The Monte Carlo process

MONTE CARLO SIMULATIONS IN PYTHON



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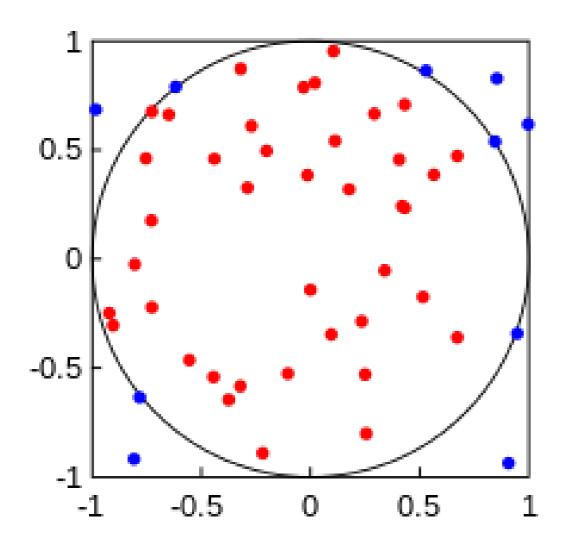


Simulation steps

- 1. Define the input variables and pick probability distributions for them
- 2. Generate inputs by sampling from these distributions
- 3. Perform a deterministic calculation of the simulated inputs
- 4. Summarize results

Calculating the value of pi

Generate random points (x, y) where x and y are in the interval from -1 to 1.



$$egin{aligned} Area_{circle} &= \pi \ Area_{square} &= 2 imes 2 = 4 \ rac{Area_{circle}}{Area_{square}} &= rac{\pi}{4} \ rac{n_{red}}{n_{all}} &= rac{\pi}{4} \ \end{array}$$

Define the input variables and pick probability distributions for them

- Inputs: the individual points represented by (x,y) coordinates
- Probability distributions: x and y follow uniform distributions from negative one to one.

```
circle_points = 0
square_points = 0
```

Generate inputs by sampling from these distributions

Sample random x and y coordinate values distributed uniformly between -1 and 1:

```
for i in range(n):
    x = random.uniform(-1, 1)
    y = random.uniform(-1, 1)
```

Perform deterministic calculation of the simulated inputs

Check whether each point lies within the circle: deterministic for given x and y

```
dist_from_origin = x**2 + y**2
```

If yes, add the point to circle_points; always add the point to square_points

```
if dist_from_origin <= 1:
    circle_points += 1
square_points += 1</pre>
```

Summarize the results to answer questions of interest

After many rounds of simulations, calculate the value of pi!

pi = 4 * circle_points/ square_points

All together now

```
n = 4000000
circle_points = 0
square_points = 0
for i in range(n):
    x = random.uniform(-1, 1)
    y = random.uniform(-1, 1)
    dist_from_origin = x**2 + y**2
    if dist_from_origin <= 1:</pre>
        circle_points += 1
    square_point += 1
pi = 4 * circle_points / square_points
print(pi)
```

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Let's practice!

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Generating discrete random variables

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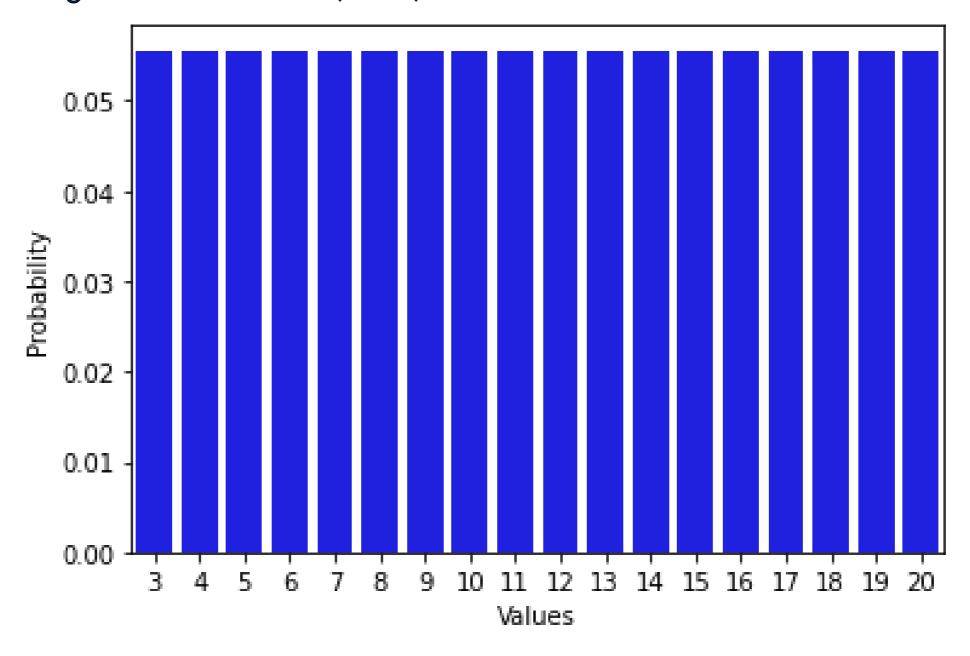
Required imports

```
import scipy.stats as st
import seaborn as sns
import pandas as pd
import numpy as np
import matplotlib.pyplot as plt
```



