

## Experiment 4

Aim: To obtain the frequency response (magnitude and phase response) of an Active Low Pass Filter, and also obtain its cut-off frequency.

## Equipment Required:

- 1 Voltage Source
- 2 Resistors (For the Filters) ( $R_1$  and  $R_2$ )
- 2 Capacitors (for the filters) ( $C_1$  and  $C_2$ )
- 1 Op-Amp (2 Supply Voltage also required for activating the Op-Amps)
- 2 Resistors (For setting the gain of the Op-Amp) ( $R_f$  and  $R$ )
- Ground.

## Formulae:

- $Q = \frac{1}{3-k}$  (where  $Q$  is Q-factor and  $k$  is gain of the Op-Amp)
- $k = 1 + \frac{R_f}{R}$  (where  $k$  is the gain of the Op-Amp)
- $f_{\text{undamped natural}} = \frac{1}{2\pi(R \cdot C)}$  (where  $f_{\text{undamped natural}}$  frequency of the active low pass filter,  $R = R_1 = R_2$  and  $C = C_1 = C_2$ )

## Procedure:

- Case 1 ( $R_1 = R_2 = 10k\Omega$  and  $C_1 = C_2 = 1nF$  and Q-factor = 1) :

Since Q-factor = 1, we get  $k=2$

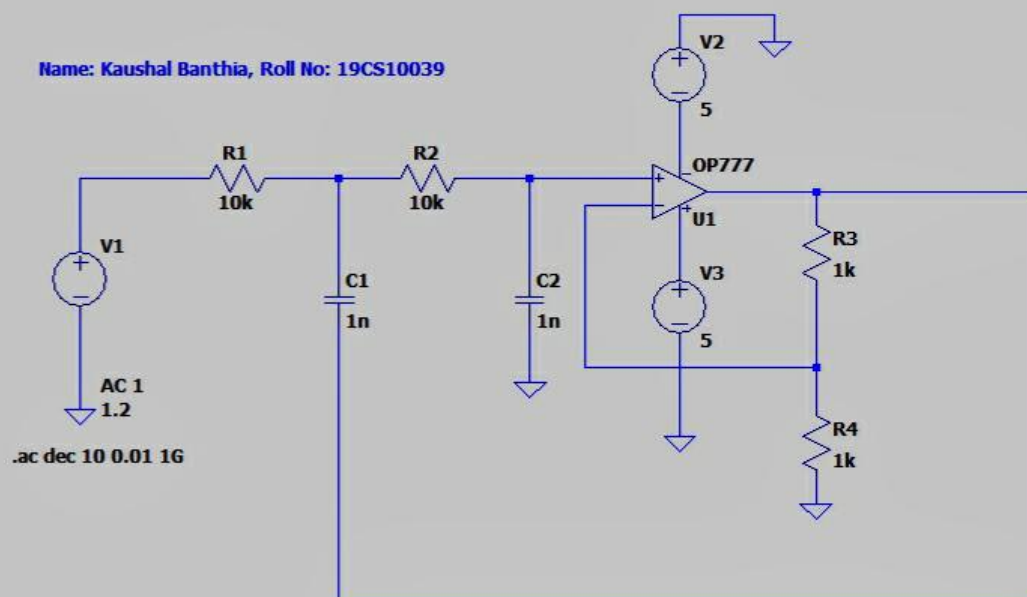
$\therefore R_f = R \Rightarrow$  we choose  $R_f = R = 1k\Omega$ .

