

# Lab 6 Solutions

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**P 1.** Consider the **Delivery Time** data set. Calculate the following measures of outliers:

- (a) Leverage point,
- (b) COOK'S D,
- (c) DFBETAS,
- (d) DFFITS,
- (e) COVRATIO.

Based on the above measures, find the outliers present in the data.

## **Code:**

```
library(car)
library(readxl)

TimeDeliveryData <- read_excel("TimeDeliveryData.xlsx") %>% as.data.frame()

model <- lm(Y ~ X1 + X2, data = TimeDeliveryData)

leverage_points <- hatvalues(model)
cooks_d <- cooks.distance(model)
dfbetas_values <- dfbetas(model)
dffits_values <- dffits(model)
covratio_values <- covratio(model)

# Print the Results
leverage_points
cooks_d
dfbetas_values
dffits_values
covratio_values

influence_measures <- influence.measures(model)
summary(influence_measures)
```

## **Output:**

```
> leverage_points
  1    2    3    4    5    6
0.10180178 0.07070164 0.09873476 0.08537479 0.07501050 0.04286693
  7    8    9   10   11   12
0.08179867 0.06372559 0.49829216 0.19629595 0.08613260 0.11365570
 13   14   15   16   17   18
```

```
0.06112463 0.07824332 0.04111077 0.16594043 0.05943202 0.09626046
  19    20    21    22    23    24
0.09644857 0.10168486 0.16527689 0.39157522 0.04126005 0.12060826
  25
0.06664345
```

```
> cooks_d
```

```
   1      2      3      4      5
1.000921e-01 3.375704e-03 9.455785e-06 7.764718e-02 5.432217e-04
   6      7      8      9     10
1.231067e-04 2.171604e-03 3.051135e-03 3.419318e+00 5.384516e-02
  11     12     13     14     15
1.619975e-02 1.596392e-03 2.294737e-03 3.292786e-03 6.319880e-04
  16     17     18     19     20
3.289086e-03 4.013419e-04 4.397807e-02 1.191868e-02 1.324449e-01
  21     22     23     24     25
5.086063e-02 4.510455e-01 2.989892e-02 1.023224e-01 1.084694e-04
```

```
> dfbetas_values
```

```
(Intercept)    X1      X2
1 -0.187267279 0.4113118750 -0.434862094
2  0.089793299 -0.0477642427  0.014414155
3 -0.003515177  0.0039483525 -0.002846468
4  0.451964743  0.0882802920 -0.273373097
5 -0.031674102 -0.0133001129  0.024240457
6 -0.014681480  0.0017921068  0.001078986
7  0.078071285 -0.0222783194 -0.011018802
8  0.071202807  0.0333823324 -0.053823961
9 -2.575739806  0.9287433421  1.507550618
10 0.107919369 -0.3381628707  0.341326746
11 -0.034274535  0.0925271540 -0.002686252
12 -0.030268935 -0.0486664488  0.053973390
13  0.072366473 -0.0356212226  0.011335105
14  0.049516699 -0.0670868604  0.061816778
15  0.022279094 -0.0047895025  0.006838236
16 -0.002693186  0.0644208340 -0.084187552
17  0.028855555  0.0064876499 -0.015696507
18  0.248558020  0.1897331043 -0.272430555
19  0.172558506  0.0235737344 -0.098968842
20  0.168036548 -0.2149950233 -0.092915080
21 -0.161928685 -0.2971750929  0.336406248
22  0.398566309 -1.0254140704  0.573140240
23 -0.159852248  0.0372930389 -0.052651959
24 -0.119720216  0.4046225960 -0.465446949
25 -0.016816024  0.0008498979  0.005592192
```

```
> dffits_values
```

```
   1      2      3      4      5
-0.570850478 0.098618619 -0.005203676 0.500801817 -0.039458989
```

```

      6      7      8      9      10
-0.018779374 0.078990030 0.093760764 4.296080927 0.398713071
      11      12      13      14      15
0.217953207 -0.067670223 0.081259033 0.097362643 0.042584374
      16      17      18      19      20
-0.097159801 0.033915978 0.365309285 0.186167873 -0.671771402
      21      22      23      24      25
-0.388501185 -1.195036104 -0.307538544 -0.571139627 -0.017626149

> covratio_values
      1      2      3      4      5      6      7
0.8710782 1.2149209 1.2756813 0.8759964 1.2396032 1.1999120 1.2397501
      8      9      10      11      12      13      14
1.2056413 0.3422132 1.3054035 1.1717266 1.2906069 1.2070490 1.2276758
      15      16      17      18      19      20      21
1.1918460 1.3692181 1.2192451 1.0692145 1.2152541 0.7598217 1.2376914
      22      23      24      25
1.3980787 0.8896761 0.9476321 1.2310981

> summary(influence_measures)
Potentially influential observations of
      lm(formula = Y ~ X1 + X2, data = TimeDeliveryData) :

      dfb.1_ dfb.X1 dfb.X2 dffit cov.r cook.d hat
9 -2.58_* 0.93 1.51_* 4.30_* 0.34_* 3.42_* 0.50_*
22 0.40 -1.03_* 0.57 -1.20_* 1.40 0.45 0.39_*