Discrete uniform distribution

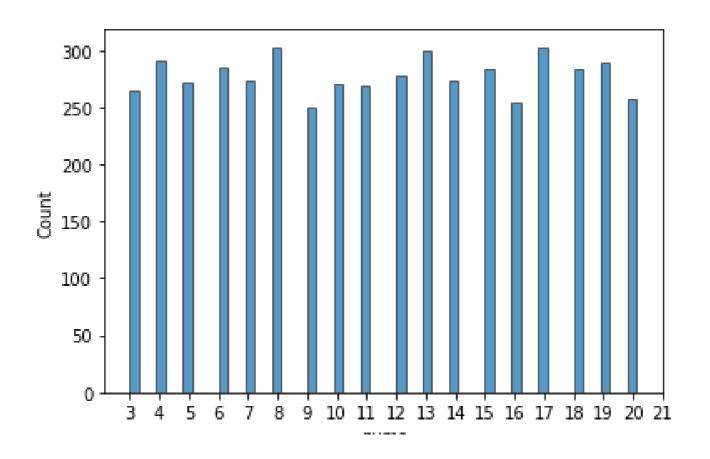
Theoretical probability mass function (PMF):





Sampling from the discrete uniform distribution

```
low = 3
high = 21
samples = st.randint.rvs(low, high, size=1000)
samples_dict = {"nums":samples}
sns.histplot(x="nums", data=samples_dict, bins=6, binwidth=0.3)
```

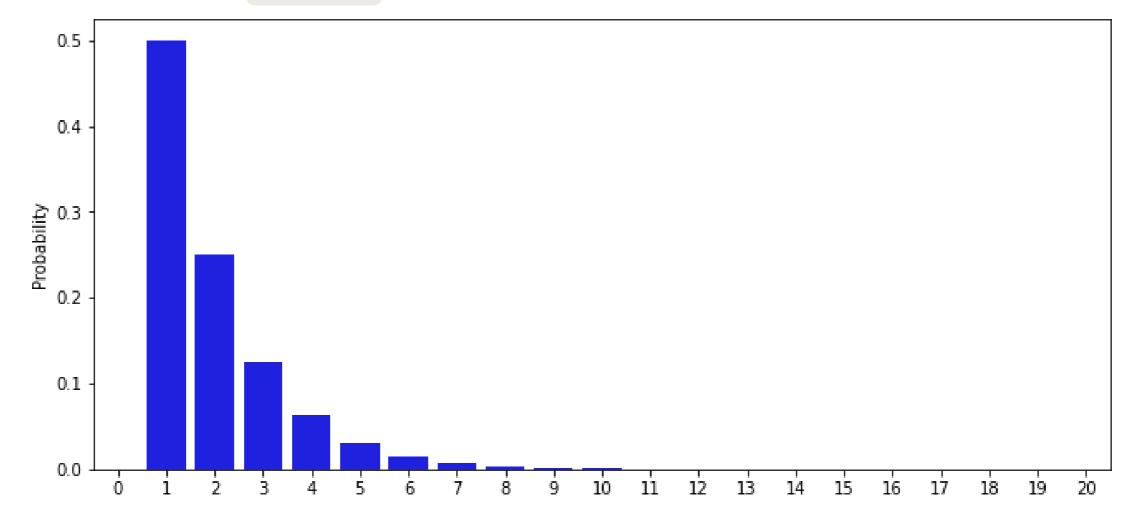




Geometric distribution

The probability distribution of the number of trials, X, needed to get one success, given the success probability, p.