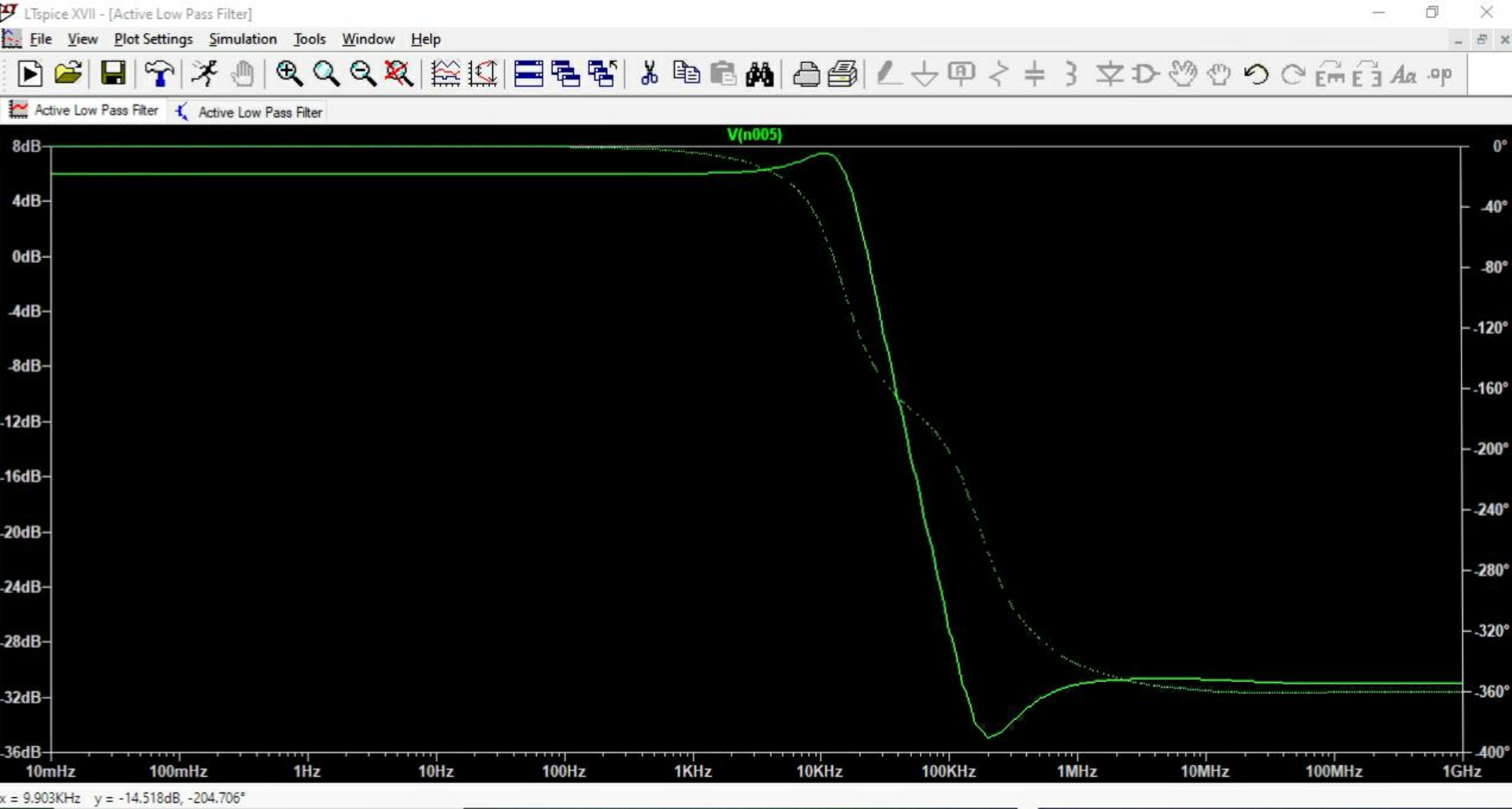
Now, theoretical  $f_{\text{undamped natural}} = \frac{1}{2\pi \times 10^4 \times 10^{-9}} = 15.915 \text{ kHz}$ .

Comments: We get a peak around the  $f_{\text{undamped natural}}$  (a characteristic of the Sallen-Key Filter). It decreases for quite a while, but for very high frequencies, the gain becomes constant. This is due to the presence of parasitic elements modelled in LTSpice. Also, the phase monotonously decreases for frequency increase, although it ~~decreases~~ becomes almost constant ( $\approx 360^\circ$ ) at very high frequencies.



Name: Kaushal Banthia, Roll No: 19CS10039







- Case 2 ( $R_1 = R_2 = 10 \text{ k}\Omega$  and  $C_1 = C_2 = 1 \text{ nF}$  and  $Q\text{-factor} = 1.5$ ):

Since  $Q\text{-factor} = 1.5$ , we get  $k = 7/3 = 2.333$

$\therefore R_f = 1.333 R \Rightarrow$  we choose  $R = 1 \text{ k}\Omega$  and  $R_f = 1.333 \text{ k}\Omega$ .

