

## Binary Search

Def:-

" Binary search is more efficient algorithm for finding an element in a sorted array. It works by repeatedly dividing the search intervals in half, making it much faster than linear search for large datasets.

Note:- Array must be sorted (Ascending order)  
for eg { 1, 10, 20, 30, 100 }

### Step-by-step Explanation

0	1	2	3	4
10	20	30	40	50
$\downarrow$				$\uparrow$

1. Divide the array & find the mid, suppose our target is 20.

$$\text{mid} = (0+4)/2 = 2$$

2. check whether the mid value is equal to target value.

arr[mid] == target  
( 30 == 20 ) {  
    False.  
}

if 20 == 20  
(mid == target)  
{  
    return mid;  
}  
    ↑  
    index value



3. If target value is greater than mid then,  
ignore right half. left half.

i.e.  $mid < target$

target = 40

0	1	2	3	4
10	20	30	40	50
$l$		mid		$r$

mid = 2

mid < target

30 < 40

0	1	2	3	4
10	20	30	40	50
		mid	$l$	$r$
$l = mid + 1$				

4. If target value is smaller than mid,  
ignore right half.

0	1	2	3	4
10	20	30	40	50
$l$		mid		$r$

target = 20;

mid > target

30 > 20



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0	1	2	3	4
10	20	30	40	50
l	r	mid		

↖

$$r = mid - 1$$

5. If the element is not present then return -1.

#Code.

```
public class BinarySearch {
```

```
    public static int binarySearch (int[] arr, int target) {
```

```
        int left = 0;
```

```
        int right = arr.length - 1;
```

```
        while (left <= right) {
```

```
            int mid = (left + right) / 2;
```

```
            // check if target is present at mid
```

```
            if (arr[mid] == target) {
```

```
                return mid;
```

```
            }
```

```
            // If target greater, ignore left half
```

```
            if (arr[mid] < target) {
```

```
                left = mid + 1;
```

```
            }
```



```
(arr[mid] > tar) // If target is smaller, ignore right half  
else {
```

```
    right = mid - 1;  
}  
}
```

```
// Target was not found  
return -1;
```

```
}
```

```
public static void main(String[] args) {
```

```
    int[] array = { 10, 20, 30, 40, 50 };  
    int target = 20;
```

```
    int result = binarySearch(array, target);
```

```
    if (result != -1) {
```

```
        System.out.println("Element " + target + " found at  
        index: " + result);
```

```
    } else {
```

```
        System.out.println("Element " + target + " not found  
        in the array.");
```

```
    }
```

```
}
```

```
}
```



## Time Complexity :-

Best case :-  $O(1)$

Average case :-  $O(\log n)$

Worst case :-  $O(\log n)$

### \* Best case :-

target element is in the middle of array. hence  $O(1)$ .

### \* Average case :-

binary search divides the search space in half with each comparison. This leads to a logarithmic number of comparisons, hence  $O(\log n)$ .

i.e number of comparisons growing logarithmically with the size of (n) increases.

as array size  $\uparrow$  increases, the number of comparisons needed to find an element grows very slowly, making binary search very efficient for large datasets.

### \* Worst case :-

$O(\log n)$