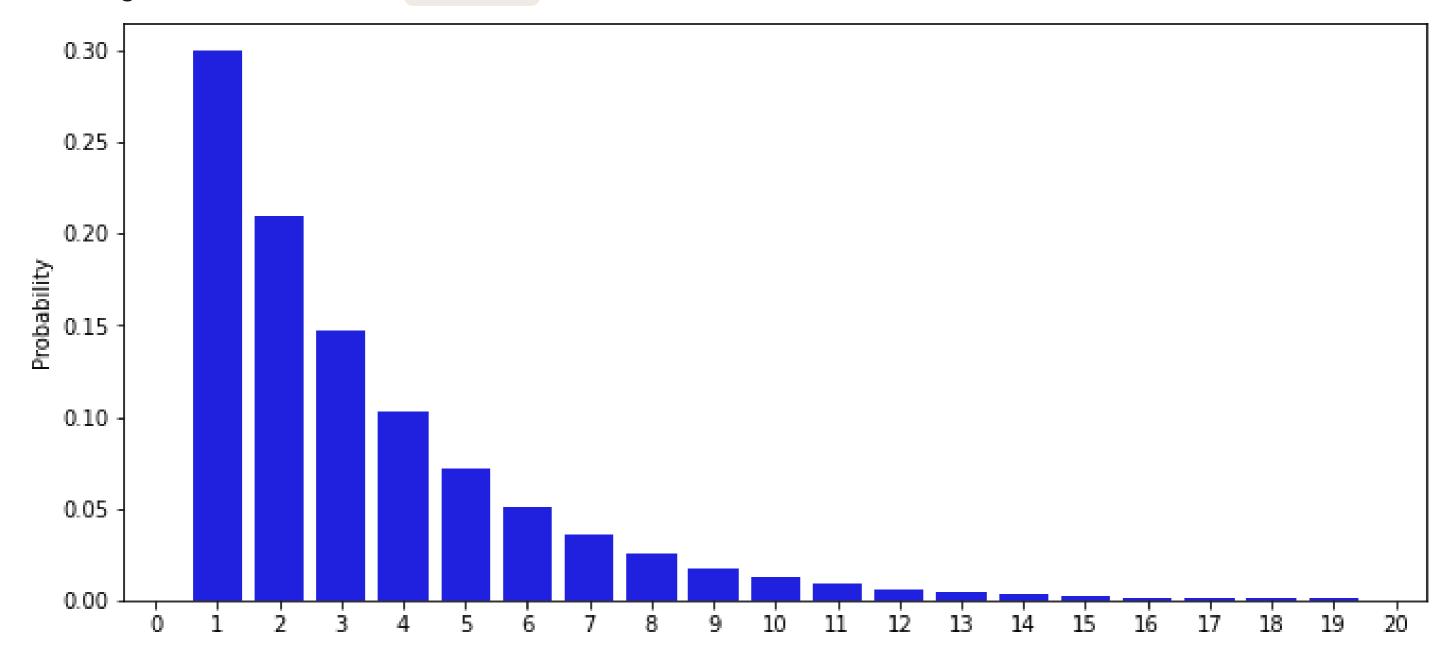
Probability Mass Function, p = 0.5





Geometric distribution

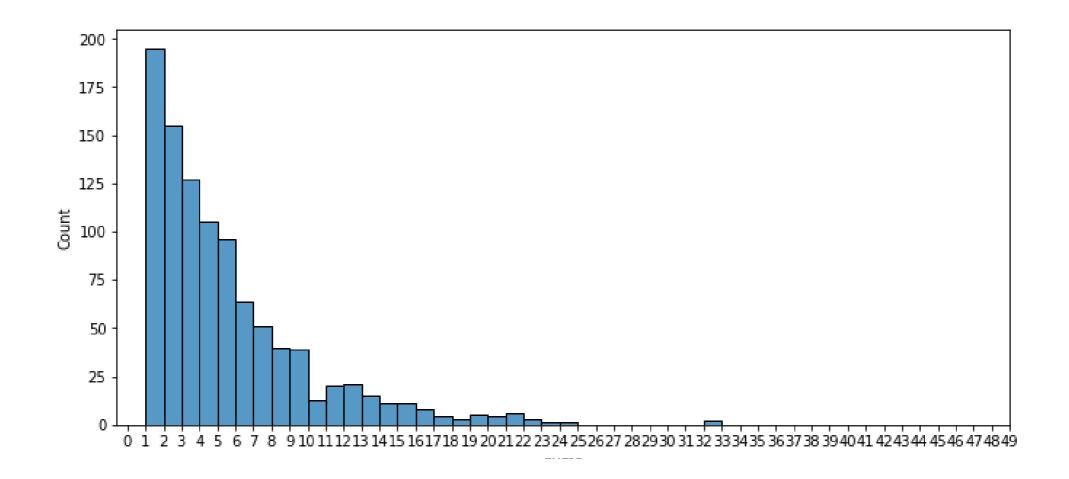
Probability Mass Function, p = 0.3





Sampling from geometric distribution

```
p = 0.2
samples = st.geom.rvs(p, size=1000)
samples_dict = {"nums":samples}
sns.histplot(x="nums", data=samples_dict)
```



More discrete probability distributions

- Poisson (scipy.stats.poisson)
 - Expresses the probability of a given number of events occurring in a fixed interval of time or space
- Binomial (scipy.stats.binom)
 - \circ Expresses probability of the number of successes in a sequence of n independent experiments.
- And more!

¹ https://docs.scipy.org/doc/scipy/reference/stats.html#discrete-distributions



Let's practice!