Now, Theoretical frequency  $f_{\text{undamped}}$  remains the same, since,  $R_1$ ,  $R_2$ ,  $C_1$  and  $C_2$  remain the same.

$$\therefore f_{\text{undamped}} = \frac{1}{2\pi \times 10^4 \times 10^{-9}} = 15.915 \text{ kHz.}$$

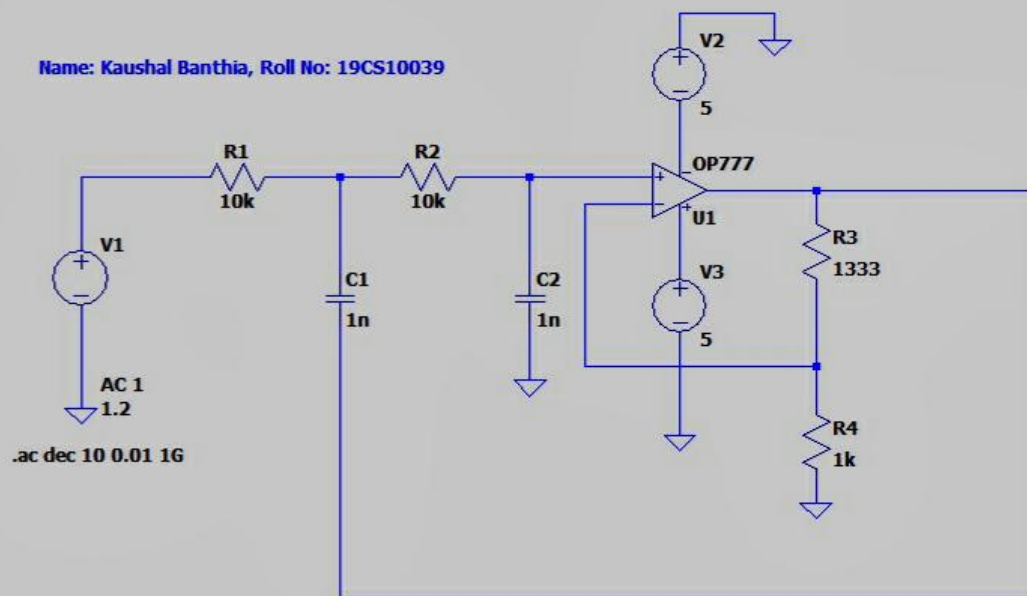
Comments: In this case too, we get the peak around the undamped <sup>natural</sup> frequency, but this time, the peak is shifted a bit towards the higher frequency side. (closer to the undamped <sup>natural</sup> frequency).

