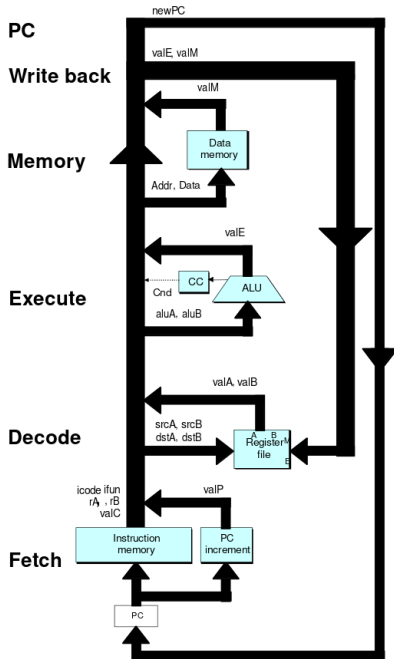
Small, fast cache of main memory close to the cpu has similar circuitry to register file

## NOT Main Memory

- ▶ While fast, **SRAM is expensive** in terms of transistors/space
- ▶ DRAM (dynamic RAM) is slower but compact and cheap enough to scale to gigabytes (will discuss DRAM soon)

## The Full Shebang

- ▶ Connect an Clock, ALU, and Register file, and you've got a quasi-computer
- ▶ Add some instruction decoding, a place to store instructions, and perhaps some main memory and a full computer is born
- ▶ Must specify exact encoding of instructions so that signals between gates/units are routed correctly
- ▶ Note that processor design to the right is broken into **stages** to help understanding



## Exercise: Timing Problems

- ▶ Each gate creates a delay: time before output to stabilize based on new inputs
- ▶ Inputs are “allowed” to change on the clock signal’s rising edge
- ▶ Simplest **sequential** implementation sets clock frequency slow enough for outputs to stabilize each cycle (tick)
- ▶ Easy to do, but... it’s **slow**

### Increasing Efficiency

Propose **two ways** that a complex, multi-part process can be completed faster

- ▶ Draw from experience/knowledge
- ▶ Think manufacturing, group projects, car wash, **Chipotle**...

# Answer: Timing Problems

General solutions to process speed are familiar to all of us

## Assembly Line



- ▶ Break single instruction into multiple “stages” which must all complete
- ▶ **Pipelined** processors execute stages simultaneously

## Multiple Resources

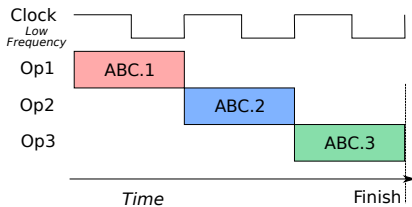


- ▶ Implement multiple functional units and do instructions in parallel
- ▶ **Superscalar** processors (and parallel processors)

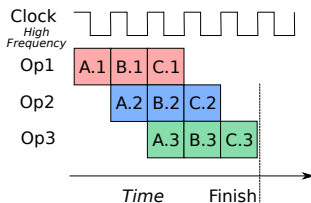
# Pipelining for Efficiency

- ▶ Break up processor into “stages” which feed into each other
- ▶ Individual instructions like `addl %ecx, %eax` go through each stage
- ▶ Instruction completes (*retires*) when all stages complete
- ▶ **Begin next instruction when previous clears first stage**
- ▶ Some multi-cycle operations like **multiplication** may be pipelined as well

## Sequential



## 3-Stage Pipeline



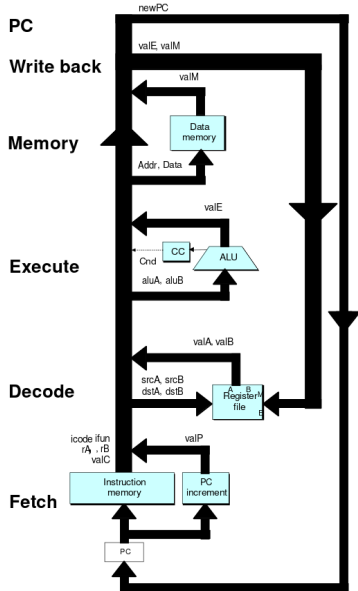
# Y86-64: Textbook Processor SEQ vs PIPE

- ▶ Textbook discusses 5-stages of a simple CPU design
  1. Fetch next PC
  2. Decode instruction
  3. Execute instruction
  4. Main Memory operations
  5. Write-back to register file
- ▶ Diagrams and Hardware Description Language for
  - ▶ SEQ: sequential implementation
  - ▶ PIPE: pipelined version of processor