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Generating continuous random variables

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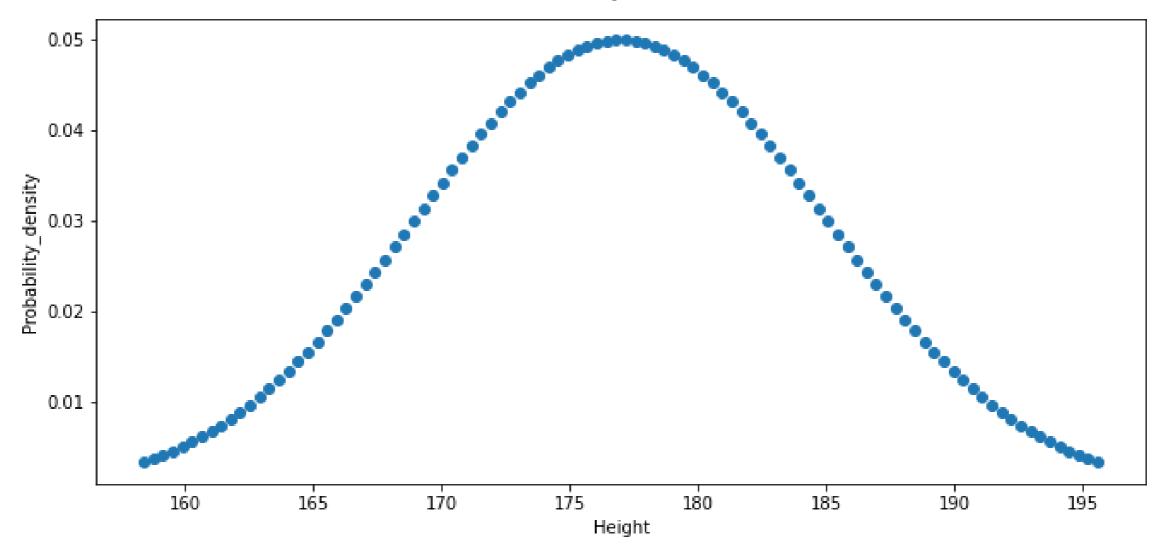
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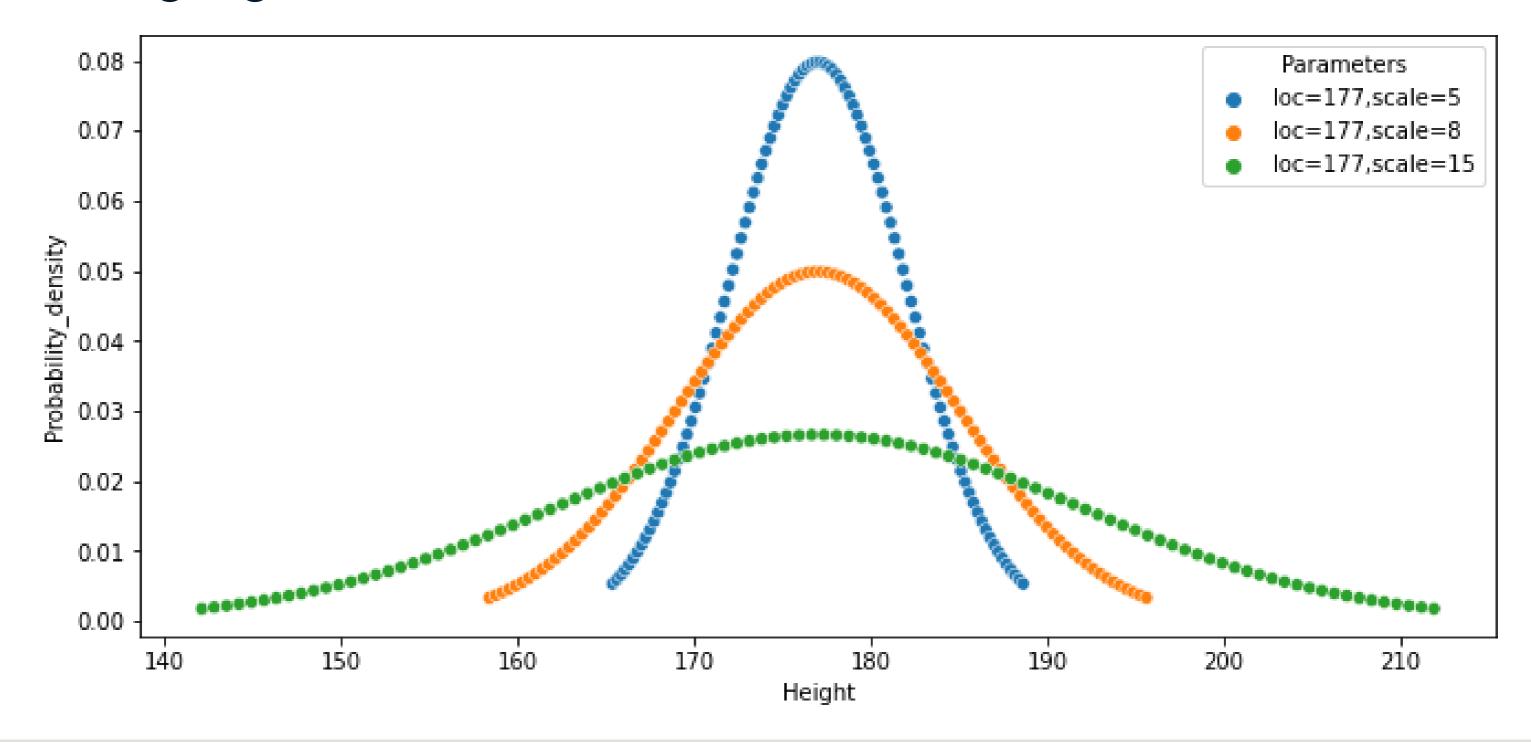
Normal distribution