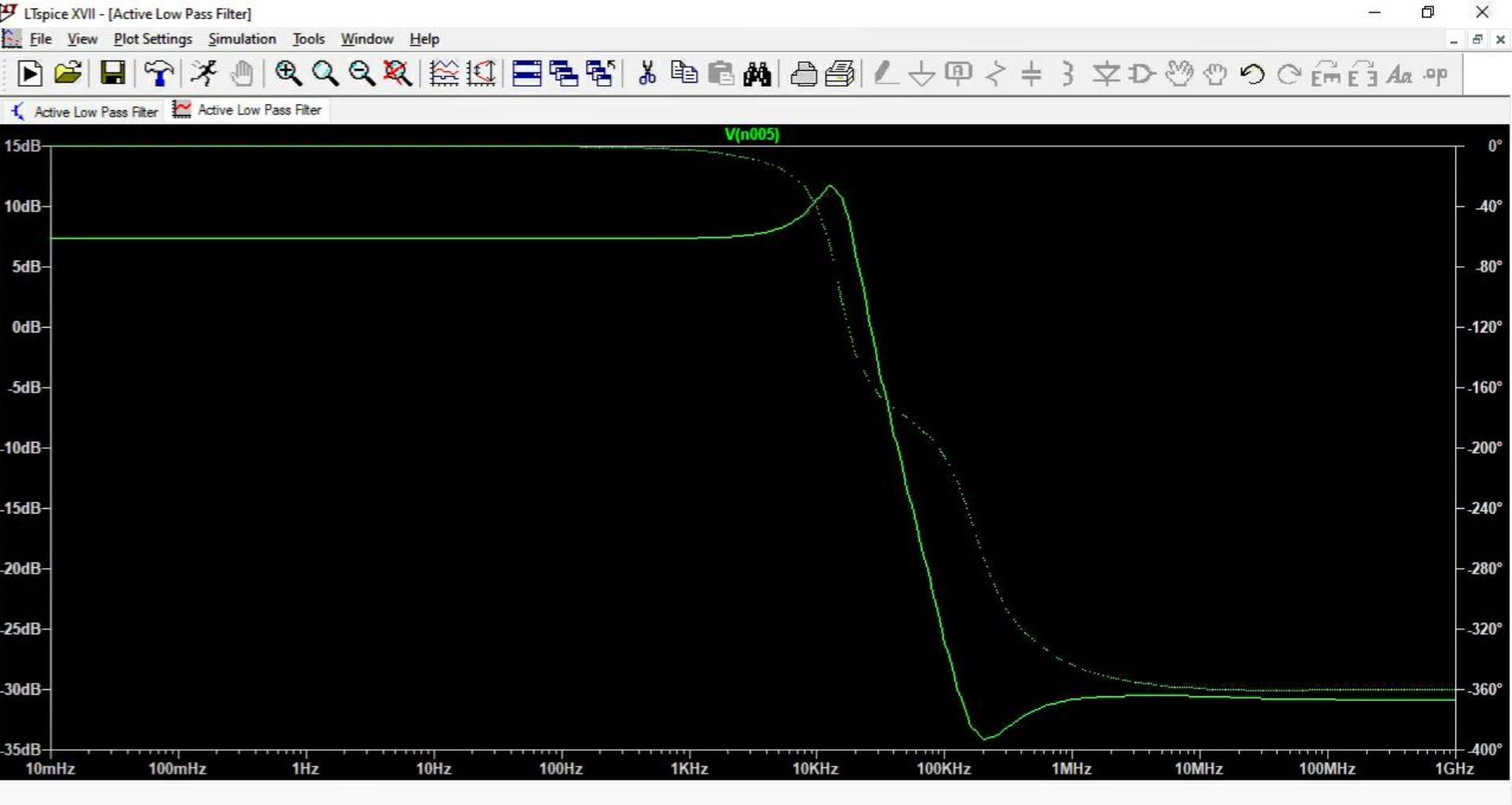
In this case too, the magnitude decreases for a while, but then becomes constant due to the parasitic elements.

Similarly, the phase response is monotonically decreasing and then becomes nearly constant ( $\approx 360^\circ$ ) for very high frequencies.

• Since this  $\phi$  filter has a higher  $Q$ -factor than the previous one, its peak is sharper and more prominent.

Name: Kaushal Banthia, Roll No: 19CS10039







- Case 3: ( $R_1 = R_2 = 10 \text{ k}\Omega$  and  $C_1 = C_2 = 1 \text{ nF}$  and  $Q\text{-factor} = 2.5$ )

Since  $Q\text{-factor} = 2.5$ , we get  $k = 2.6$ .

$\therefore R_f = 2.6 \text{ k}\Omega$ .  $\Rightarrow$  We choose  $R = 1 \text{ k}\Omega$  and  $R_f = 2.6 \text{ k}\Omega$ .

Now Theoretical cutoff frequency  $f_{\text{cutoff}}$  again remains same, since none among  $R_1$ ,  $R_2$ ,  $C_1$  and  $C_2$  were changed and  $f_{\text{undamped natural}}$  depends only on these parameters.

$$\therefore f_{\text{undamped natural}} = \frac{1}{2\pi \times 10^{-4} \times 10^{-9}} = 15.915 \text{ kHz}.$$

Comments: Again in this case, the peak is found close to the undamped <sup>natural</sup> frequency. Here the peak is closer to the <sup>undamped natural</sup> than before lie, it is shifted to the right.

