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① $f(A, B, C) = ABC' + A'BC + AB'C$

A	B	C	f
0	0	0	0
0	0	1	0
0	1	0	0
0	1	1	1
1	0	0	0
1	0	1	1
1	1	0	1
1	1	1	0

⇒ Not T-Preserving
⇒ F-Preserving
⇒ Not Counting
⇒ Not Monotonic
⇒ Not Self Dual

Not T-Preserving, since

$f(F, T, T) = F$

F-Preserving, since

$f(F, F, F) = F$

Not Counting, since

$f(0, 0, 0) = 0$
and
$f(0, 0, 1) = 0.$

But position 'C' is not dummy, since,

$f(1, 1, 0) = 1$
$f(1, 1, 1) = 0$

~~Not Monotonic, since~~
~~$f(0, 1, 1) = 1$~~
~~$f(1, 1, 1) = 0$~~

Not Monotonic, since

(i) $f(0, 1, 1) = 1$
(ii) $f(1, 1, 1) = 0$

Here for position A, in $x_{A(i)} \leq x_{A(ii)}$

(0 ↓, 1 ↓)

But $f_{(i)} \geq f_{(ii)}$
(1 ↓, 0 ↓)

Not self dual, since

$f(0, 0, 0) = 0$
$f(1, 1, 1) = 0.$

(self dual requires $f(\sim 0, \sim 0, \sim 0) = \sim 0$)
$\Rightarrow (f(1, 1, 1) = 1)$
But that is not the case

∴ Since $f(A, B, C)$ is F Preserving, thus, its not functionally complete.