Bell-shaped and centered at the mean (or loc); width defined by standard deviation (or scale)

The heights of American adult males are normally distributed:

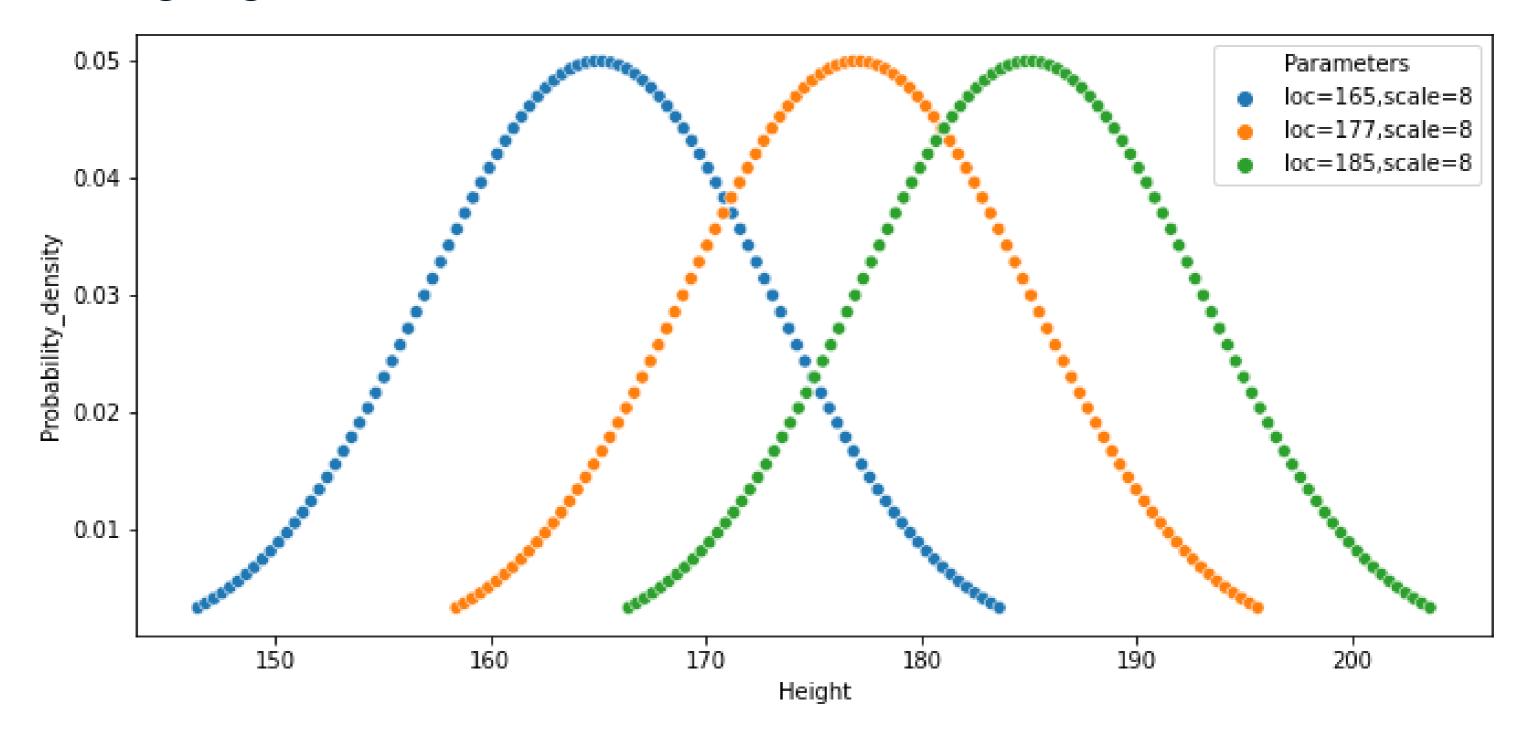


Changing the scale (standard deviation)