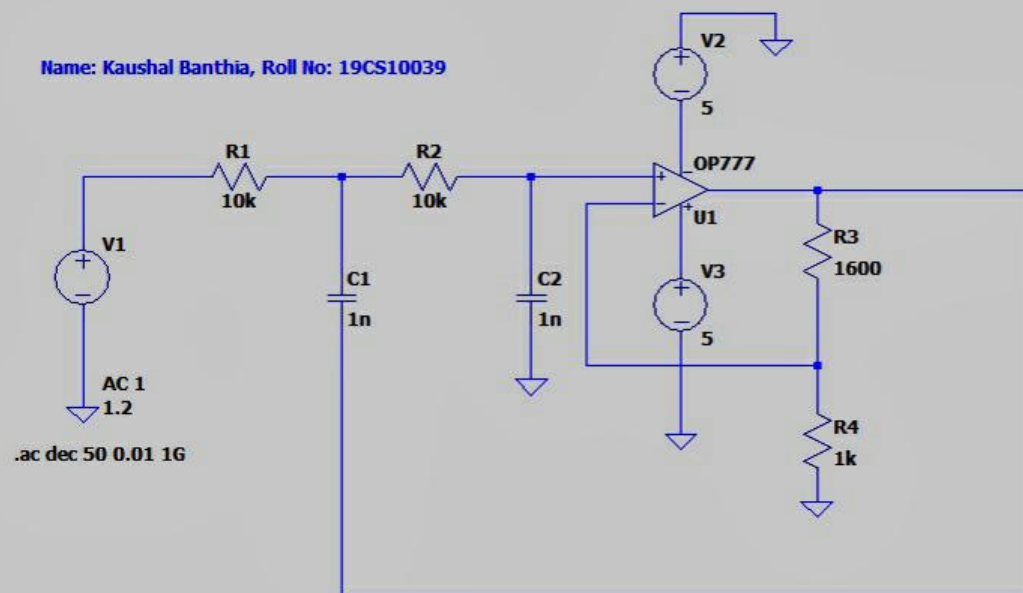
As before, the magnitude decreases with an increase in frequency, but at very ~~for~~ high frequencies, it ~~se~~ becomes constant (due to the parasitic elements, especially parasitic capacitors).

The phase response remains the shape as of before, with the only difference being that the concavity and the convexity of the graph increases by a good amount and that change is visible. This is because, now the ~~the~~ phase decreases faster around the cutoff frequency.

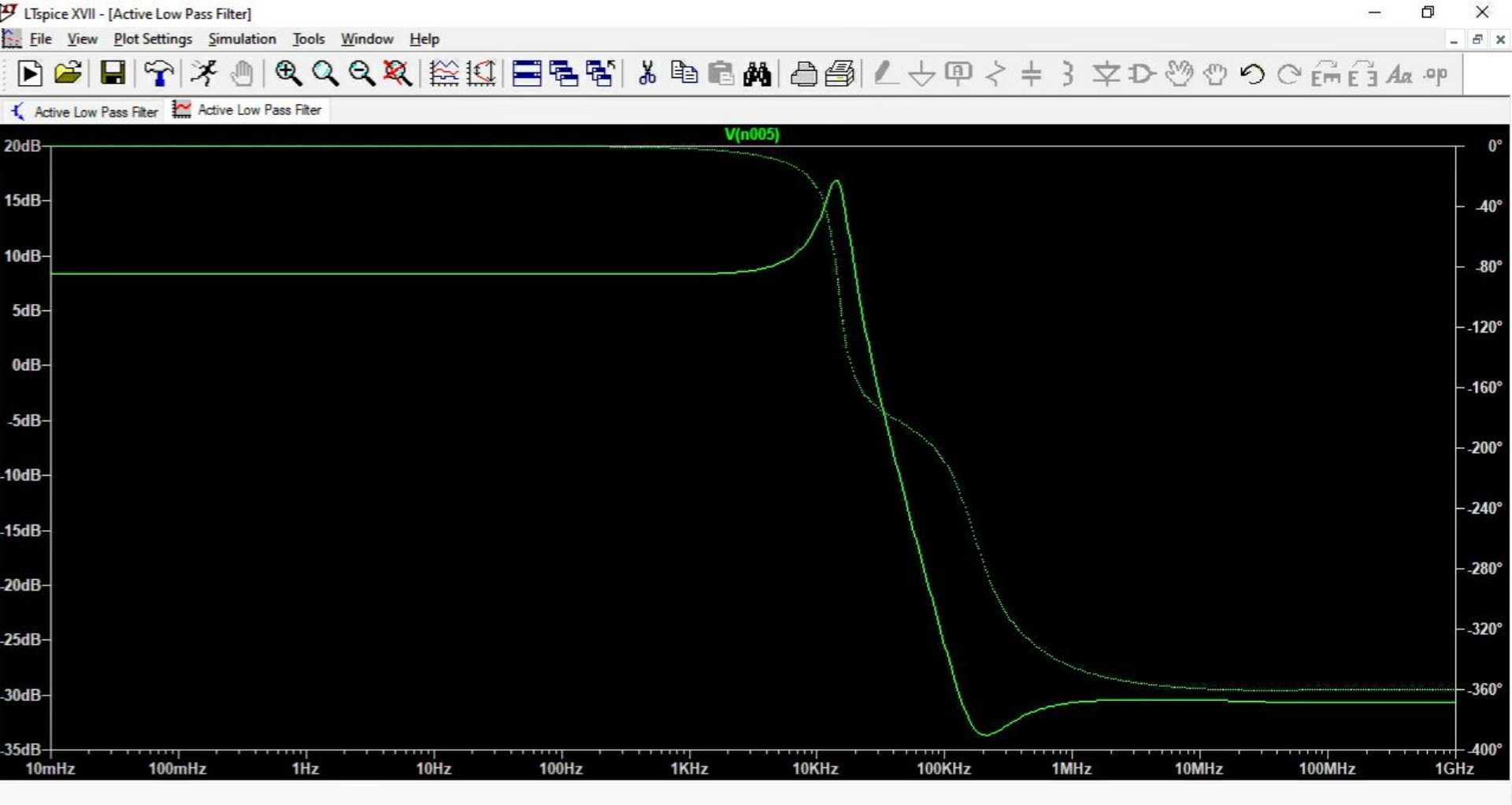
Since this filter has a  $Q\text{-factor}$  than the previous one, its peak is more sharper than before.



