

## More Quicksort Lecture 34.

Quicksort is the fastest in certain conditions.

How to make Quicksort faster than mergesort?

Tommy Hoards In-place partitioning:

- Left pointer loves small items.  $\rightarrow$  Relative to pivot.
- Right pointer loves large items.  $\rightarrow$
- Big idea: Walk towards each other, swap what they don't like.

17 15 14 32 2 26 41 17 17  $\rightarrow$  17 15 17 32 2 26 41 17 14  
     $\uparrow$   $\uparrow$   $\uparrow$   $\uparrow$   
    L L L L

- Walk pointers towards each other until it meets a hated item.

- When both pointers stop, swap & move pointers by one.
- When pointers cross, you're done walking.

- Swap pivot w/ G.

- Repeat for the "less" and "greater" side with the first being the first item.

Median:

Cost to compare median is too high. Runtime goes too high.

QuickSelect

- Partitioning can be used to find the median.

[9] 550 14 6 10 5 330 817 913

Partition 2

6 5 [9] 550 14 10 330 817 913

Median has to be in middle, so we look to the right of the current pivot!

[ ] [ ] [ ] [550] 14 10 330 817 913

[ ] [ ] [ ] [14 10 330] [550] 817 913

[14] 10 330  $\rightarrow$  10 [14] 330  $\rightarrow$  14 is median.

Time Complexity of QuickSelect:

$[0, 2, 3, \dots, N]$

$\rightarrow \Theta(N^2)$  Worst case

$[1, 2, \dots]$

$[1, 2, 3, 4, \dots, \frac{N}{2}, \dots, N]$

Expected RT:  $\Theta(N)$

Quick select to find exact median is still pretty slow.

Stability, Optimizations

A sort is stable if order of equivalent items is preserved.

Stable?

Heapsort

No

Insertion

Yes

Merge

Yes

Quicksort (Tony Hoare)

No

Additional tricks

- Switch to Insertion sort when size is  $n < 15$
- Make adaptive sort: exploit existing order in array.
- Exploit restrictions on set of keys. If number of keys is some constant, we can sort in  $\Theta(N)$ .
- Quick sort: If you go too deep, swap to insertion sort.

Shuffling

Easiest way:

- Generate  $N$  random numbers, attach one to each array item
- Sort the items by the attached random number.