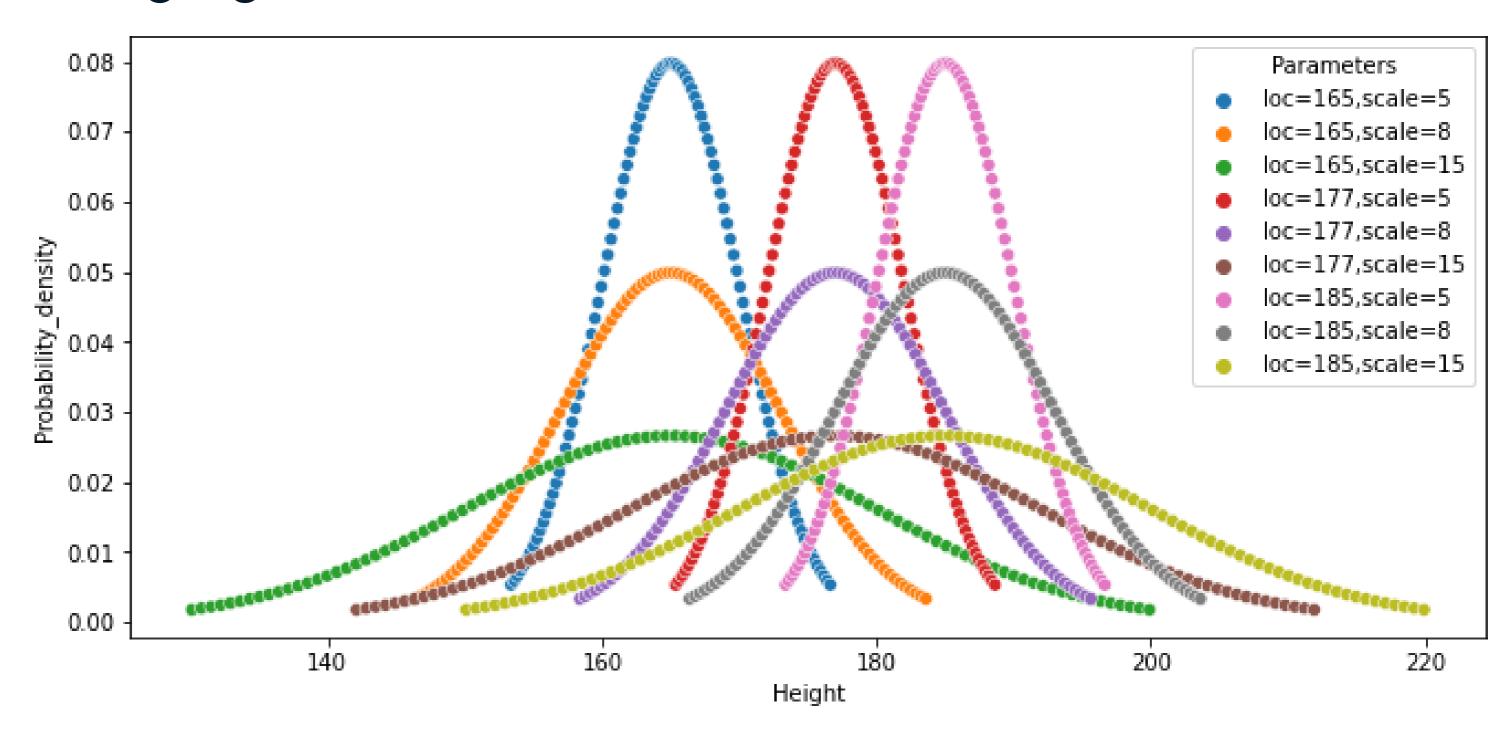


Changing the loc (mean)