Name: Kaushal Banthia, Roll No: 19CS10039







Case 4: ( $R_1 = R_2 = 10k\Omega$  and  $C_1 = C_2 = 1pF$  and  $Q$ -factor = 2.5)

Since  $Q$ -factor is the same as before, we get the same value of  $k = 2.6$ .

$\therefore R_f = 1.6k\Omega \Rightarrow R_1 = R_2 = 1k\Omega$  and  $R_f = 1.6k\Omega$ .

This time, since the value of  $C_1 = C_2$  has changed, the theoretical <sup>natural</sup> undamped frequency will also change accordingly.

$$\Rightarrow f_{\text{undamped}}^{\text{natural}} = \frac{1}{2\pi(10^4 \times 10^{-12})} = 15.915 \text{ MHz.}$$

Since  $C_1 = C_2$  decreased by  $10^{-3}$ , the  $f_{\text{undamped}}^{\text{natural}}$  increased by  $10^3$ .

Since  $f_{\text{undamped}}^{\text{natural}} \propto \frac{1}{C}$ .

Comments 1 As with the previous graphs, the magnitude decreases with increasing frequency but then gets constant at very high frequencies (due to the parasitic capacitances). The phase also decreases monotonically until it becomes nearly constant ( $\approx 360^\circ$ ) at very high frequencies.

NOTE: The parasitic capacitances modelled in LTSpice are <sup>usually</sup> attached in parallel to the circuit elements. They have very low capacitance values. Hence at ~~very~~ low and medium frequencies, their reactance ( $X_L = \frac{1}{j\omega C}$ ) is very large. Since they are attached in parallel, they are ignored. But when the frequency becomes very high, then  $X_L$  becomes a small value and thus current to flow through it, leading to a voltage drop. Thus, the gain decreases, since some of the voltage gets dropped across the parasitic capacitors.



The graph is different from the previous graphs wrt to its peak. A reason ~~Another reason~~ could be that, ~~the~~ due to the shifting of the undamped natural frequency to a higher value <sup>(by an order of  $10^3$  Hz)</sup>, the Op-amp may be unable to function, since this frequency might be out of its Bandwidth. Thus, the Op-amp is as good as removed. Then, the circuit remains just like a normal second order filter, which has no characteristic peak at the undamped natural frequency.

KAUSHAL BANTHIA

19CS10039



Name: Kaushal Banthia, Roll No: 19CS10039