```

**P 2.** Consider the **Acetylene** data set.

- Normalise the data set by subtracting the associated mean and dividing by the square root of  $(n - 1) \times$  the sample variance of each variables.
- Consider all the regressors including the interactions and second order terms. Find the correlation matrix. Observe the correlation.
- Find the VIF for the regression model where all the regressors including the interactions and second order terms are considered.

### Code:

```

library(car)
library(dplyr)
library(readxl)

Acetylene_Data <- read_excel("Acetylene_Data.xlsx") %>% as.data.frame()

# Normalize the dataset
acetylene_norm <- lapply(Acetylene_Data, function(x) ((x - mean(x)) / sqrt((length(x) - 1) * var(x)))) %>%
as.data.frame()

```

```
# Create interaction and second-order terms
```

```
acetylene_final <- cbind(acetylene_norm,  
  X1X2 = acetylene_norm$X1 * acetylene_norm$X2,  
  X1X3 = acetylene_norm$X1 * acetylene_norm$X3,  
  X2X3 = acetylene_norm$X2 * acetylene_norm$X3,  
  X1_sq = acetylene_norm$X1^2,  
  X2_sq = acetylene_norm$X2^2,  
  X3_sq = acetylene_norm$X3^2)
```

```
# Calculate correlation matrix
```

```
corr <- cor(acetylene_final)
```

```
# Print correlation matrix
```

```
cat("Correlation Matrix: ")  
corr
```

```
# Calculate VIF
```

```
model <- lm(Y ~ ., data = acetylene_final)  
vif_values <- vif(model)
```

```
# Print VIF values
```

```
cat("VIF Values: ", vif_values)
```

### **Output:**

```
> acetylene_norm
```

	Y	X1	X2	X3
1	0.27978969	0.28022427	-0.22544387	-0.231055577
2	0.30582925	0.28022427	-0.15704118	-0.231055577
3	0.31233914	0.28022427	-0.06583759	-0.235136028
4	0.26893987	0.28022427	0.04816689	-0.222894673
5	0.24724023	0.28022427	0.20777317	-0.218814222
6	0.18214132	0.28022427	0.48138393	-0.231055577
7	-0.17590268	-0.04003204	-0.32576781	-0.002550282
8	-0.09995395	-0.04003204	-0.22544387	-0.018872089
9	-0.03485504	-0.04003204	-0.06583759	-0.067837509
10	-0.02400522	-0.04003204	0.04816689	-0.116802929
11	0.04109369	-0.04003204	0.20777317	-0.051515703
12	0.05194350	-0.04003204	0.48138393	0.005610621
13	-0.45799795	-0.36028835	-0.32576781	0.356529466
14	-0.41459868	-0.36028835	-0.22544387	0.470782113
15	-0.33864995	-0.36028835	-0.06583759	0.421816693
16	-0.14335322	-0.36028835	0.20777317	0.372851273

```
> acetylene_final
```