Changing both scale and loc





Sampling from normal distributions

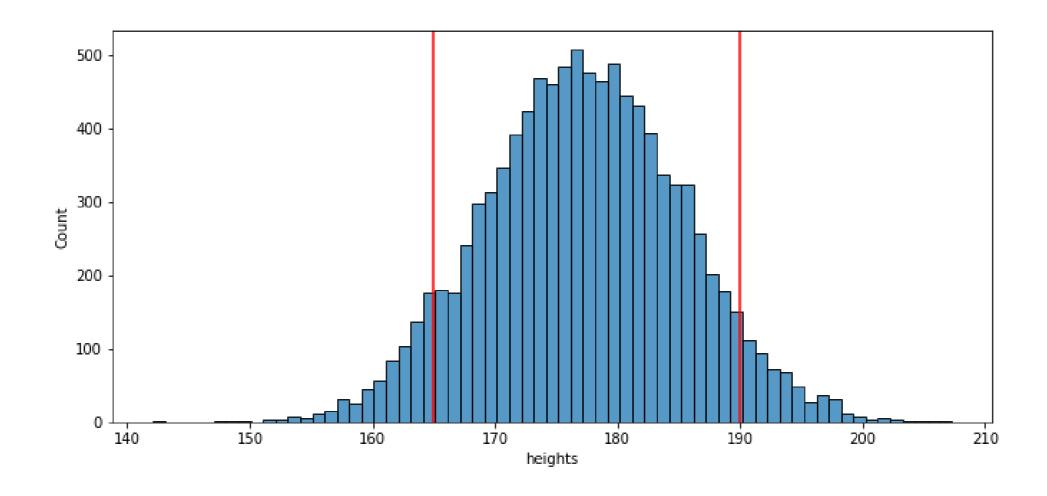
- Normally distributed US adult male heights; mean = 177 cm; standard deviation = 8 cm
- What's the percentage of people with a height either above 190 or below 165 cm?

```
heights = st.norm.rvs(loc=177, scale=8, size=10000)
qualified = (heights < 165) | (heights > 190)
print(np.sum(qualified) * 100/10000)
```

12.28

Plotting simulation results

```
heights_dict = {"heights":heights}
sns.histplot(x="heights", data=heights_dict)
plt.axvline(x=165, color="red")
plt.axvline(x=190, color="red")
```





More continuous probability distributions

- Continuous Uniform distribution (st.uniform)
 - The continuous analog of the discrete uniform distribution
- Exponential distribution (st.expon)
 - The continuous analog of the geometric distribution

¹ https://docs.scipy.org/doc/scipy/tutorial/stats/continuous.html



Let's practice!

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Generating multivariate random variables

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Sampling from multivariate distributions

Multinomial distribution

- Variables each follow binomial distribution
- Probabilities of these variables sum to one

Example: simulating the results of flipping a biased coin

scipy.stats.multinomial.rvs()



Sampling from multivariate distributions

Multivariate normal distribution

- Variables each follow normal distribution
- Variables can be correlated with each other or not

Example: simulating price and demand

scipy.stats.multivariate_normal.rvs()



Sampling from multinomial distributions

```
Simulation: .rvs(n, p, size)
```

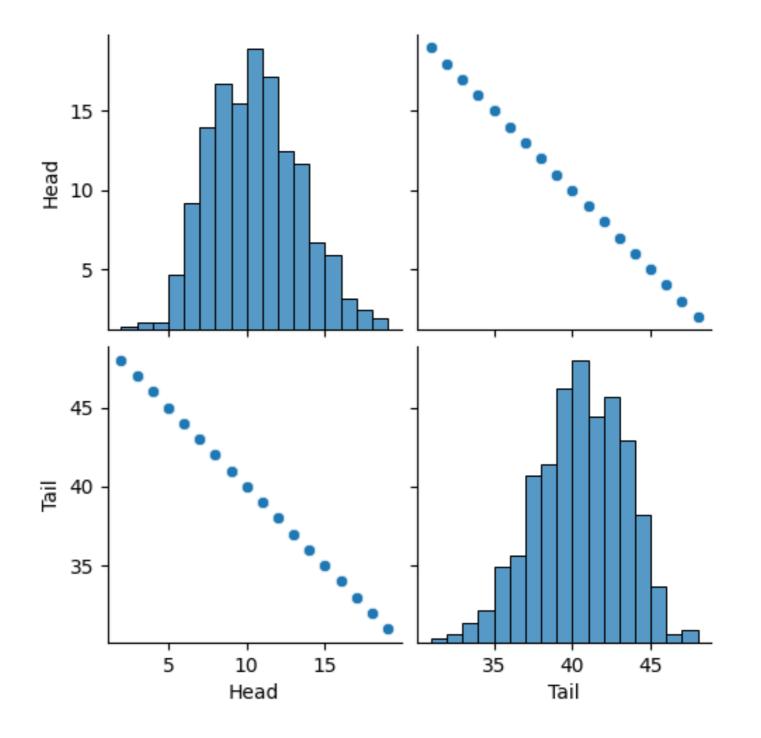
```
• n: 50
```

• p: [0.2, 0.8]

• size: 500

```
results = st.multinomial.rvs(50,
      [0.2, 0.8], size=500)

df_results=pd.DataFrame(
      {"Head":results[:, 0],
       "Tail":results[:, 1]})
sns.pairplot(df_results)
```