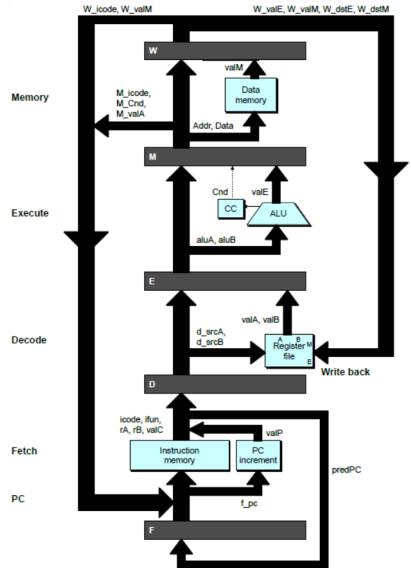
## PIPE Version

- ▶ Each of 5 stages happens in parallel
- ▶ Up to 5 instructions in flight
- ▶ Introduces internal registers to facilitate pipeline

## Y86-64 SEQ sequential



## Y86-64 PIPE 5-stage pipeline





# Pipelines Aren't All that and a Bag of Chips

- ▶ Pipelining is effective with predictable control flow and independent instructions
- ▶ Cases exist in which this doesn't play out: pipeline **hazards**

## Data Interdependencies

# INDEPENDENT

```
imull $3, %eax # mul and add
addl $1, %edx # different reg
```

# DEPENDENT: "Hazard"

```
imull $3, %eax # mul and add
addl $1, %eax # same reg
```

- ▶ Dependencies between register results break the pipeline
- ▶ Must serialize instructions (sequential execution)

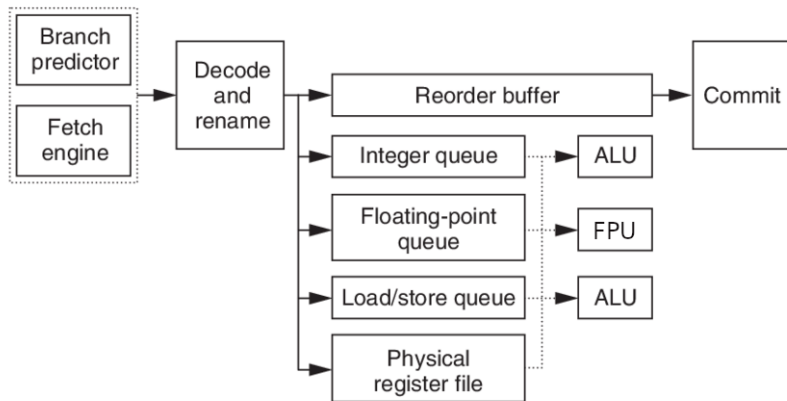
## Branching

.LOOP:

```
addl %edx,%eax
addl $1, %ecx
cmp %esi,%ecx
jlt .LOOP # which instruction
popq %rbx # next? "hazard"
```

- ▶ Modern Processors use **branch prediction** to guess the next instruction
- ▶ Incorrect guesses lead to restarting the pipeline

# Superscalar Block Diagram



Source: Kilo-Instruction Processors: Overcoming the Memory Wall by Cristal et al.

Note several ALUs, separate queues for different instructions, asynchronous execution of instructions

# Superscalar Processing

- ▶ Modern processors may have several **functional units** to do arithmetic, logic, other ops
- ▶ Allows **instruction-level parallelism**: do two things simultaneously
- ▶ Example:

```
# SEQ 1: Multiply only
imull $3, %eax

# SEQ 2: Multiply and Add
imull $3, %eax
addl  $5, %edx
```
- ▶ SEQ 1 and SEQ 2 may take the same amount of time
- ▶ Separate mult/add units used simultaneously
- ▶ Instruction parallelism automatically done at the hardware level leading to naming conventions for processors:
  - ▶ “Scalar”: sequential only, one thing at a time
  - ▶ “**Superscalar**”: automatic instruction parallelism, no explicit control
  - ▶ “Parallel”: explicit instructions that do multiple things simultaneously
- ▶ Modern processors are an amalgam of the above

# Modern Processors are Weird

## Assembly Code as an Interface

- ▶ Assembly/Binary Opcodes are a target for high level languages
- ▶ Modern processors execute these, guarantee correctness BUT make no guarantees about **how** or in what order
- ▶ Most use **very deep** pipelines which must be “fed” to keep speed high
- ▶ Has led to exotic processor designs with speculative and out of order execution: keep things in the pipeline
- ▶ This hasn't always gone well: [Meltdown](#) / [Spectre](#)

## Lab10 + HW10: Timing Arithmetic Codes

- ▶ Leads to surprising results
- ▶ Explainable by considering CPU is pipelined and superscalar
- ▶ Timing results vary with different CPUs

# Additional Resources the Architecture-Inclined

## Building an 8-bit breadboard computer! by Ben Eater (Youtube)

- ▶ Discusses many components we briefly touched on in more detail with a very practical bent of using them
- ▶ Results in a full CPU + Memory system that you can “see”
- ▶ A great introduction to components, breadboards, and general small electronics work

## MIT 6.004 Computation Structures, Spring 2017 (Youtube)

- ▶ Much deeper detail on many aspects of CPU design
- ▶ Includes discussion of Multiplier circuits, power considerations, etc.