	Y	X1	X2	X3	X1X2
1	0.27978969	0.28022427	-0.22544387	-0.231055577	-0.063174843
2	0.30582925	0.28022427	-0.15704118	-0.231055577	-0.044006749
3	0.31233914	0.28022427	-0.06583759	-0.235136028	-0.018449290
4	0.26893987	0.28022427	0.04816689	-0.222894673	0.013497533

```

5 0.24724023 0.28022427 0.20777317 -0.218814222 0.058223085
6 0.18214132 0.28022427 0.48138393 -0.231055577 0.134895461
7 -0.17590268 -0.04003204 -0.32576781 -0.002550282 0.013041150
8 -0.09995395 -0.04003204 -0.22544387 -0.018872089 0.009024978
9 -0.03485504 -0.04003204 -0.06583759 -0.067837509 0.002635613
10 -0.02400522 -0.04003204 0.04816689 -0.116802929 -0.001928219
11 0.04109369 -0.04003204 0.20777317 -0.051515703 -0.008317584
12 0.05194350 -0.04003204 0.48138393 0.005610621 -0.019270780
13 -0.45799795 -0.36028835 -0.32576781 0.356529466 0.117370347
14 -0.41459868 -0.36028835 -0.22544387 0.470782113 0.081224798
15 -0.33864995 -0.36028835 -0.06583759 0.421816693 0.023720516
16 -0.14335322 -0.36028835 0.20777317 0.372851273 -0.074858253
      X1X3      X2X3      X1_sq      X2_sq      X3_sq
1 -0.0647473801 0.0520900627 0.078525641 0.050824937 5.338668e-02
2 -0.0647473801 0.0362852397 0.078525641 0.024661931 5.338668e-02
3 -0.0658908217 0.0154807893 0.078525641 0.004334588 5.528895e-02
4 -0.0624604969 -0.0107361442 0.078525641 0.002320050 4.968204e-02
5 -0.0613170553 -0.0454637249 0.078525641 0.043169691 4.787966e-02
6 -0.0647473801 -0.1112264424 0.078525641 0.231730492 5.338668e-02
7 0.0001020930 0.0008307999 0.001602564 0.106124668 6.503940e-06
8 0.0007554882 0.0042545967 0.001602564 0.050824937 3.561557e-04
9 0.0027156738 0.0044662581 0.001602564 0.004334588 4.601928e-03
10 0.0046758594 -0.0056260344 0.001602564 0.002320050 1.364292e-02
11 0.0020622786 -0.0107035809 0.001602564 0.043169691 2.653868e-03
12 -0.0002246046 0.0027008628 0.001602564 0.231730492 3.147907e-05
13 -0.1284534116 -0.1161458245 0.129807692 0.106124668 1.271133e-01
14 -0.1696173089 -0.1061349402 0.129807692 0.050824937 2.216358e-01
15 -0.1519756387 -0.0277713943 0.129807692 0.004334588 1.779293e-01
16 -0.1343339684 0.0774684917 0.129807692 0.043169691 1.390181e-01

```

```
> cat("Correlation Matrix: ")
```

```
Correlation Matrix:
```

```
> corr
```

```

      Y      X1      X2      X3      X1X2
Y  1.00000000 0.9450377 0.37003503 -0.91397769 -0.36615167
X1  0.94503771 1.0000000 0.22362776 -0.95820405 -0.13241739
X2  0.37003503 0.2236278 1.00000000 -0.24023098 0.03868762
X3 -0.91397769 -0.9582041 -0.24023098 1.00000000 0.19498531
X1X2 -0.36615167 -0.1324174 0.03868762 0.19498531 1.00000000
X1X3 0.42055075 0.4428236 0.19226267 -0.66052652 -0.26485039
X2X3 0.41877316 0.2055387 -0.02306559 -0.27411884 -0.97448134
X1_sq -0.24850590 -0.2707456 -0.14771083 0.50096224 0.24631222
X2_sq -0.03803937 0.0309599 0.49754636 -0.01751058 0.39789760
X3_sq -0.55517440 -0.5767868 -0.22390584 0.76515318 0.27476802
      X1X3      X2X3      X1_sq      X2_sq      X3_sq
Y  0.4205507 0.41877316 -0.2485059 -0.03803937 -0.5551744
X1  0.4428236 0.20553866 -0.2707456 0.03095990 -0.5767868
X2  0.1922627 -0.02306559 -0.1477108 0.49754636 -0.2239058
X3 -0.6605265 -0.27411884 0.5009622 -0.01751058 0.7651532

```

```
X1X2 -0.2648504 -0.97448134 0.2463122 0.39789760 0.2747680
X1X3 1.0000000 0.32351596 -0.9722442 0.12583104 -0.9721670
X2X3 0.3235160 1.00000000 -0.2792725 -0.37460454 -0.3585293
X1_sq -0.9722442 -0.27927248 1.0000000 -0.12359068 0.8936644
X2_sq 0.1258310 -0.37460454 -0.1235907 1.00000000 -0.1579789
X3_sq -0.9721670 -0.35852931 0.8936644 -0.15797895 1.0000000
```

```
> cat("VIF Values: ", vif_values)
```

```
VIF Values: 375.2478 1.740631 680.28 31.03706 6563.345 35.61129 1762.575 3.164318 1156.766
```