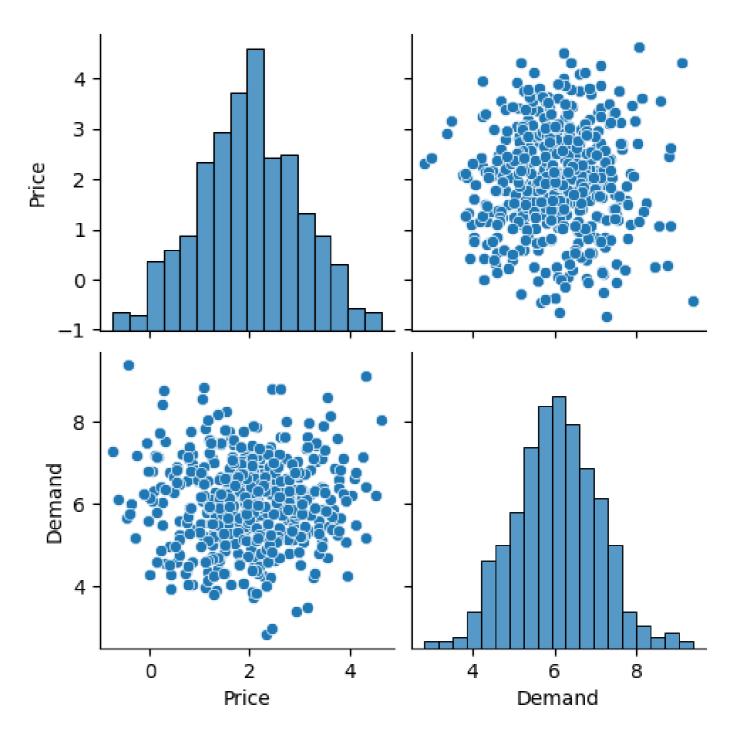


Sampling from multivariate normal distributions

```
Simulation: .rvs(mean, size)mean: [2, 6]size: 500
```

```
results=st.multivariate_normal.rvs(
    mean=[2, 6], size=500)

df_results=pd.DataFrame(
    {"Price":results[:, 0],
     "Demand":results[:, 1]})
sns.pairplot(df_results)
```



Covariance matrix

- Captures the variance and covariances of variables
- Definition using two random variables x and y:

```
\left[ egin{array}{c} \mathbf{x} & \mathbf{y} & \mathbf{y} \\ \mathbf{x} & \left[ egin{array}{c} var(x) & cov(x,y) \\ cov(x,y) & var(y) \end{array} 
ight]
```

Example:

```
df_historical.cov()
```

Multivariate normal sampling with defined covariance

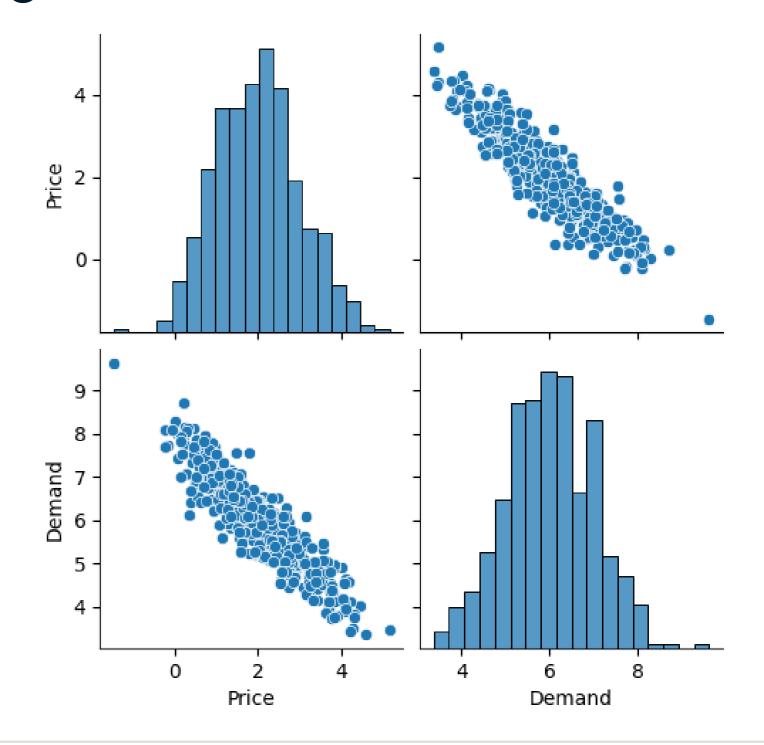
```
Simulation: .rvs(mean, size)mean: [2, 6]
```

• size: 500

cov: np.array([[1, -0.9], [-0.9, 1]])

```
cov_mat = np.array([[1,-0.9], [-0.9,1]])
results = st.multivariate_normal.rvs(
    mean=[2,6], size=500, cov=cov_mat)

df_results = pd.DataFrame(
    {"Price":results[:,0],
        "Demand":results[:,1]})
sns.pairplot(df_results)
```



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